

Seminar, Tsukuba Univ., Jan.19, 2011

RHICとLHCにおける楕円型 フローの相対論的流体モデル による解析

東京大学大学院理学系研究科



平野哲文

T.H., P.Huovinen, Y.Nara, arXiv:1012.3955; arXiv:1010.6222(PRC,
in press); invited review article in Progress of Particle and Nuclear
Physics (in preparation)

Outline

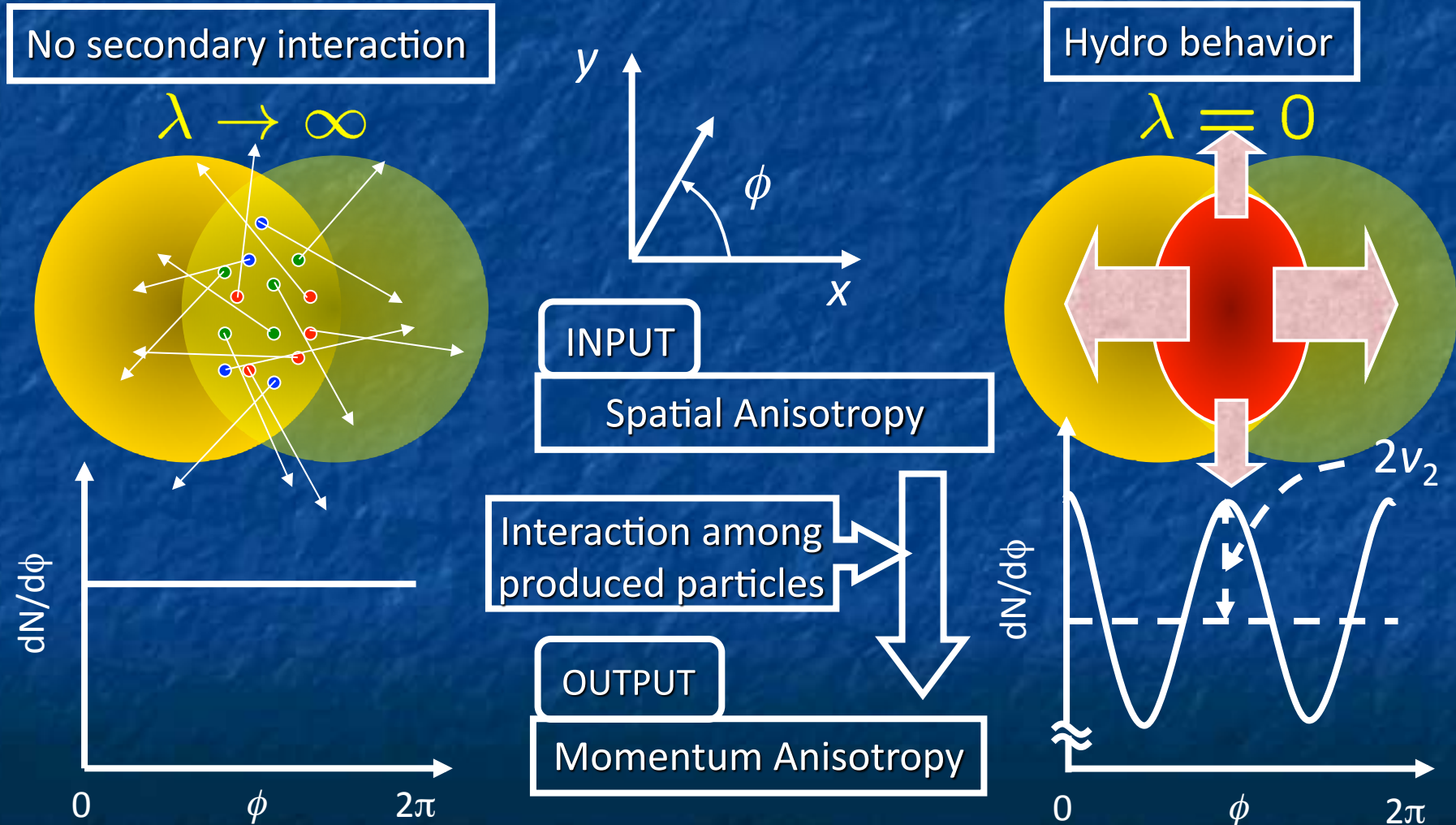
- Introduction
- Some highlights from the hybrid model
- Model: QGP fluid + hadronic cascade picture
- Results at RHIC:
 - v_2
 - source function
- Prediction and Postdiction at RHIC and LHC:
 - v_2 in U+U collisions
 - v_2 in Pb+Pb collisions
- Summary

Introduction

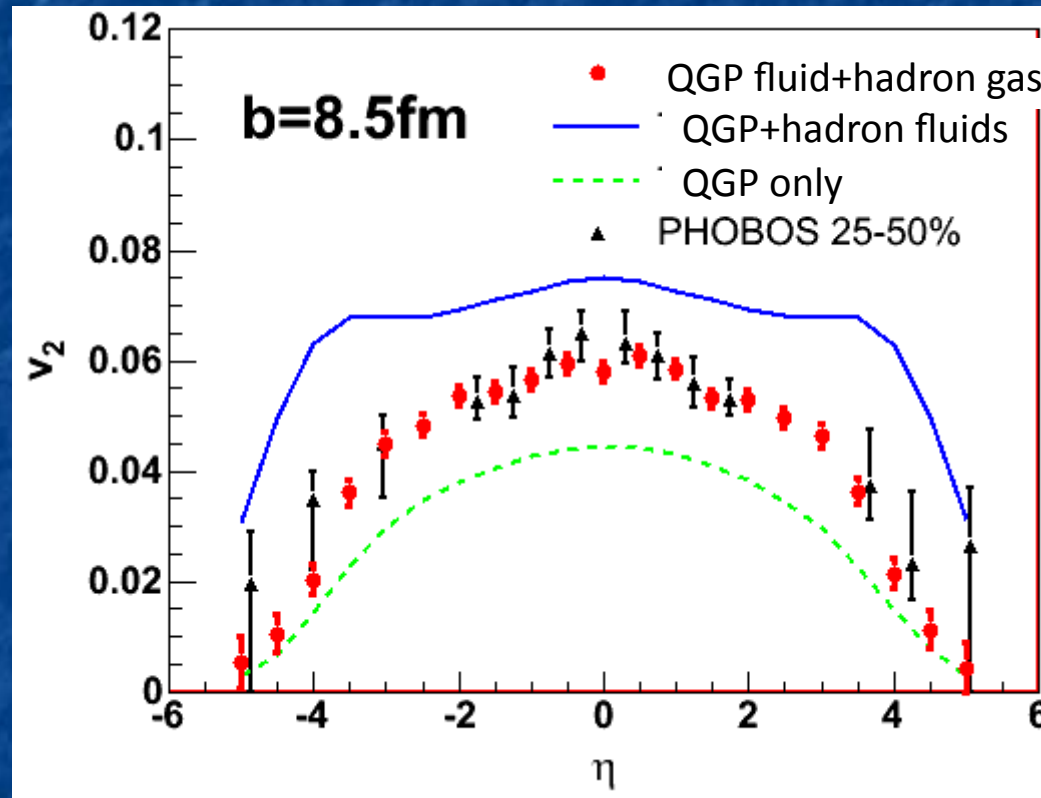
- Main aim: Understanding RHIC data based on a systematic analysis with QGP perfect fluid picture
- After press release of perfect fluid discovery in 2005 → Much progress: hadronic dissipation, eccentricity fluctuation, lattice EoS, CGC initial condition...
- Set a baseline for viscous hydro calculations
- Prediction for U+U at RHIC and Pb+Pb at LHC

Elliptic Flow

How does the system respond to spatial anisotropy?



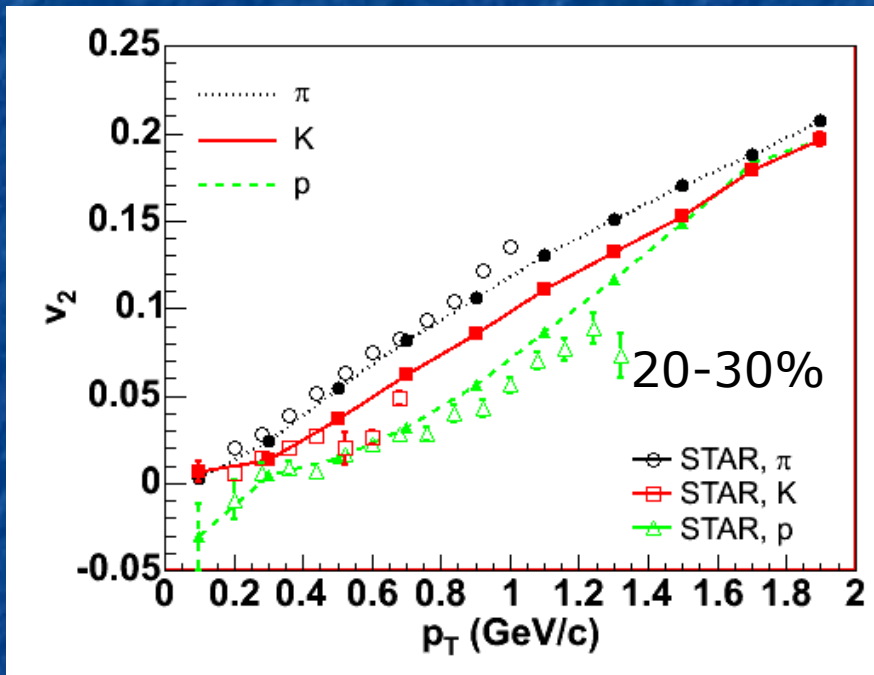
Importance of Hadronic Dissipation



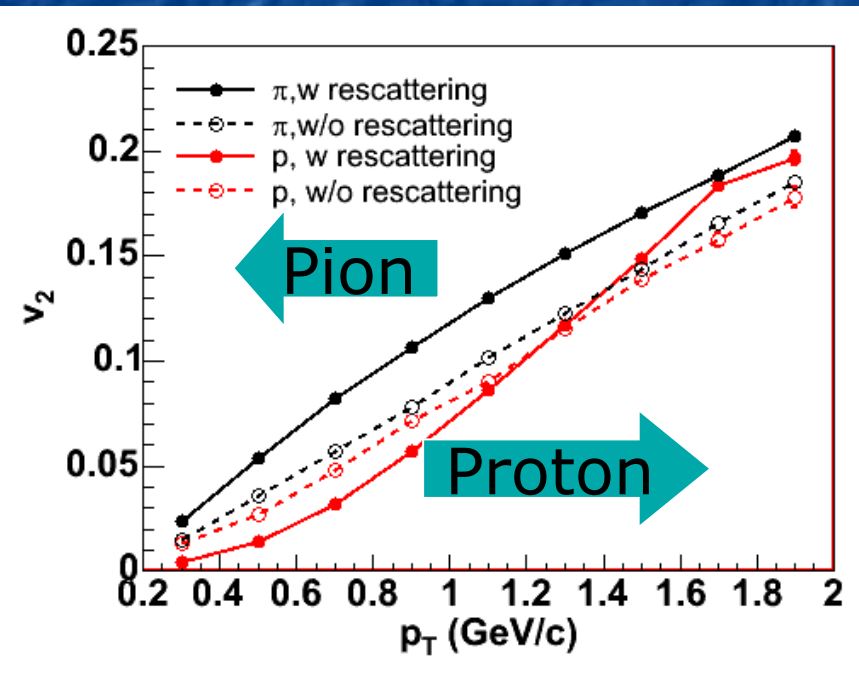
Suppression in forward and backward rapidity
Importance of hadronic viscosity

TH et al.,('05)

Mass Splitting = Hadronic effects



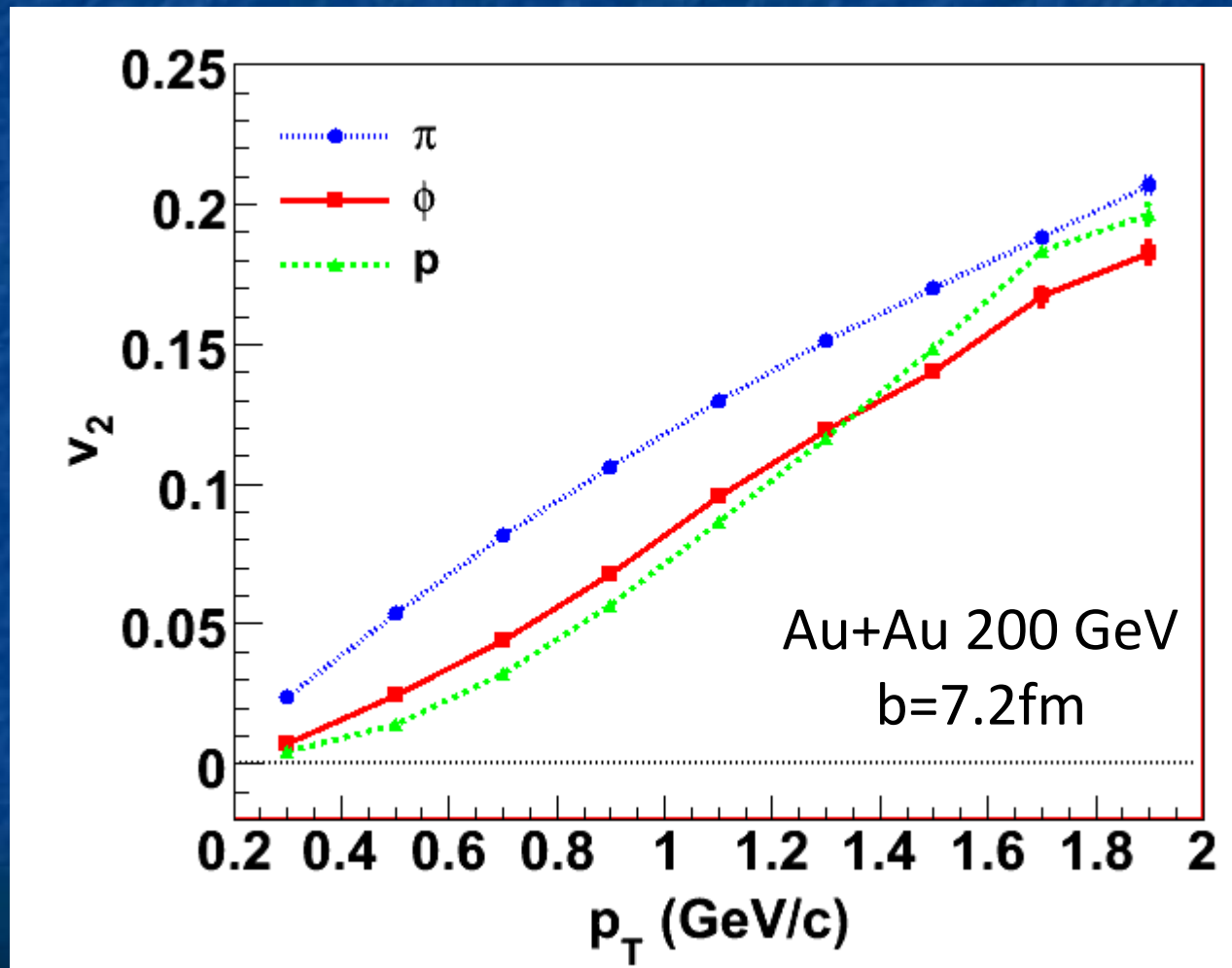
Mass dependence is o.k. from hydro+cascade.
When mass splitting appears?



Mass ordering comes from hadronic rescattering effect.
Interplay btw. radial and elliptic flows.



TH et al.,('08)

Violation of Mass Splitting

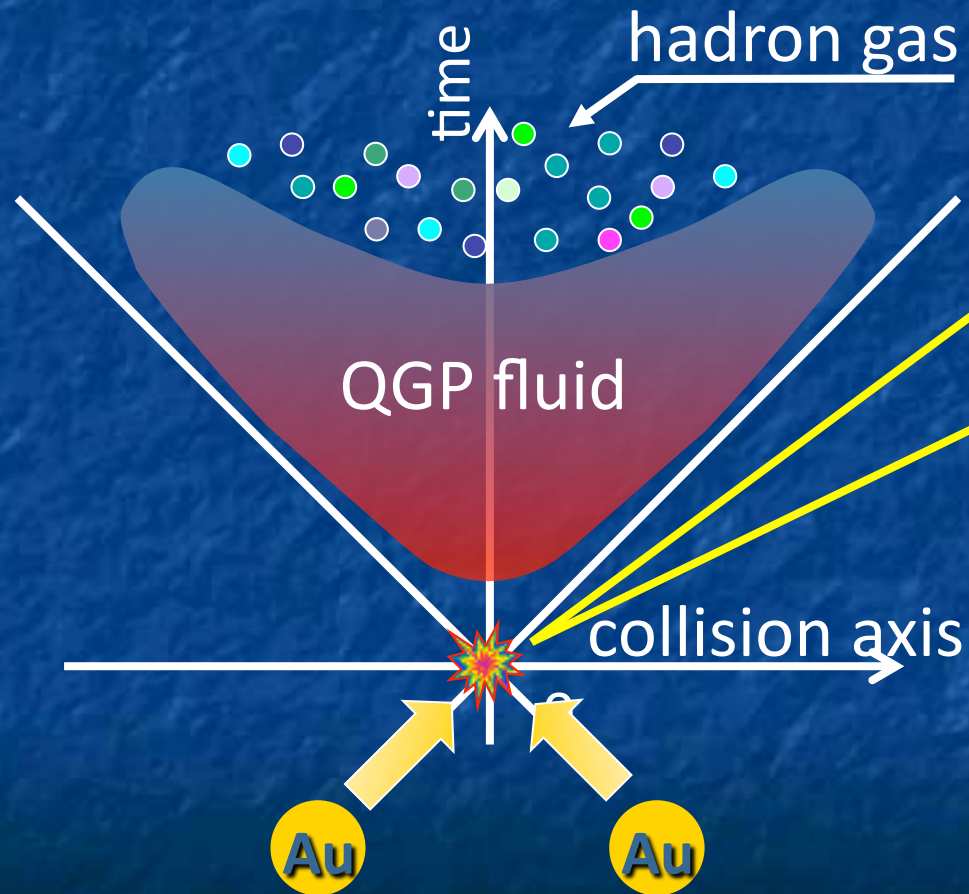


TH et al.,('08)

