



Azimuthal angle dependence of HBT radii in Au+Au collisions at RHIC-PHENIX

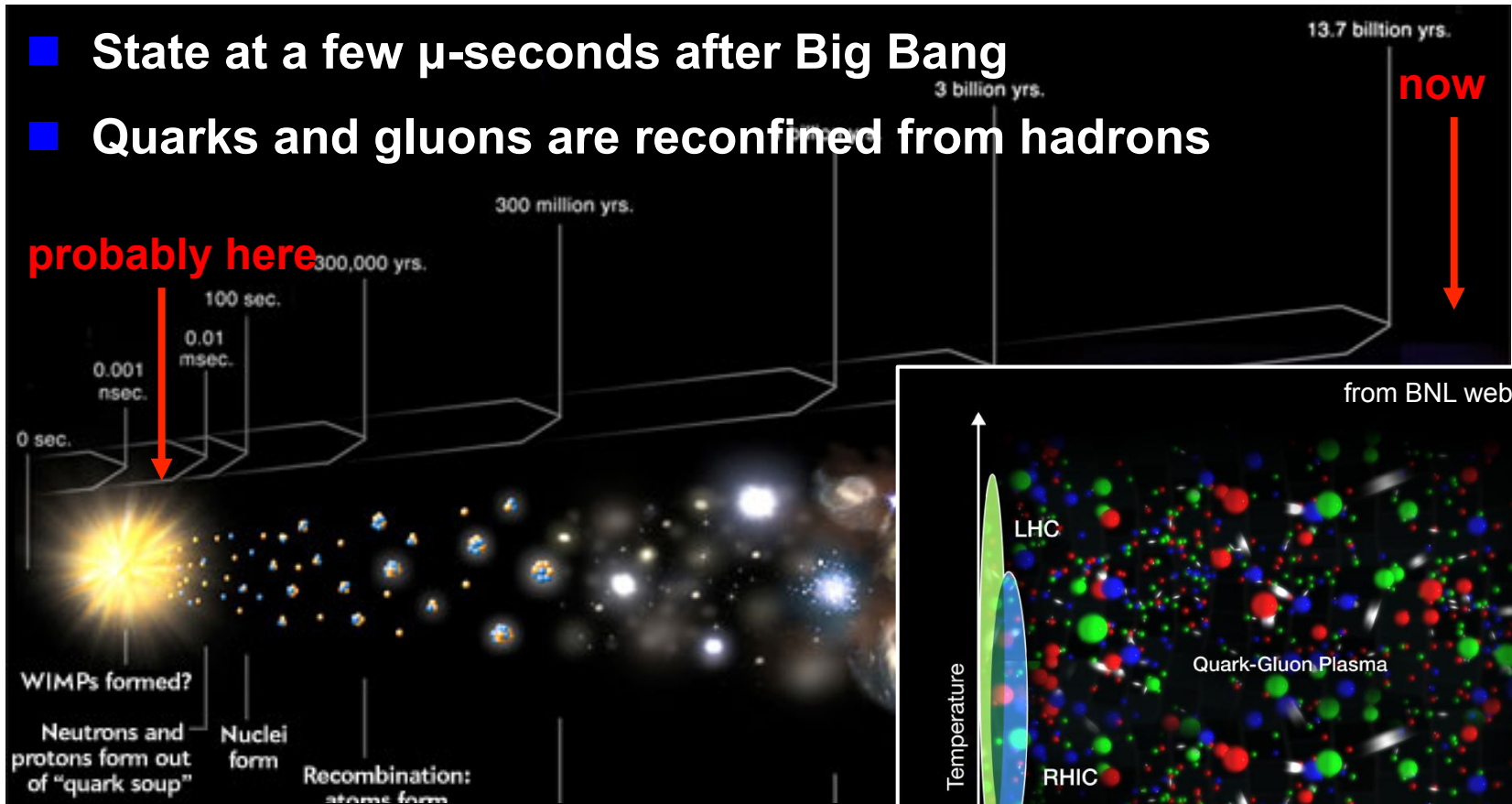
Takafumi Niida for the PHENIX Collaboration
University of Tsukuba

The 12th Asia Pacific Physics Conference

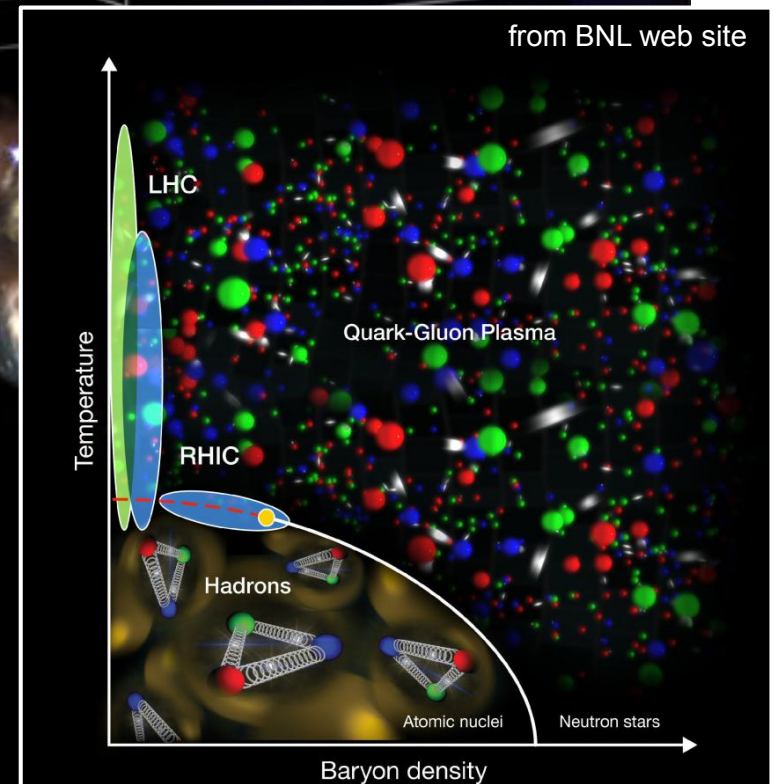
Quark Gluon Plasma (QGP)

<http://www.scientificamerican.com/>

- State at a few μ -seconds after Big Bang
- Quarks and gluons are reconfined from hadrons

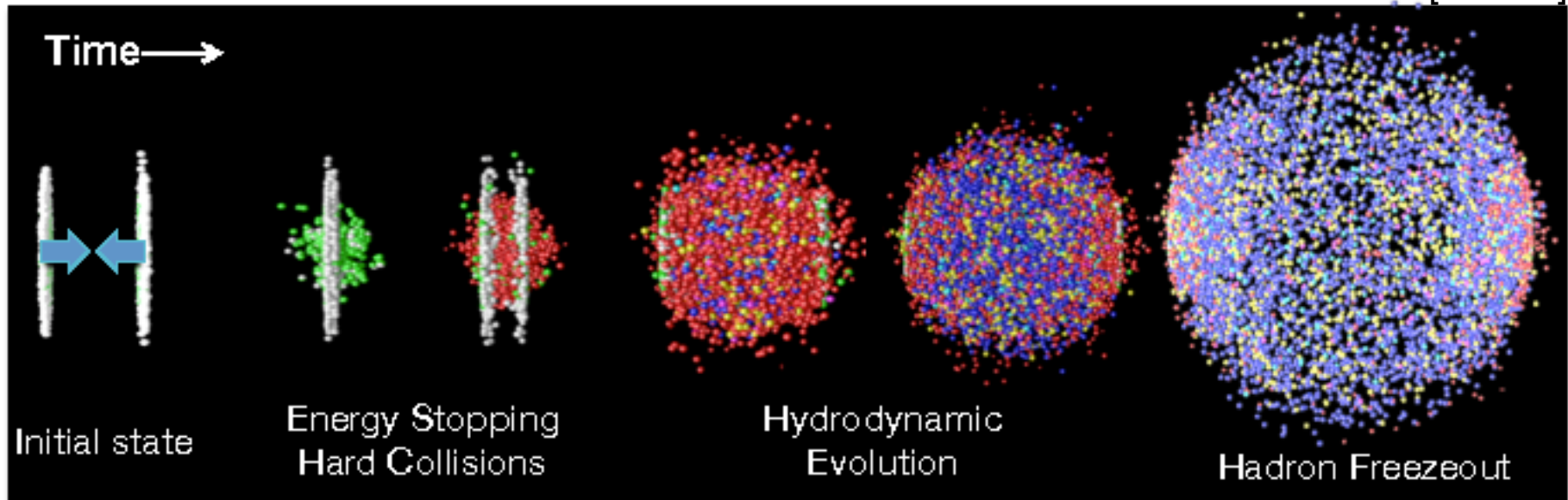


- QGP will be created at extreme temperature and energy density
- Relativistic heavy ion collisions is a unique way to study the QGP



Space-Time evolution in HI collisions

arXiv:1201.4264 [nucl-ex]



- Space-time extent at freeze-out reflects the properties of system evolution, such as the phase transition, hydrodynamic expansion and hadron rescattering etc.
- **HBT interferometry** is a powerful tool to study the space-time evolution in Hheavy Ion collisions.

HBT Interferometry

■ R. Hanbury Brown and R. Twiss

✧ In 1956, the angular diameter of Sirius was measured.

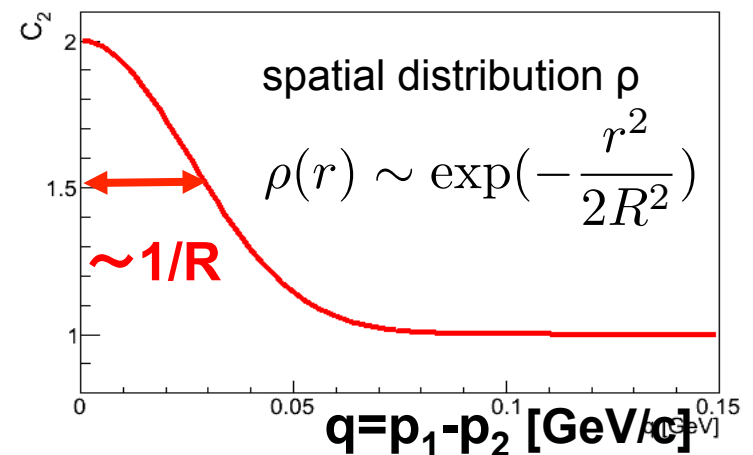
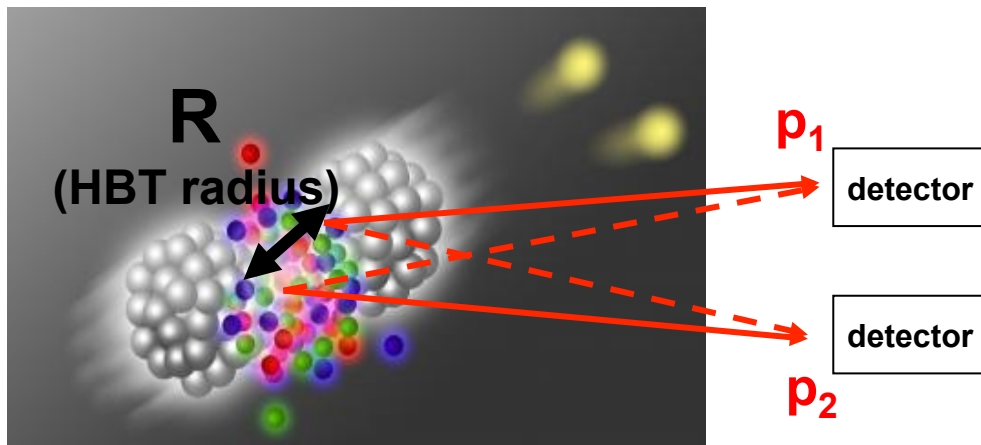
■ Goldhaber *et al.*

✧ In 1960, correlation among identical pions in $p+\bar{p}$ collision was observed.

