

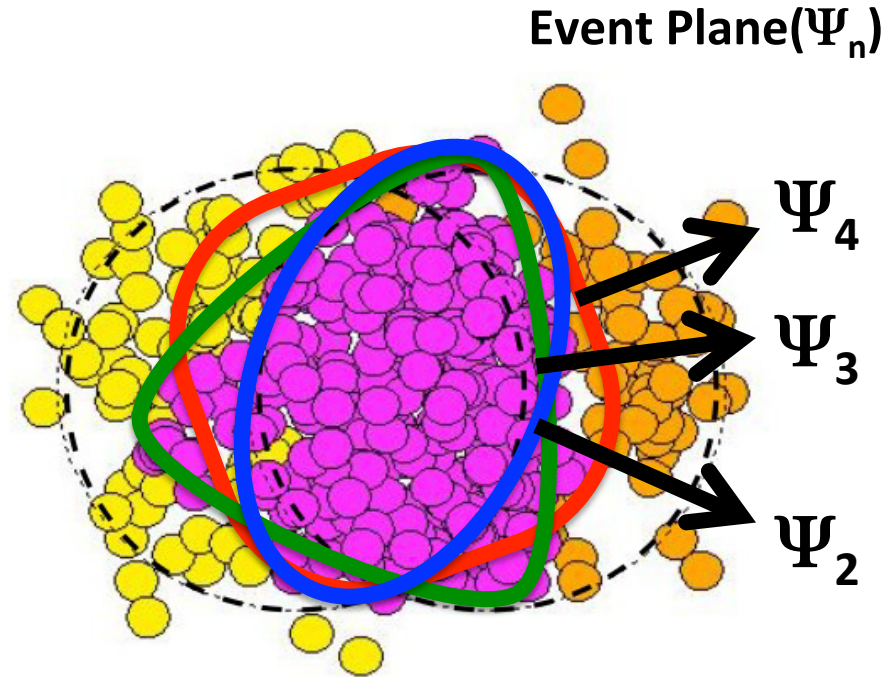
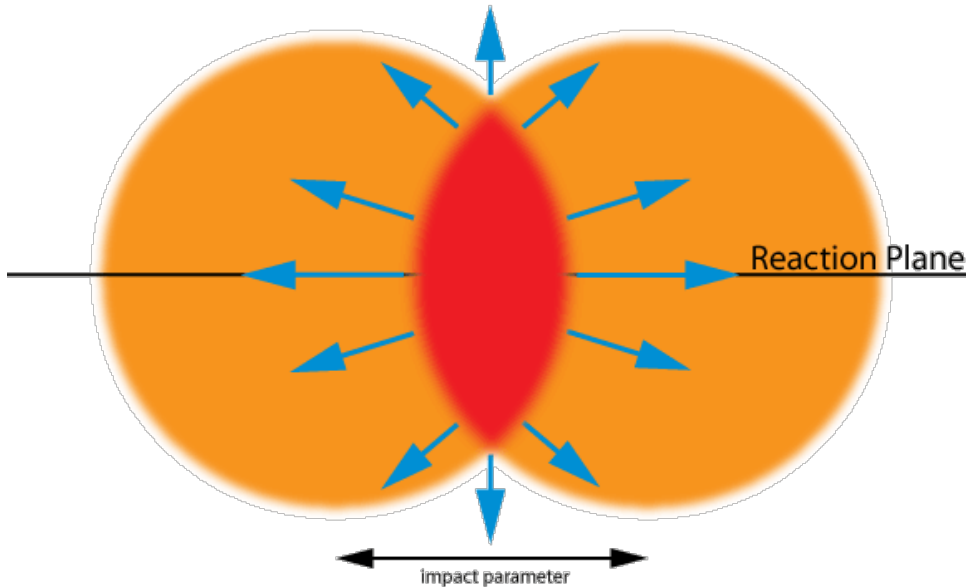
# Study Of Identified Particle Higher Order Azimuthal Anisotropy At RHIC-PHENIX Experiment

