



Detailed HBT measurement with respect to the Event plane in Au+Au 200 GeV collisions at PHENIX

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日本物理学会第68回年次大会

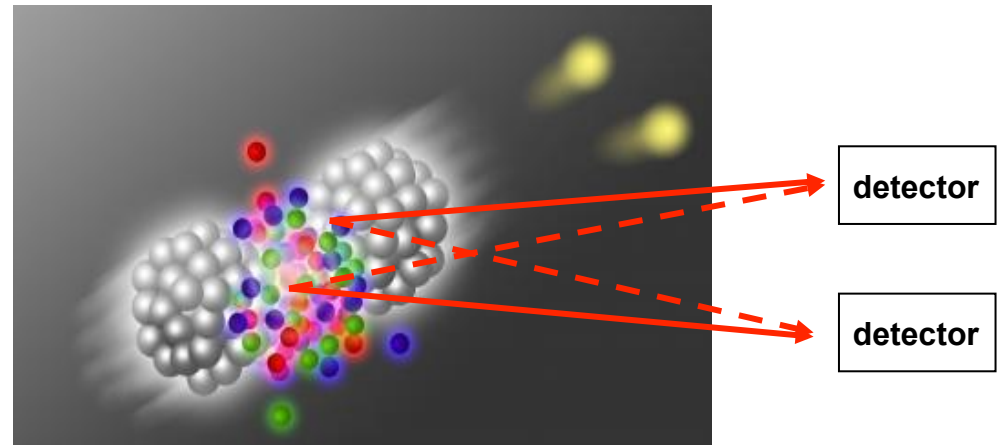
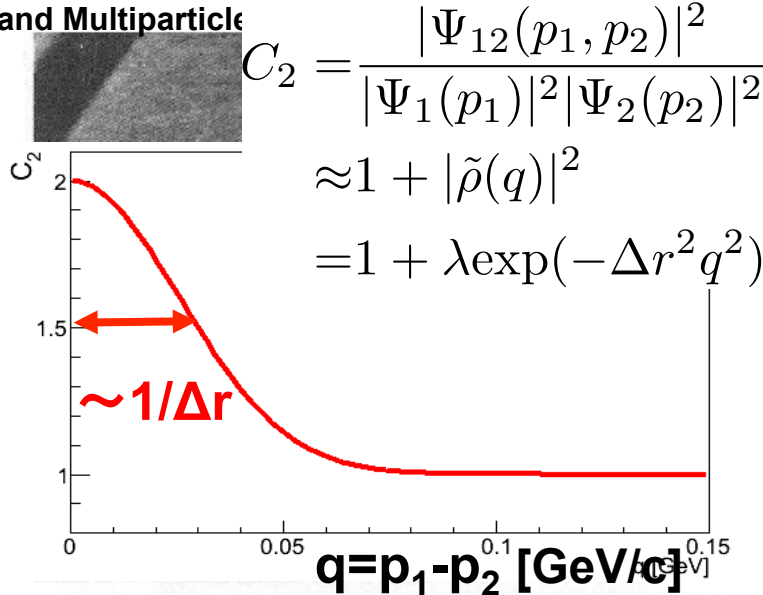


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HBT Interferometry

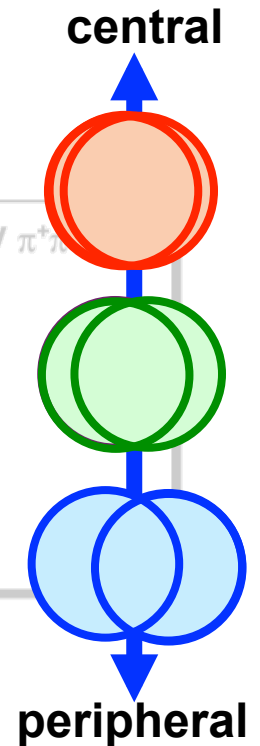
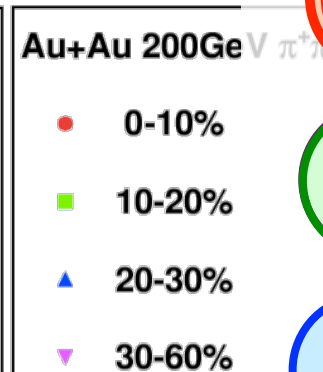
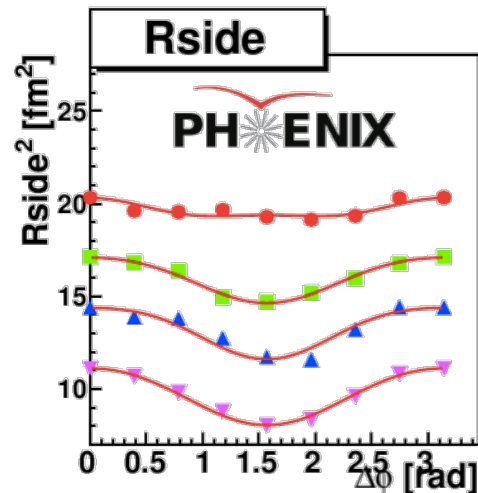
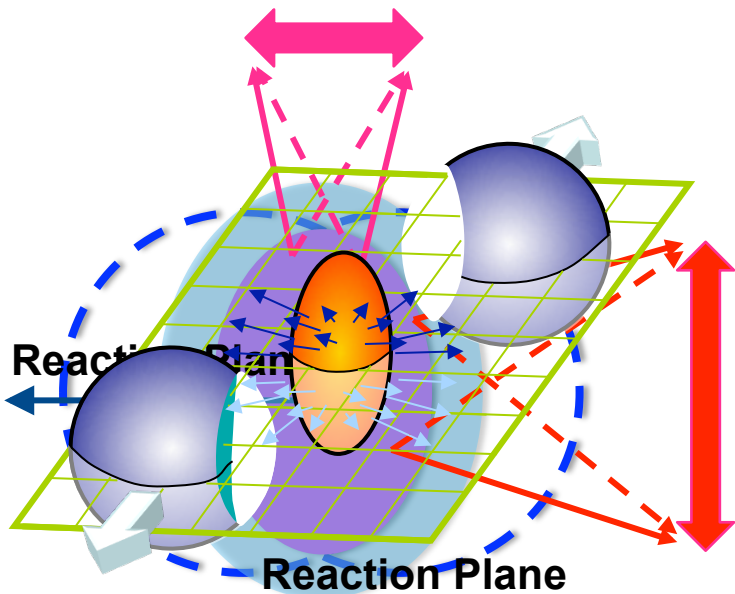
- HBT effect is quantum interference between two identical particles.
- R. Hanbury Brown and R. Twiss
 - ✧ In 1956, they measured the angular diameter of Sirius.
- Goldhaber *et al.*
 - ✧ In 1960, they observed the correlations among identical pions in p+anti-p collision independent of HBT.

G. Goldhaber, Proc. Int. Workshop on Correlations and Multiparticle



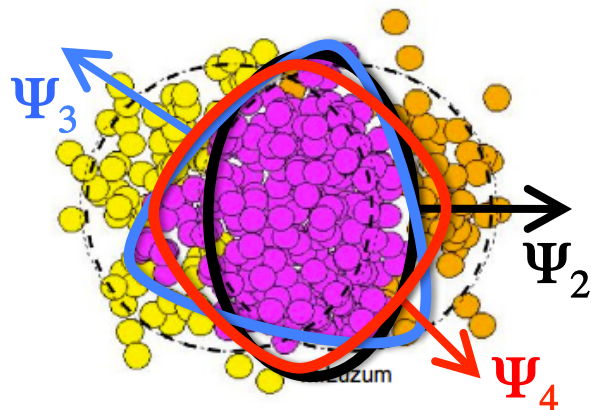
HBT with respect to Reaction Plane

- Azimuthal HBT can give us the source shape at freeze-out.
- Final eccentricity is determined by **initial eccentricity**, **velocity profile** and **expansion time**.
- Very useful tool to investigate space-time evolution in HI !



Azimuthal HBT w.r.t 3rd-order event plane

- Higher-order flow v_n and Event plane Ψ_n

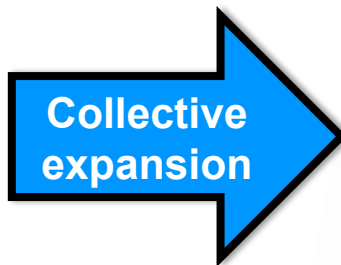
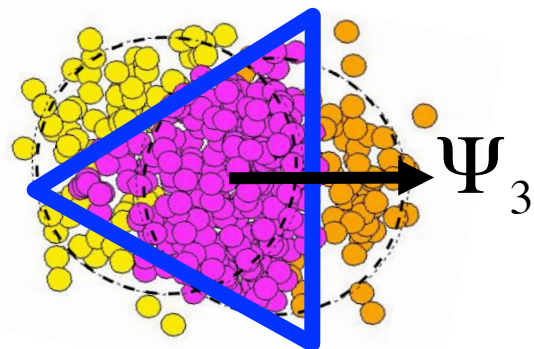


$$\frac{dN}{d\phi} \propto 1 + 2v_2 \cos 2(\phi - \Psi_2) + 2v_3 \cos 3(\phi - \Psi_3) + 2v_4 \cos 4(\phi - \Psi_4)$$

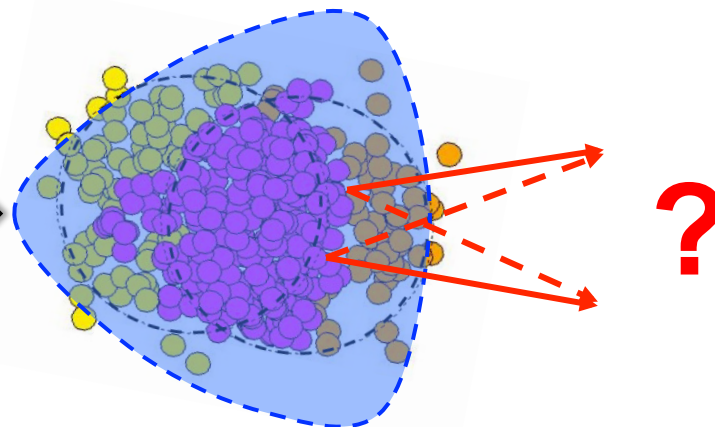
$$v_n = \langle \cos n(\phi - \Psi_n) \rangle$$

- Is the deformation due to initial fluctuations is preserved until freeze-out?