■ Quantum interference between two identical particles

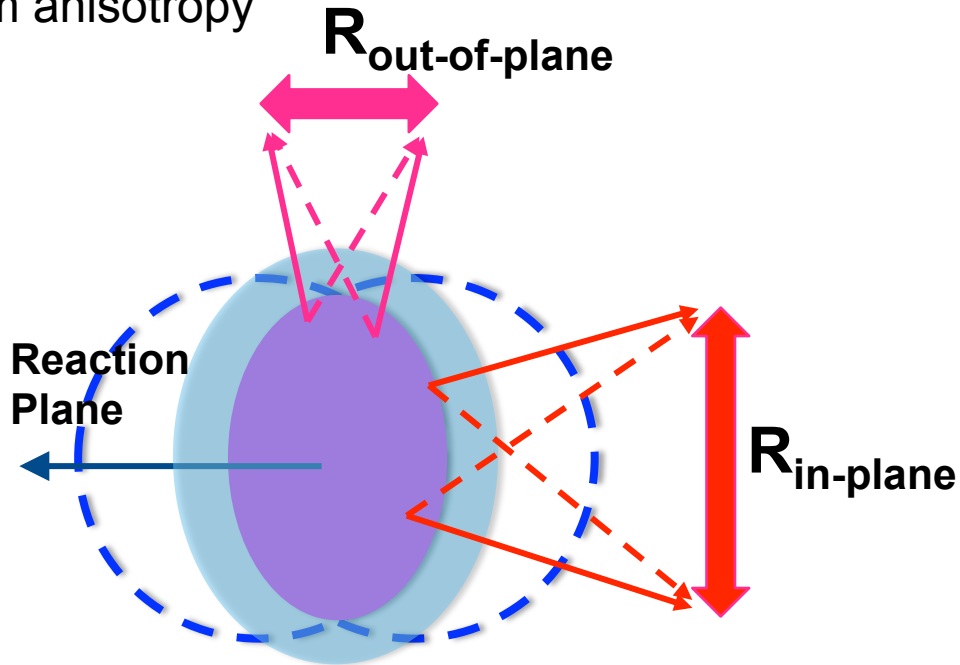
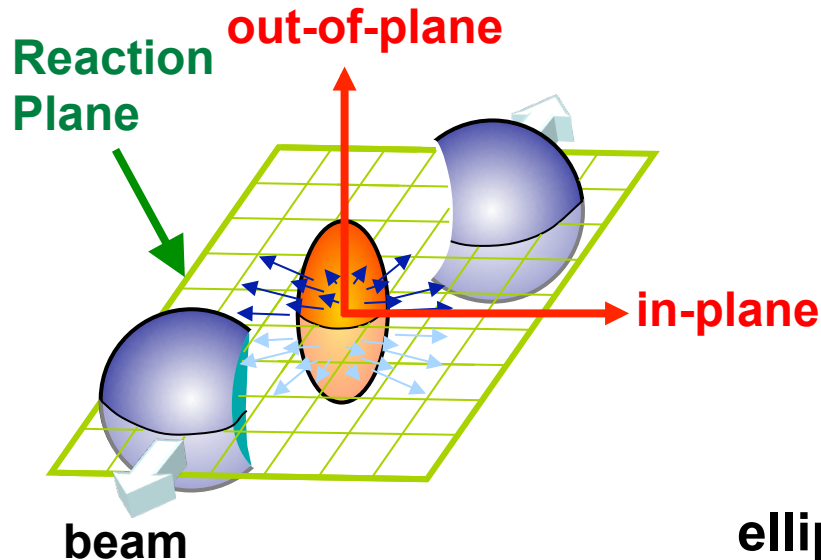
wave function for
2 bosons(fermions): $\Psi_{12} = \frac{1}{\sqrt{2}}[\Psi(x_1, p_1)\Psi(x_2, p_2) \pm \Psi(x_2, p_1)\Psi(x_1, p_2)]$

$$C_2 = \frac{P(p_1, p_2)}{P(p_1)P(p_2)} \approx 1 + |\tilde{\rho}(q)|^2 = 1 + \exp(-R^2 q^2)$$



Azimuthal angle dependence

- HBT w.r.t Reaction Plane give us source shape at freeze-out.
 - ✧ R.P defined by beam axis and vector between centers of colliding nuclei
- Final eccentricity is determined by initial eccentricity, velocity profile and expansion time etc.
 - ✧ Initial anisotropy causes momentum anisotropy

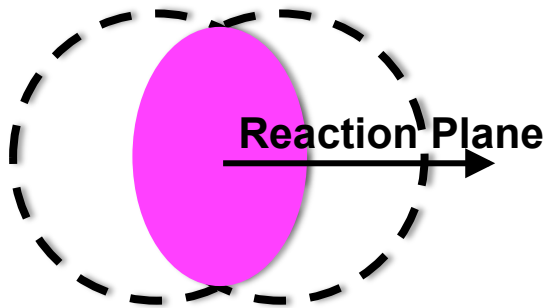


elliptical shape : $R_{\text{in-plane}} > R_{\text{out-of-plane}}$
spherical shape : $R_{\text{in-plane}} = R_{\text{out-of-plane}}$

Higher Harmonic Flow and Event Plane

- Initial density fluctuations cause higher harmonic flow v_n
- Azimuthal distribution of emitted particles:

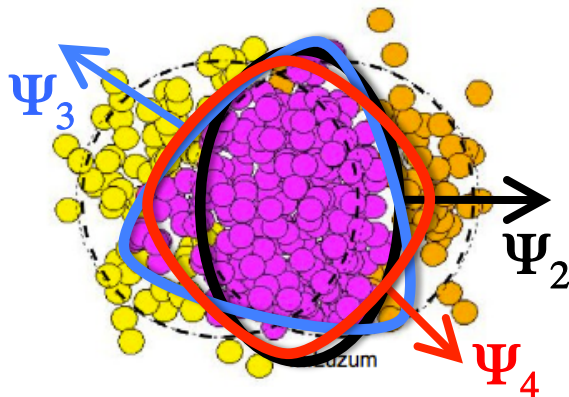
smooth picture



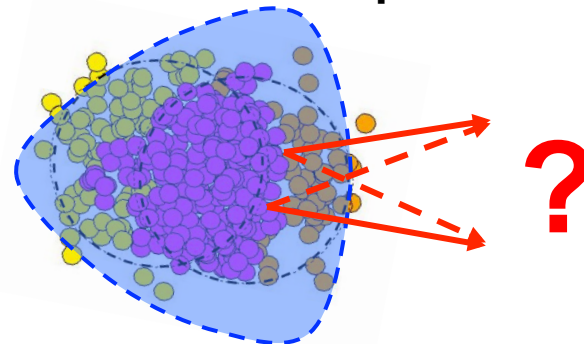
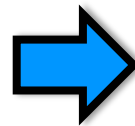
$$\frac{dN}{d\phi} \propto 1 + 2v_2 \cos 2(\phi - \Psi_2) + 2v_3 \cos 3(\phi - \Psi_3) + 2v_4 \cos 4(\phi - \Psi_4) \quad v_n = \langle \cos n(\phi - \Psi_n) \rangle$$

v_n : strength of higher harmonic flow
 Ψ_n : higher harmonic **Event plane**
 ϕ : azimuthal angle of emitted particles

fluctuating picture



What is final shape ?



3D HBT radii

■ “Out-Side-Long” frame

- ✧ Bertsch-Pratt parameterization
- ✧ Longitudinal Center of Mass System ($p_{z1}=p_{z2}$)

$$C_2 = 1 + \lambda G$$

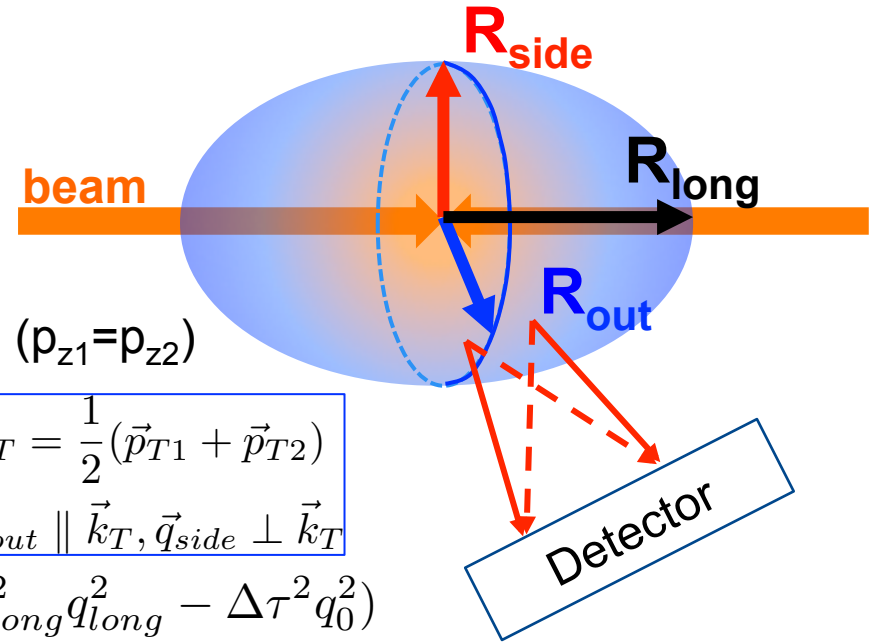
$$G = \exp(-\mathbf{R}^2 \mathbf{q}^2)$$

$$= \exp(-R_{side}^2 q_{side}^2 - R_{out}^{*2} q_{out}^2 - R_{long}^2 q_{long}^2 - \Delta\tau^2 q_0^2)$$

$$\stackrel{\text{LCMS}}{\approx} \exp(-R_{side}^2 q_{side}^2 - \underbrace{(R_{out}^{*2} + \beta_T \Delta\tau^2)}_{=R_{out}^2} q_{out}^2 - R_{long}^2 q_{long}^2)$$