## RHIC-PHENIX実験における 高次方位角異方性の粒子依存性測定



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29a-HA-12

# Azimuthal anisotropy



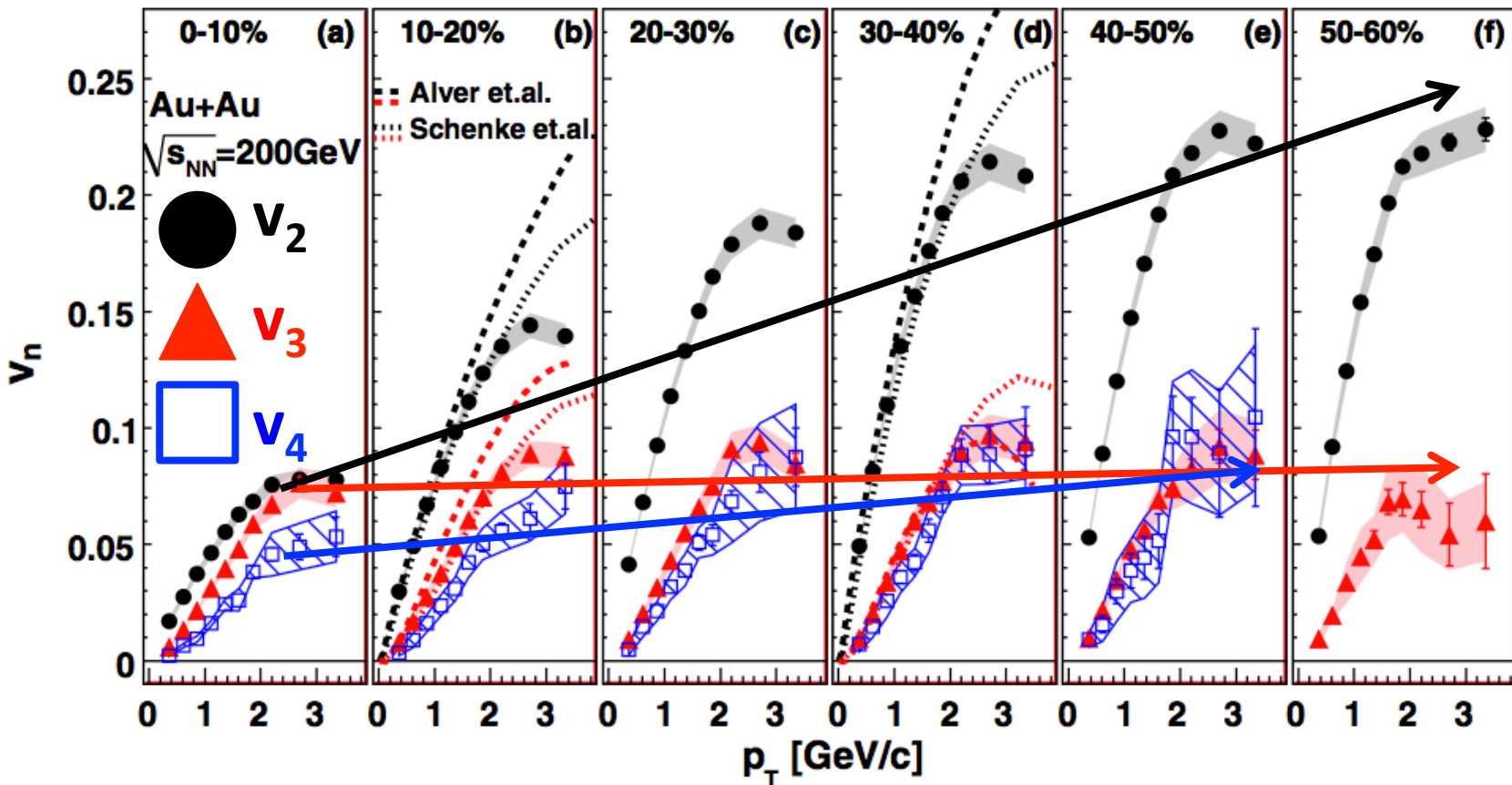
$$E \frac{d^3 N}{dp^3} = \frac{1}{2\pi p_T dp_T dy} \frac{d^2 N}{dp^2} \left[ 1 + 2 \sum_{n=1}^{\infty} \nu_n \cos \{n(\phi - \Psi_n)\} \right]$$

$$\nu_n = \langle \cos \{n(\phi - \Psi_n)\} \rangle$$

Because higher harmonics flows are more sensitive to initial geometry and  $\eta/s$  of QGP, they are studied actively in order to determine the calculating model of initial geometry and constrain  $\eta/s$ .

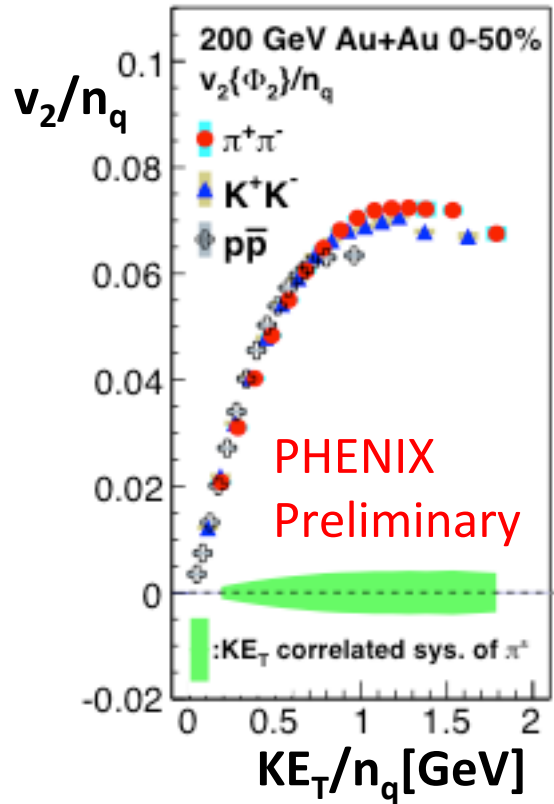
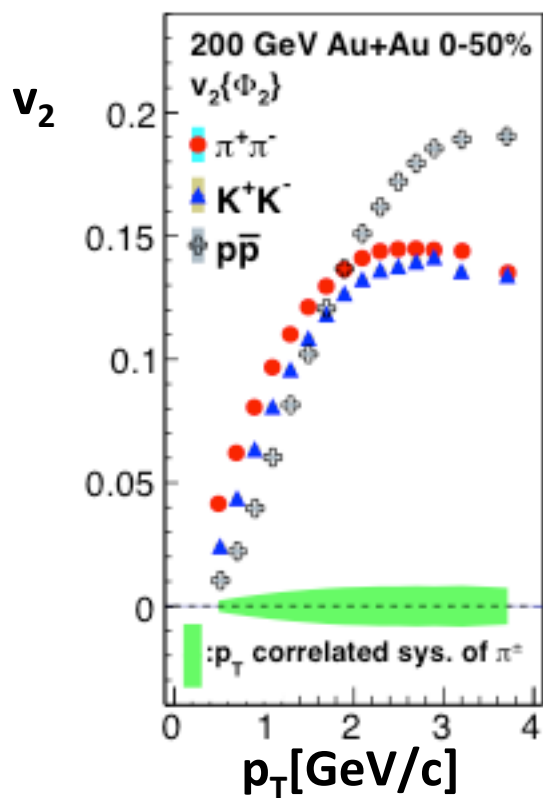
# Charged particle azimuthal anisotropy