Model

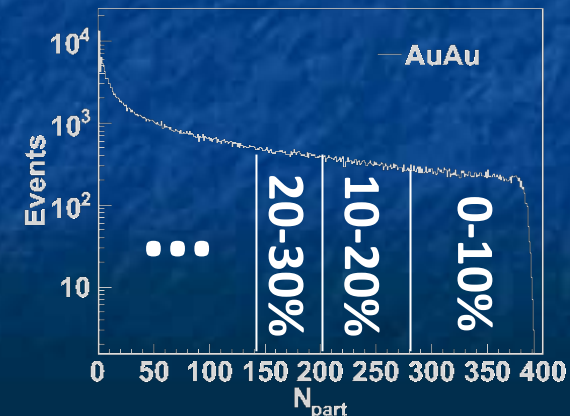
- No single model to understand heavy ion collision as a whole.
- Idea: Employ “cutting edge” modules as far as possible
 - 3D ideal hydro
 - Hadronic transport model, JAM
 - Lattice EoS + resonance gas in JAM 
 - Monte Carlo Glauber/KLN for initial condition 

A Hybrid Approach: Initial Condition



Model*

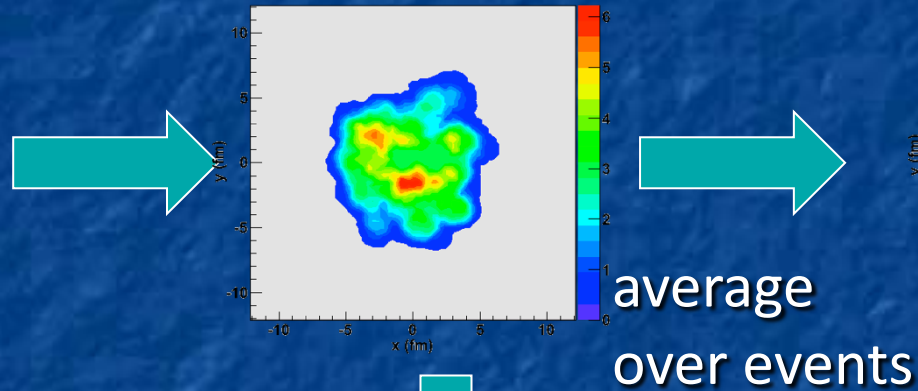
- MC-Glauber
- MC-KLN (CGC)
- $\epsilon_{\text{part}}, \epsilon_{\text{R.P.}}$
- Centrality cut



*H.J.Drescher and Y.Nara (2007)

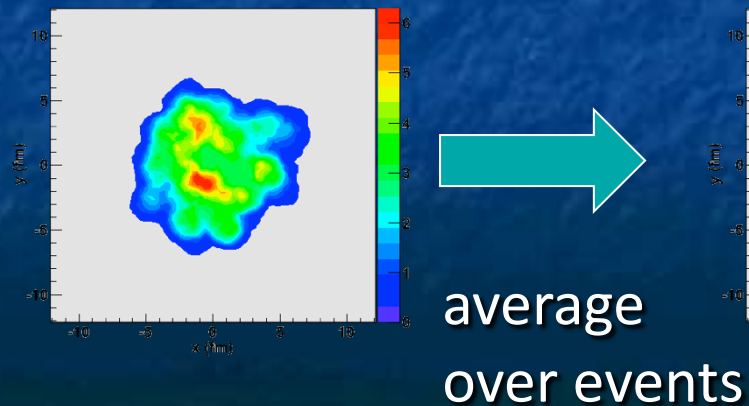
Initial Condition w.r.t. Participant Plane

Throw a dice
to choose b
and calculate
 N_{part}

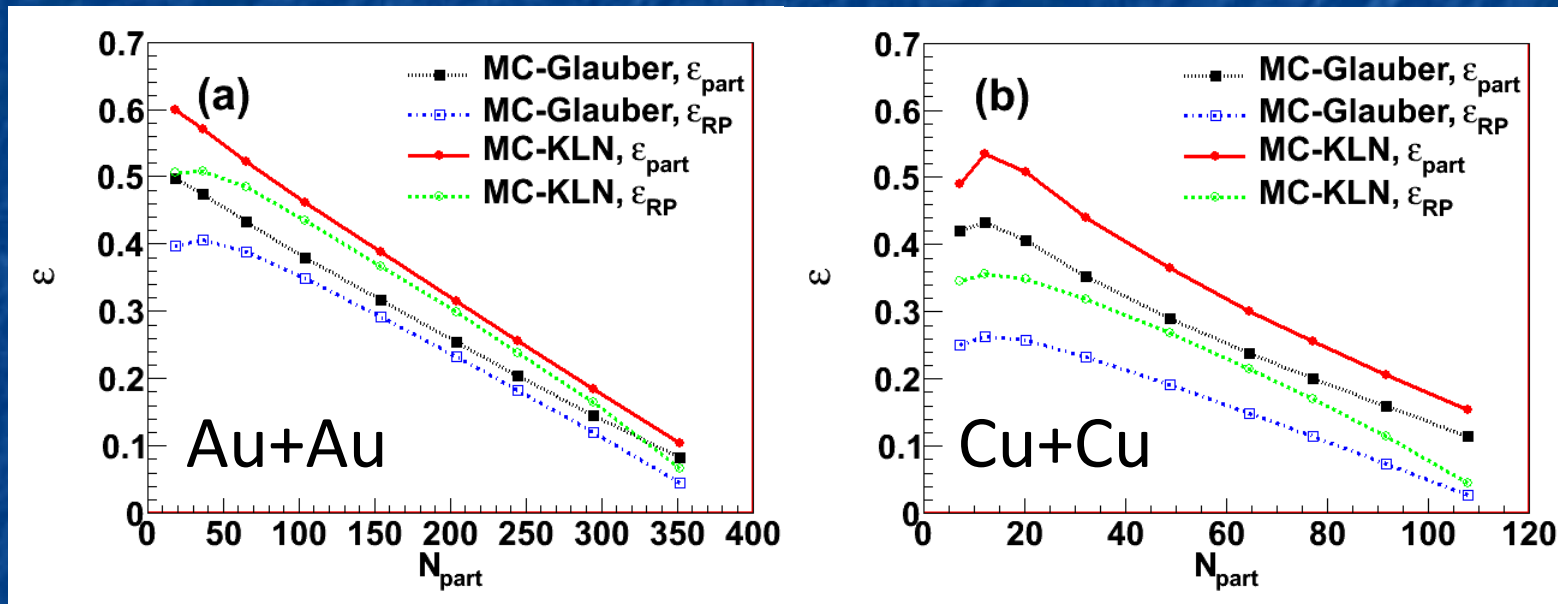


Shift: $\langle x \rangle, \langle y \rangle$
Rotation: Ψ

E.g.)
 $N_{\text{part}}^{\text{min}} = 279$
 $N_{\text{part}}^{\text{max}} = 394$
in Au+Au collisions
at 0-10% centrality



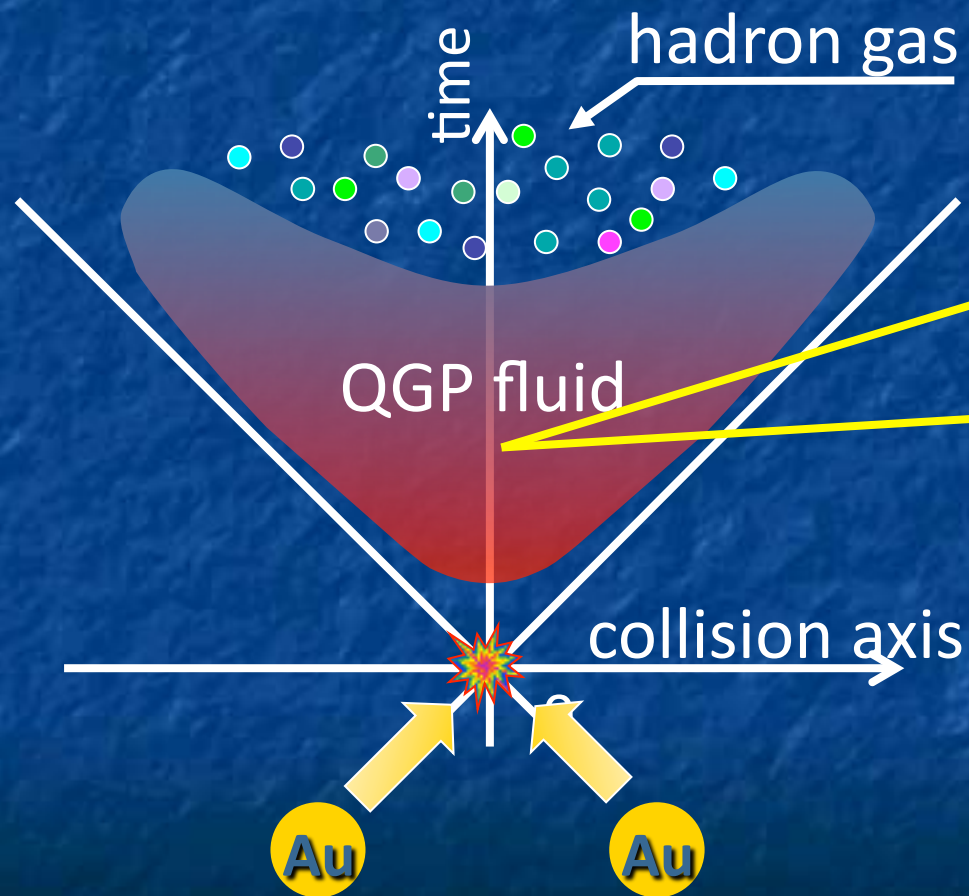
$\varepsilon_{\text{part}}$ and $\varepsilon_{\text{R.P.}}$



- Eccentricity enhanced due to fluctuation
- Significant in small system, e.g., Cu+Cu, peripheral Au+Au
- MC-KLN > MC-Glauber *

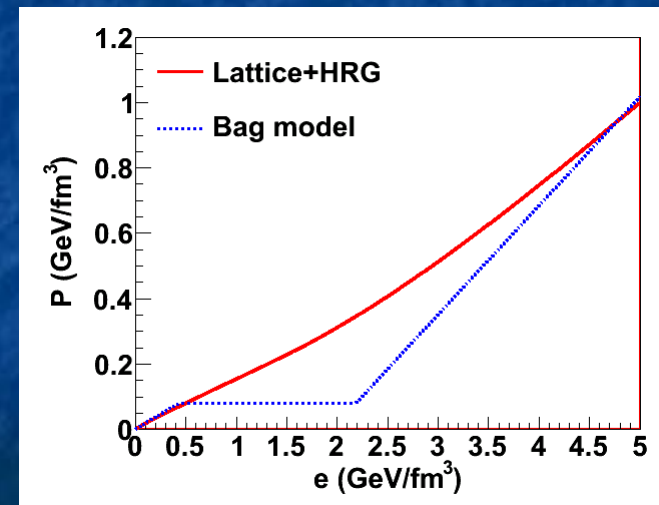
*See, Drescher and Nara, PRC 75, 034905 (2007).

A Hybrid Approach: Hydrodynamics



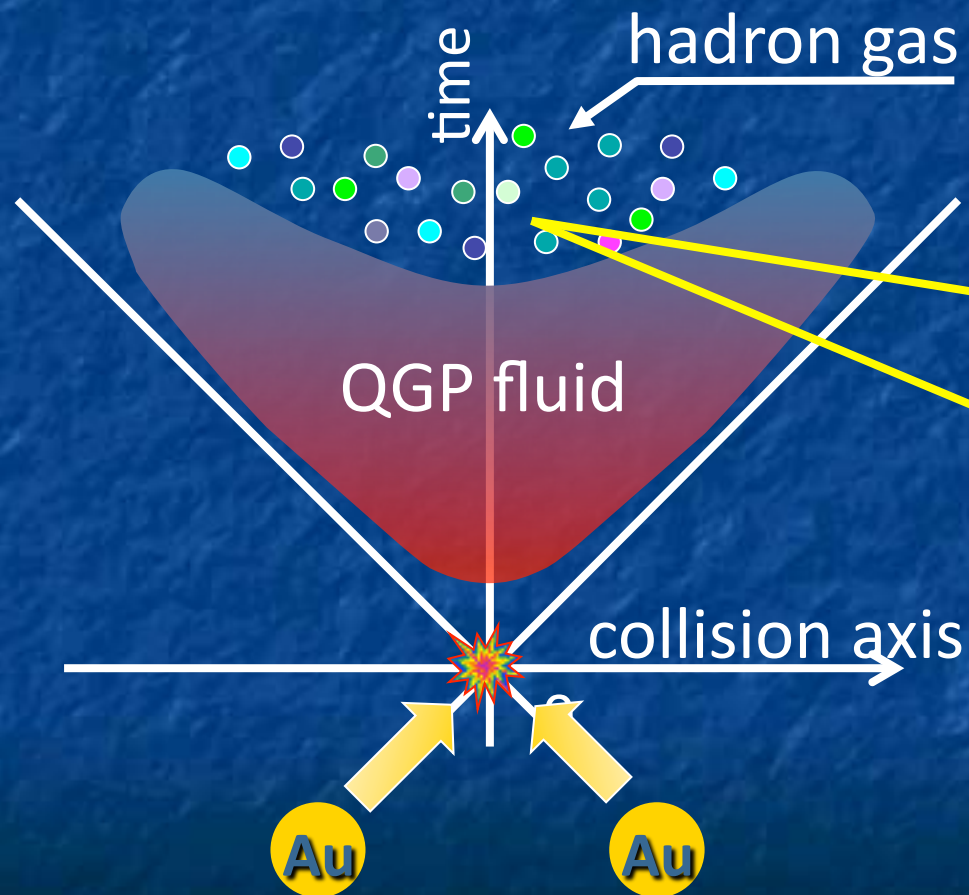
Ideal Hydrodynamics[#]

- Initial time 0.6 fm/c
- Lattice + HRG EoS*



[#]Hirano (2002), ^{*}Huovinen and Petreczky (2010) + JAM HRG

A Hybrid Approach: Hadronic Cascade



Interface

- Cooper-Frye formula at switching temperature $T_{sw} = 155 \text{ MeV}$

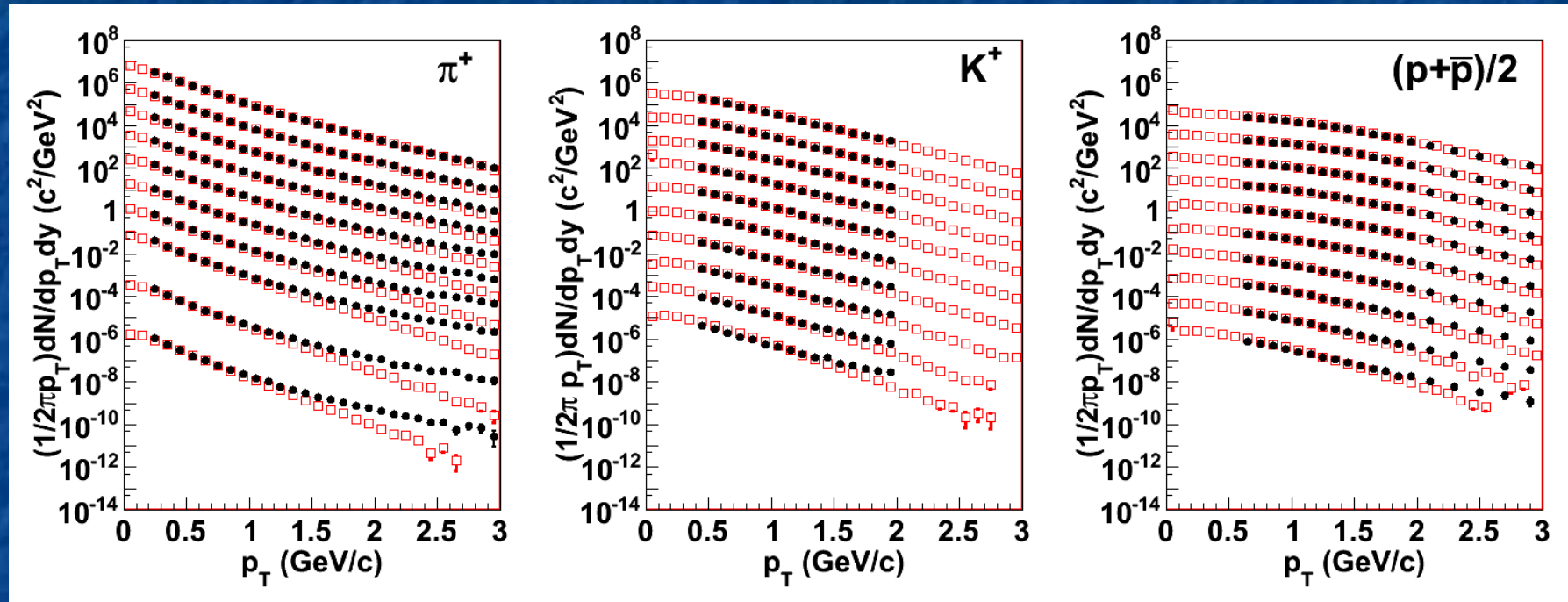
Hadronic afterburner

- Hadronic transport model based on kinetic theory \rightarrow JAM*

Comparison of Hydro+Cascade Results with Available Data

Filled: PHENIX, PRC69, 034909 (2004), Open: Hydro+cascade
 From top to bottom, 0-5, 5-10, 10-15, ..., 70-80% centrality

p_T Spectra: MC-Glauber

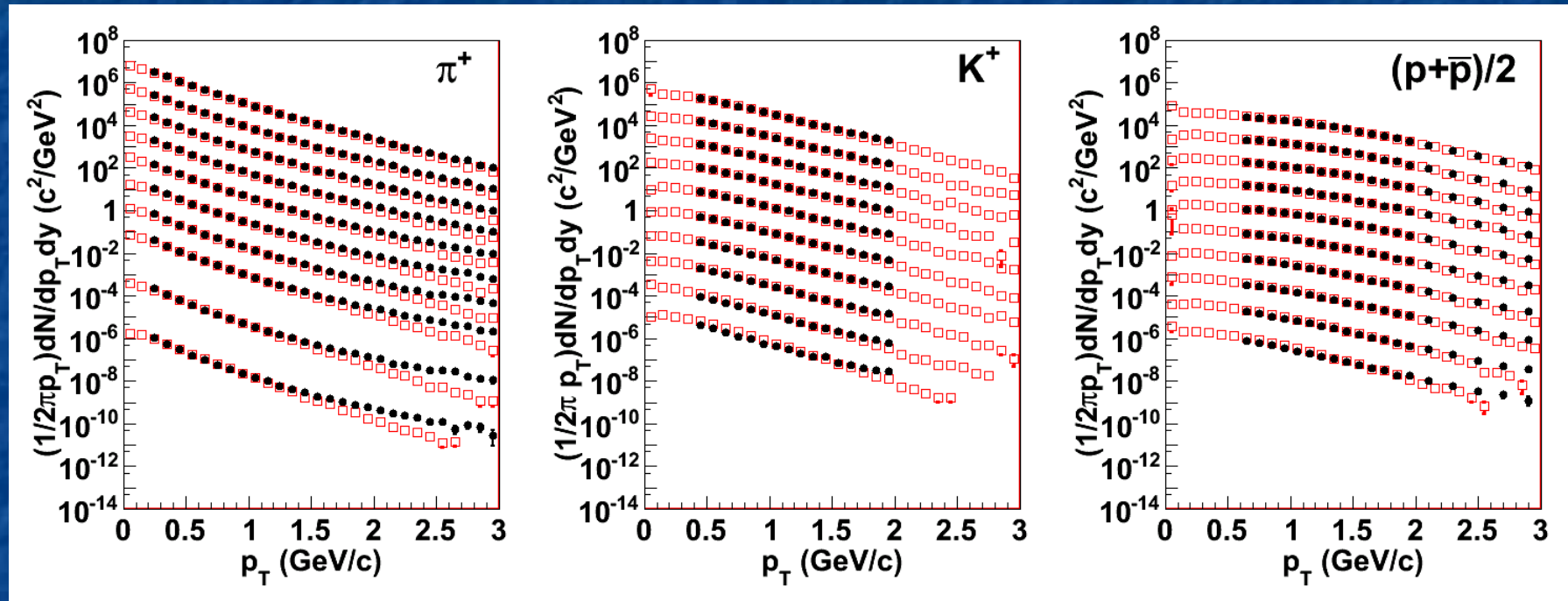


(1) Absolute value of entropy, (2) soft/hard fraction $\alpha = 0.18$, and (3) switching temperature $T_{sw} = 155 \text{ MeV}$.