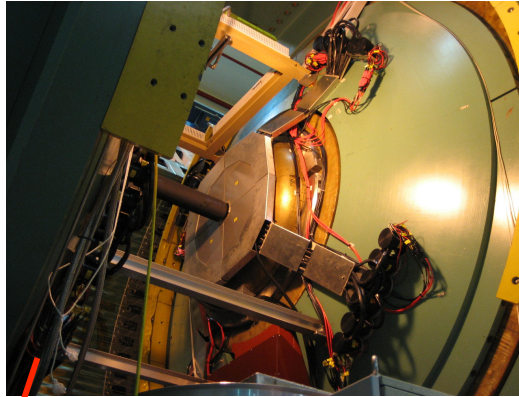
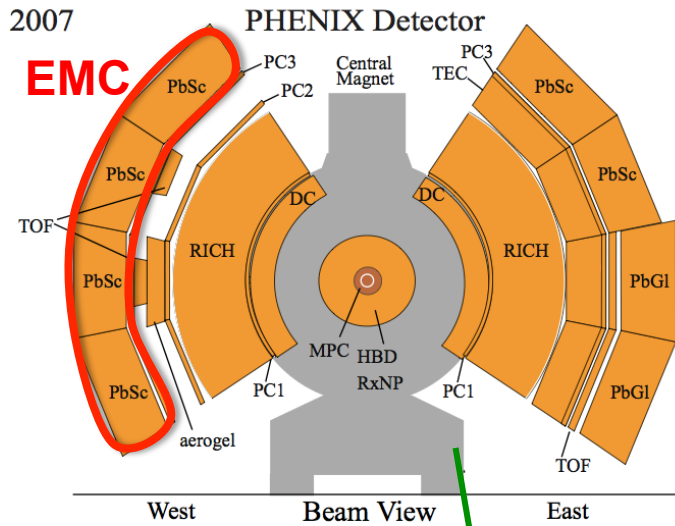
Initial spatial fluctuation



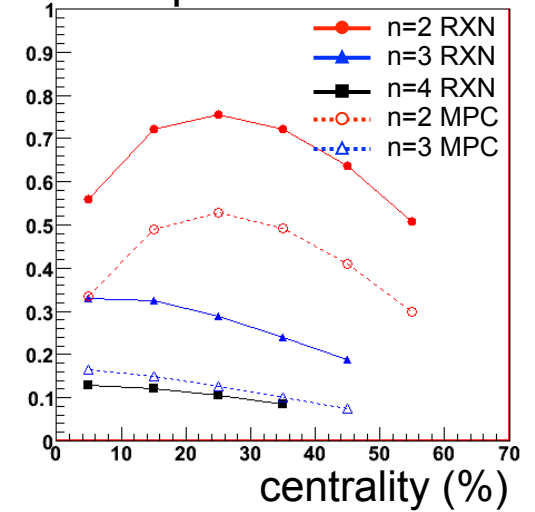
What is final shape ?



Measurement by PHENIX Detectors



Event plane resolution

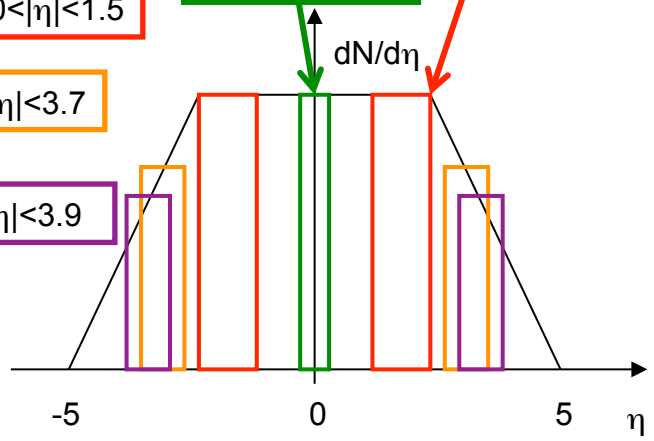


RXN in: $1.5 < |\eta| < 2.8$
& out: $1.0 < |\eta| < 1.5$

CNT: $|\eta| < 0.35$

MPC: $3.1 < |\eta| < 3.7$

BBC: $3.0 < |\eta| < 3.9$



- ★ PID by EMC-PbSc
 - ➡ select charged π
- ★ Ψ_n by forward detector RXN
- ★ Correlation function C_2

$$C_2 = \frac{R(q)}{M(q)}$$

$R(q), M(q)$: relative momentum dist.
for real and mixed pairs

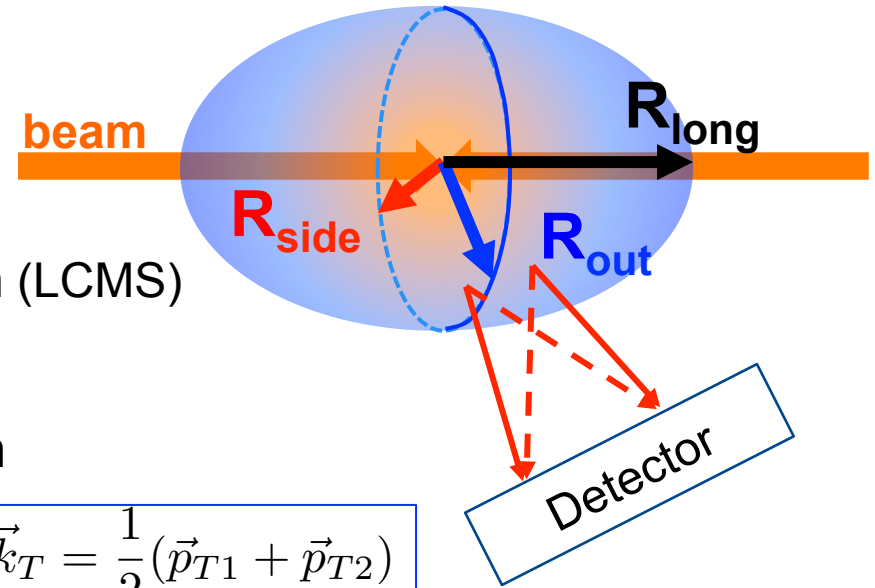
3-dimensional HBT analysis

■ “Out-Side-Long” system

- ✧ Bertsch-Pratt parameterization
 - ✓ Longitudinally Co-Moving System (LCMS)

■ Core-halo model

- ✧ To deal with Coulomb interaction



$$C_2 = C_2^{core} + C_2^{halo}$$

$$= N[\lambda(1 + G)F] + [1 - \lambda]$$

$$\vec{k}_T = \frac{1}{2}(\vec{p}_{T1} + \vec{p}_{T2})$$

$$\vec{q}_{out} \parallel \vec{k}_T, \vec{q}_{side} \perp \vec{k}_T$$

$$G = \exp(-R_{side}^2 q_{side}^2 - R_{out}^2 q_{out}^2 - R_{long}^2 q_{long}^2 - 2R_{os} q_{side} q_{out})$$

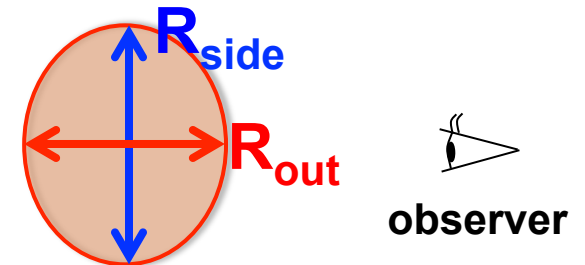
λ : chaoticity

R_{side} : transverse size

R_{out} : transverse size + emission duration

R_{os} : cross term between “out” and “side”

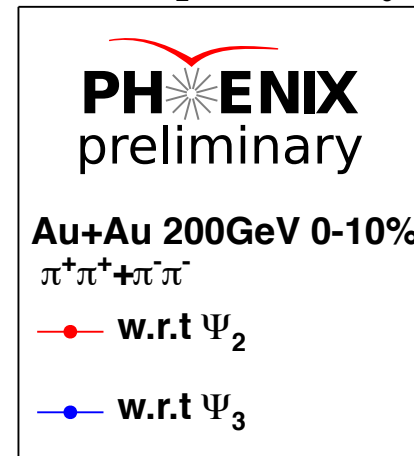
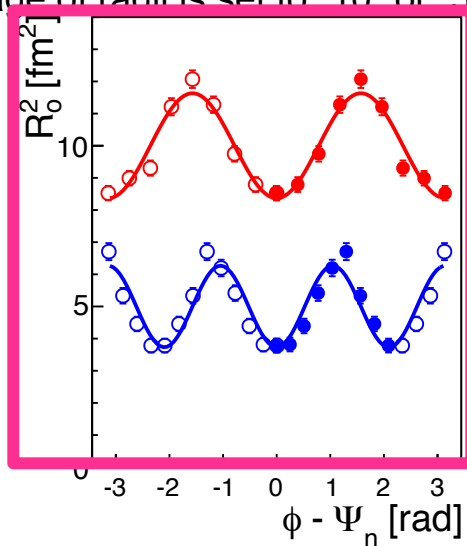
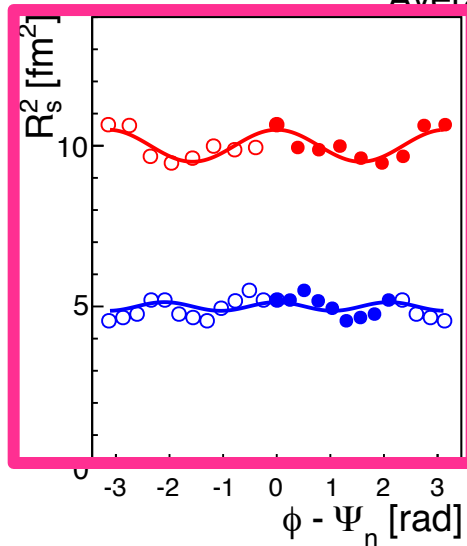
R_{long} : longitudinal size



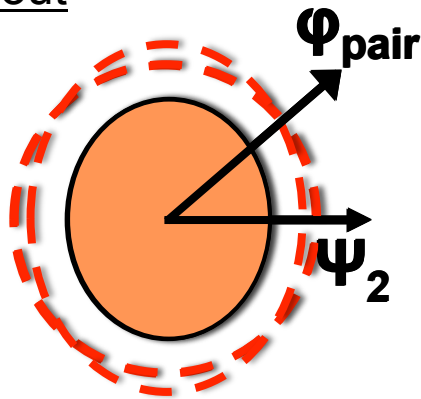
Comparison of 2nd and 3rd order component

- In 0-10%, R_{out} have stronger oscillation for Ψ_2 and Ψ_3 than R_{side}
- ✧ Does the emission duration depend on azimuthal angle ?
- ✧ Different sensitivity for possible sources to make the oscillation ?