P.R.L. 107, 252301(2011)



$v_3$  and  $v_4$  have weak centrality dependence while  $v_2$  has strong dependence. It indicates  $v_3, v_4$  are created by the initial geometry deformation.

# The number of constituent quark scaling of $v_2$

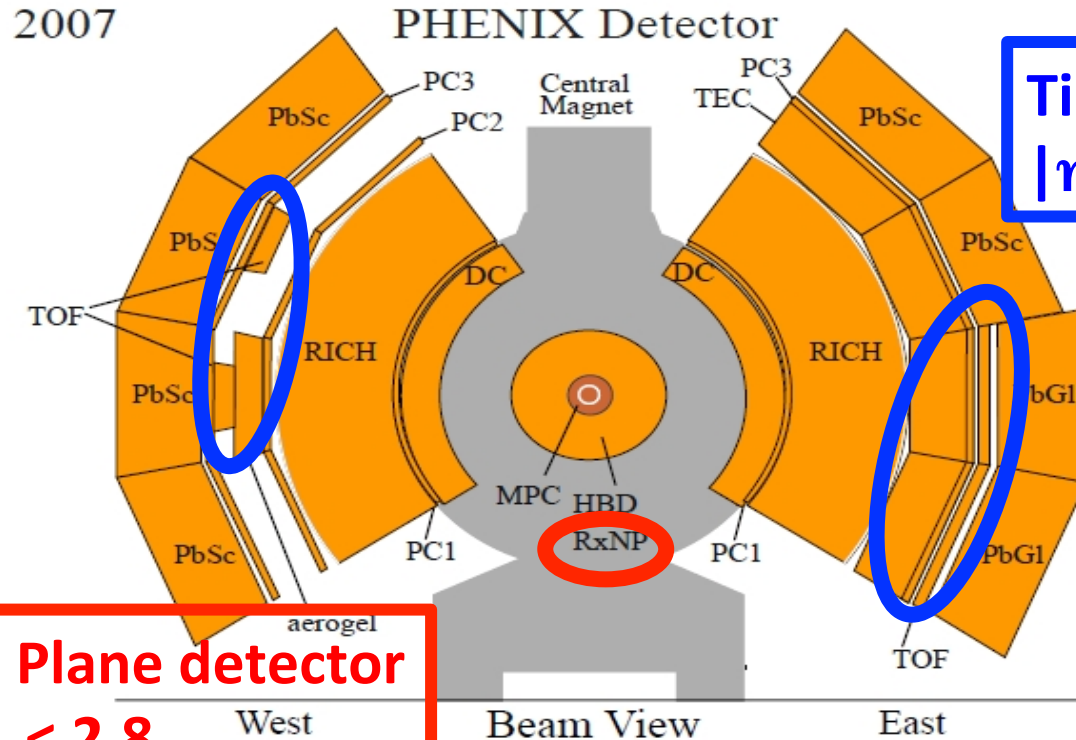


- $\pi^+\pi^-$
- ▲  $K^+K^-$
- ⊕  $p\bar{p}$

$$KE_T = \sqrt{m_0^2 + p_T^2} - m_0$$

$v_2$  has mass ordering in low  $p_T$  and meson/baryon dependence higher  $p_T$  region.  
 $v_2(KE_T)$  is well scaled by the number of constituent quarks, less than 1.0[GeV].  
 It is known that hydrodynamic model can describe  $v_2$  in low  $p_T$  region.