$$\frac{dS}{d^2 x_{\perp}} \propto \left[\frac{1 - \alpha}{2} \frac{dN_{\text{part}}}{d^2 x_{\perp}} + \alpha \frac{dN_{\text{coll}}}{d^2 x_{\perp}} \right]$$

Filled: PHENIX, PRC69, 034909 (2004), Open: Hydro+cascade
 From top to bottom, 0-5, 5-10, 10-15, ..., 70-80% centrality

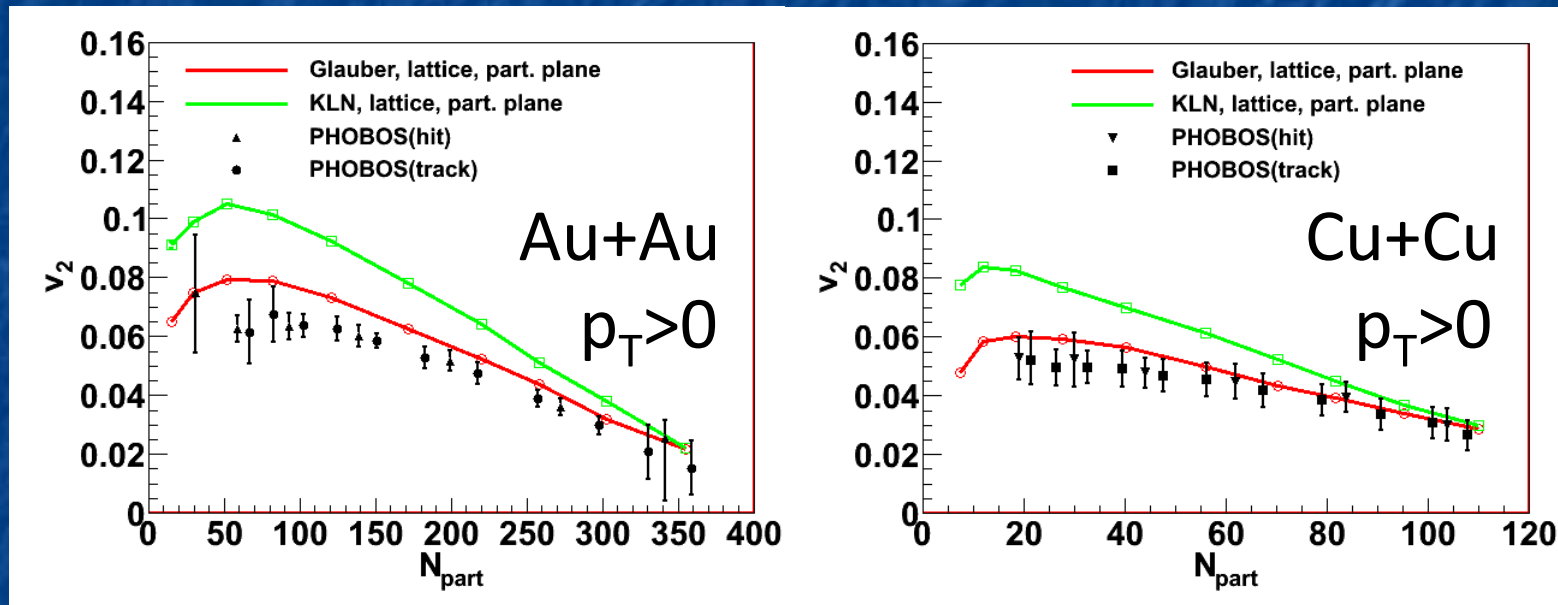
p_T Spectra: MC-KLN



(1) Absolute value of saturation scale and (2) scaling parameters $\lambda=0.28$ and (3) switching temperature $T_{\text{sw}} = 155 \text{ MeV}$

$$Q_{s,A}^2(x_\perp) \propto t_A(x_\perp) x^{-\lambda}$$

$$v_2(N_{\text{part}})$$



MC-Glauber:

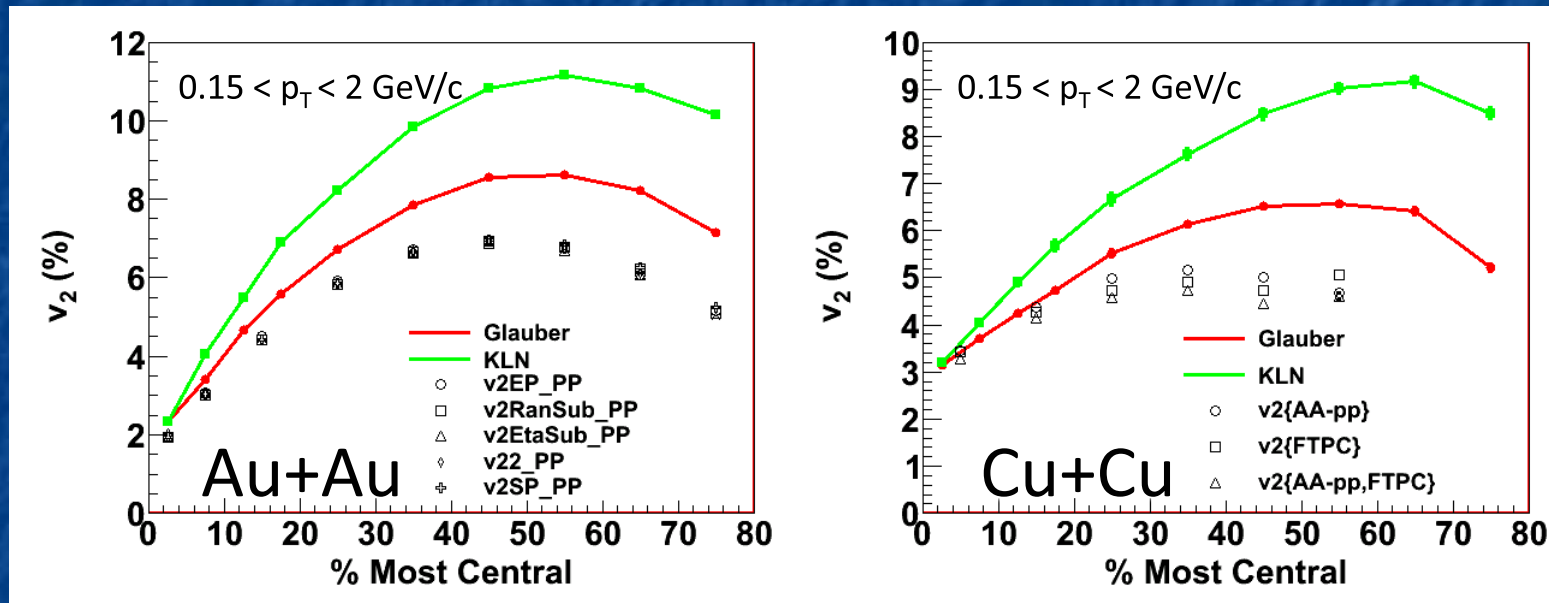
Apparent reproduction. No room for QGP viscosity?

MC-KLN:

Overshoot due to larger eccentricity. How small QGP viscosity?

PHOBOS, PRC72, 051901 (2005); PRL98, 242302 (2007).

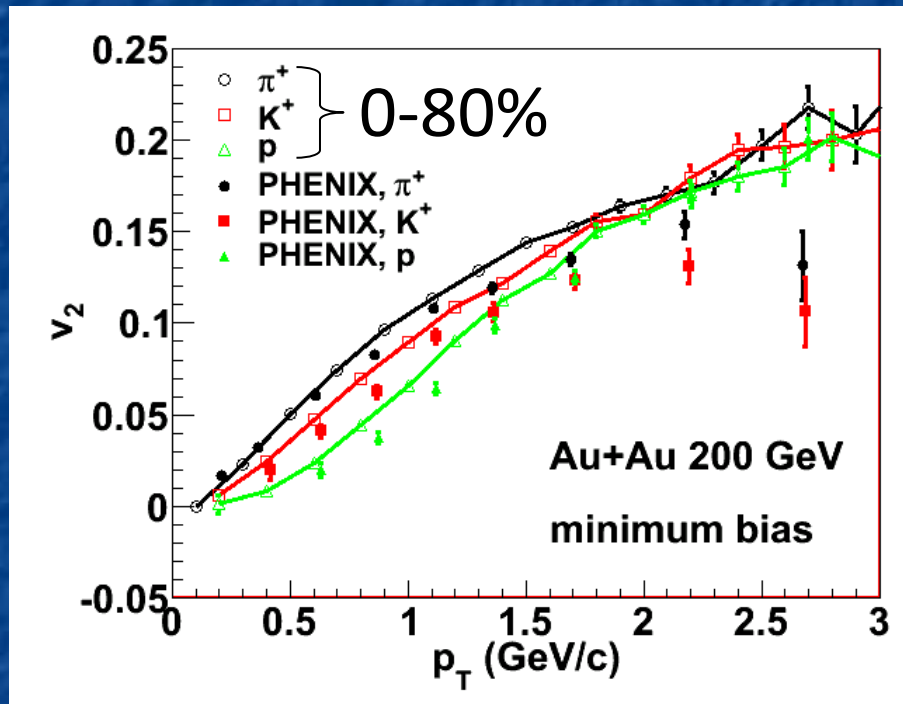
$v_2(\text{centrality})$



- p_T cut enhances v_2 by $\sim 10\%$
- STAR data in Au+Au corrected by Ollitrault et al.*
- v_2 w.r.t. participant plane

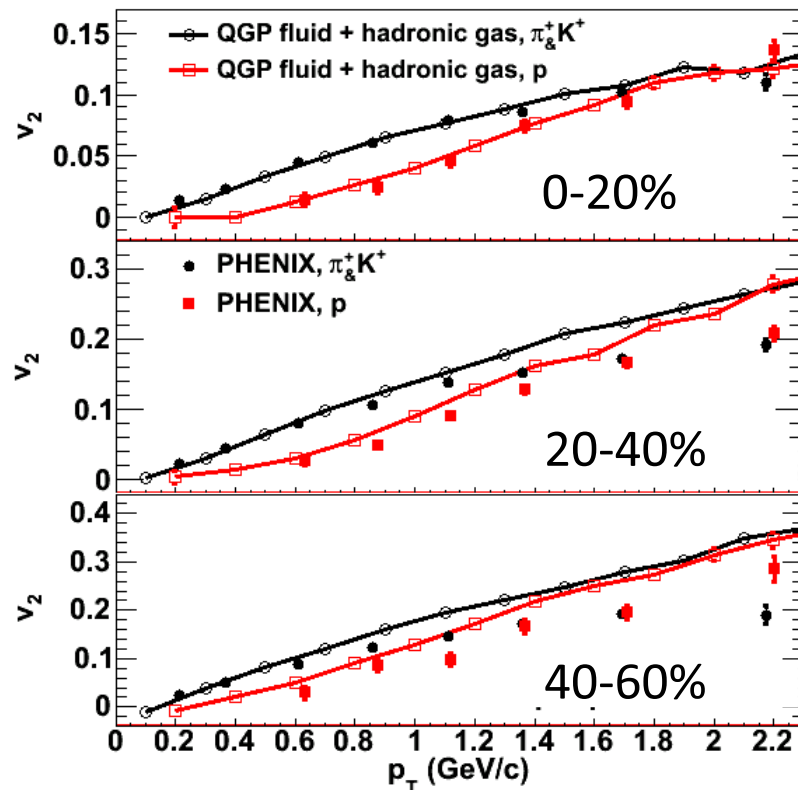
*J.Y.Ollitrault, A.M.Poskanzer and S.A.Voloshin, PRC80, 014904 (2009).

$v_2(p_T)$ for PID Particles



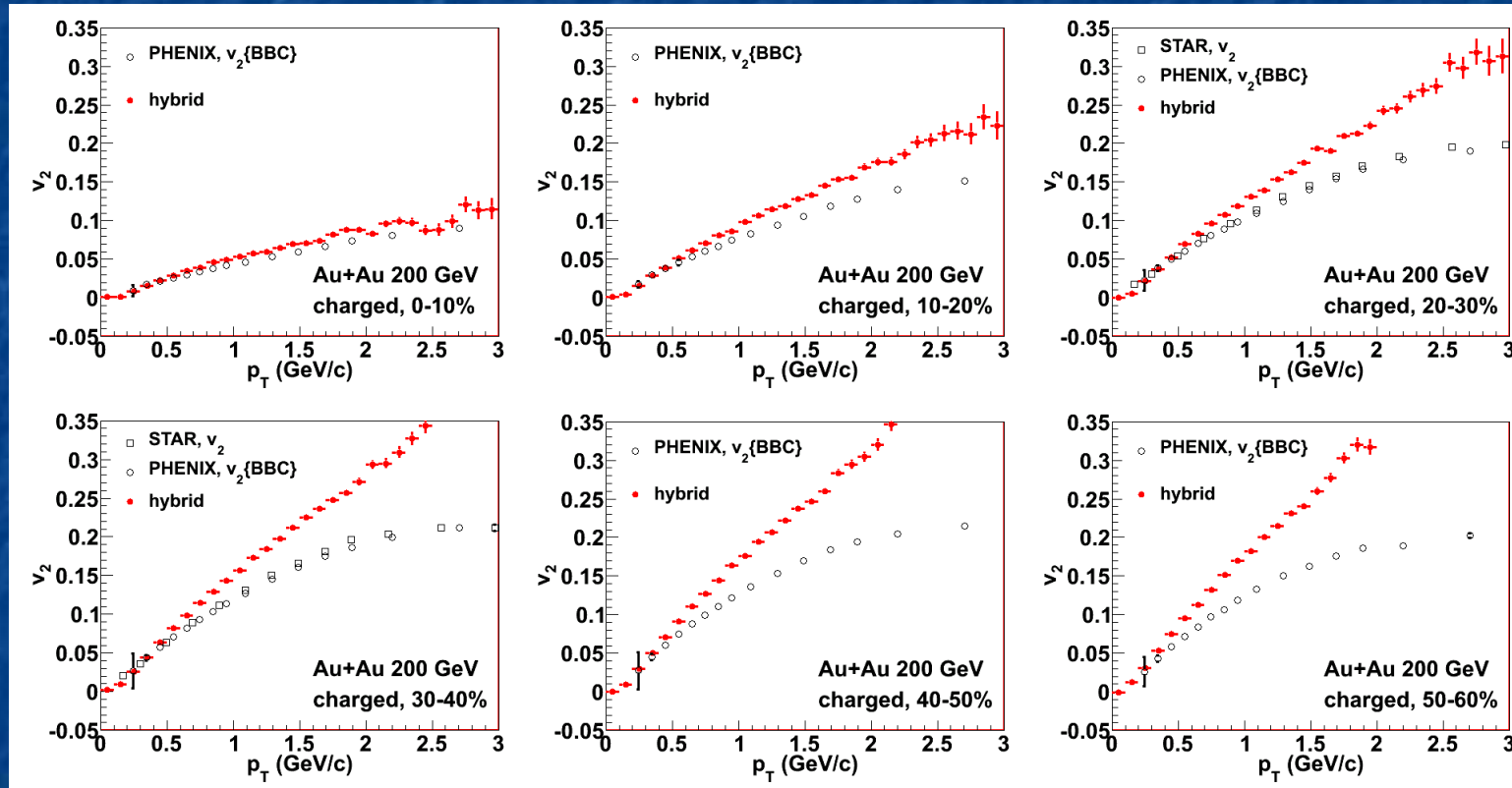
- Results based on MC-Glauber initialization
- Mass splitting pattern OK
- A little bit overshoot even in low p_T region
→ Centrality dependence (next slide)?