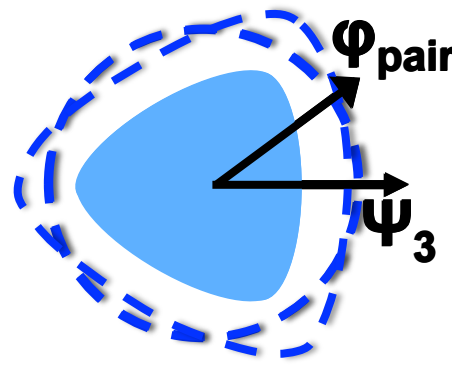
Average of radii is set to "10" or "5" for w.r.t Ψ_2 and w.r.t Ψ_3



R_{out}



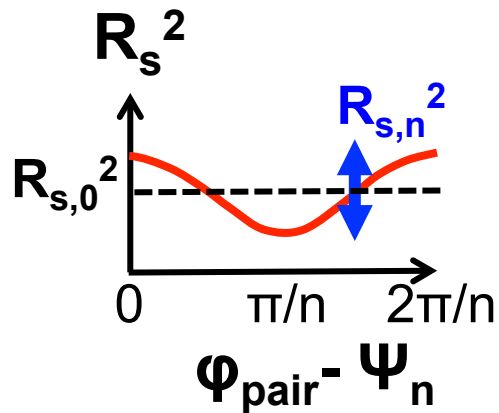
R_{side}



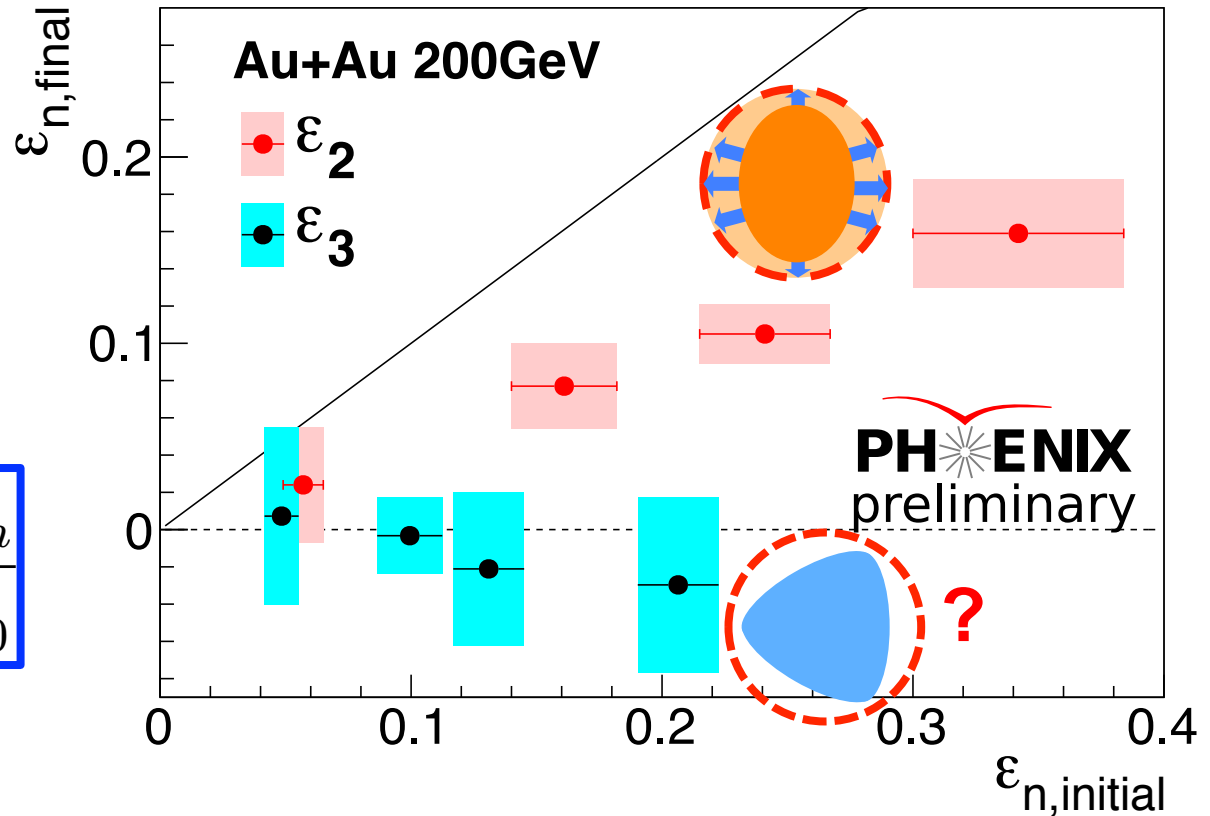
Oscillation of R_s

- Relative amplitude of R_s for 2nd-order is used to represent “Eccentricity” at freeze-out

✧ Strong expansion to in-plane direction, but still elliptical shape !



$$\epsilon_{n,final} = 2 \frac{R_{s,n}^2}{R_{s,0}^2}$$



- ☆ Relative amplitudes for 3rd-order show zero~negative.
What does it indicate? Zero triangularity?

Simulation for Triangular shape

■ Main possible sources to make Ψ_3 dependence of HBT radii

- ✧ Spatial triangular shape in expanding source
- ✧ Triangular flow v_3

■ Setup of Monte-Carlo Simulation

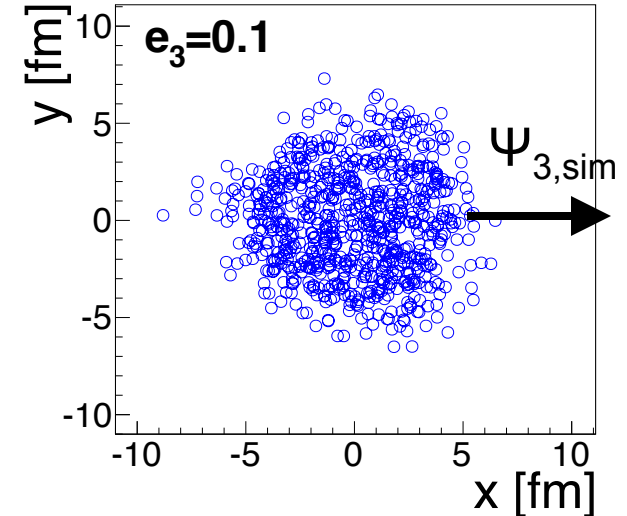
- ✧ Assuming Woods-Saxon distribution
- ✧ Triangular shape controlled by “ e_3 ”
- ✧ Triangular flow controlled by “ β_3 ”
 - ✓ β_0 for radial flow is fixed as 0.8.

$$R_{xy} = R(1 - e_3 \cos(3\Delta\phi))$$

$$\beta_T = \tanh(\rho)$$

$$\rho = \tanh^{-1}[\beta_0 + \beta_3 \cos(3\Delta\phi)] \left(\frac{r_{xy}}{R_{xy}} \right)$$

- ✧ HBT correlation: $1 + \cos(\Delta r \times \Delta p)$
- ✧ p_T spectra with $T_f = 160$ MeV
- ✧ No Coulomb interaction, no opacity



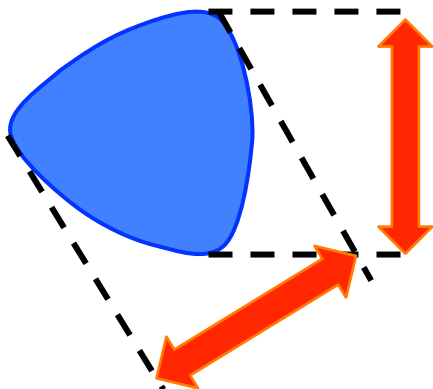
Simulation Results

■ Static source

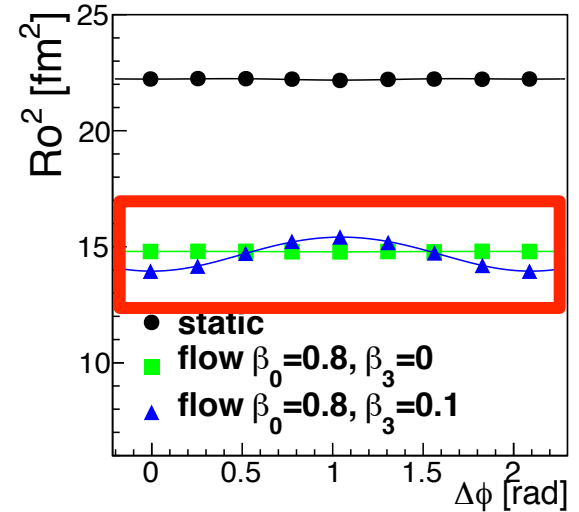
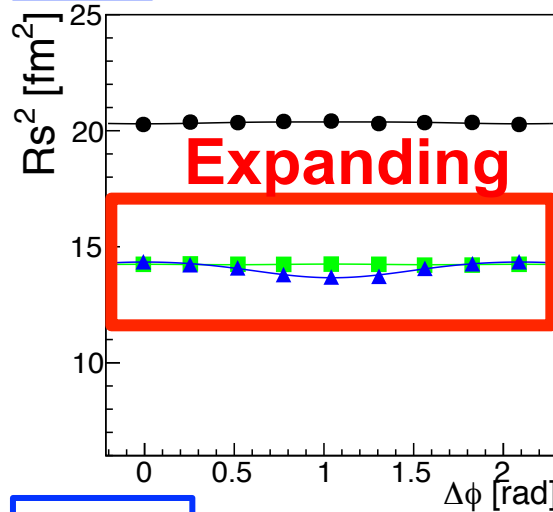
- ✧ No oscillation for triangular shape