# Data set and PHENIX detector



Time of Flight  
 $|\eta| < 0.35$

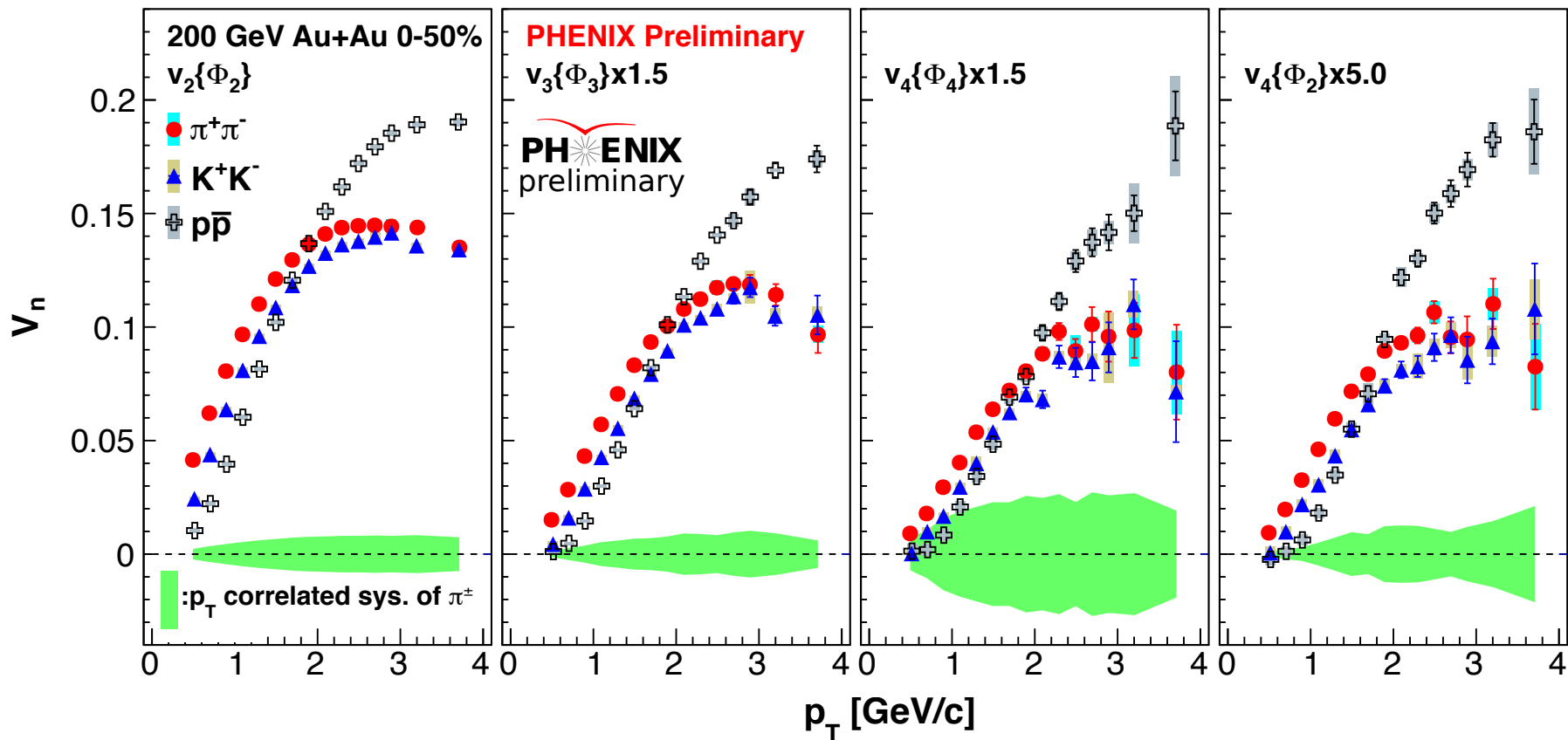
Reaction Plane detector  
 $1.0 < |\eta| < 2.8$

$$v_n = \langle \cos \{ n(\phi - \Psi_n) \} \rangle$$

Data set is Au+Au 200 GeV taken in 2007 period.

In order to reduce the effect of non-flow, the detectors which measure Event Plane and emitted particle angles should have some distances.