$v_2(p_T)$ for PID Particles: Centrality Dependence



- Hydro+cascade with MC-Glauber at work in 0-20% centrality
- Need QGP viscosity
- Or, need jet or recombination/coalescence components?
- MC-KLN results not available yet due to less statistics

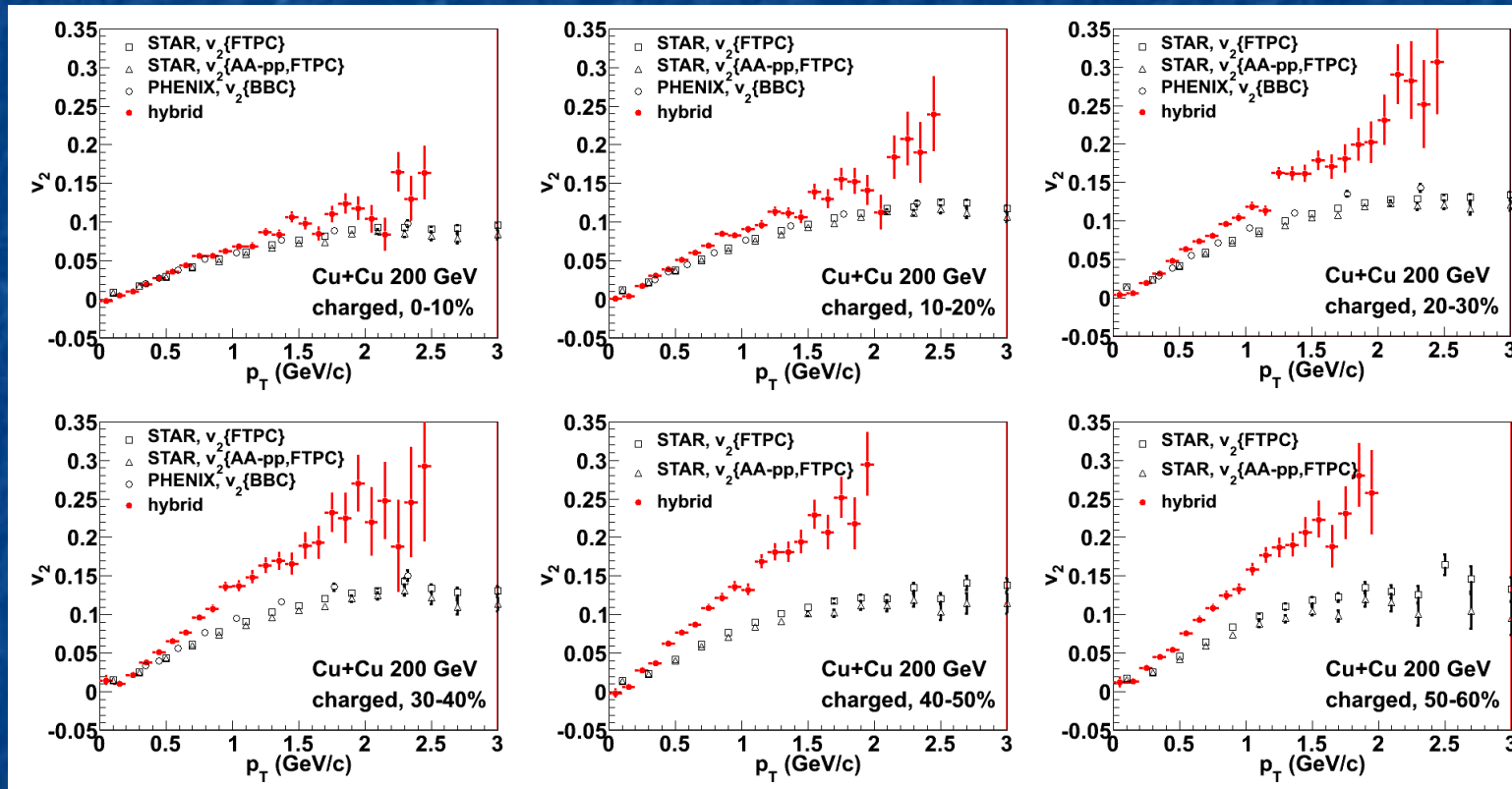
$v_2(p_T)$ for Charged Particles: Au+Au



- Hydro+cascade with MC-Glauber at work in low p_T
 - p_T region at work shrinks as moving to peripheral
- Importance of viscosity

PHENIX, PRC80, 024909 (2009).
STAR, PRC72, 014904 (2005).

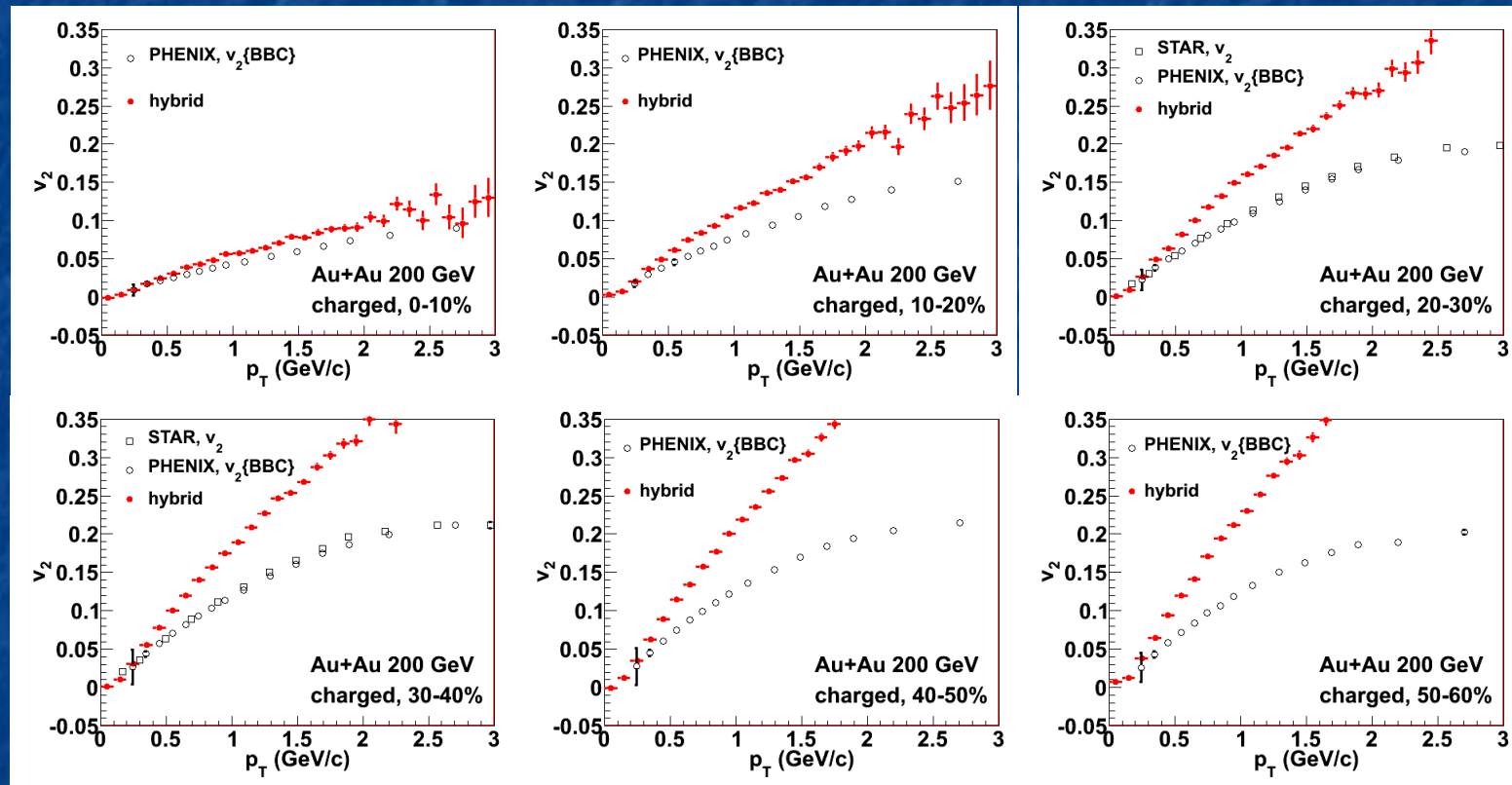
$v_2(p_T)$ for Charged Particles: Cu+Cu



- Tendency is the same as that in Au+Au collisions

PHENIX, PRL98, 162301 (2007).
STAR, PRC81, 044902 (2010).

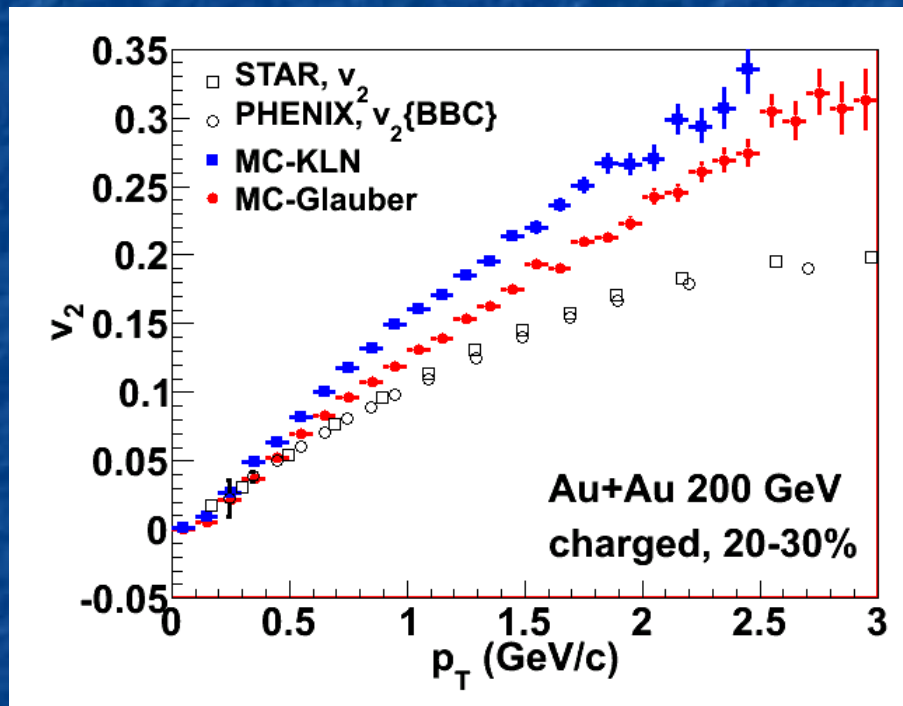
$v_2(p_T)$ for Charged Particles: Au+Au



- Hydro+cascade with MC-KLN at work in central collisions

PHENIX, PRC80, 024909 (2009).
STAR, PRC72, 014904 (2005).

MC-KLN vs. MC-Glauber



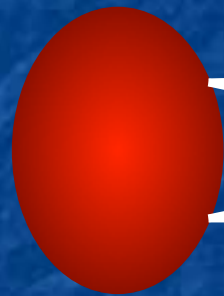
Slope of $v_2(p_T)$
steeper in MC-KLN
than in MC-Glauber

$$\leftarrow v_{2,\text{MC-KLN}} > v_{2,\text{MC-Glauber}}$$

- p_T dependent viscous correction at $T=T_{\text{sw}}$ might interpret the data
- Extracted transport coefficients depend on initial condition

Conventional Femtoscopic Analysis

Particle source

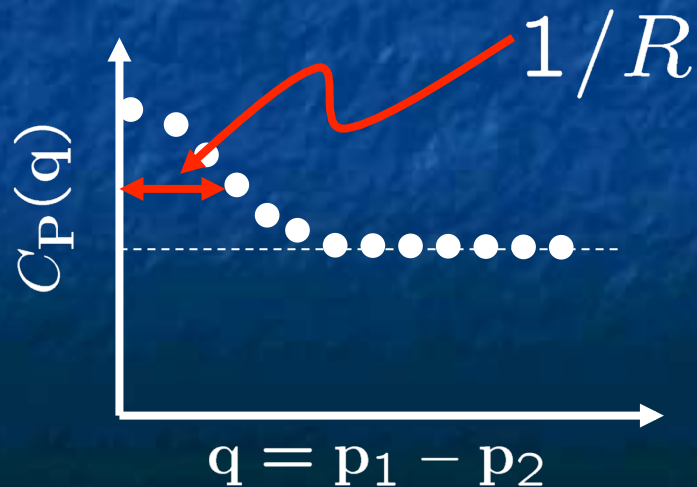


Detector 1

Detector 2

Hanbury Brown – Twiss (1956)

Goldhaber – Goldhaber – Lee – Pais (1960)



Source size of
particle emission R
(Homogeneity region)
→ Information in
configuration space



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Tuesday, July 20, 2010

In The News

Science Program for Underprivileged Students at JBEI



***In Memoriam:* Renowned Berkeley Lab Physicist Gerson Goldhaber**



Gerson Goldhaber, an award-winning physicist with Berkeley Lab's Physics Division and UC Berkeley Professor of Physics Emeritus, passed away Monday morning (July 19) of natural causes, at home surrounded by his family. He was 86. Goldhaber played key roles in discoveries that spanned more than five decades and included both particle physics and astrophysics. He is survived by his wife, Judith, a long-time science writer for Berkeley Lab, son Nathaniel, daughters Michaela and Shaya, daughter-in-law Marilyn, and three grandsons, Ben, Charles and Sam. A detailed obituary will be posted by the Lab soon.

New Technique: Source Imaging

Source function and emission rate:

$$\mathcal{D}_P(r') = \int dt' \int d^4 R \mathcal{S}_1(x_1, p_1) \mathcal{S}_2(x_2, p_2)$$

$$x_1 = R + r/2, \quad x_2 = R - r/2$$

$$\mathcal{S}(x, p) = \frac{Ed^7 N}{d^4 x d^3 p} \bigg/ \frac{Ed^3 N}{d^3 p}$$



Inverse problem

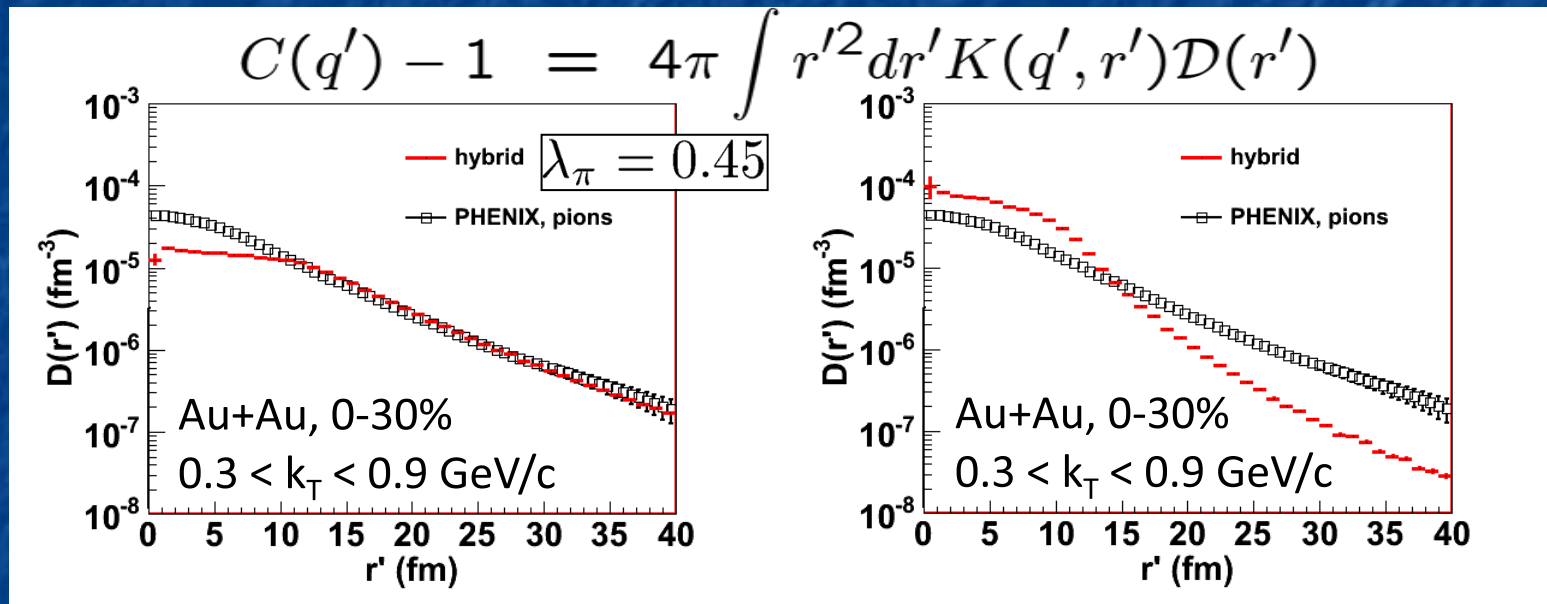
Koonin-Pratt eq.:

$$C_P(q') - 1 = \int d^3 r' K(q', r') \mathcal{D}_P(r')$$

$$P = p_1 + p_2, \quad q = (p_1 - p_2)/2$$

Primed (') variables in Pair Center-of-Mass System

1D Source Function for Pions

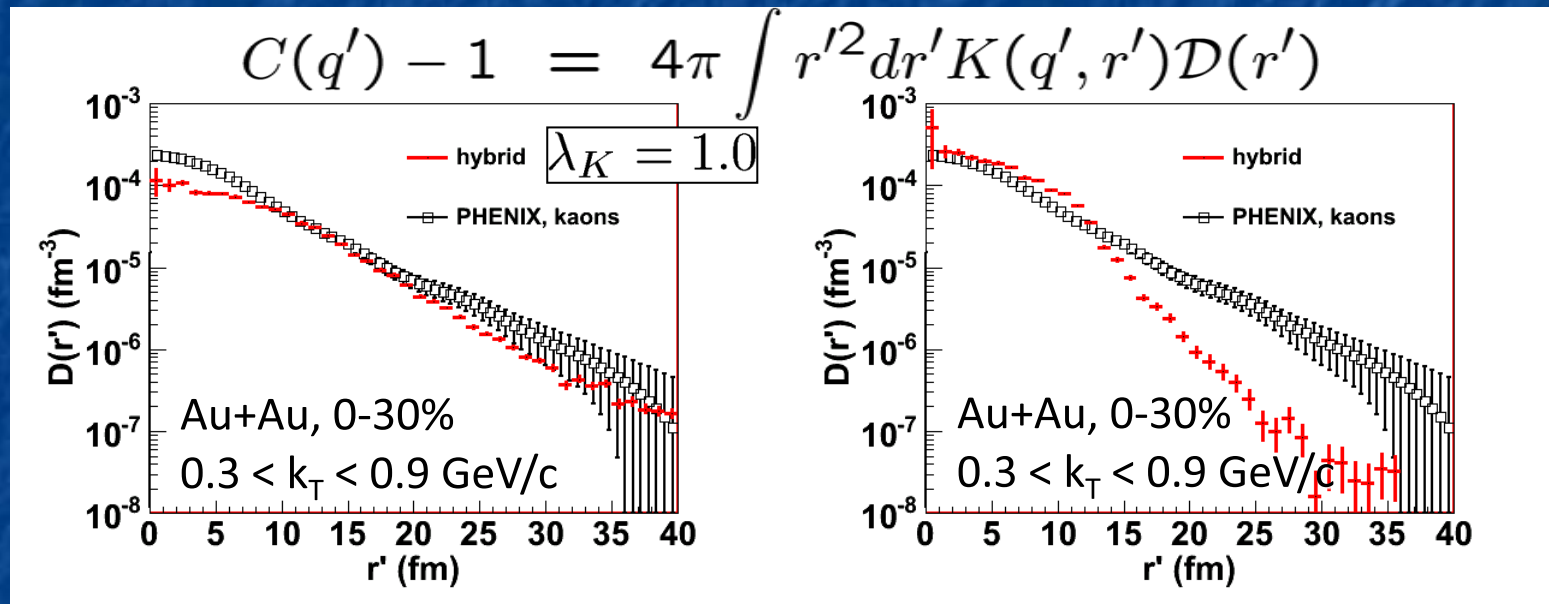


With hadronic
rescattering and decays

Without hadronic
rescattering and decays

Non-Gaussian tail in pion source function
from hybrid model

1D Source Function for Kaons

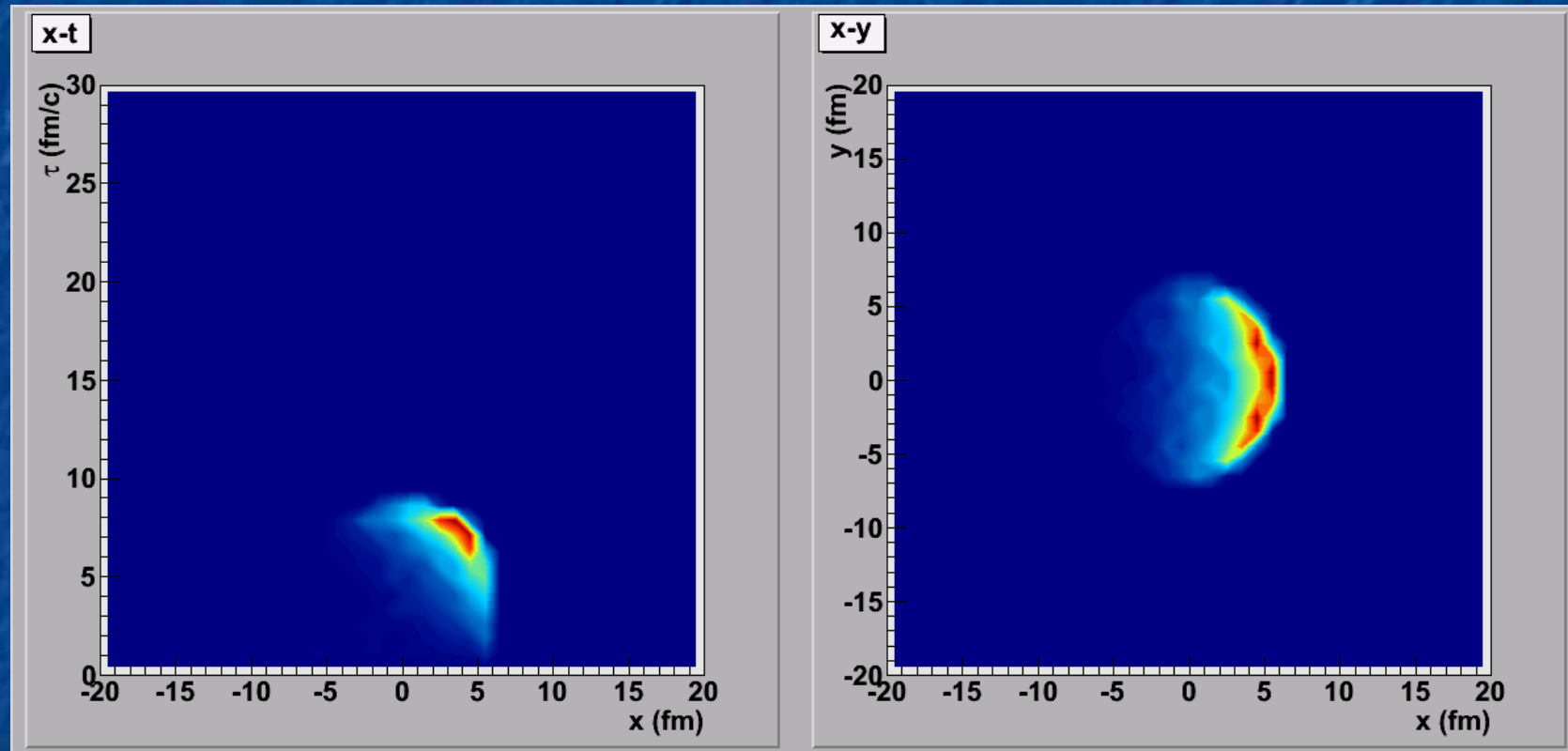


With hadronic
rescattering and decays

Without hadronic
rescattering and decays

Non-Gaussian tail in kaon source function
from hybrid model

Emission Rate for Pions

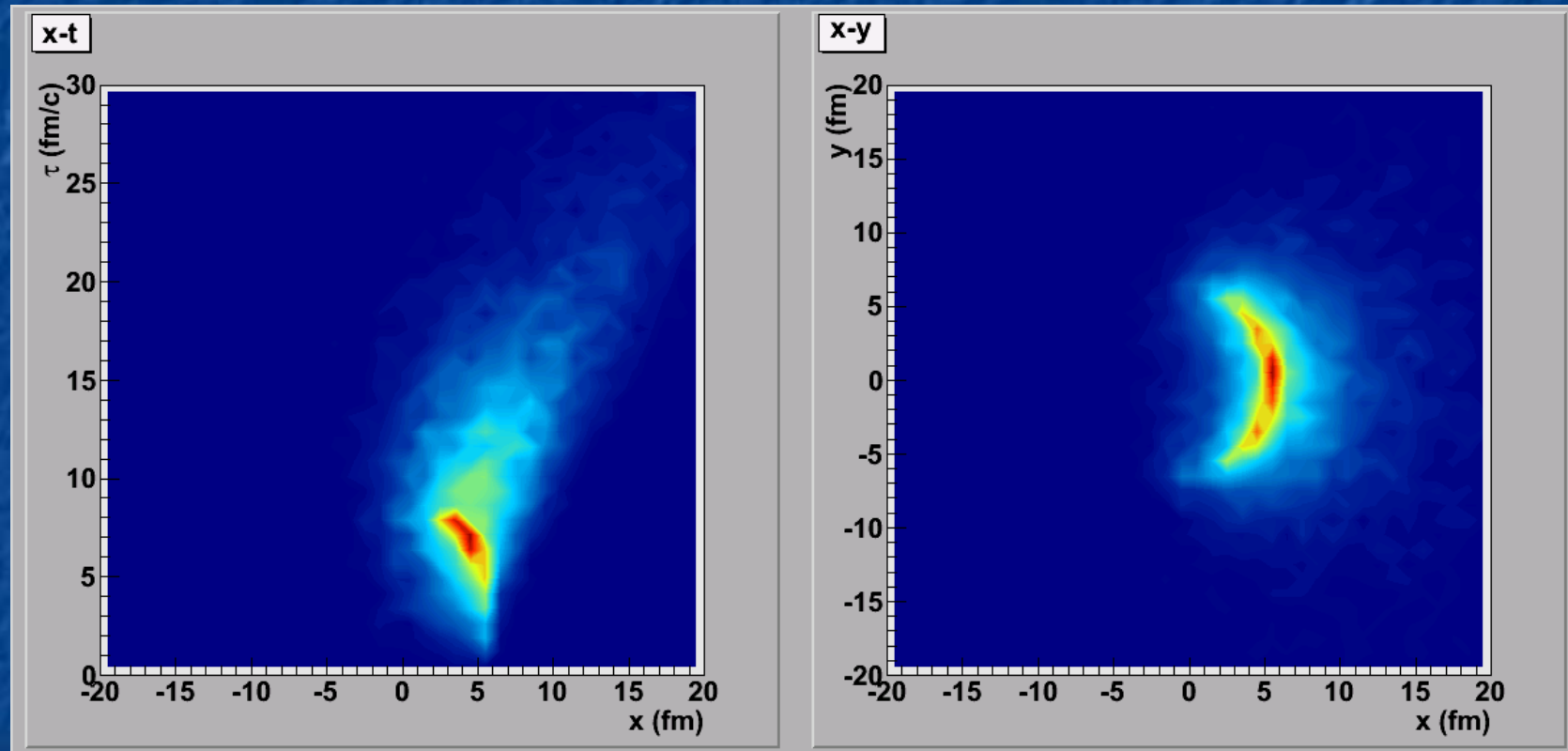


0-30% Au+Au, pions, $0.3 < p_x < 0.9$ GeV/c

Without hadronic rescattering or decays

→ Negative x-t correlation

Emission Rate for Pions

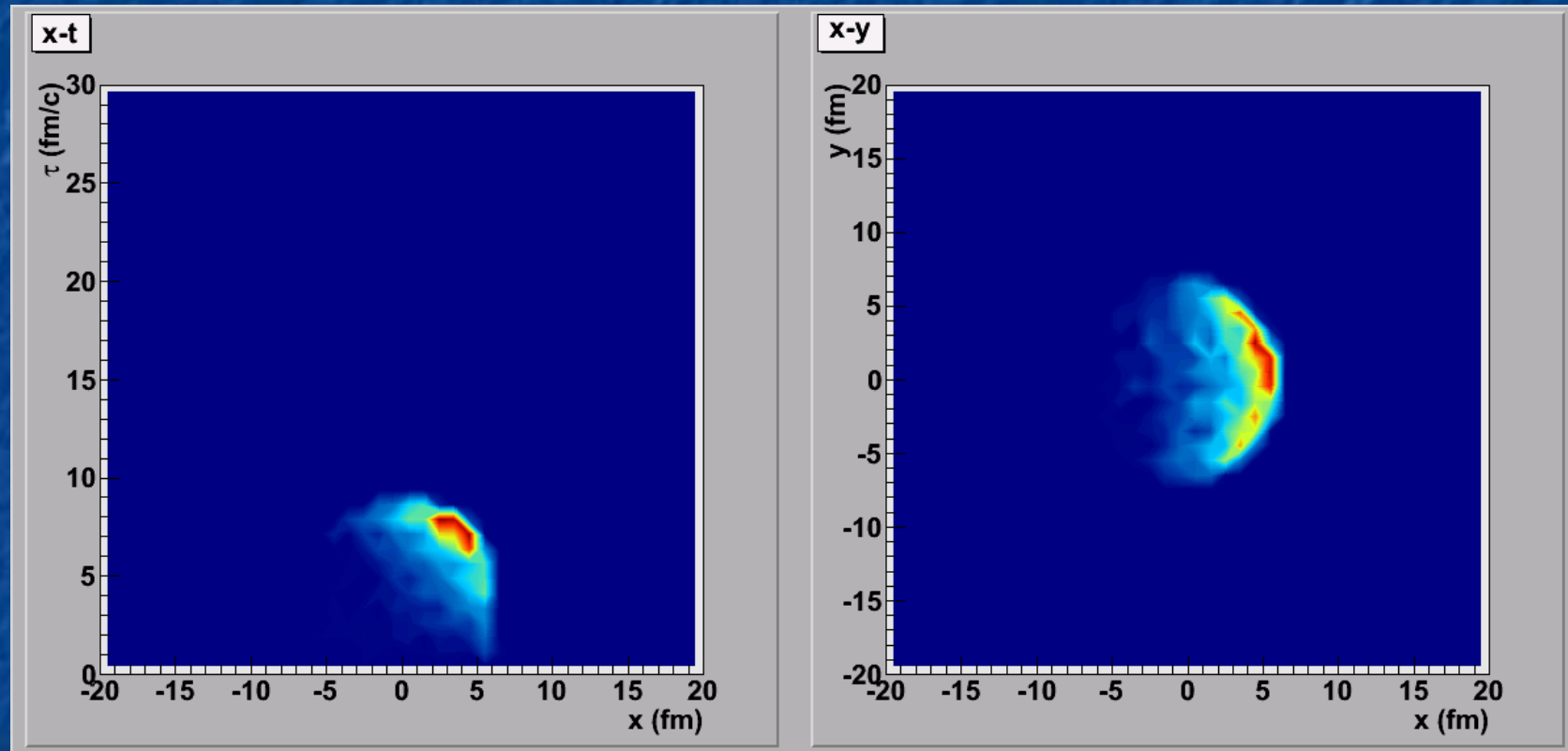


0-30% Au+Au, pions, $0.3 < p_x < 0.9$ GeV/c

With hadronic rescattering and decays

→ Positive x-t correlation(?)

Emission Rate for Kaons

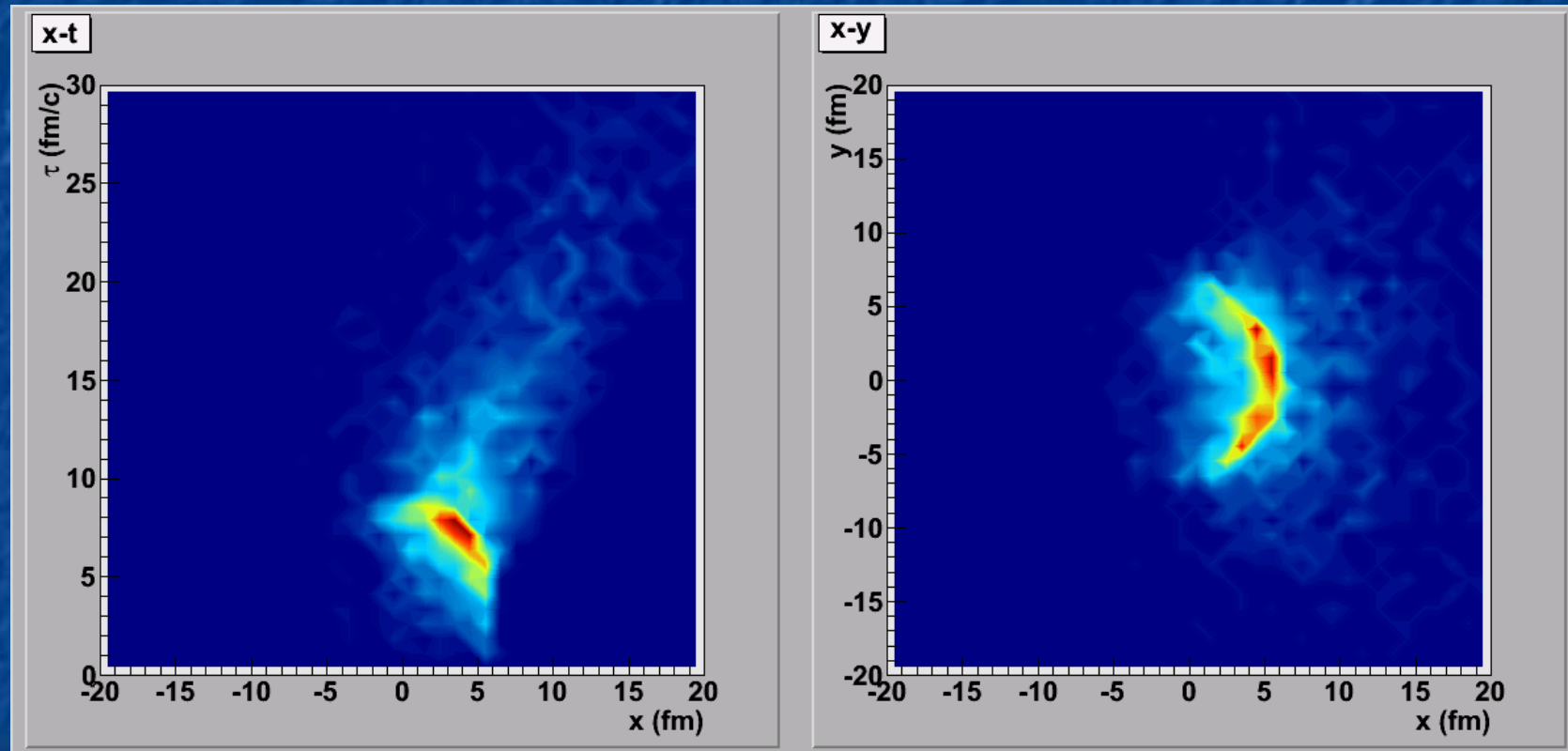


0-30% Au+Au, kaons, $0.3 < p_x < 0.9$ GeV/c

Without hadronic rescattering or decays

→ Negative x-t correlation

Emission Rate for Kaons



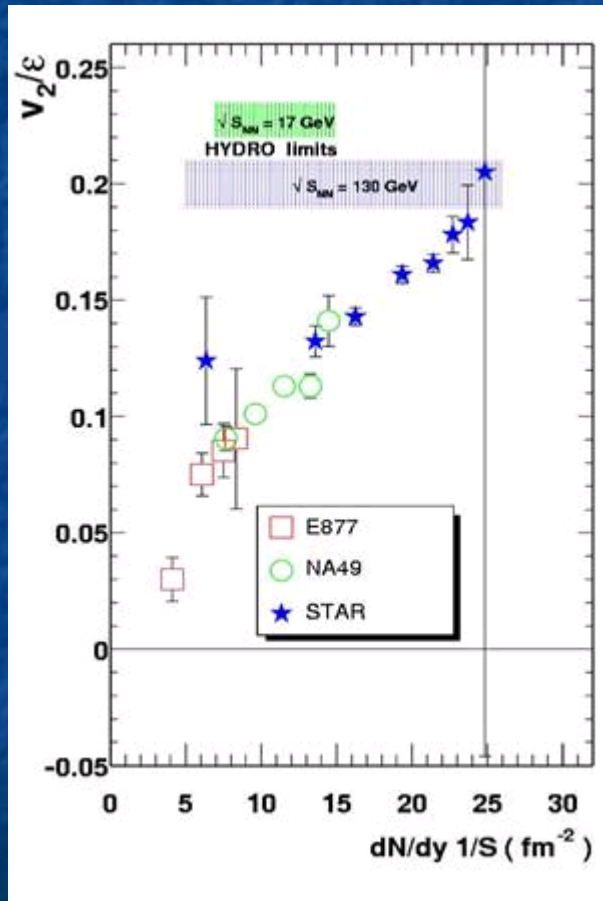
0-30% Au+Au, kaons, $0.3 < p_x < 0.9$ GeV/c

With hadronic rescattering and decays

→ Positive x-t correlation(?)

Predictions and Postdiction from Hydro+Cascade Model

Collisions of Deformed Nuclei at RHIC



STAR, PRC66, 034904 (2002)

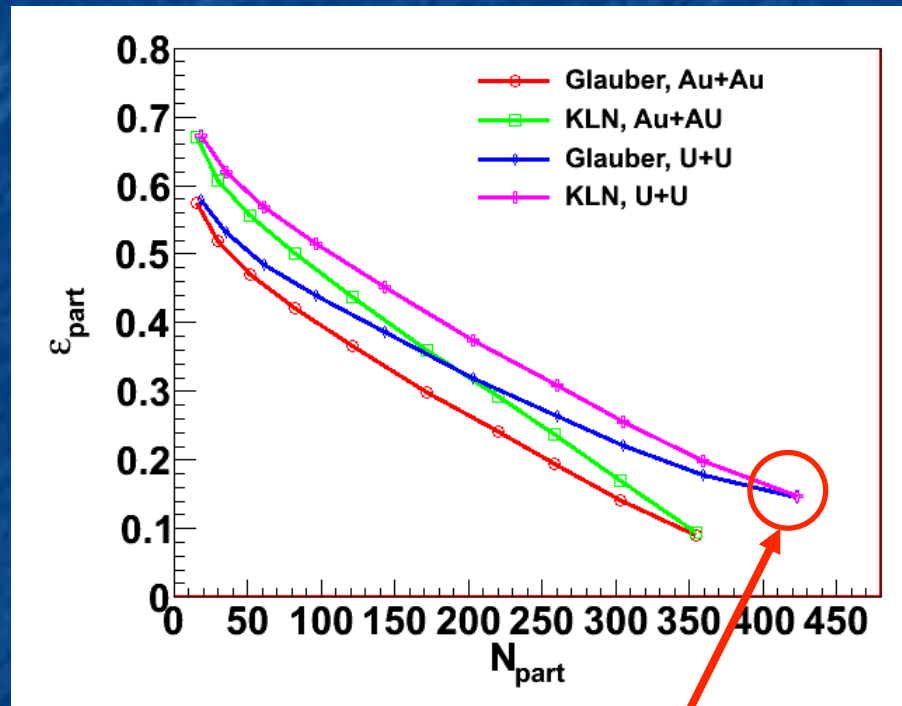
- How v_2/ϵ behaves as increasing multiplicity?*
- Saturate?
- Still enhance?