■ Expanding source

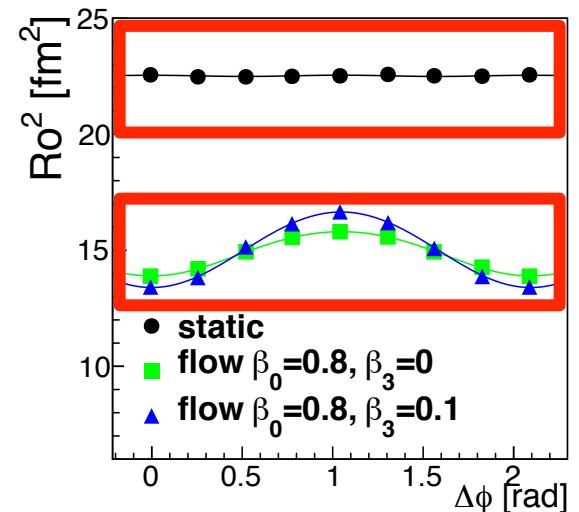
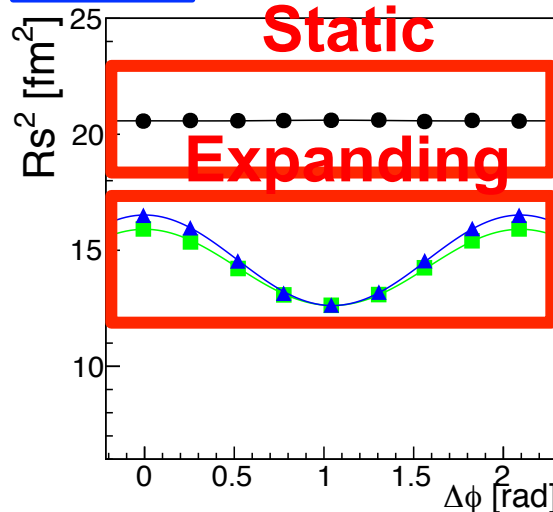
- ✧ Triangular shape
 - ✓ Oscillation appears !
- ✧ Spherical shape
 - ✓ β_3 makes oscillation !



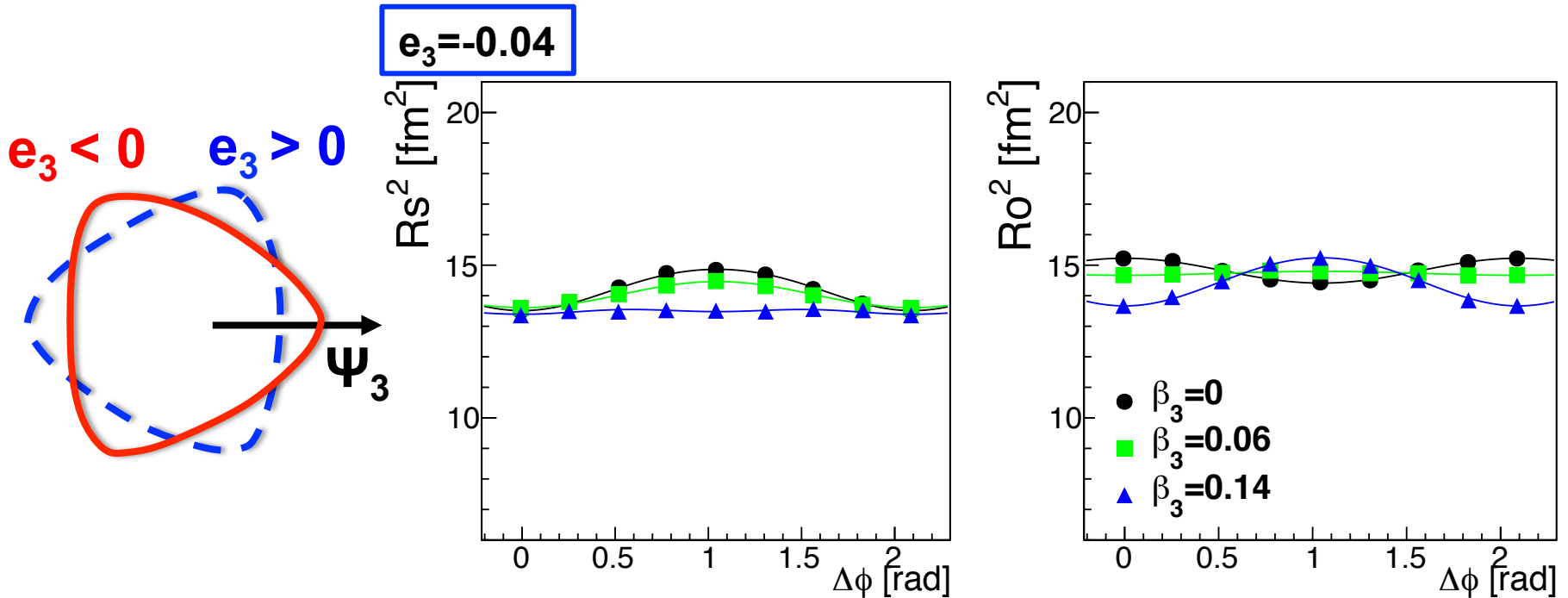
$e_3=0$



$e_3=0.1$



Simulation Results



- Oscillation is determined by triangular shape and β_3
- Zero oscillation does not necessarily indicate the spherical source
 - ✧ Data is close to the situation with $e_3 < 0$ and finite β_3
 - ✧ Negative e_3 may indicate that initial triangular deformation is modified by triangular flow

Summary

■ Azimuthal HBT radii w.r.t v_3 plane

- ✧ First measurement of Ψ_3 dependent HBT radii have been presented.
- ✧ Oscillation of R_s is very weak, almost zero or slightly negative sign.
- ✧ R_0 clearly has finite oscillation in most central collisions.
 - 👉 Different emission duration for azimuthal angle ?

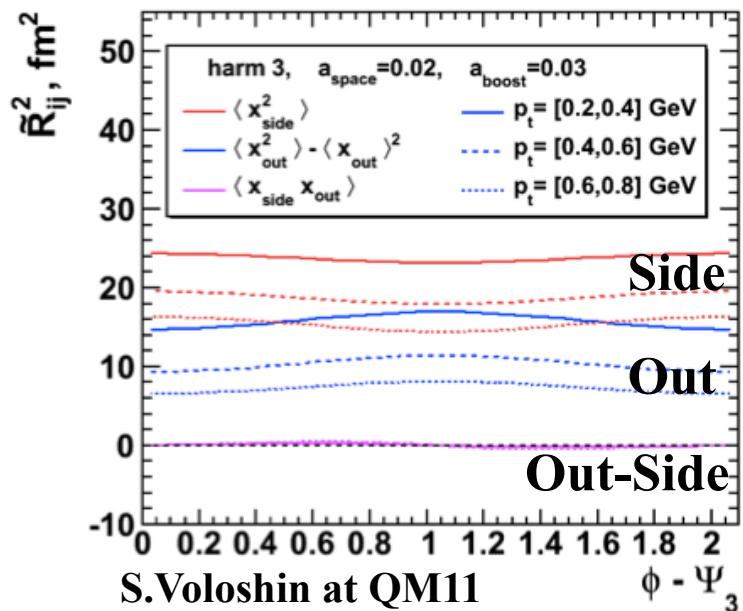
■ Monte-Carlo simulation of HBT for triangular source

- ✧ Ψ_3 dependence of HBT radii will be determined by the balance of triangular flow and spatial triangularity.
- ✧ Data in 0-10% is close to the source with negative e_3 and finite β_3 . Initial triangular deformation may be modified by triangular flow.