# $v_n$ of charged $\pi, K, p$ result



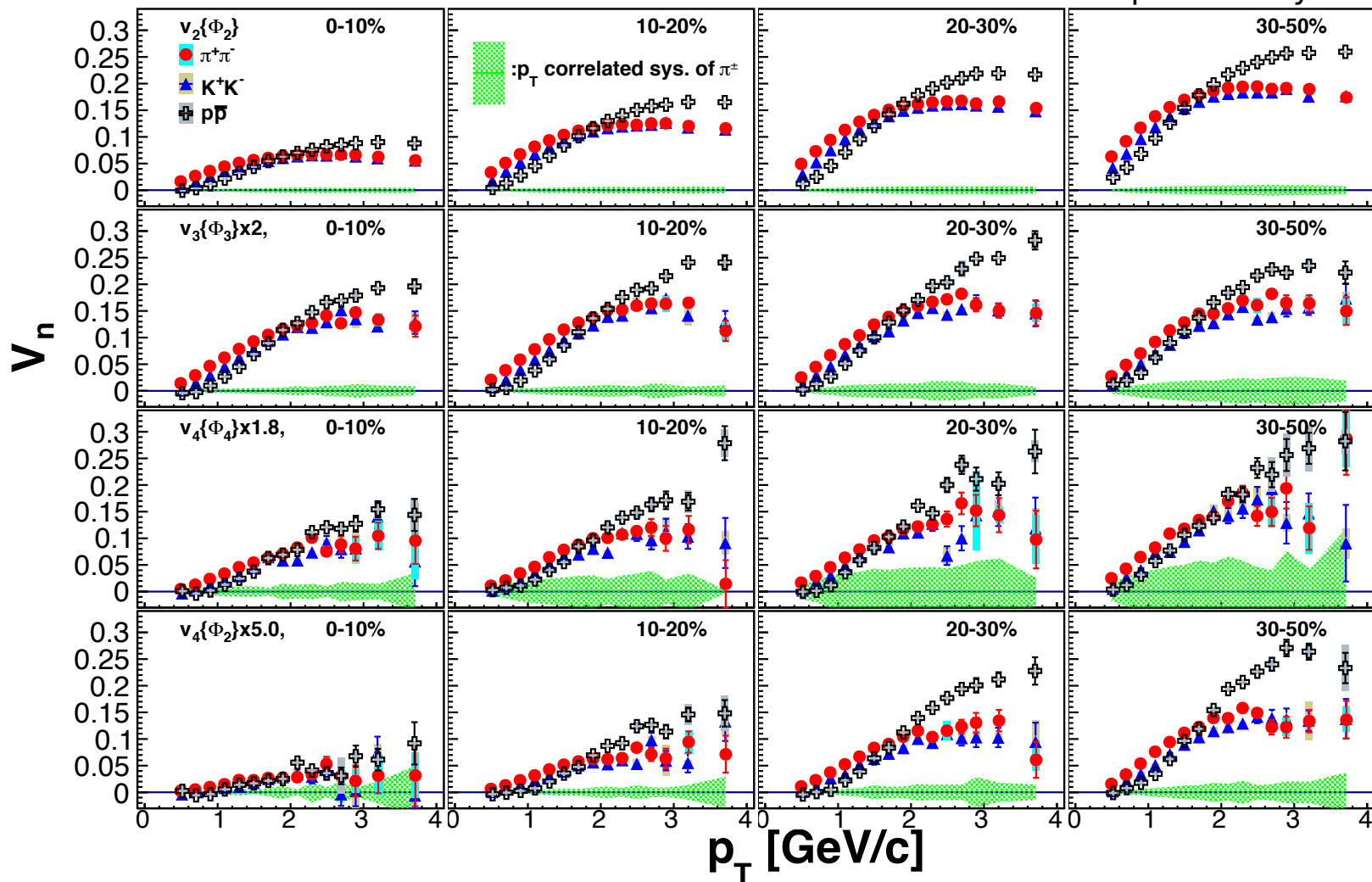
Azimuthal anisotropy has particle species dependence, which are mass dependence and meson/baryon dependence.

Higher harmonics are created from initial geometry deformation, they are affected by the effect of QGP expansion.