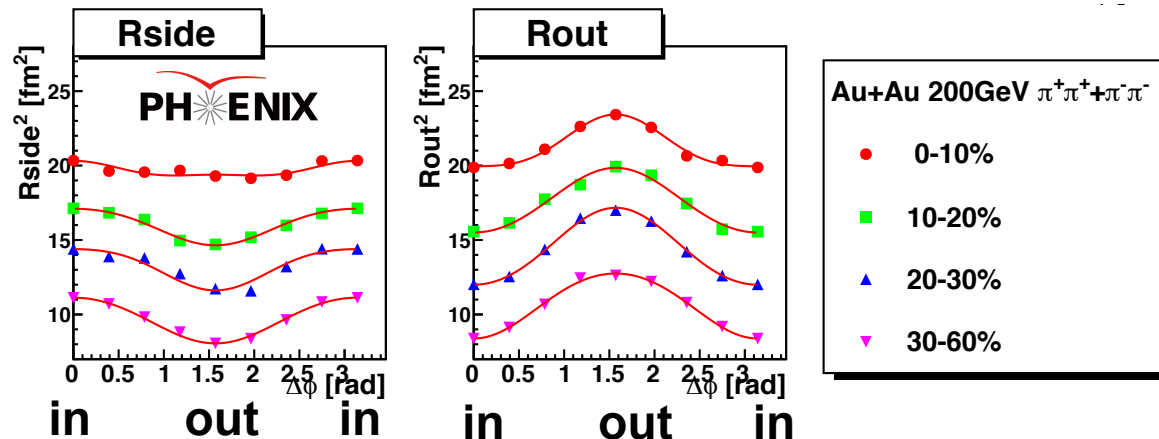
$$= R_{out}^2$$

$$G = \exp(-R_{side}^2 q_{side}^2 - R_{out}^2 q_{out}^2 - R_{long}^2 q_{long}^2 - 2R_{os}^2 q_{side} q_{out})$$



λ	: chaoticity
R_{side}	: transverse HBT radius
R_{out}	: transverse HBT radius + $\Delta\tau$ (emission duration)
R_{long}	: longitudinal HBT radius
R_{os}	: cross term for ϕ -dependent analysis

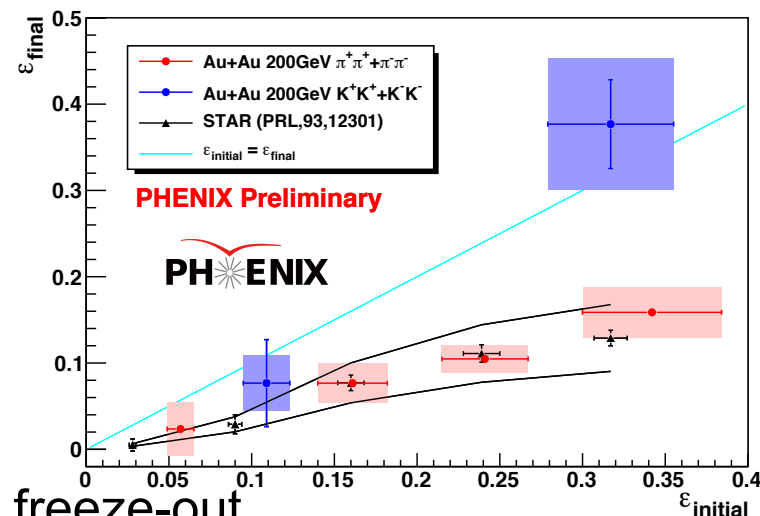
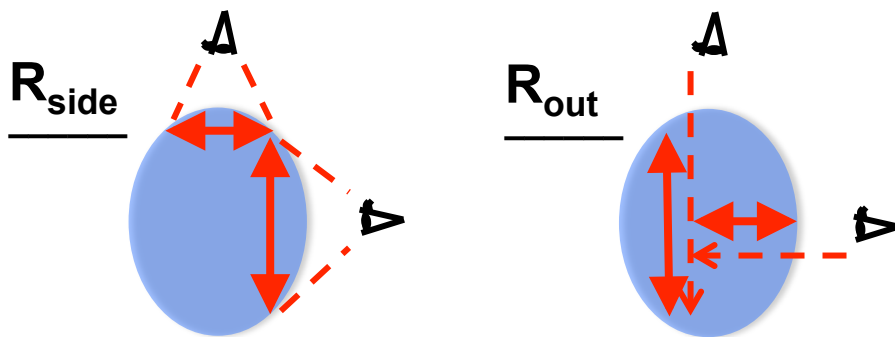
HBT radii w.r.t 2nd-order event plane



PRC70, 044907 (2004)

$$R_{s,n}^2 = \langle R_s^2(\Delta\phi) \cos(n\Delta\phi) \rangle$$

$$\varepsilon_{final} = 2R_{s,2}^2/R_{s,0}^2$$



■ $\varepsilon_{final} \approx \varepsilon_{initial}/2$ for pion

✧ expansion to in-plane, but still elliptical at freeze-out

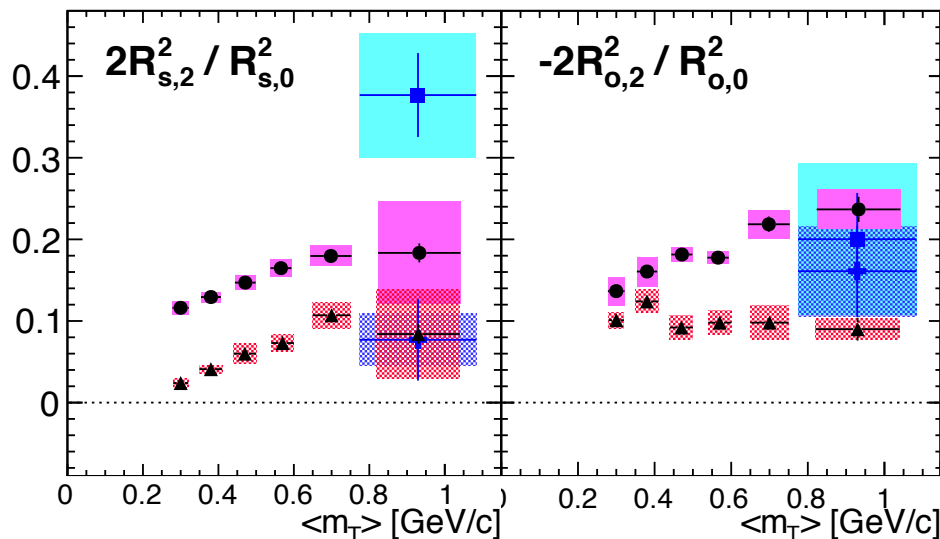
✧ consistent with STAR experiment

■ $\varepsilon_{final} \approx \varepsilon_{initial}$ for kaon

✧ emission region we're looking at is different?

m_T dependence

- HBT does not measure the whole size but the emission region for expanding source
 - ✧ HBT radii depend on pair transverse momentum mass m_T
 - ✧ Kaon has higher m_T than pion
- $R_{s,2}^2/R_{s,0}^2$ shows difference even at the same m_T in 20-60%
 - ✧ m_T scaling works well for average radius of π/K (PRL103.142301(2009))
 - ✧ Different freeze-out dynamics for both species ?

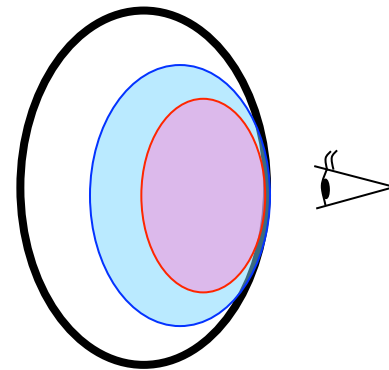


PHENIX Preliminary

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preliminary

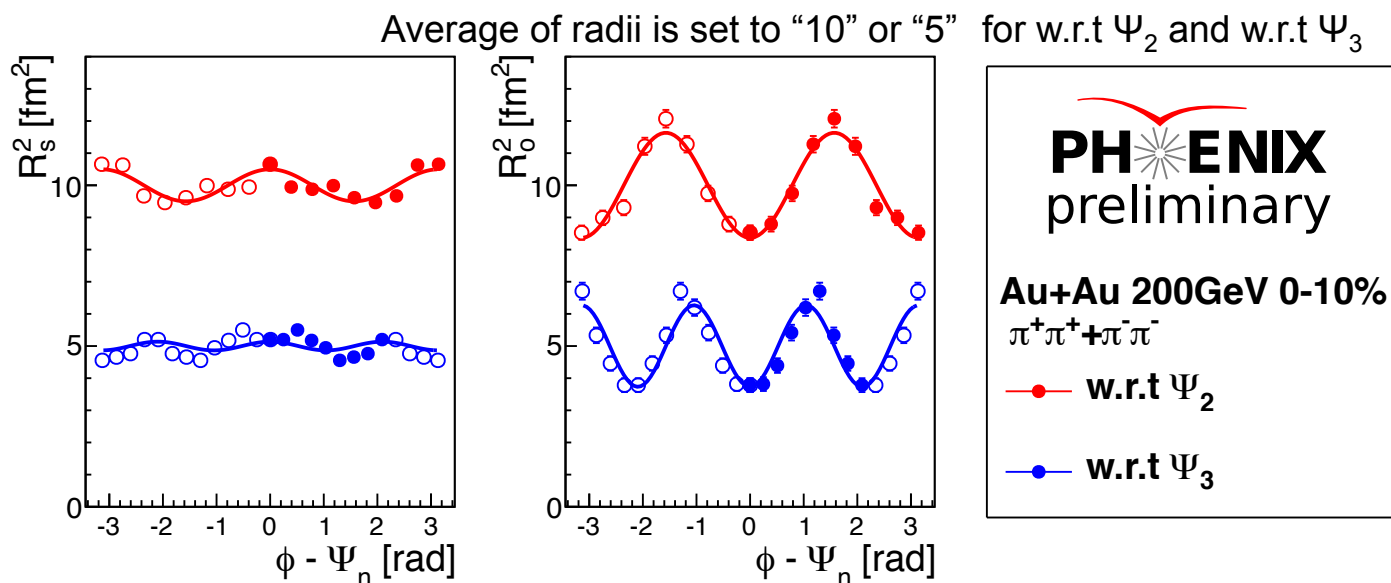
Au+Au 200GeV

- $\pi^+\pi^+\pi^-\pi^-$ 0-20%
- $\pi^+\pi^+\pi^-\pi^-$ 20-60%
- $K^+K^+K^-K^-$ 0-20%
- $K^+K^+K^-K^-$ 20-60%



$$m_T = \sqrt{k_T^2 + m^2}$$

HBT radii w.r.t 3rd-order event plane



■ R_{out} clearly shows a finite oscillation w.r.t Ψ_3 in most central event

✧ Strength w.r.t Ψ_3 is comparable to w.r.t Ψ_2

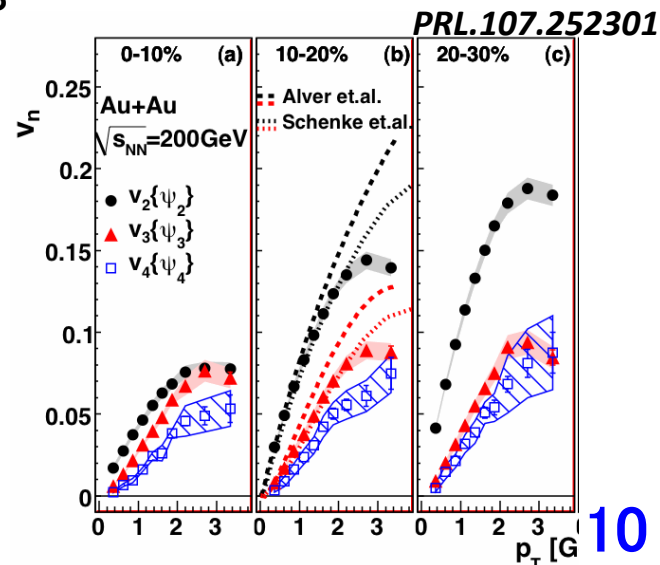
■ What make this R_o oscillation?