U+U collision in run12 at RHIC(?)

- More multiplicity
- Larger eccentricity

*U.Heinz and A. Kuhlman, PRL94, 132301 (2005).

Eccentricity in U+U Collisions at RHIC

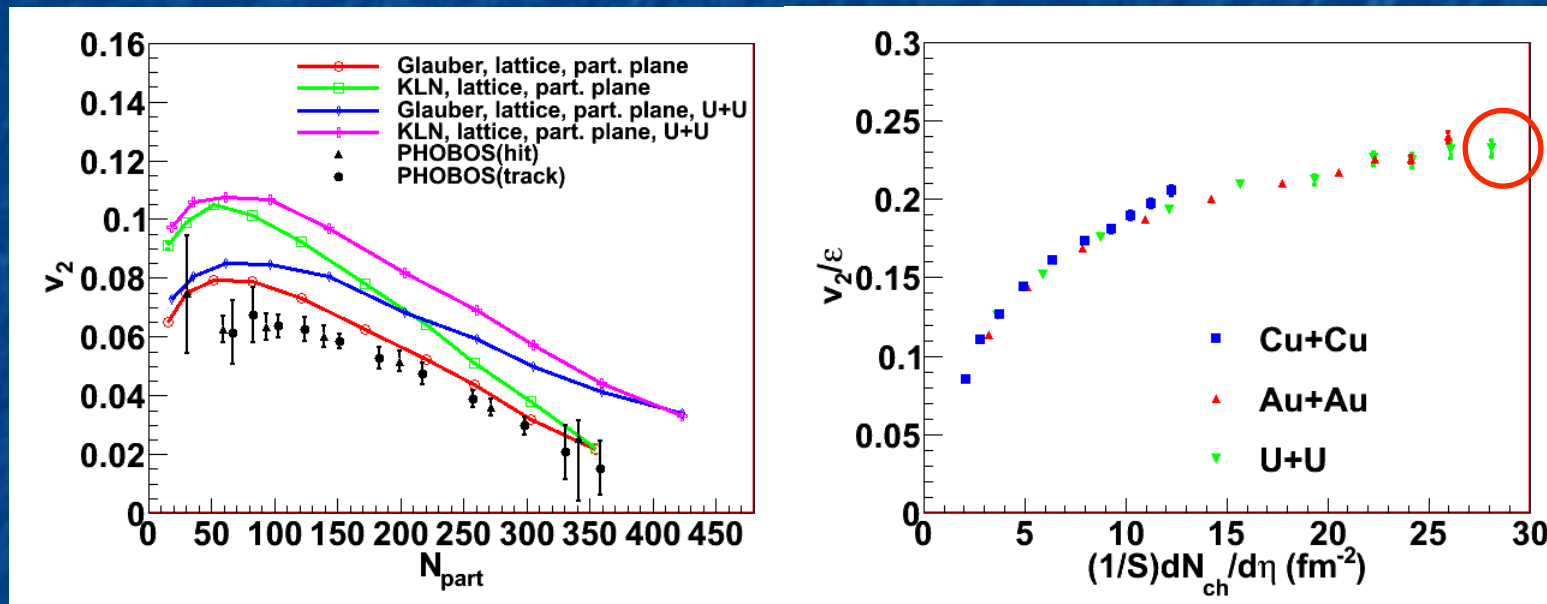


- Larger eccentricity
- Finite eccentricity at zero impact parameter body-body collision
- Unable to control configuration → Need Monte-Carlo study and event selection*

0-5% → 0.146 (MC-Glauber), 0.148 (MC-KLN)

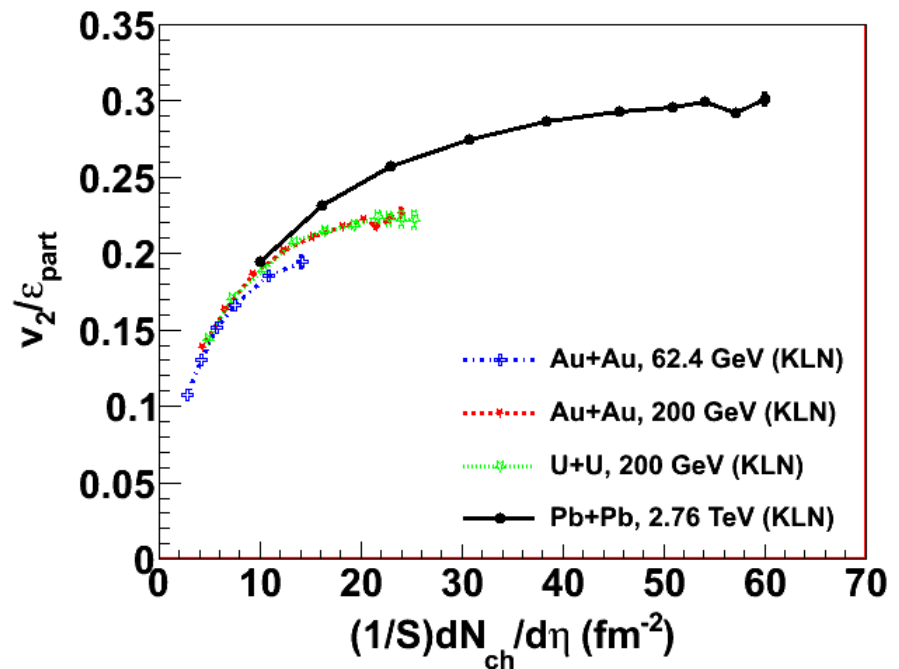
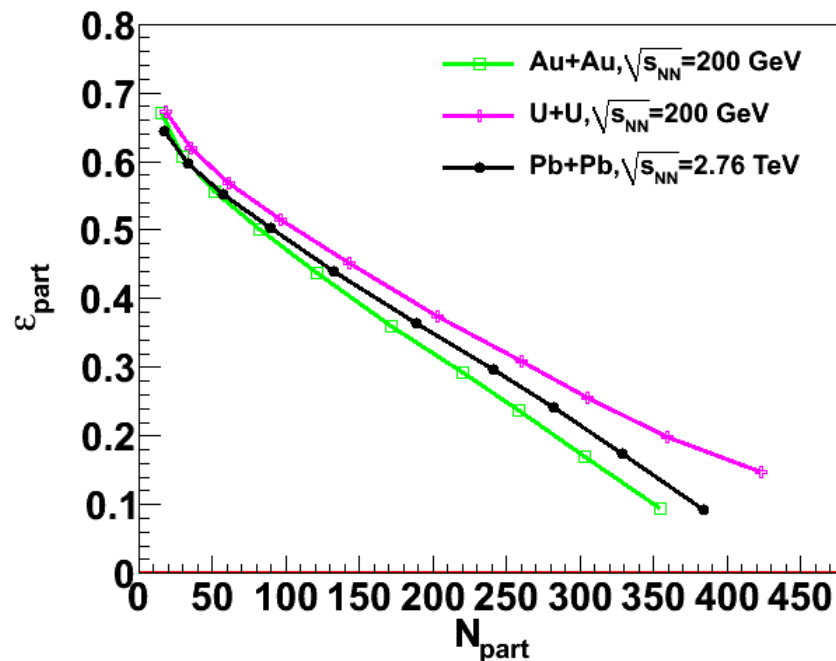
*See, e.g., P.Filip et al. PRC80, 054903 (2009).

v_2 in U+U Collisions



- v_2 increases due to deformation of colliding nuclei.
- v_2/ϵ scales with transverse density.
- Maximum transverse density increases only by $\sim 10\%$ in central U+U collisions.

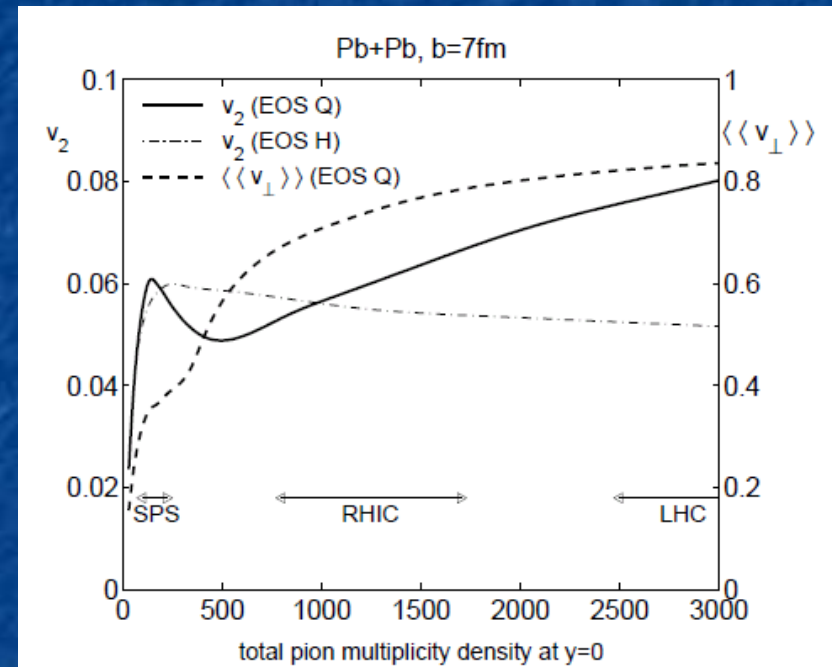
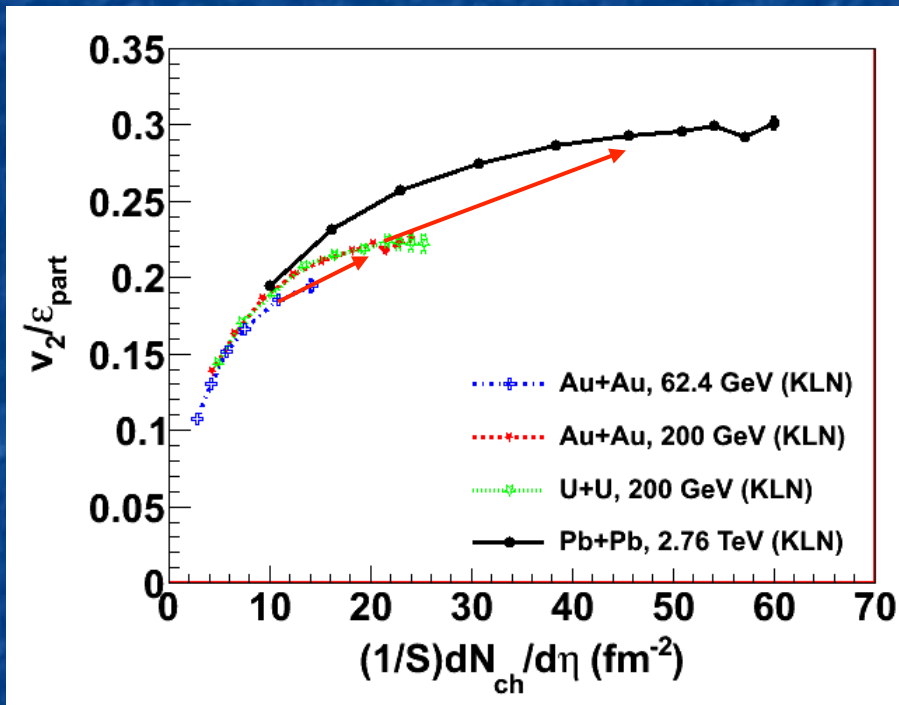
Prediction at LHC



Eccentricity does not
change from RHIC to LHC!
Change due solely to size

v_2/ϵ does not follow
RHIC scaling curve

v_2/ε Scales at Fixed Collision Energy




Pick up points
with fixed centrality



Increase multiplicity
with fixed centrality.

The First Heavy Ion Data at LHC

PRL 105, 252302 (2010)

 Selected for a Viewpoint in *Physics*
PHYSICAL REVIEW LETTERS

week ending
17 DECEMBER 2010



Elliptic Flow of Charged Particles in Pb-Pb Collisions at $\sqrt{s_{NN}} = 2.76$ TeV

K. Aamodt *et al.**

(ALICE Collaboration)

(Received 18 November 2010; published 13 December 2010)

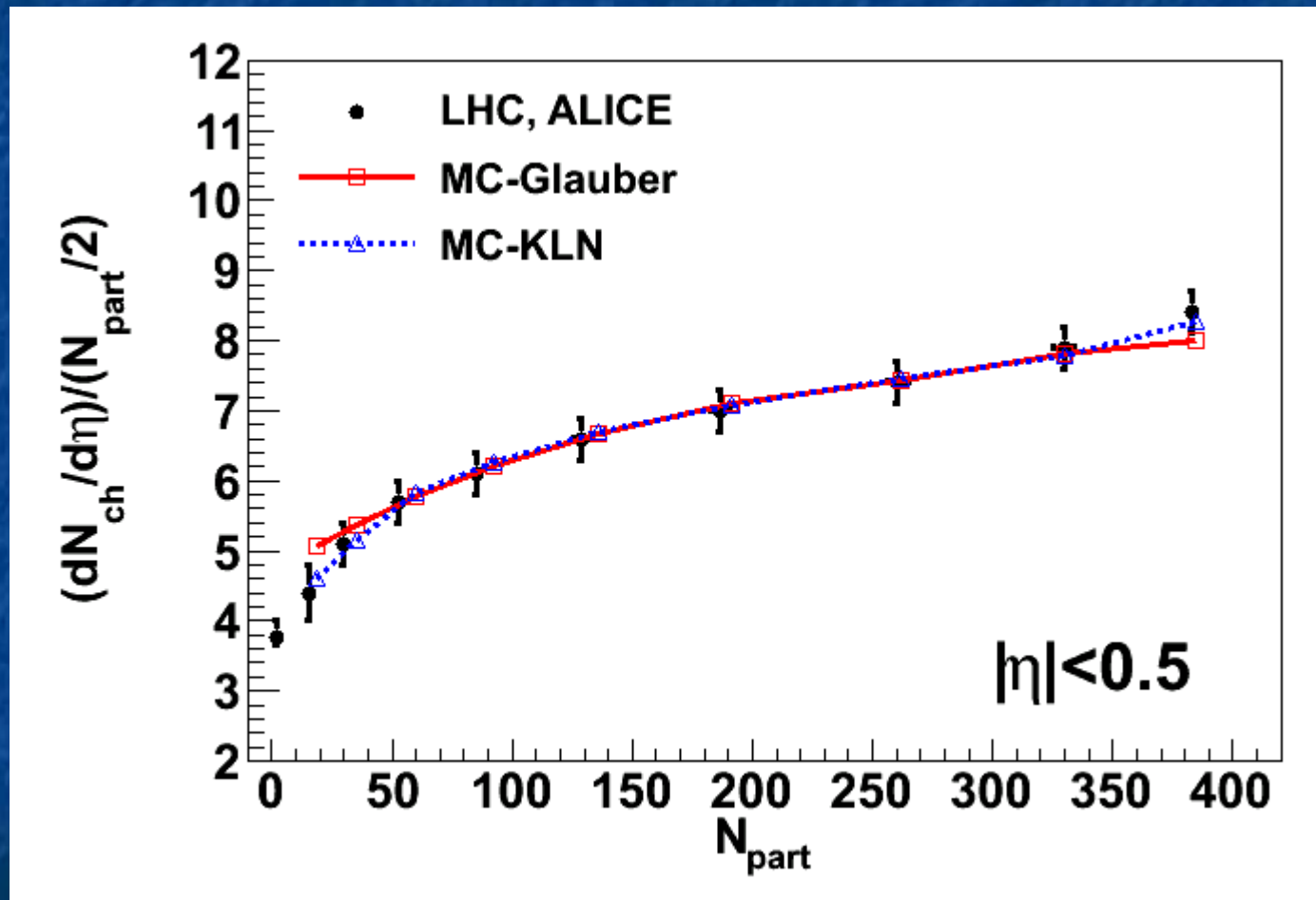
We report the first measurement of charged particle elliptic flow in Pb-Pb collisions at $\sqrt{s_{NN}} = 2.76$ TeV with the ALICE detector at the CERN Large Hadron Collider. The measurement is performed in the central pseudorapidity region ($|\eta| < 0.8$) and transverse momentum range $0.2 < p_t < 5.0$ GeV/ c . The elliptic flow signal v_2 , measured using the 4-particle correlation method, averaged over transverse momentum and pseudorapidity is $0.087 \pm 0.002(\text{stat}) \pm 0.003(\text{syst})$ in the 40%–50% centrality class. The differential elliptic flow $v_2(p_t)$ reaches a maximum of 0.2 near $p_t = 3$ GeV/ c . Compared to RHIC Au-Au collisions at $\sqrt{s_{NN}} = 200$ GeV, the elliptic flow increases by about 30%. Some hydrodynamic model predictions which include viscous corrections are in agreement with the observed increase.

DOI: 10.1103/PhysRevLett.105.252302

PACS numbers: 25.75.Ld, 25.75.Gz, 25.75.Nq

Congrats!!!