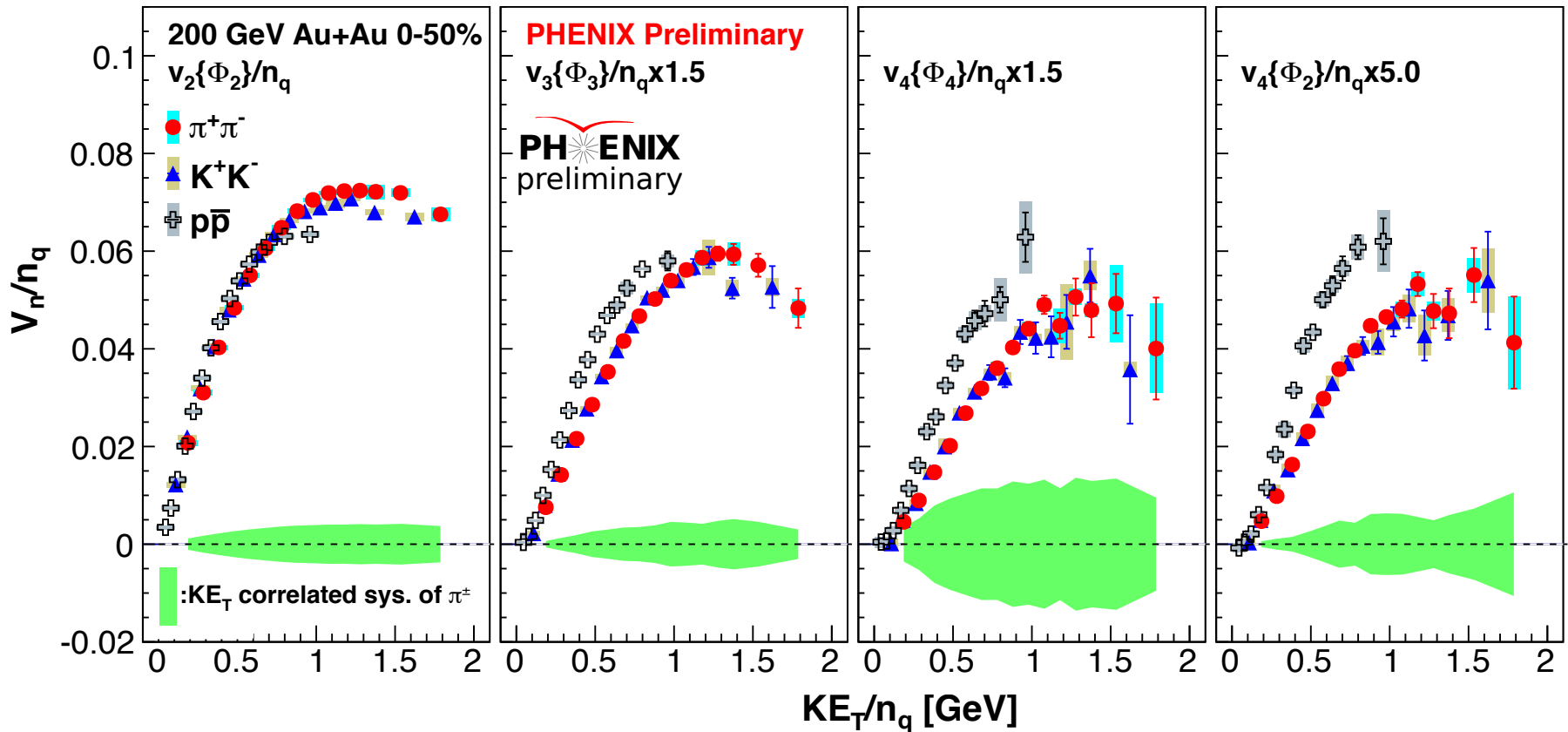
# PIDed $v_n$ with fine centrality bin

Au+Au  $\sqrt{s_{NN}}=200$  GeV PHENIX Preliminary

PHENIX preliminary



# Break the number of constituent quark scaling

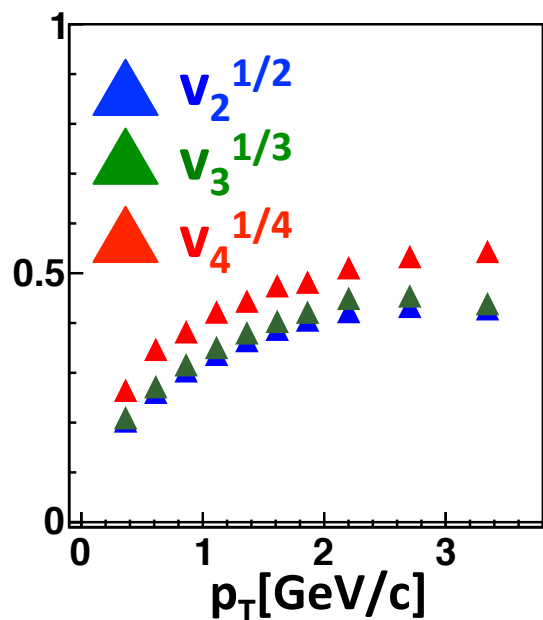
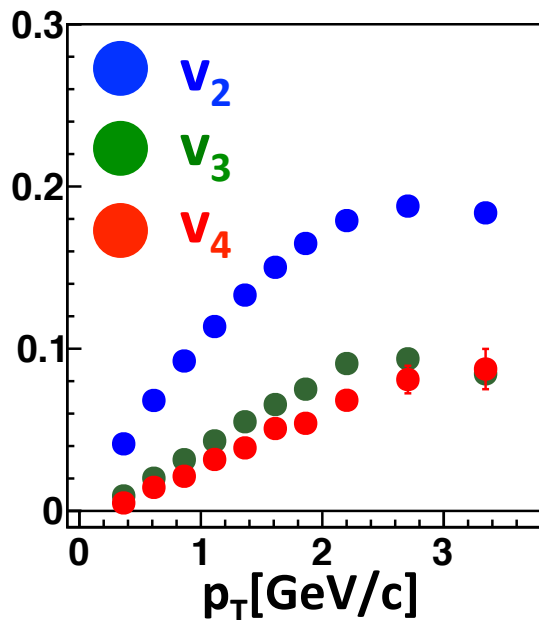


While  $v_2$  is well scaled, higher harmonics have deviation.  
 The scaling for all harmonics and particle species are searched.