✧ Triangular spatial shape?

✧ Triangular flow?

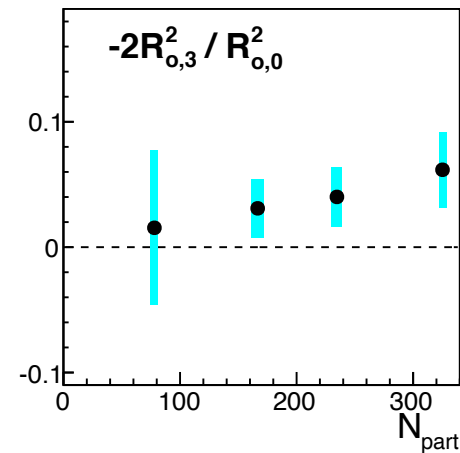
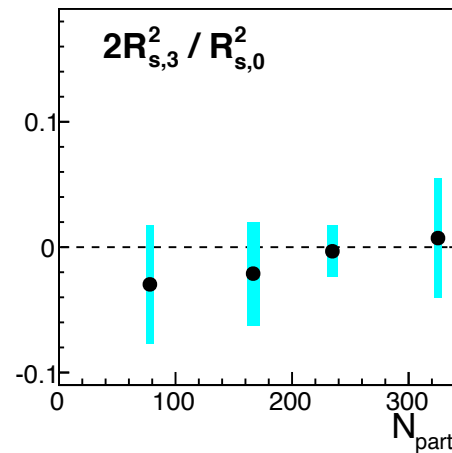
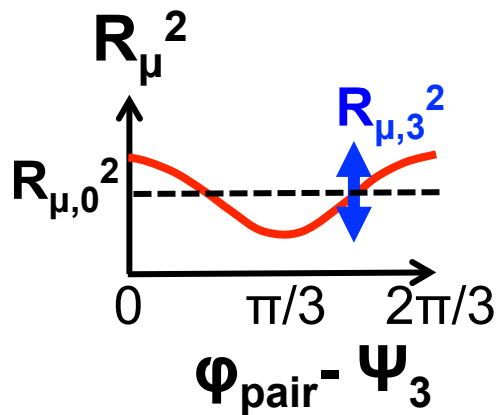
✓ v_3 is comparable to v_2 in most central

✧ Emission duration?



Centrality dependence of relative amplitudes

- Oscillation of R_s shows is almost zero within systematic error
 - ✧ Slightly negative value in peripheral ?
- R_o has finite oscillation except peripheral event



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preliminary

Au+Au 200GeV

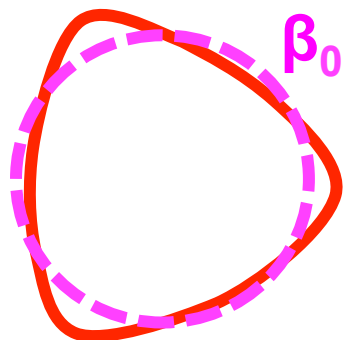
$\pi^+\pi^+\pi^-\pi^-$

Possible explanation of R_o oscillation

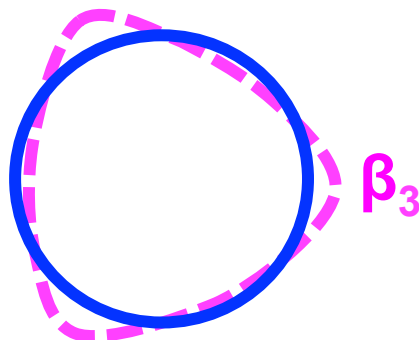
- HBT w.r.t Ψ_3 with toy model have been reported in arXiv:1306.1485[nucl-ex] (2013)

✧ assuming Gaussian source with triangular geometric deformation and triangular flow

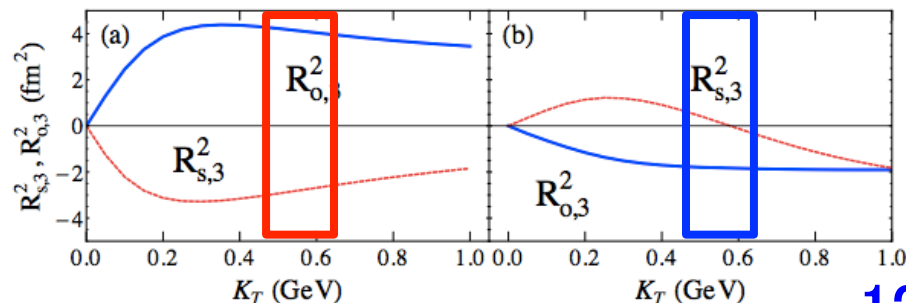
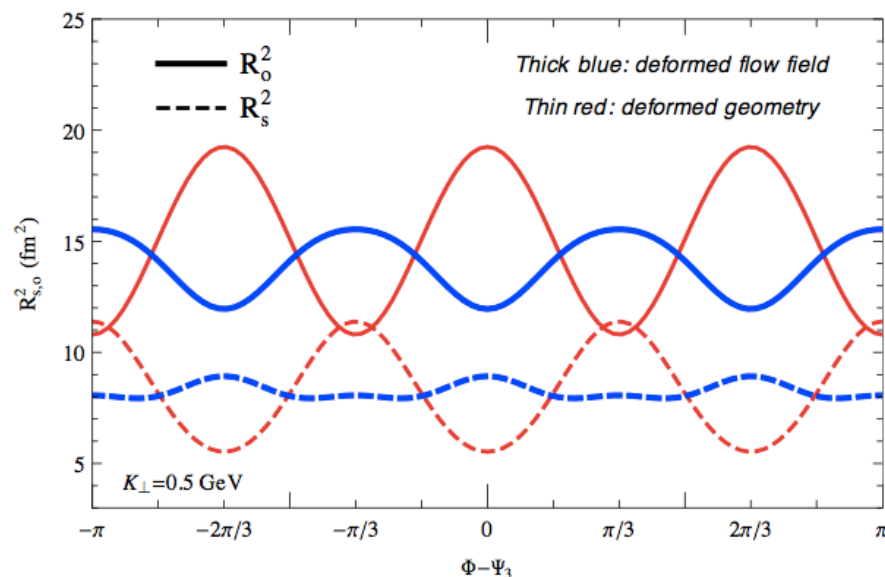
triangular source without flow anisotropy



spherical source with flow anisotropy



- ✧ Close to “flow dominated” case ?
- ✧ Need to check the k_T dependence to constraint ε_3/β_3



Summary

- **Azimuthal angle dependence of HBT radii with respect to 2nd- and 3rd-order event plane have been presented.**

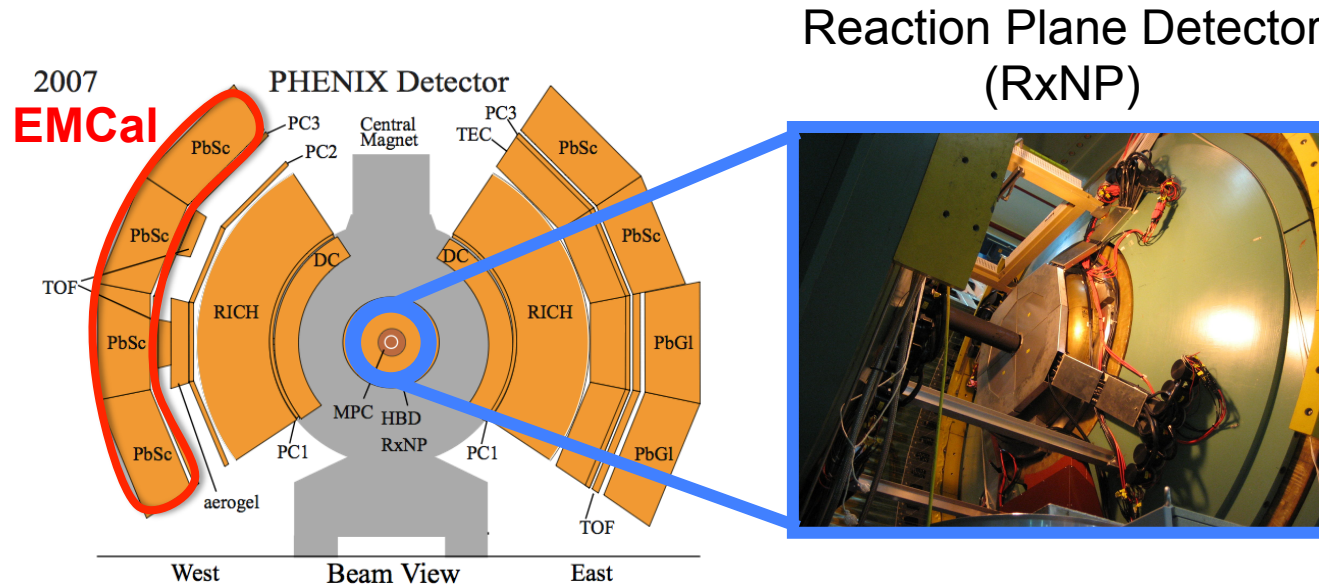
- ✧ Final eccentricity of kaons shows higher value than that of pions even at the same m_T
- ✧ Oscillation of R_0 w.r.t Ψ_3 has been observed in most central event, while R_s doesn't show any signal beyond systematic error
 - ✓ R_0 oscillation may be explained by triangular flow

- **Outlook**

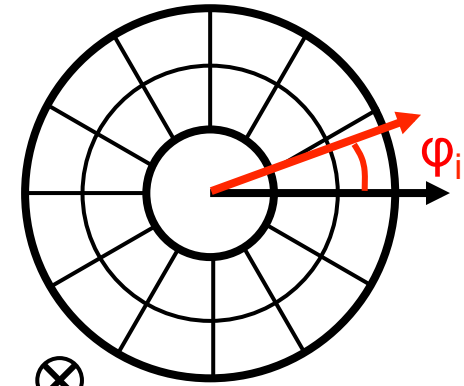
- ✧ k_T dependence of oscillation amplitudes w.r.t Ψ_3 will be measured, which will provide us information on the relative magnitude of geometrical and flow anisotropy

Back up

PHENIX Detectors



24 scintillator segments



beam axis

$$\Psi_n = \frac{1}{n} \tan^{-1} \left(\frac{\sum w_i \cos(n\phi_i)}{\sum w_i \sin(n\phi_i)} \right)$$

★ Particle Identification by EMCAL

- ★ π/K separation up to $\sim 1\text{GeV}$

★ Centrality by Beam-Beam Counter

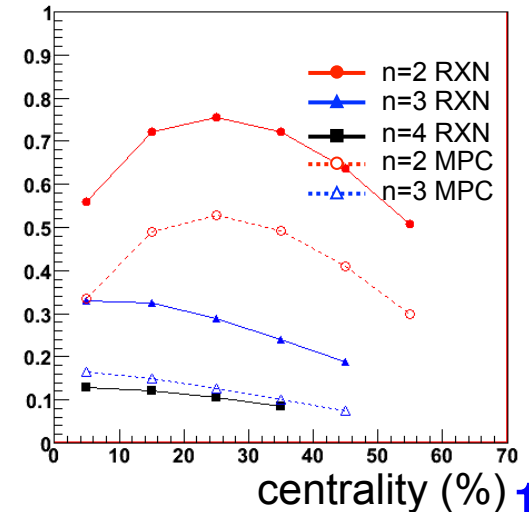
- ★ measure charge sum from participants