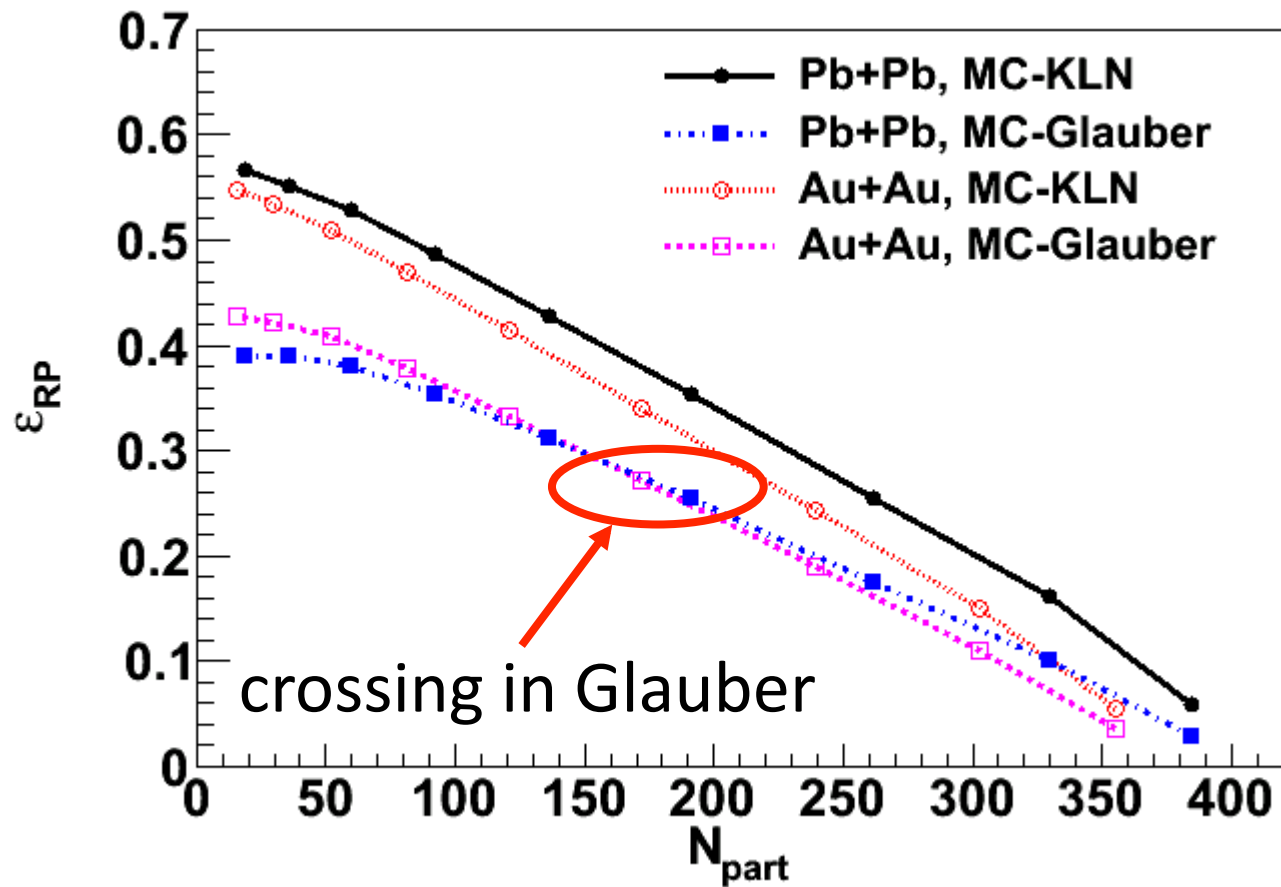
Centrality Dependence of Multiplicity



MC-KLN: Default, MC-Glauber: $\alpha = 0.08$

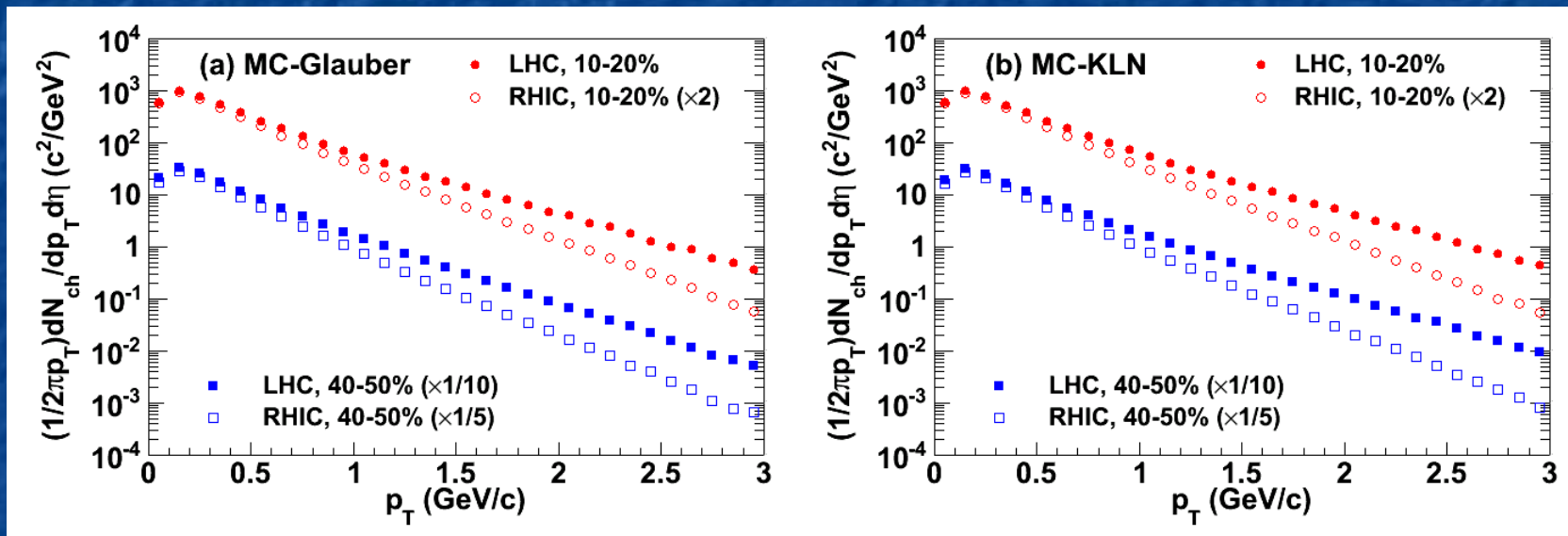
ALICE, arXiv:1012.1657

Eccentricity



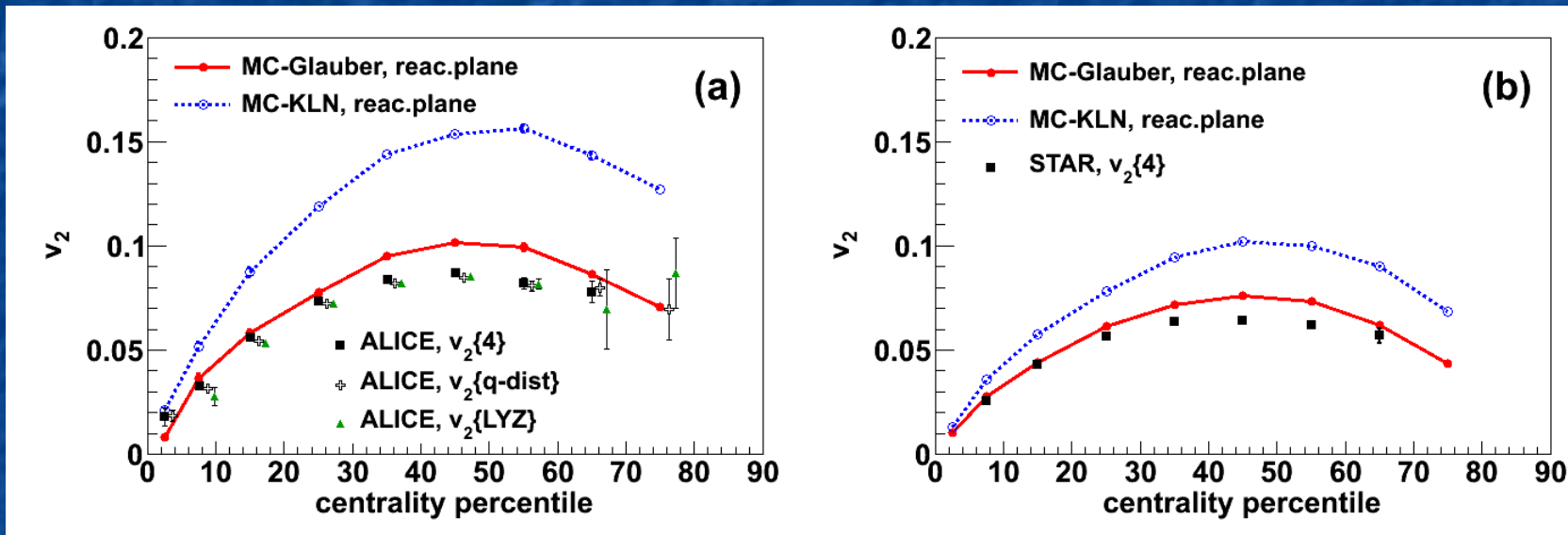
Crossing → Due to smearing effects

p_T Spectra of Charged Hadrons



Spectra at LHC get harder than at RHIC

Integrated v_2

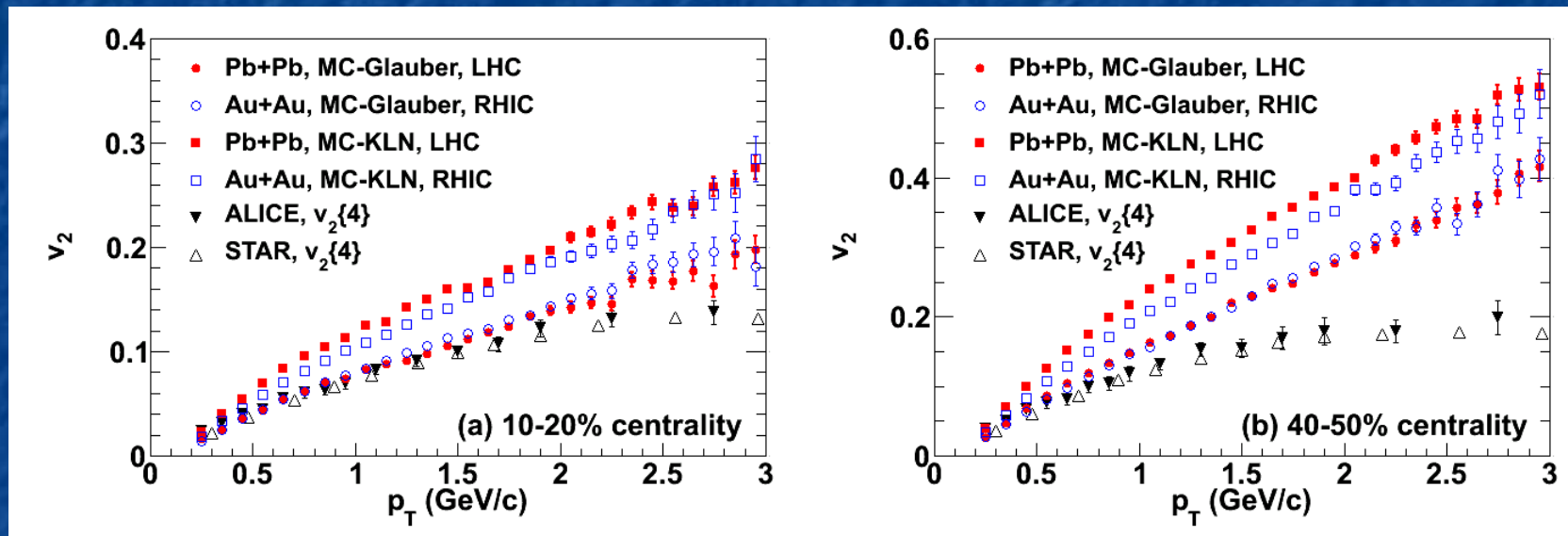


If the Nature chooses MC-KLN, viscous effects would be larger at LHC than at RHIC.

→ Importance of understanding initial conditions

ALICE, PRL105, 0252302(2010).

Differential v_2



- $v_2(p_T)$ at LHC is almost identical to $v_2(p_T)$ at RHIC, in particular, in MC-Glauber.
- Steeper slope in MC-CGC leads to larger v_2 even if increase of mean p_T in MC-CGC is identical to that in MC-Glauber.

ALICE, PRL105, 0252302(2010).

Summary

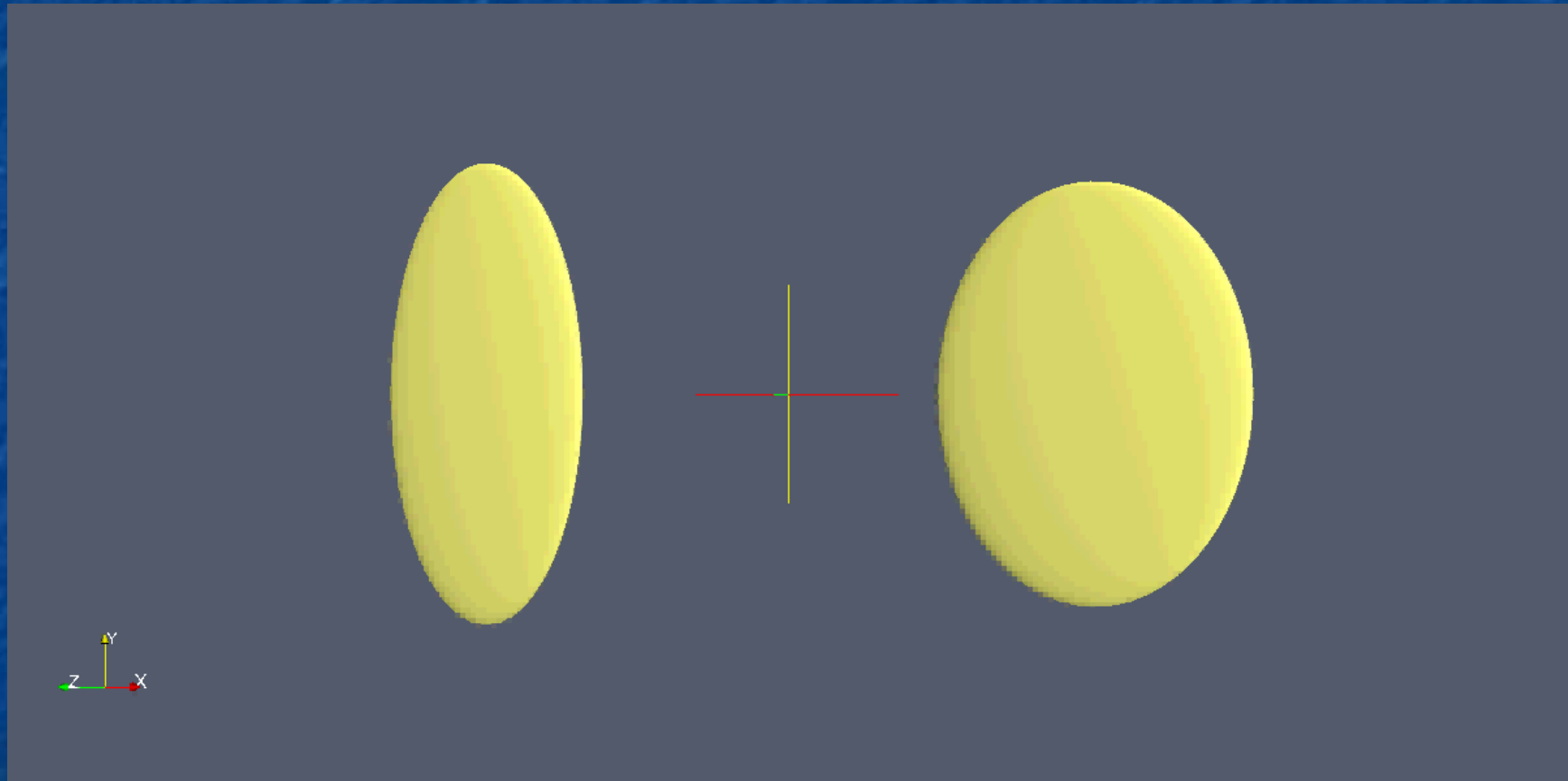
- Current status of the hybrid approach
 - Elliptic flow
 - MC-Glauber initialization gives a reasonable agreement with data in very central collisions.
 - Results deviate from data as moving away from central collisions.
 - QGP viscosity?
 - Source function
 - Non-Gaussian tail is seen through hadronic rescatterings and decays
 - Prediction
 - Results in U+U collisions follow scaling behavior, extend $(1/S)$ $dN_{ch}/d\eta$ by $\sim 10\%$
 - v_2/ϵ at LHC does not follow scaling seen at RHIC

Summary (contd.)

- Postdiction

- QGP viscosity at LHC (higher T) is larger than at RHIC (lower T) in MC-KLN?
- Understanding of transverse dynamics and initial state is important.

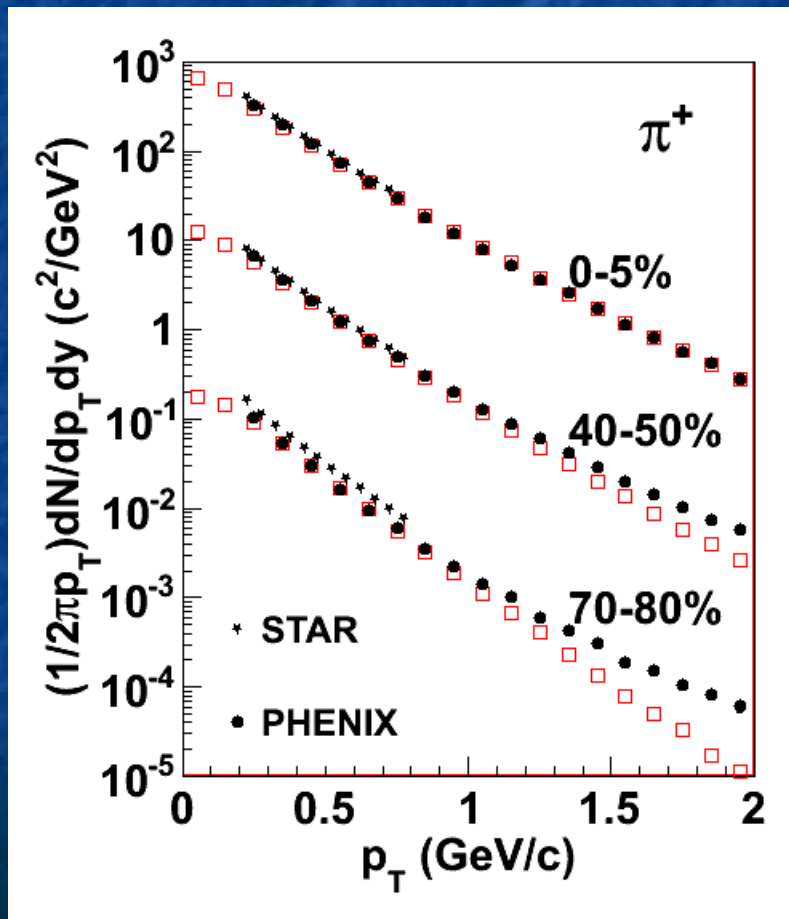
Thank You!