Back up

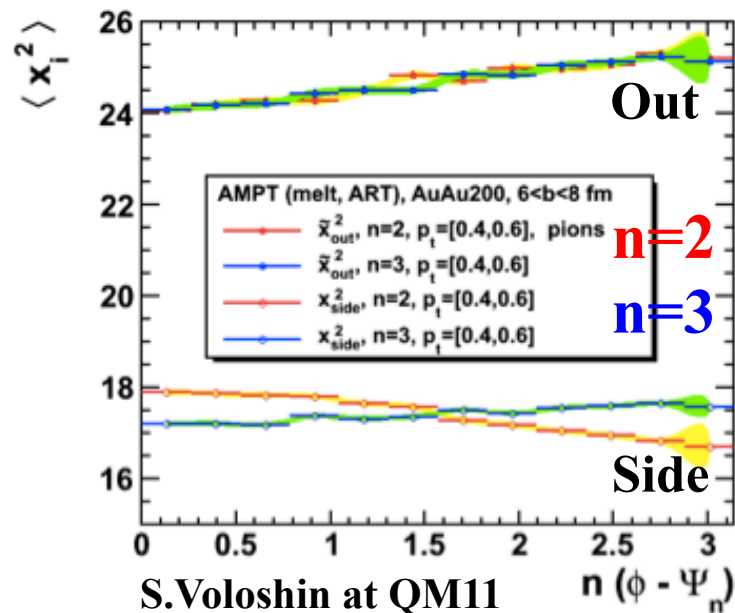
Model Calculations

Blast-wave model



$$T=100[\text{MeV}], \rho=r'\rho_{\text{max}}(1+\cos(n\phi))$$

AMPT

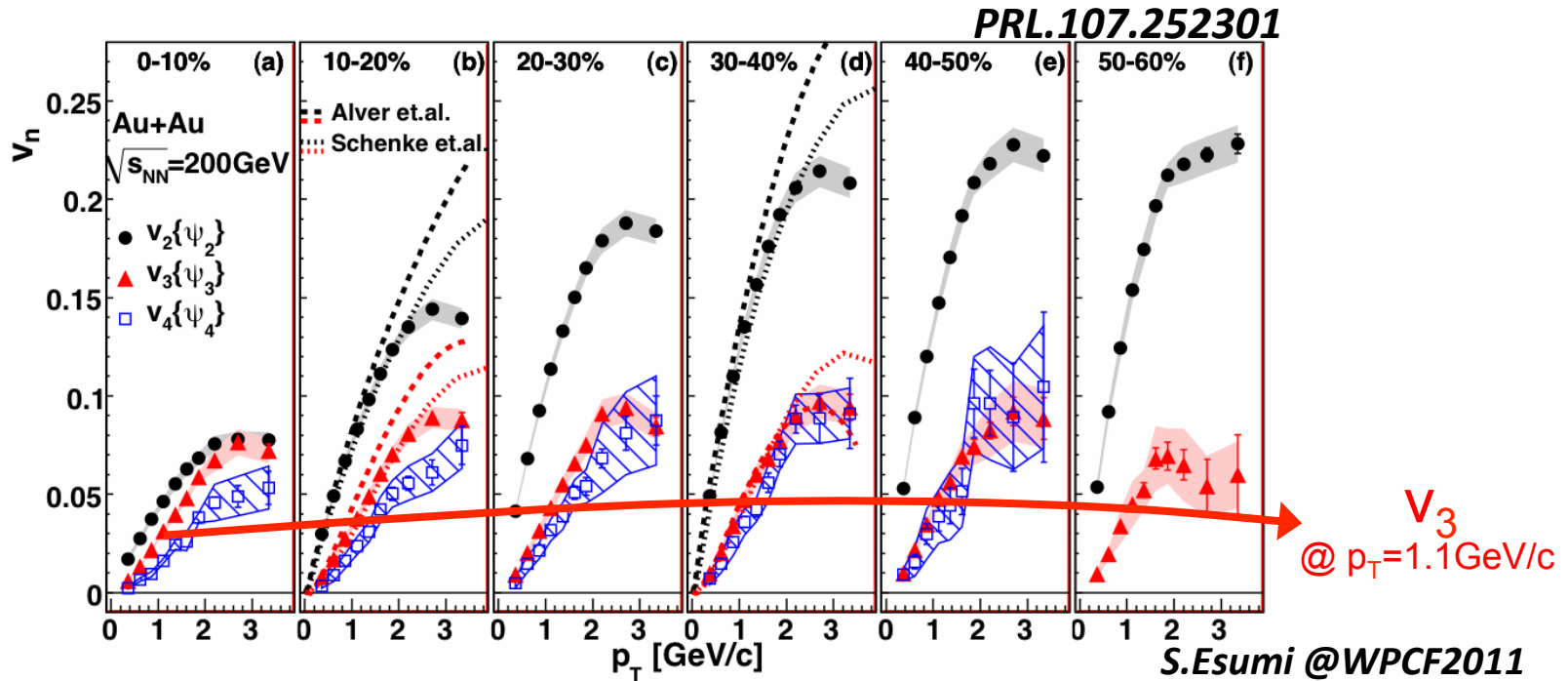


Both models predict weak oscillation will be seen in R_{side} and R_{out} .

BW \triangleright **Opposite** sign of R_{side} and R_{out}

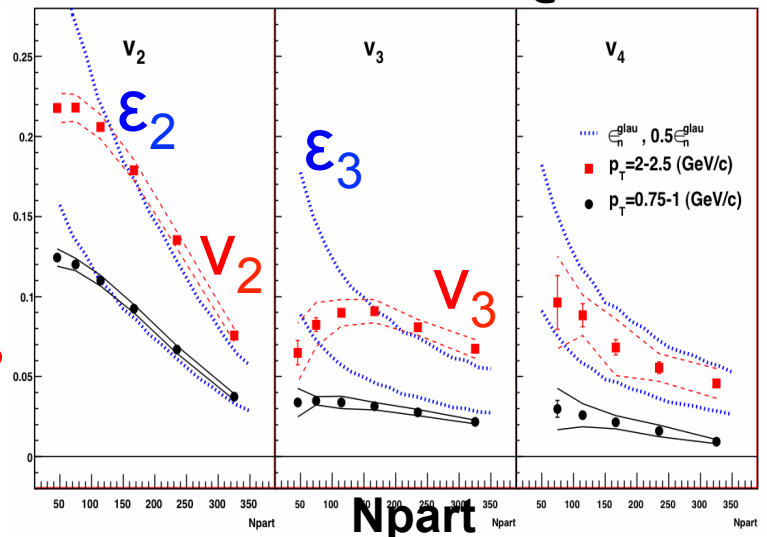
AMPT \triangleright **Same** sign of R_{side} and R_{out}

Centrality dependence of v_3 and ϵ_3



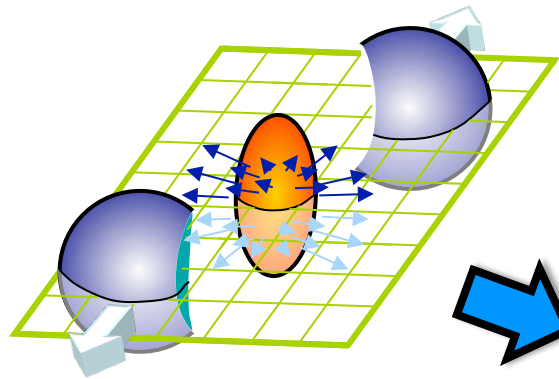
- Weak centrality dependence of v_3
- Initial ϵ_3 has centrality dependence

🍄 Final ϵ_3 has any centrality dependence?

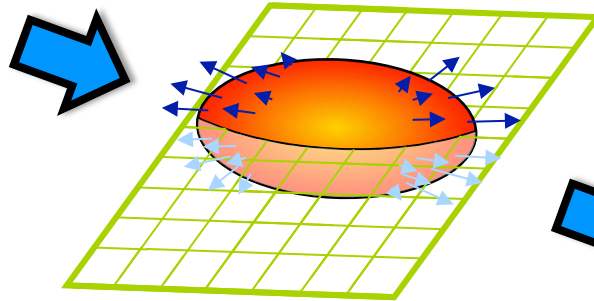


Azimuthal HBT w.r.t v_2 plane

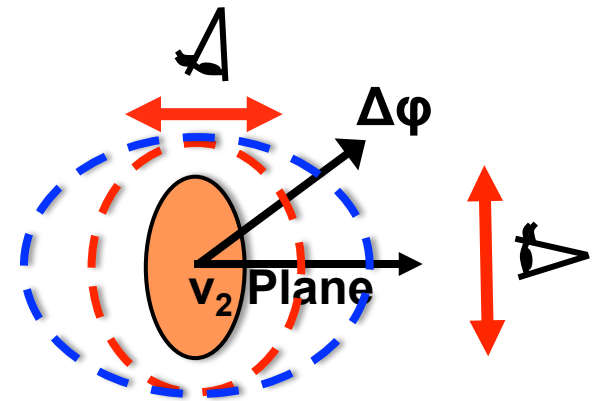
Initial spatial eccentricity



Momentum anisotropy v_2



What is the final eccentricity ?

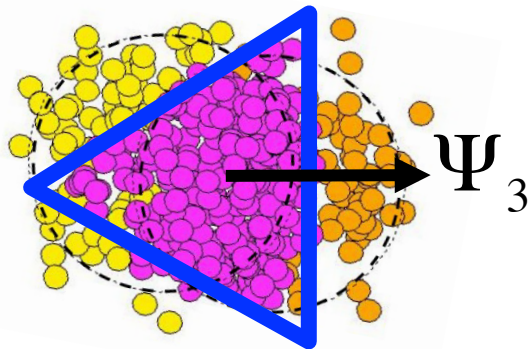


■ Final eccentricity can be measured by azimuthal HBT

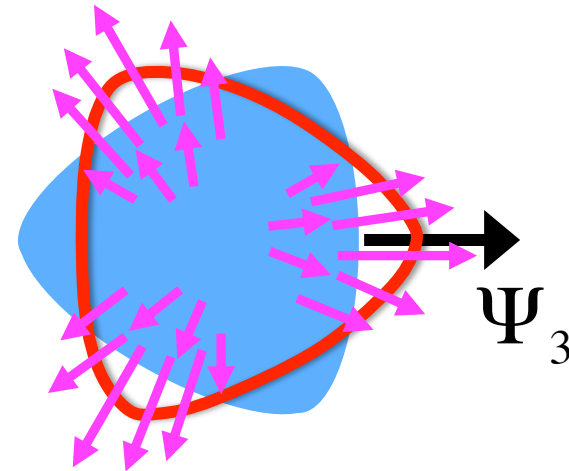
- ✧ It depends on initial eccentricity, pressure gradient, expansion time, and velocity profile, etc.
- ✧ Good probe to investigate system evolution

Azimuthal HBT w.r.t v_3 plane

Initial spatial fluctuation
(triangularity)



Momentum anisotropy
triangular flow v_3



- Final triangularity could be observed by azimuthal HBT w.r.t v_3 plane (Ψ_3) if it exists at freeze-out