★ Event plane Ψ_n determined by RxNP

- ★ $\text{Res}(\Psi_2) \sim 0.75$, $\text{Res}(\Psi_3) \sim 0.32$

$\text{Res}(\Psi_n)$

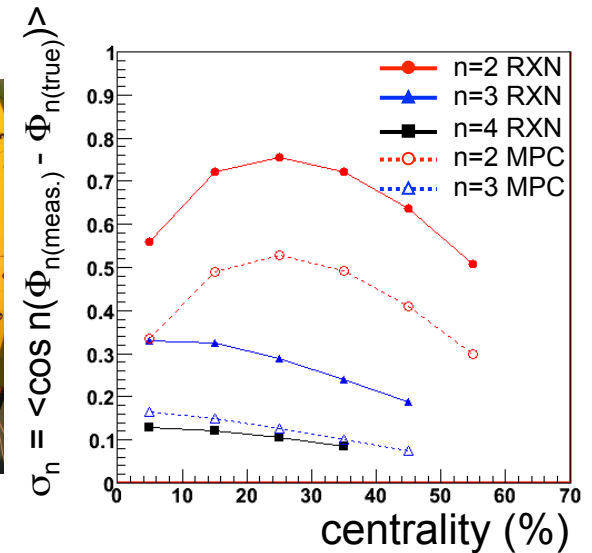
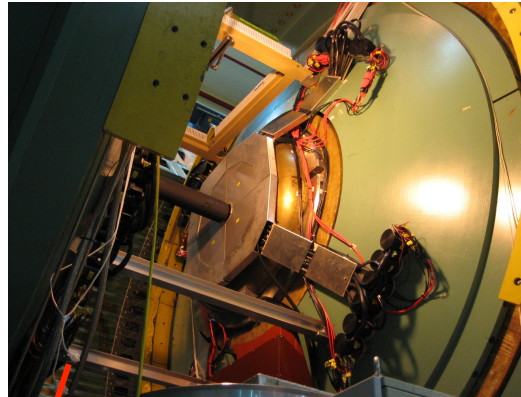
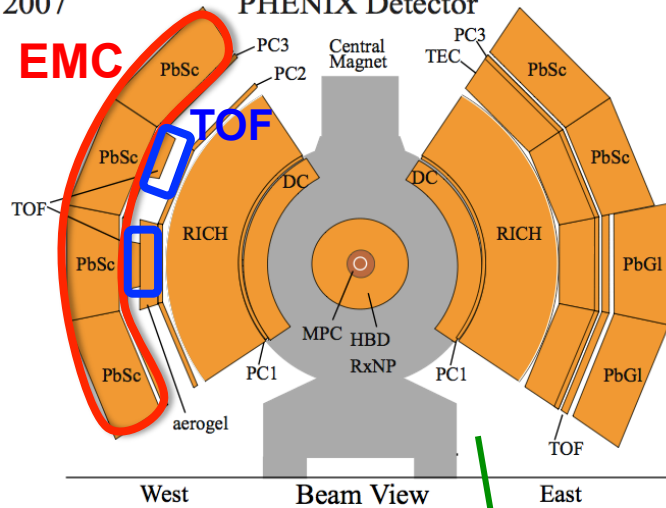
$$= \langle \cos n(\Psi_{n(\text{meas})} - \Psi_{n(\text{true})}) \rangle$$



PHENIX Detectors

2007

PHENIX Detector



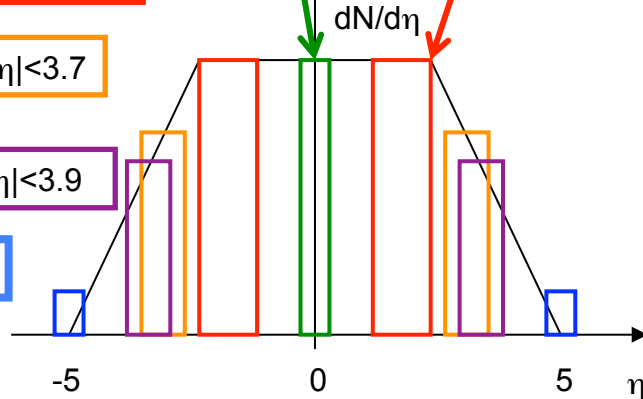
RXN in: $1.5 < |\eta| < 2.8$
& out: $1.0 < |\eta| < 1.5$

CNT: $|\eta| < 0.35$

MPC: $3.1 < |\eta| < 3.7$

BBC: $3.0 < |\eta| < 3.9$

ZDC/SMD



$$C_2 = \frac{R(q)}{M(q)}$$

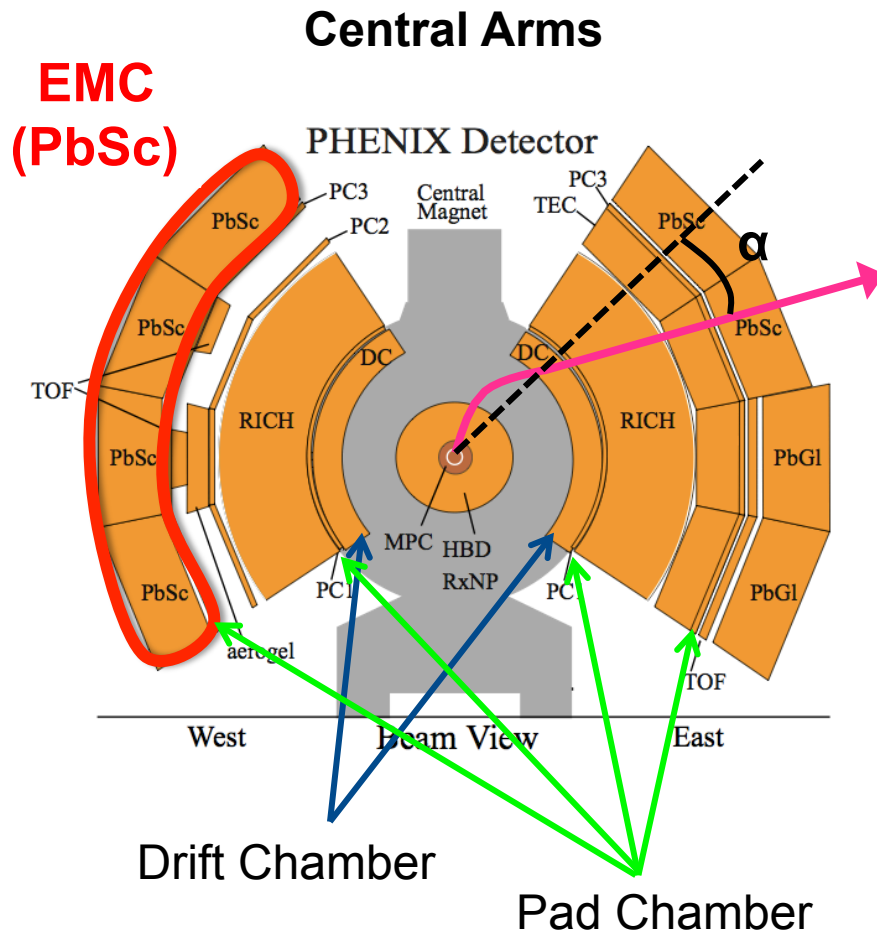
$R(q), M(q)$:
relative momentum dist.
for real and mixed pairs

★ PID by EMC&TOF

⇒ charged π/K are selected

★ Ψ_n by forward detector RXN

Track Reconstruction



■ Drift Chamber

- ## ✧ Momentum determination

$$p_T \simeq \frac{K}{\alpha}$$

K: field integral
 α : incident angle

■ Pad Chamber (PC1)

- ✧ Associate DC tracks with hit positions on PC1
 - ✓ p_z is determined

- **Outer detectors (PC3, TOF, EMCal)**

- ✧ Extend the tracks to outer detectors

Particle IDentification

■ EMC-PbSc is used.

✧ timing resolution ~ 600 ps

■ Time-Of-Flight method

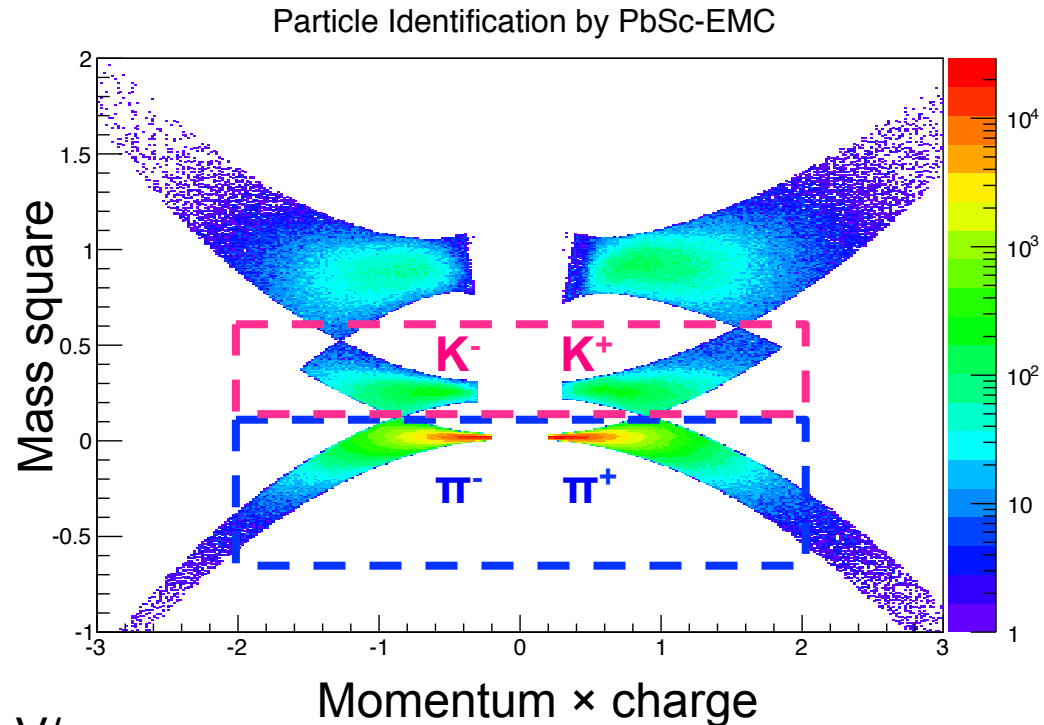
$$m^2 = p^2 \left(\left(\frac{ct}{L} \right)^2 - 1 \right)$$