Available at 

BACKUP SLIDES

p_T Spectra in STAR and PHENIX



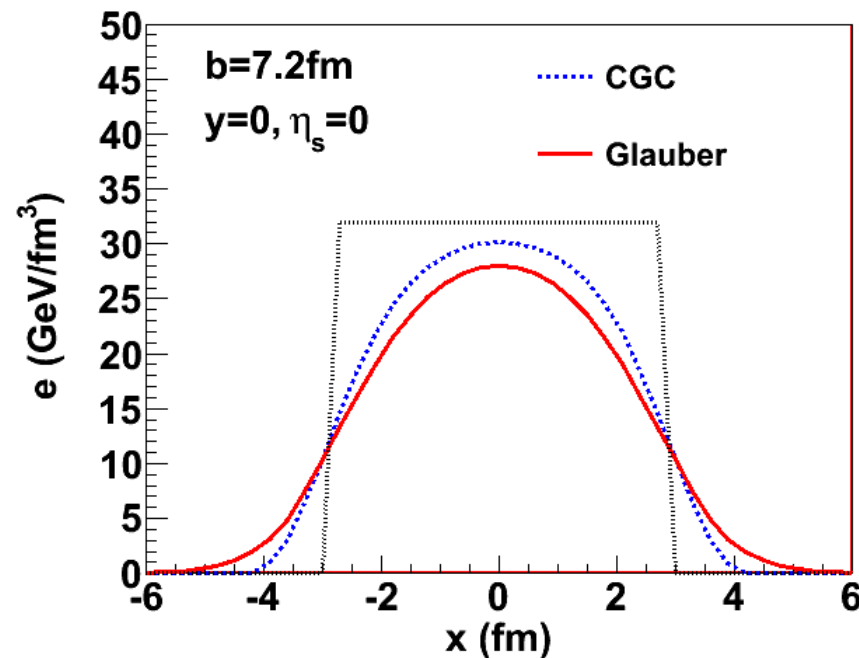
Central:
Consistent btw.
STAR and PHENIX

Peripheral:
(STAR) > (PHENIX)
STAR data are 50 %
larger than PHENIX data

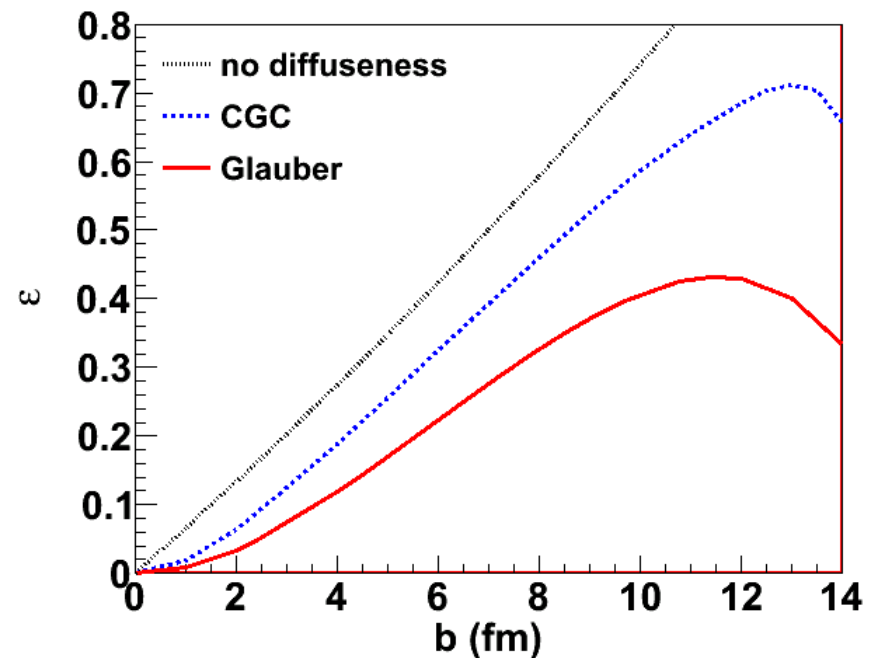
STAR, PRC 79, 034909 (2009)

PHENIX, PRC69, 034909 (2004)

Steeper Transverse Profile in CGC

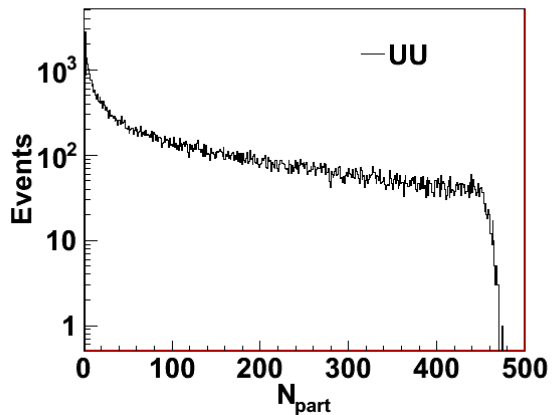
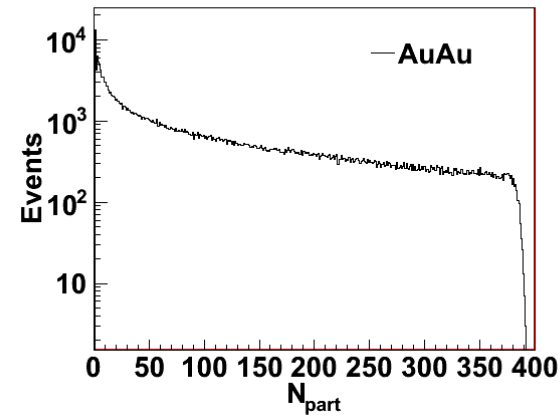
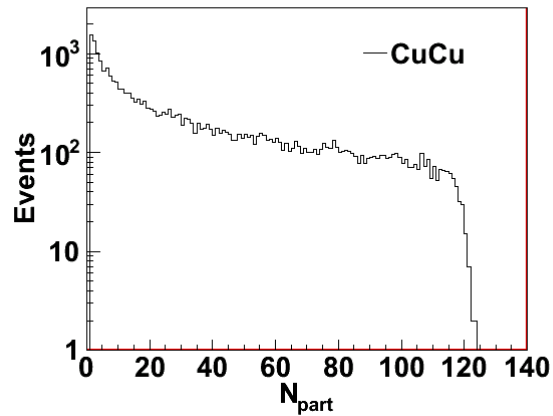


Closer to hard sphere
than Glauber



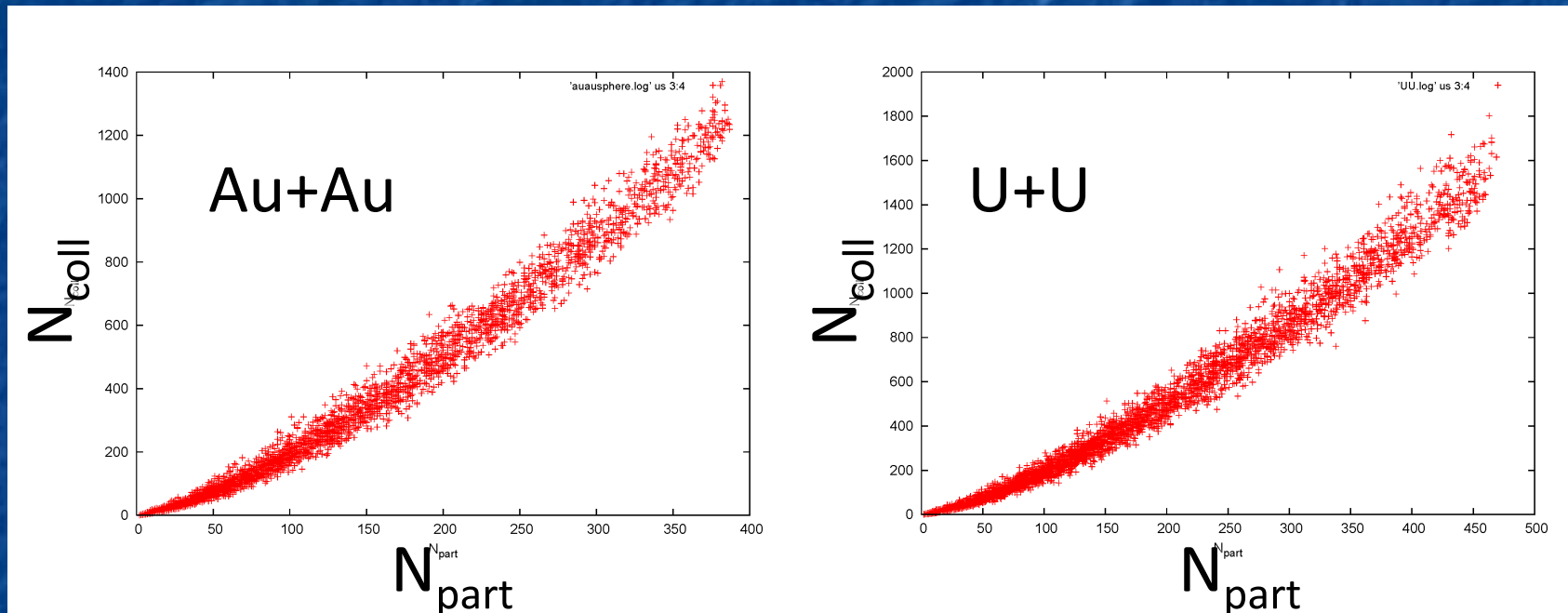
Note: Original KLN
model (not fKLN)

Event Distributions from Monte Carlo



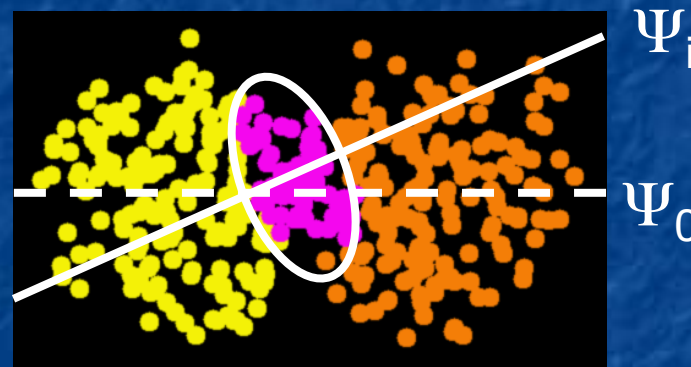
Centrality cut is done
according to N_{part}

Correlation btw. N_{part} and N_{coll}



Eccentricity Fluctuation

Adopted from D.Hofman(PHOBOS),
talk at QM2006



A sample event
from Monte Carlo
Glauber model

Interaction points of participants vary event by event.

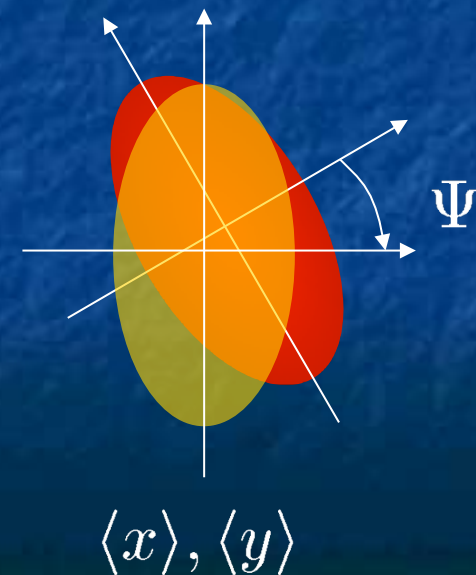
→ Apparent reaction plane also varies.

→ The effect is significant for smaller system such as Cu+Cu collisions

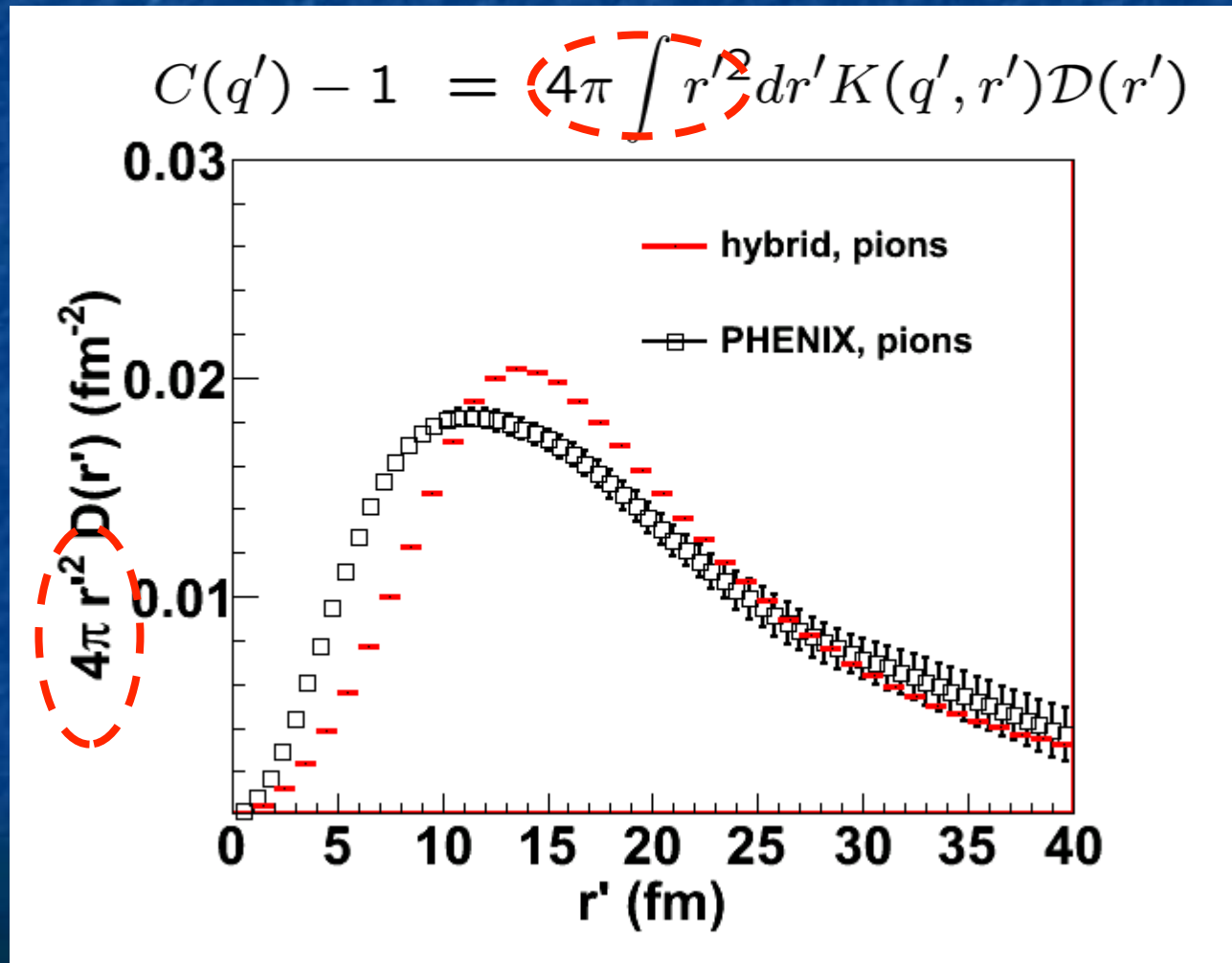
Event-by-Event Eccentricity

$$\begin{aligned}\sigma_x^2 &= \langle x^2 \rangle - \langle x \rangle^2, \\ \sigma_y^2 &= \langle y^2 \rangle - \langle y \rangle^2, \\ \sigma_{xy} &= \langle xy \rangle - \langle x \rangle \langle y \rangle.\end{aligned}\quad \langle \cdots \rangle = \frac{\int d^2 x_{\perp} \cdots s_0(\mathbf{x}_{\perp})}{\int d^2 x_{\perp} s_0(\mathbf{x}_{\perp})},$$

$$\begin{aligned}\varepsilon_{\text{RP}} &= \frac{\sigma_y^2 - \sigma_x^2}{\sigma_y^2 + \sigma_x^2} \\ \varepsilon_{\text{part}} &= \frac{\sqrt{(\sigma_y^2 - \sigma_x^2)^2 + 4\sigma_{xy}^2}}{\sigma_y^2 + \sigma_x^2} \\ \tan 2\Psi &= \frac{\sigma_y^2 - \sigma_x^2}{2\sigma_{xy}}.\end{aligned}$$

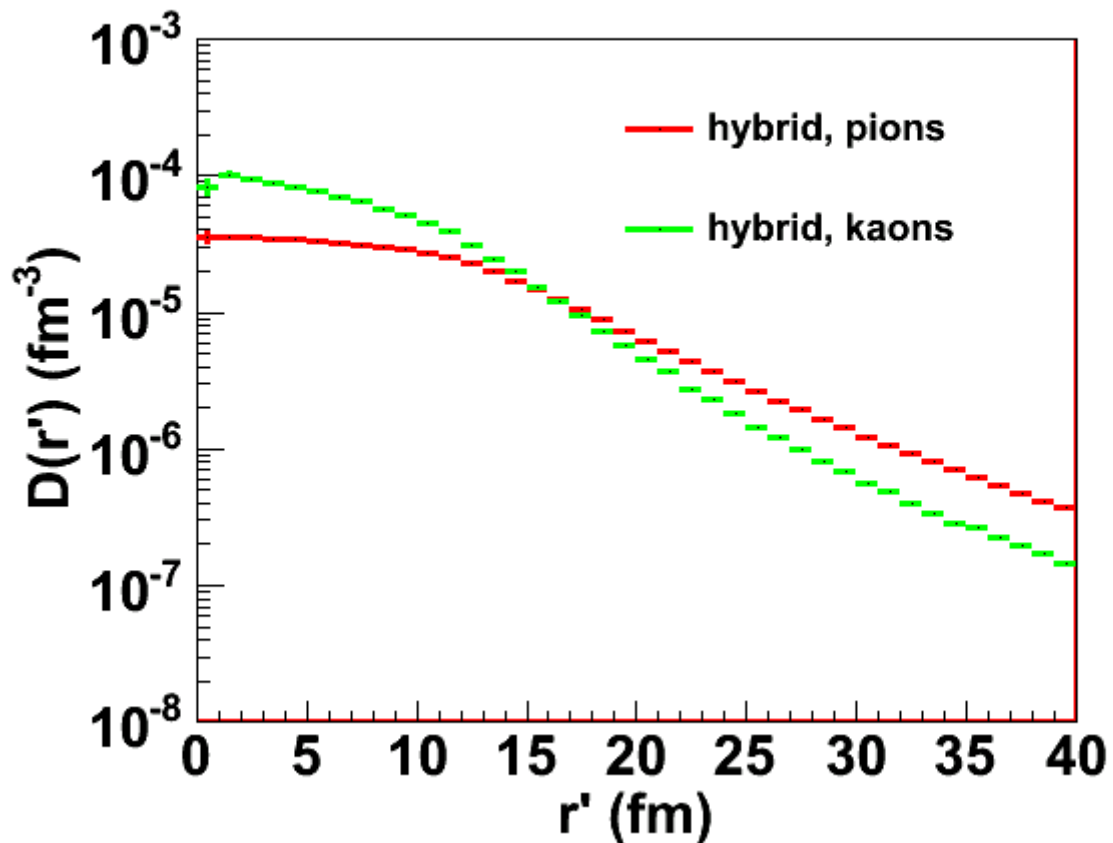


Normalization in Source Function



Source function multiplied by phase space density

Comparison of Source Functions



Both normalized to be unity

Normalization in PHENIX???