- ✧ Related to initial triangularity, v_3 , and expansion time, etc.
- ✧ Detailed information on space-time evolution can be obtained

3D HBT radii

- “Out-Side-Long” system

- ✧ Bertsch-Pratt parameterization

- Core-halo model

- ✧ Particles in core are affected by coulomb interaction

$$C_2 = C_2^{core} + C_2^{halo}$$

$$= N[\lambda(1+G)F] + [1-\lambda]$$

$$G = \exp(-R_{inv}^2 q_{inv}^2)$$

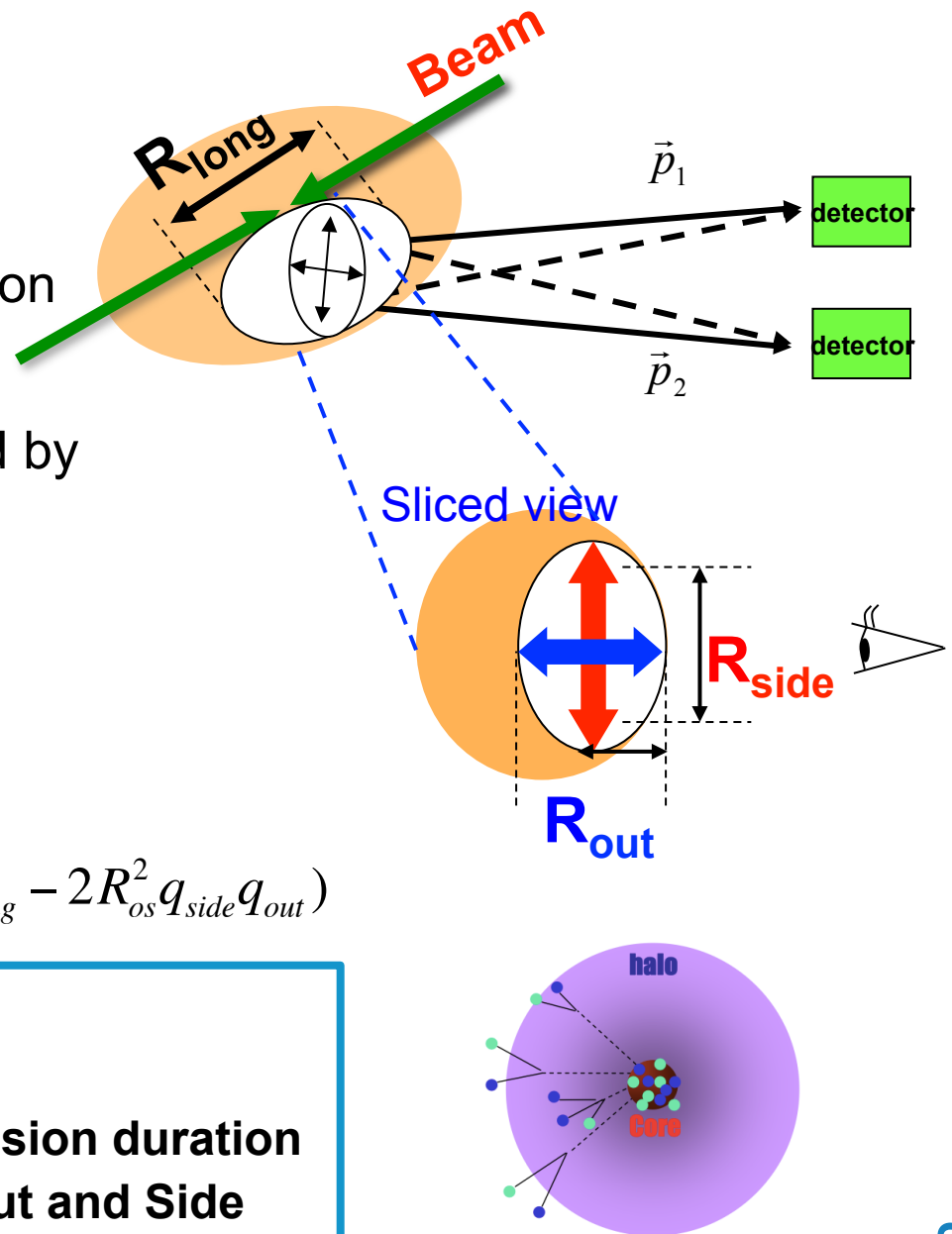
$$= \exp(-R_{side}^2 q_{side}^2 - R_{out}^2 q_{out}^2 - R_{long}^2 q_{long}^2 - 2R_{os} q_{side} q_{out})$$

R_{long} : Longitudinal size

R_{side} : Transverse size

R_{out} : Transverse size + emission duration

R_{os} : Cross term between Out and Side



Analysis method for HBT

■ Correlation function

$$C_2 = \frac{R(q)}{M(q)}$$

- ✧ Ratio of real and mixed q-distribution of pairs
q: relative momentum

■ Correction of event plane resolution

- ✧ U.Heinz et al, PRC66, 044903 (2002)

■ Coulomb correction and Fitting

- ✧ By Sinyukov's fit function
- ✧ Including the effect of long lived resonance decay

$$\begin{aligned} C_2 &= C_2^{core} + C_2^{halo} \\ &= N[\lambda(1+G)F] + [1-\lambda] \\ G &= \exp(-R_{side}^2 q_{side}^2 - R_{out}^2 q_{out}^2 - R_{long}^2 q_{long}^2 - 2R_{os}^2 q_{side} q_{out}) \end{aligned}$$

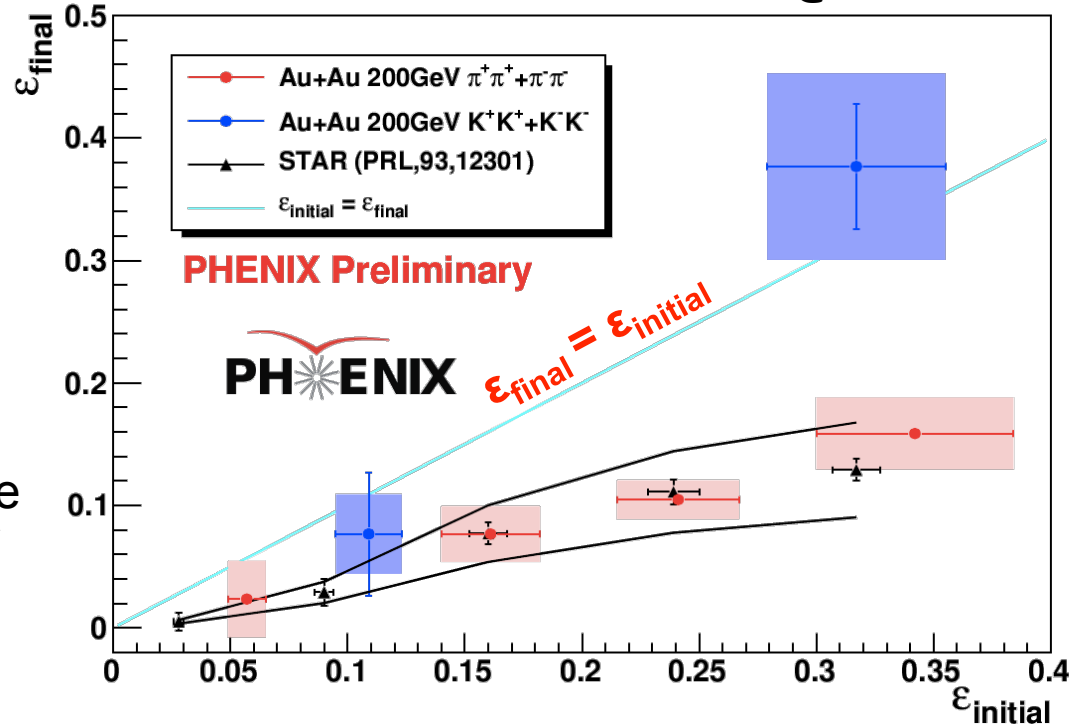
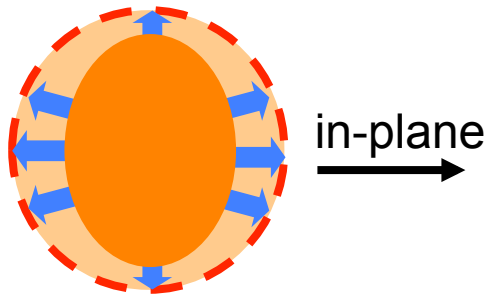
Eccentricity at freeze-out