p: momentum L: flight path length
t: time of flight

■ Charged π/K within 2σ

✧ π/K separation up to ~ 1 GeV/c

✧ K/p separation up to ~ 1.6 GeV/c



Correlation Function

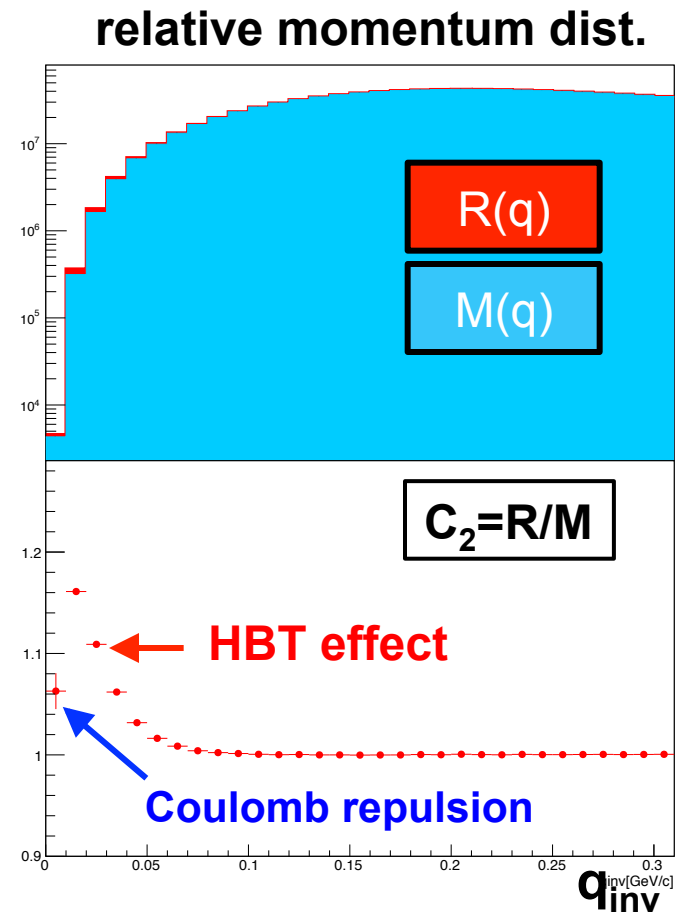
■ Experimental Correlation Function C_2 is defined as:

- ✧ $R(q)$: **R**ead pairs at the same event.
- ✧ $M(q)$: **M**ixed pairs selected from different events.

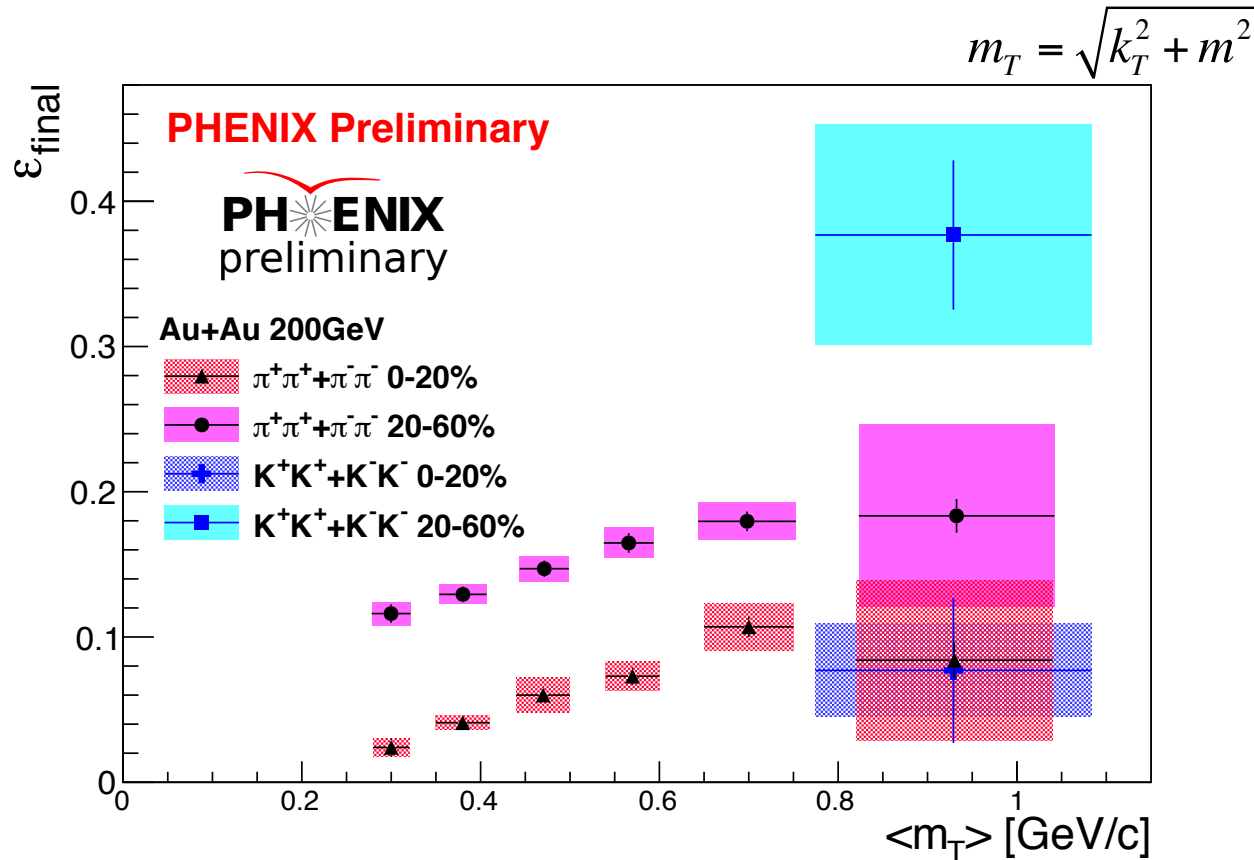
Event mixing was performed using events with similar z-vertex, centrality, E.P.

$$C_2 = \frac{R(\mathbf{q})}{M(\mathbf{q})}$$
$$\mathbf{q} = \mathbf{p}_1 - \mathbf{p}_2$$

- ✧ Real pairs include HBT effects, Coulomb interaction and detector inefficient effect. Mixed pairs doesn't include HBT and Coulomb effects.

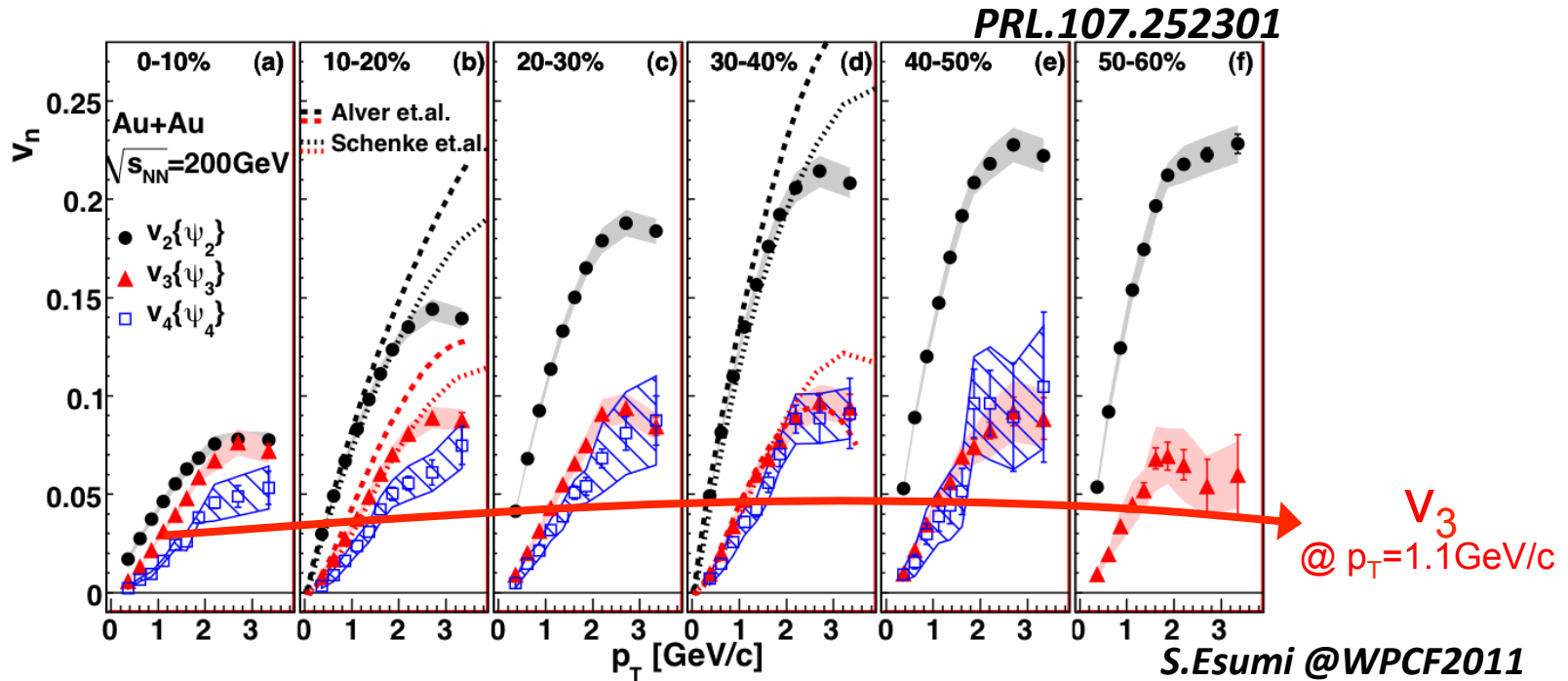


m_T dependence of ϵ_{final}



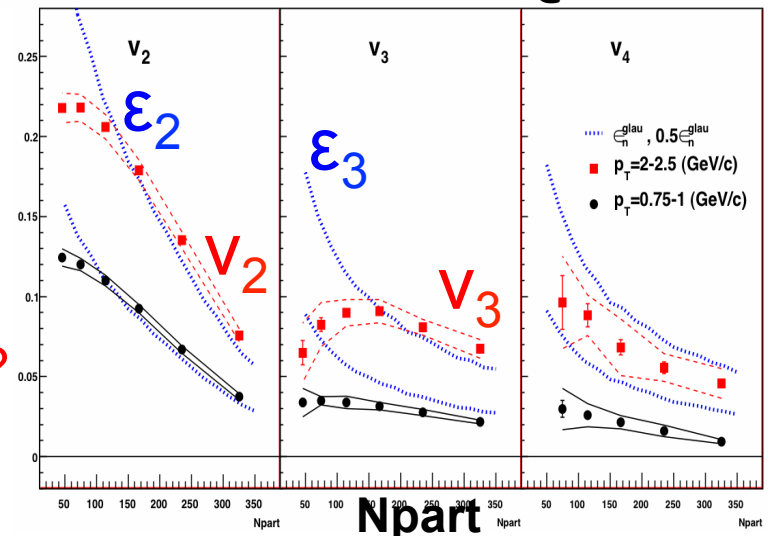
- ϵ_{final} of pions increases with m_T in most/mid-central collisions
- There is still difference between π/K for mid-central collisions even in same m_T
- ✧ Indicates sooner freeze-out time of K than π ?