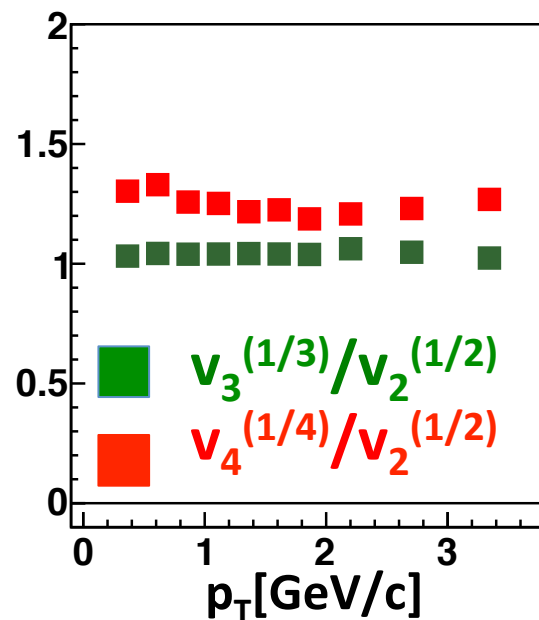


# $v_n^{1/n}$ scaling among harmonics

20 - 30%



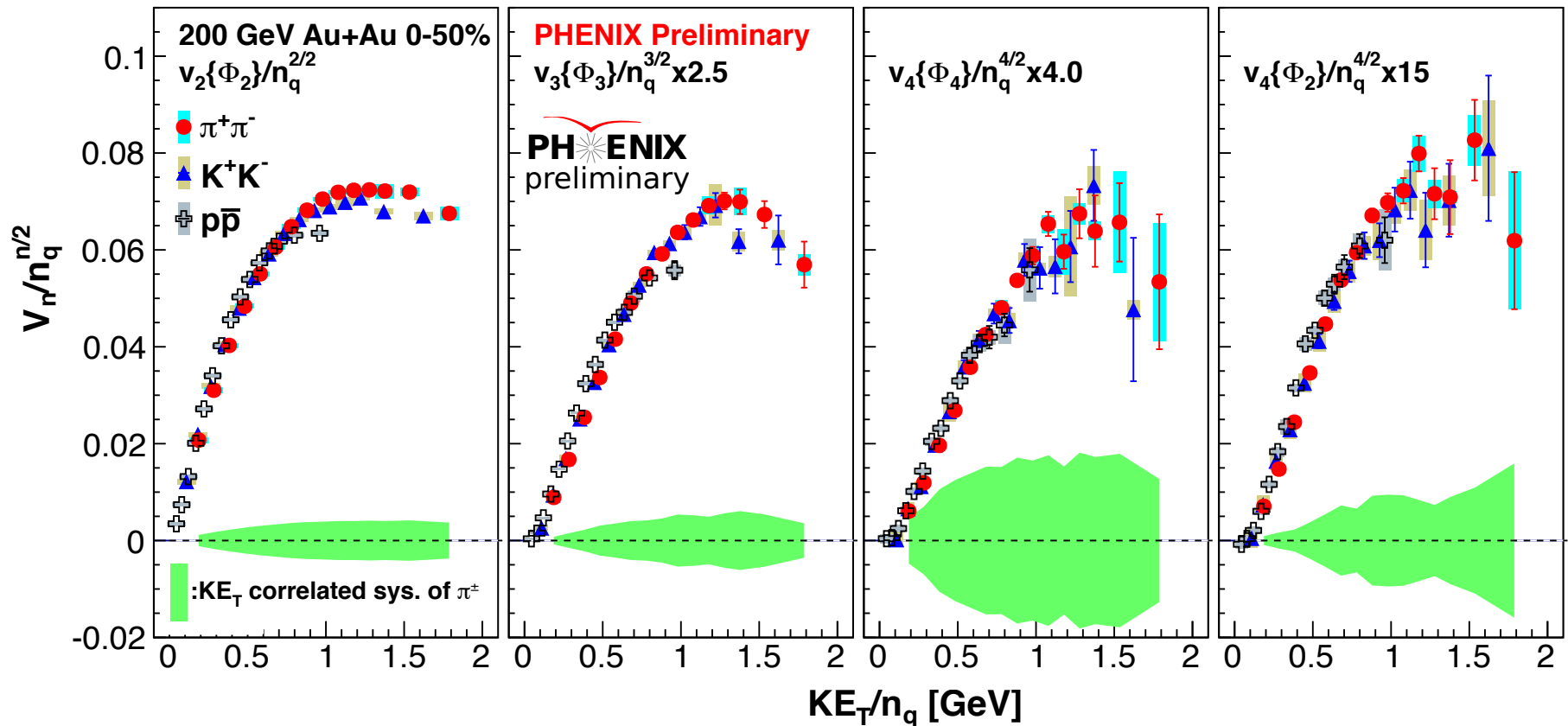
arXiv:1105.3782(2011)



Charged particle  $v_n^{(1/n)}$  is scaled beyond harmonics.  
 $v_n^{1/n}/v_2^{1/2}$  ratio shows flat dependence on  $p_T$ .

$$v_2(K E_T/n_q)/n_q \rightarrow (v_2(K E_T/n_q)/n_q)^{n/2} \rightarrow v_n(K E_T/n_q)/n_q^{n/2}$$

# Modified the quark number scaling



Modified scaling works well for all harmonics.

$$v_2(KE_T/n_q)/n_q \rightarrow (v_2(KE_T/n_q)/n_q)^{n/2} \rightarrow v_n(KE_T/n_q)/n_q^{n/2}$$

(a) :  $v_2(KE_T)/n_q$   
 (b) :  $v_n^{1/n}$  scaling  
 (a)+(b) :  $v_n(KE_T)/n_q^{n/2}$

## Summary

$v_2, v_3, v_4, v_4(\Psi_2)$  of charged  $\pi, K, p$  are measured.

It is found that there are mass ordering in low  $p_T$  and meson/baryon dependence larger than 2 [GeV/c] as  $v_2$ .

The number of constituent quarks scaling are tested.

The scaling which works well for  $v_2(K_{E_T})$ , doesn't work for  $v_n(K_{E_T})_{n>2}$ .

Modified scaling  $v_n(K_{E_T}/n_q)/n_q^{n/2}$  is checked to work well for all harmonics.

## Next step

$v_n$  of  $\phi$  will be measured, because it is meson and heavier than proton.

And scaling test will be operated.

$v_n$  of photon will be measured.