@WPCF2011

R_s^2 PRC70, 044907 (2004)

$$R_{s,n}^2 = \langle R_{s,n}^2(\Delta\phi) \cos(n\Delta\phi) \rangle$$

$$\epsilon_{final} = 2 \frac{R_{s,2}^2}{R_{s,0}^2}$$



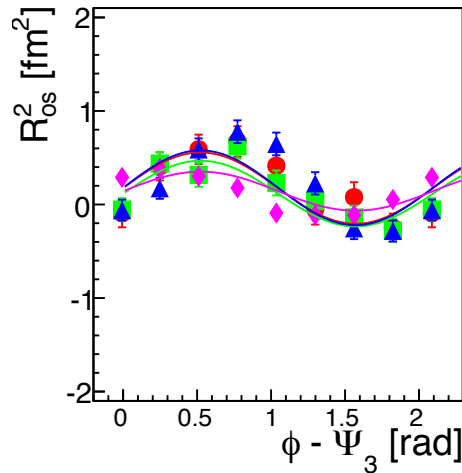
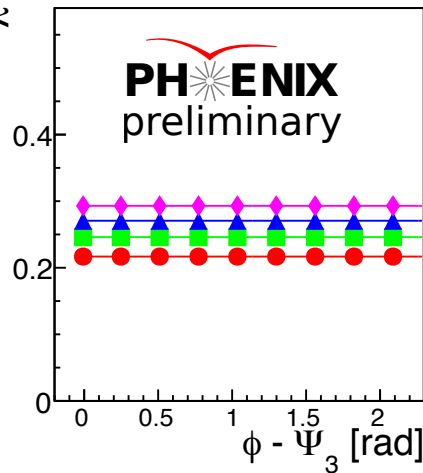
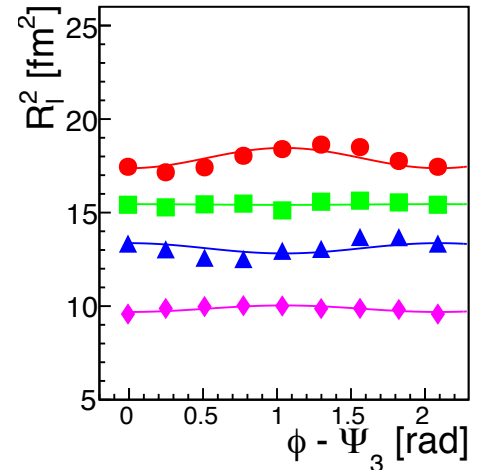
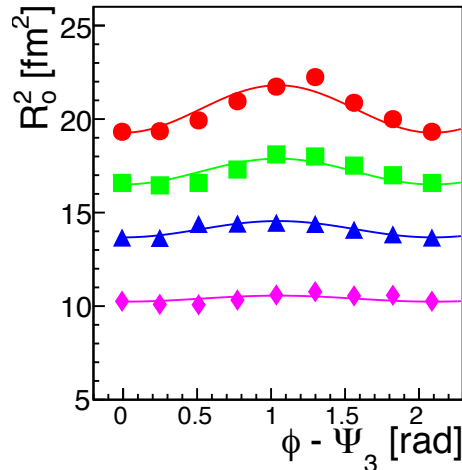
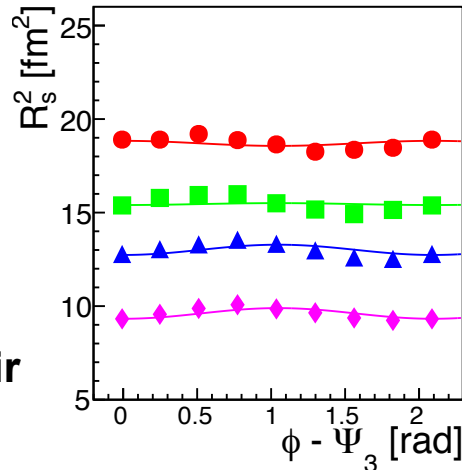
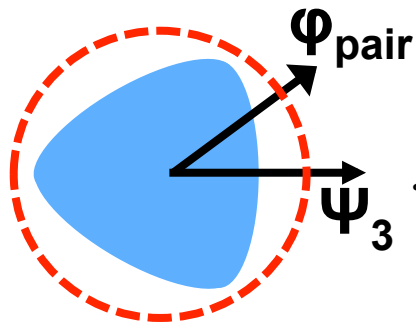
- $\epsilon_{final} \approx \epsilon_{initial}/2$ for pion

- ✧ Indicates that source expands to in-plane direction, and still elliptical shape
- ✧ PHENIX and STAR results are consistent

- $\epsilon_{final} \approx \epsilon_{initial}$ for kaon

- ✧ Kaon may freeze-out sooner than pion because of less cross section
- ✧ Need to check the difference of m_T between π/K ?

Azimuthal HBT radii w.r.t Ψ_3



PHENIX Preliminary

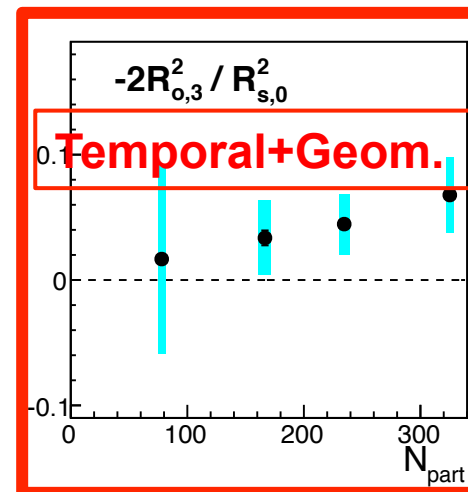
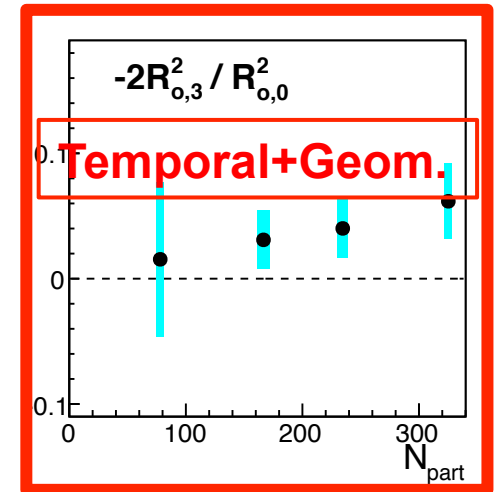
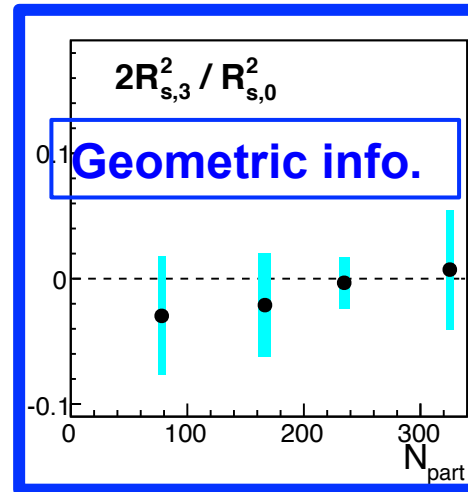
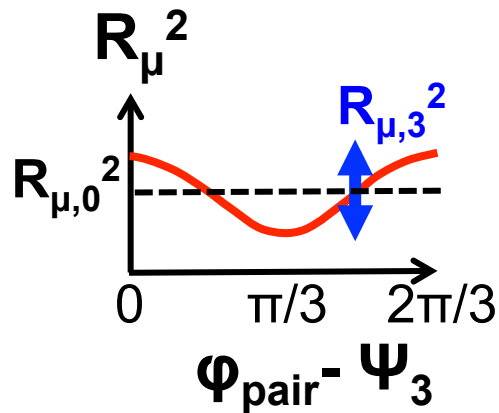
Au+Au 200GeV $\pi^+\pi^+$ & $\pi^-\pi^-$

- 0-10%
- 10-20%
- ▲ 20-30%
- ◆ 30-60%

- R_{side} is almost flat
- R_{out} have a oscillation in most central collisions

Relative amplitude of HBT radii

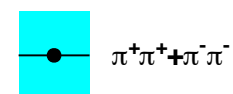
- Similar definition with “final eccentricity”
- Relative amplitude of R_{out} increases with increasing N_{part}



PHENIX Preliminary

PHENIX
preliminary

Au+Au 200GeV



Freeze-out parameters extracted by Blast wave model

S. Mizuno, QM12

■ Blast wave fit for spectra & v_n

✧ Parameters used in the model

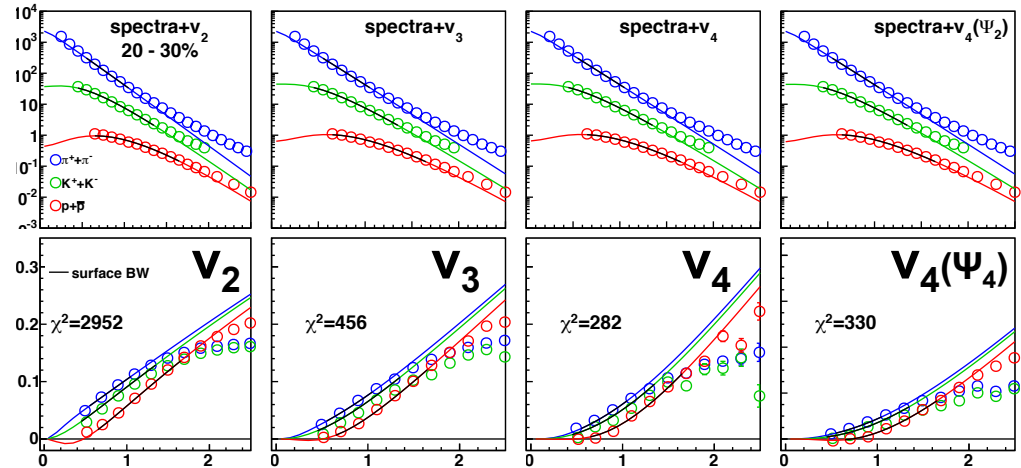
T_f : temperature at freeze-out

ρ_0 : average velocity

ρ_n : anisotropic velocity

s_n : spatial anisotropy

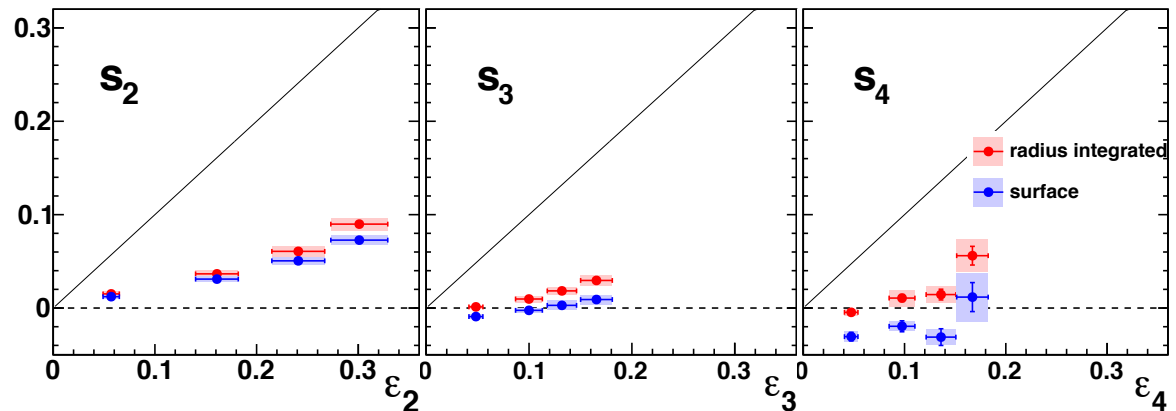
✓ s_2 and s_3 correspond to final eccentricity and triangularity