Centrality dependence of v_3 and ϵ_3

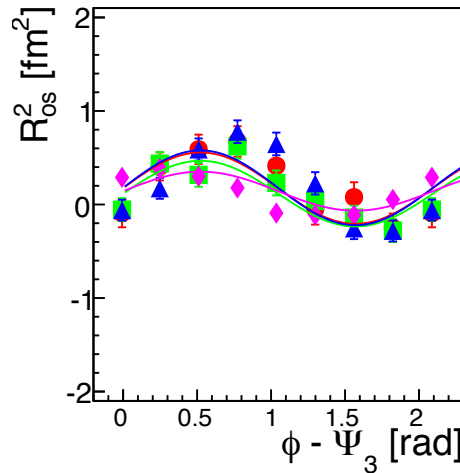
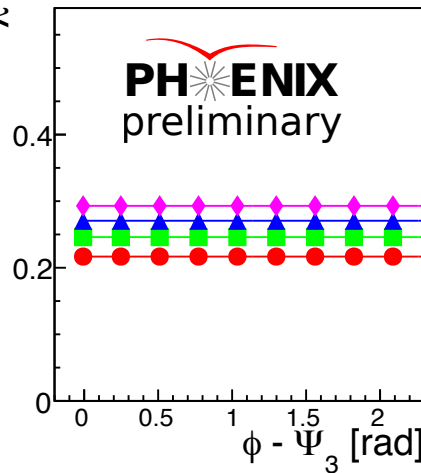
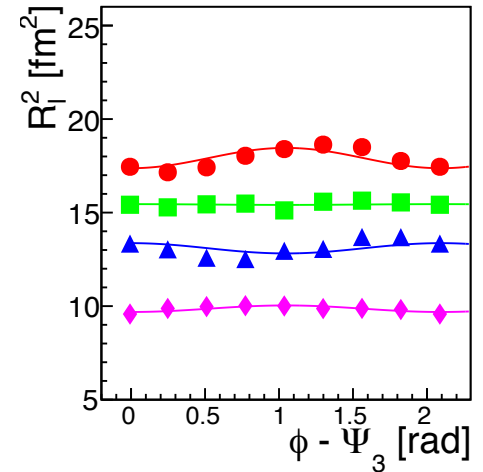
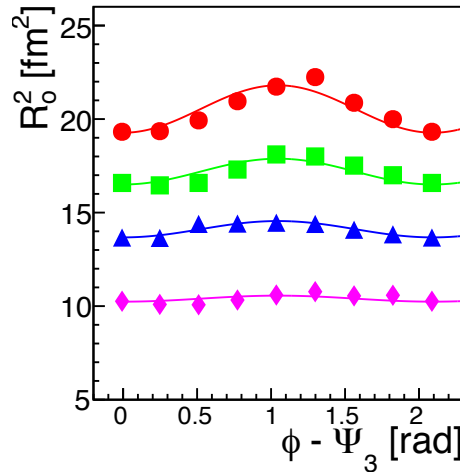
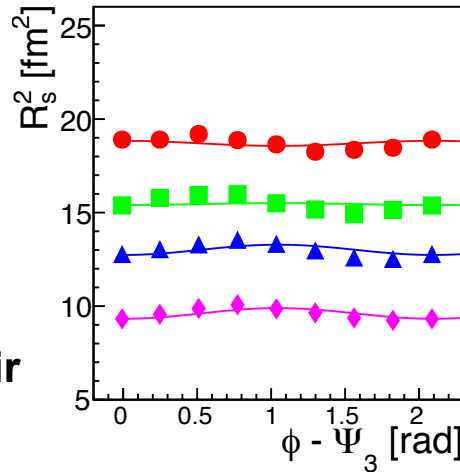
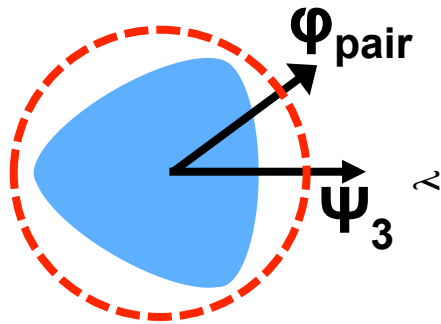


- Weak centrality dependence of v_3
- Initial ϵ_3 has centrality dependence

🍣 Final ϵ_3 has any centrality dependence?



Azimuthal HBT radii w.r.t Ψ_3



PHENIX Preliminary

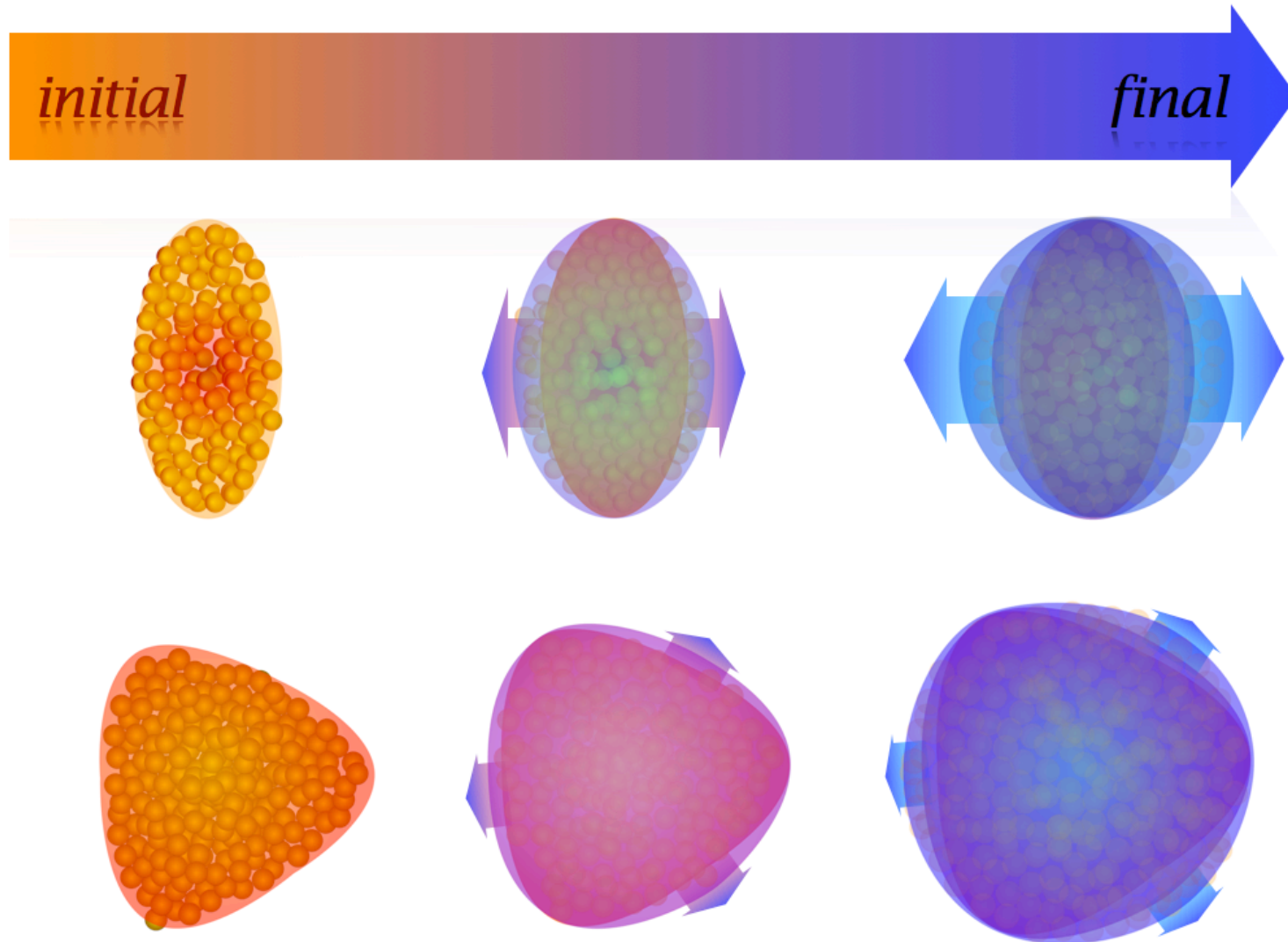
Au+Au 200GeV $\pi^+\pi^+$ & $\pi^-\pi^-$

- 0-10%
- 10-20%
- ▲ 20-30%
- ◆ 30-60%

■ R_{side} is almost flat

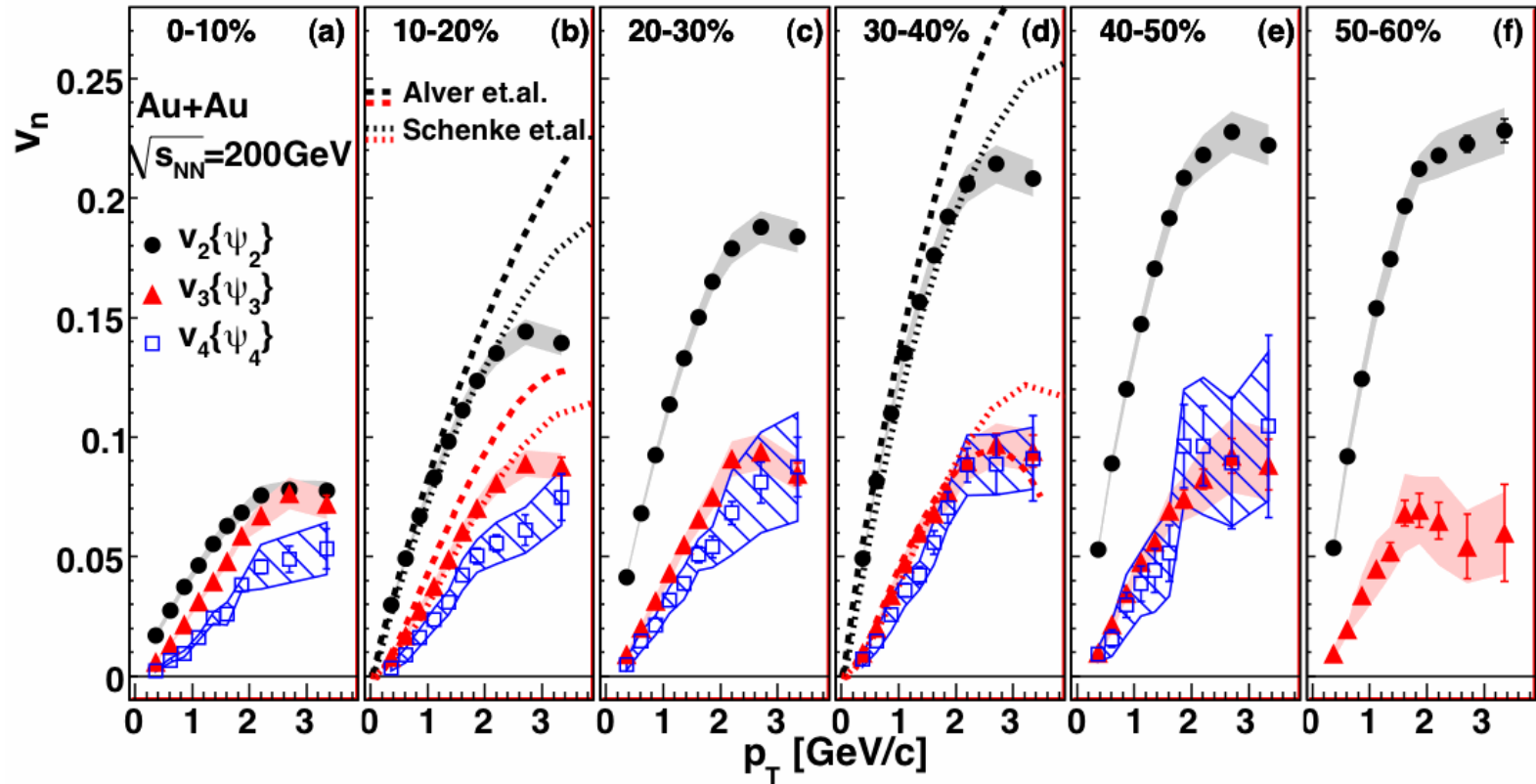
■ R_{out} have a oscillation in most central collisions

Image of initial/final source shape



Charged hadron v_n at PHENIX

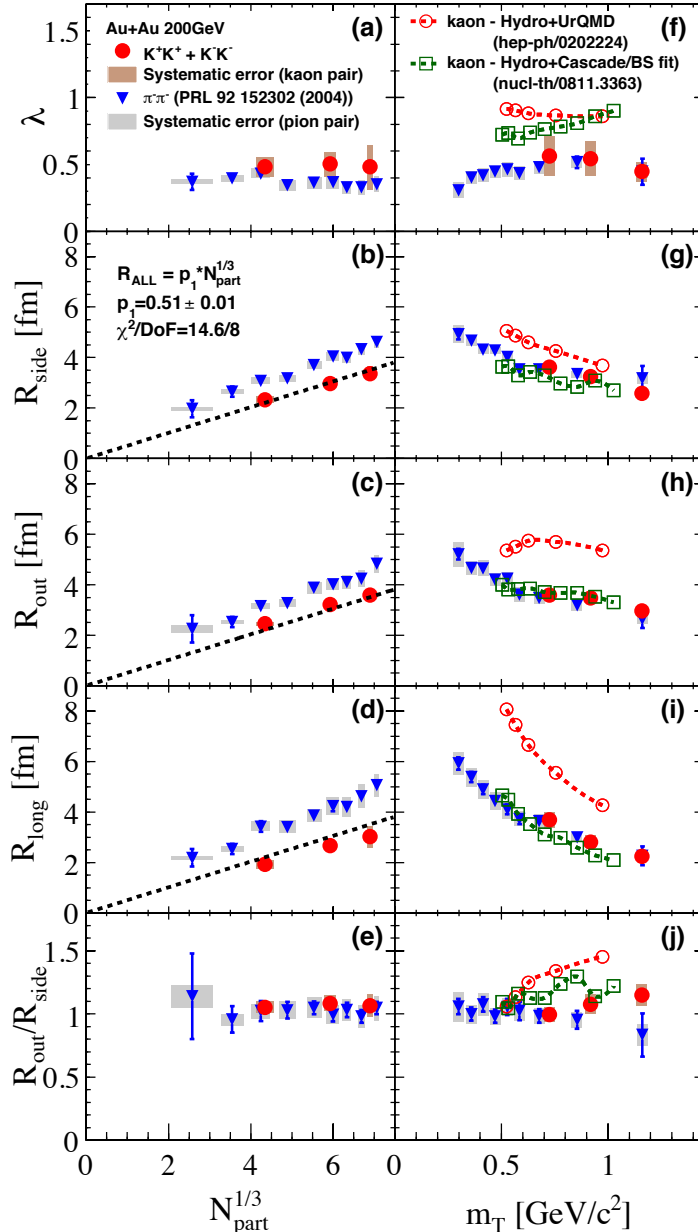
PRL.107.252301



- v_2 increases with increasing centrality, but v_3 doesn't
- v_3 is comparable to v_2 in 0-10%
- v_4 has similar dependence to v_2

The past HBT Results for charged pions and kaons

PRL103.142301(2009)



■ Centrality / m_T dependence have been measured for pions and kaons

✧ higher transverse mass m_T for kaons leads to smaller radii compared to pions

✓ pion $\langle m_T \rangle \sim 0.47$ GeV/c

✓ kaon $\langle m_T \rangle \sim 0.89$ GeV/c

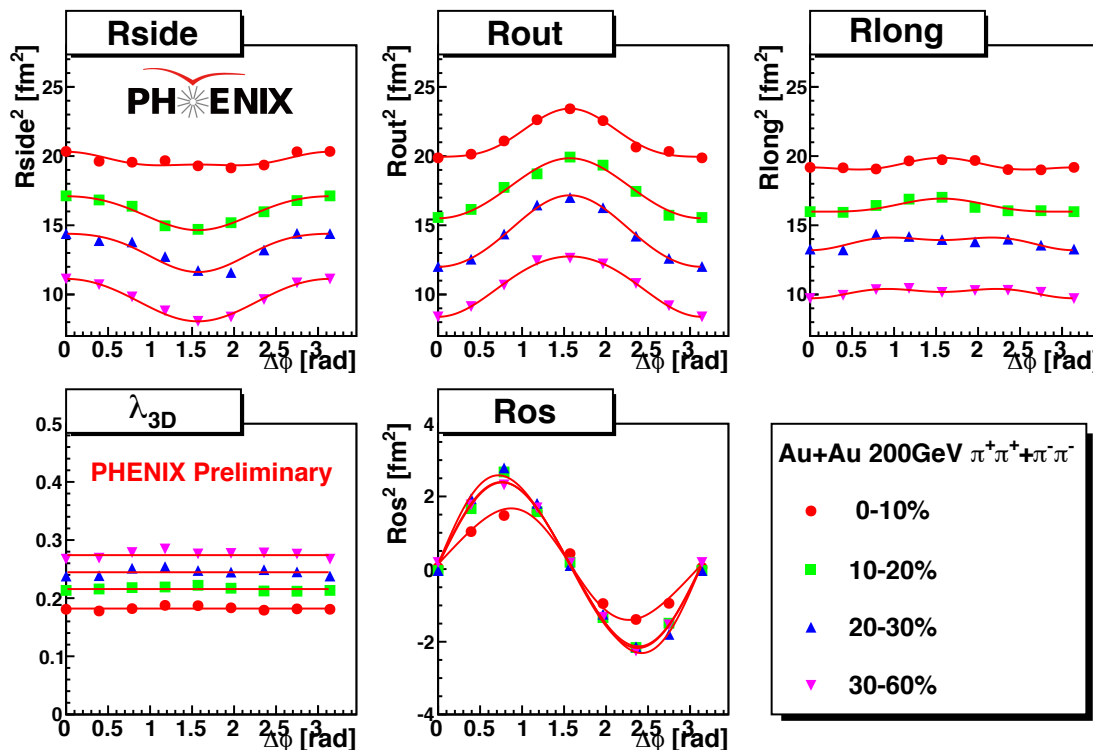
✧ m_T scaling works well

Azimuthal HBT radii for pions

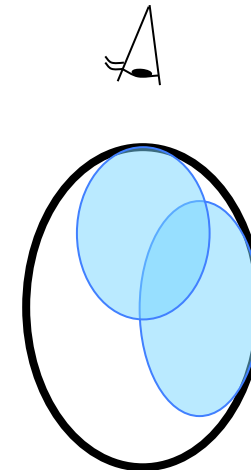
■ Observed oscillation for R_{side} , R_{out} , R_{os}

■ R_{out} in 0-10% has oscillation

✧ Different emission duration between in-plane and out-of-plane?



out-of-plane



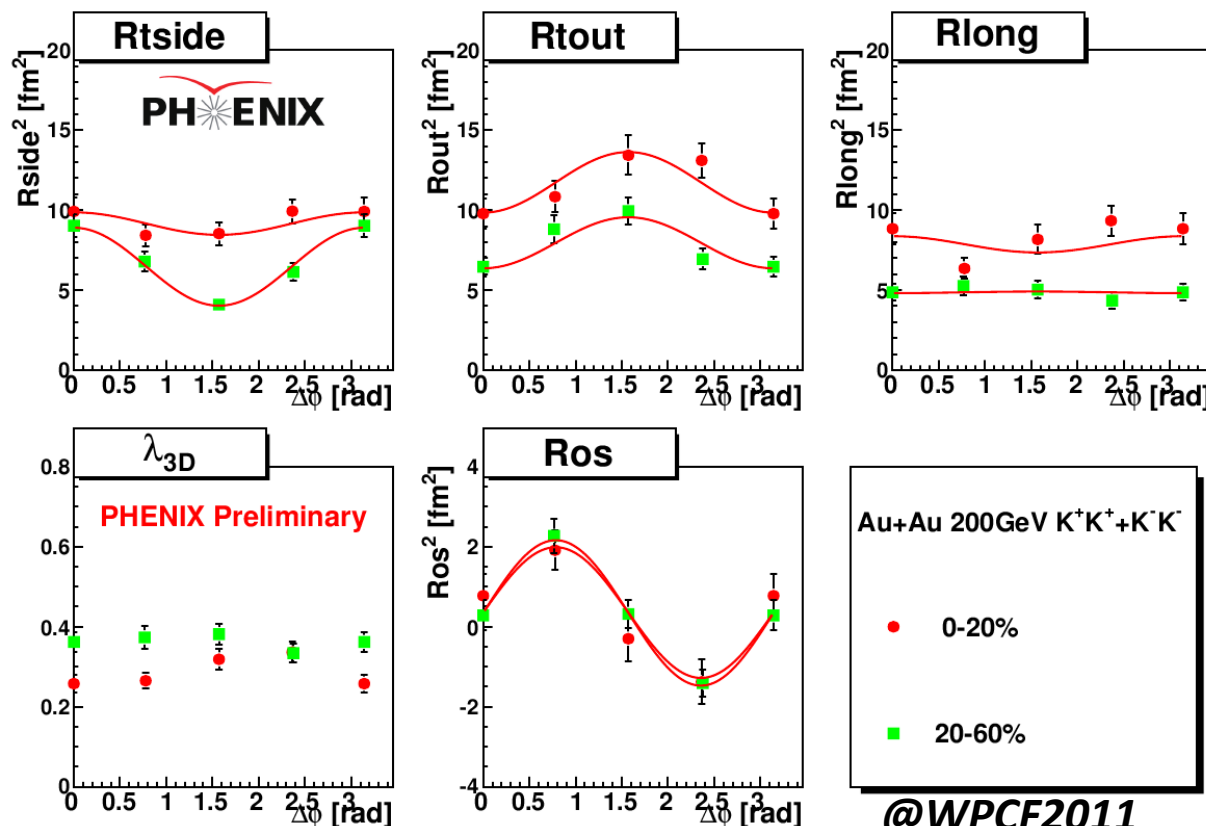
in-plane



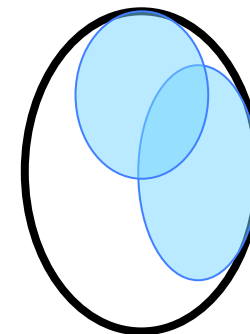
Azimuthal HBT radii for kaons

- Observed oscillation for R_{side} , R_{out} , R_{os}
- Final eccentricity is defined as $\epsilon_{\text{final}} = 2R_{s,2} / R_{s,0}$

$$\diamond R_{s,n}^2 = \langle R_{s,n}^2(\Delta\phi) \cos(n\Delta\phi) \rangle \quad \text{PRC70, 044907 (2004)}$$



in-plane



out-of-plane