✧ s_2 increase with going to peripheral collisions

✧ s_3 is almost zero

Initial vs Final spatial anisotropy

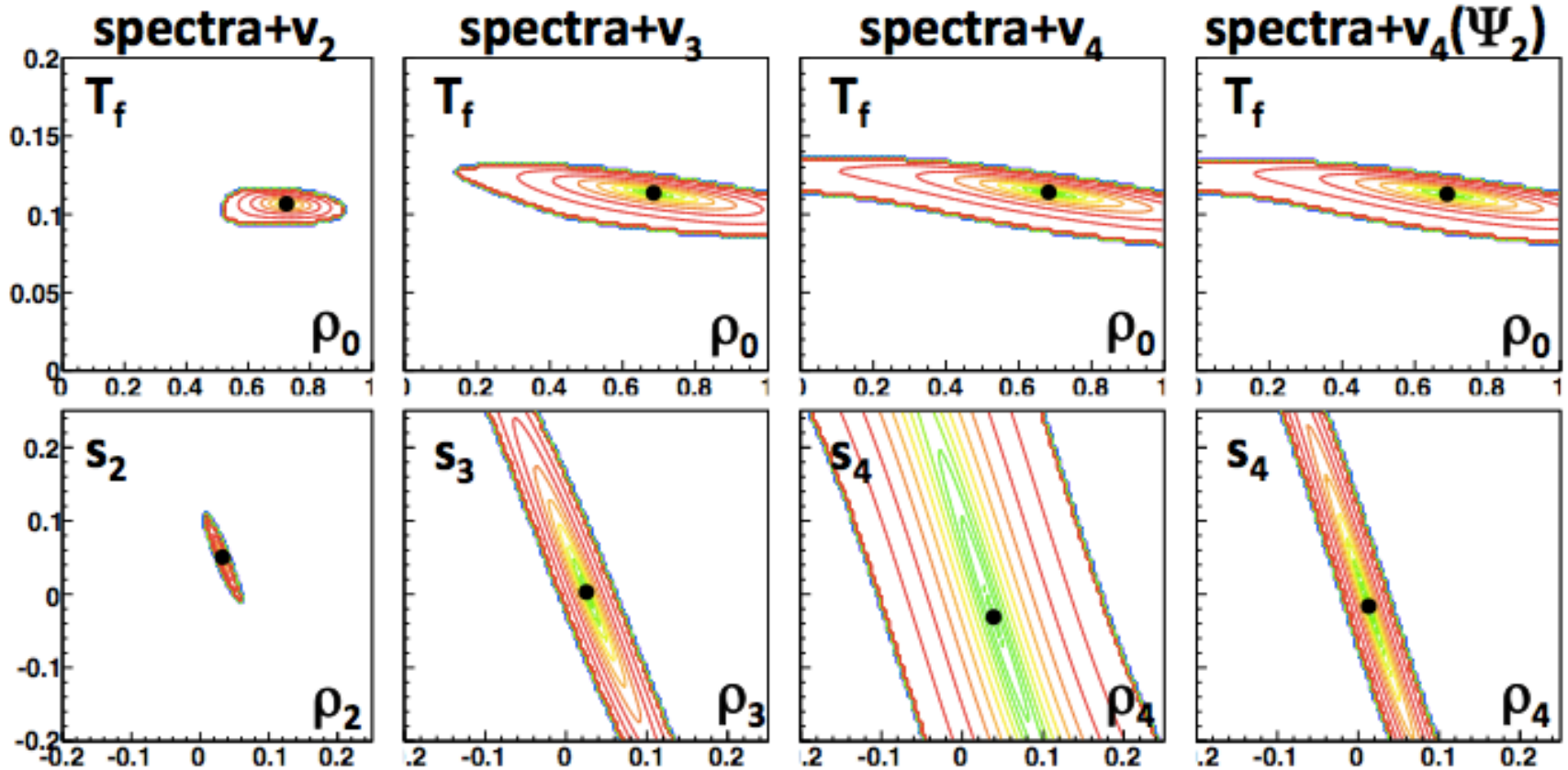


☞ Similar results with HBT

Contour plot ρ_n vs s_n

S. Mizuno, QM12

χ^2 contour plots 20-30%

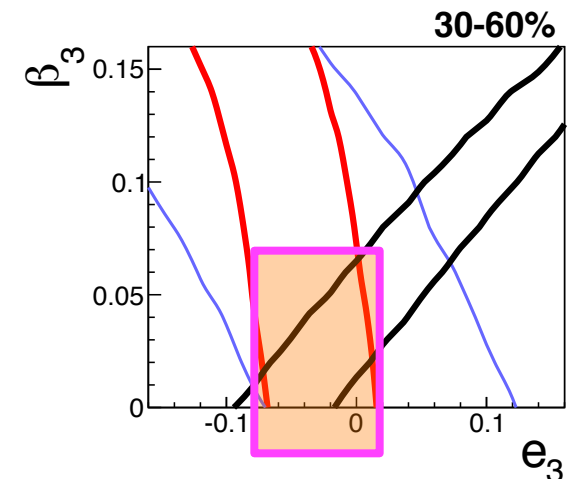
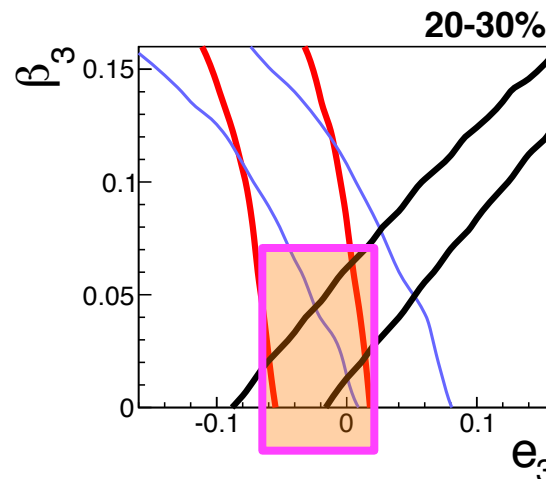
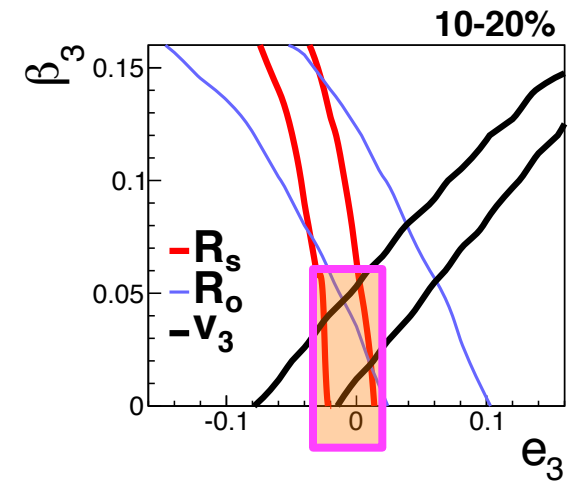
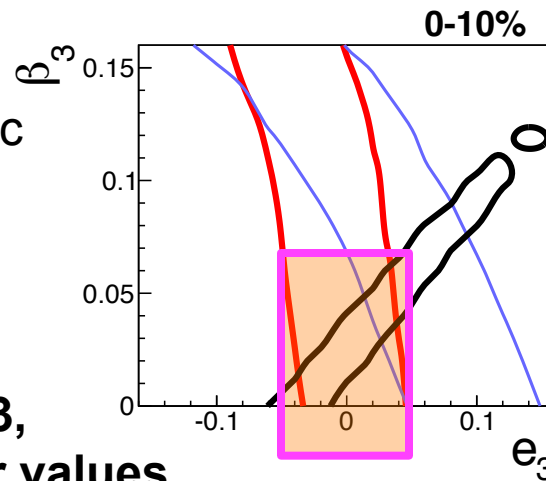
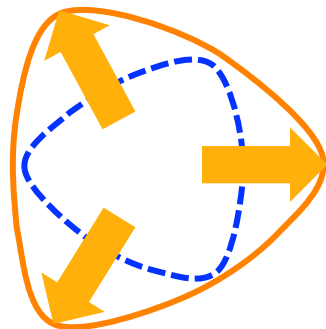


Parameter Search of β_3 vs e_3

- Difference between data and simulation are shown as contour plot

- The contours for R_μ represents the systematic error of the data.

- Overlap of v_3 and R_s indicates 0~negative e_3 , where β_3 shows similar values in all centralities.



★ v_3 flow may overcome the initial triangular deformation !

Summary

■ Azimuthal HBT radii w.r.t v_3 plane

- ✧ First measurement of Ψ_3 dependent HBT radii have been presented.
- ✧ Oscillation of R_s is very weak, almost zero or slightly negative sign.
- ✧ R_o clearly has finite oscillation in most central collisions.
 - 👉 Different emission duration for azimuthal angle ?

■ Monte-Carlo simulation of HBT for triangular source

- ✧ Ψ_3 dependence of HBT radii will be determined by the balance of triangular flow and spatial triangularity.
- ✧ R_s and v_3 indicates that the parameter e_3 has a zero to negative value. Initial triangular deformation may be modified by triangular flow.
- ✧ R_o oscillation doesn't seem to be explained only by e_3 and β_3 .
 - ✓ Related to different sensitivity to β_3 between R_s and R_o ?
 - ✓ Different emission duration for azimuthal angle ?