**BACK UP**

# Blast Wave Model

QGP variables are extracted by comparison with Blast Wave model, which can describe final state from information at freeze-out such as temperature.

$$\frac{dN}{p_T dp_T} \propto \int \int r dr d\phi m_T I_0(\alpha_T) K_1(\beta_T)$$

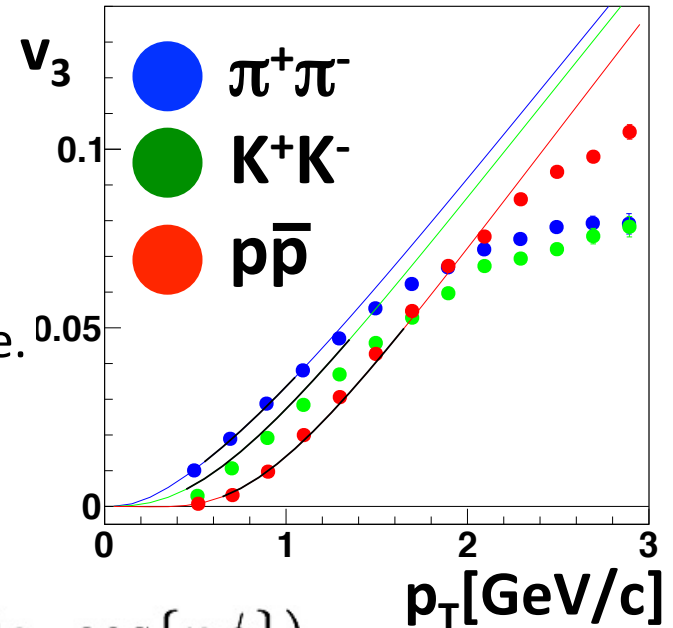
$$v_n = \frac{\int \int r dr d\phi \cos\{n\phi\} I_n(\alpha_T) K_1(\beta_T) (1 + 2s_n \cos\{n\phi\})}{\int \int r dr d\phi I_0(\alpha_T) K_1(\beta_T) (1 + 2s_n \cos\{n\phi\})}$$

$T_f$  : temperature

$\rho_0$  : average velocity

$\rho_n$  : velocity anisotropy  
(anisotropy in velocity)

$s_n$  : geometrical anisotropy  
(like eccentricity at freeze-out)



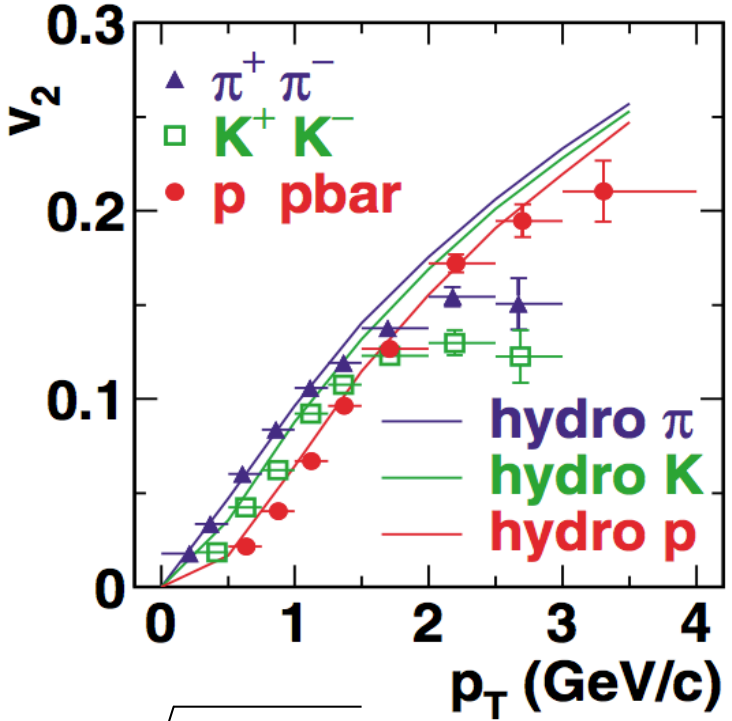
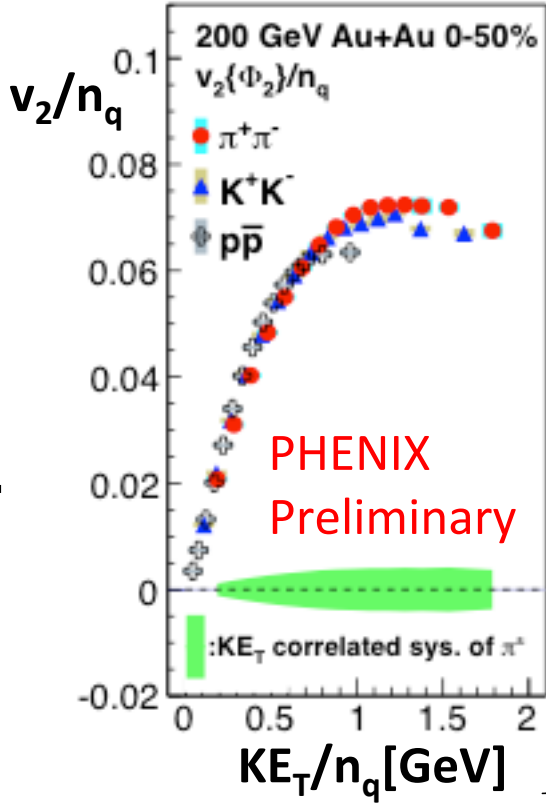
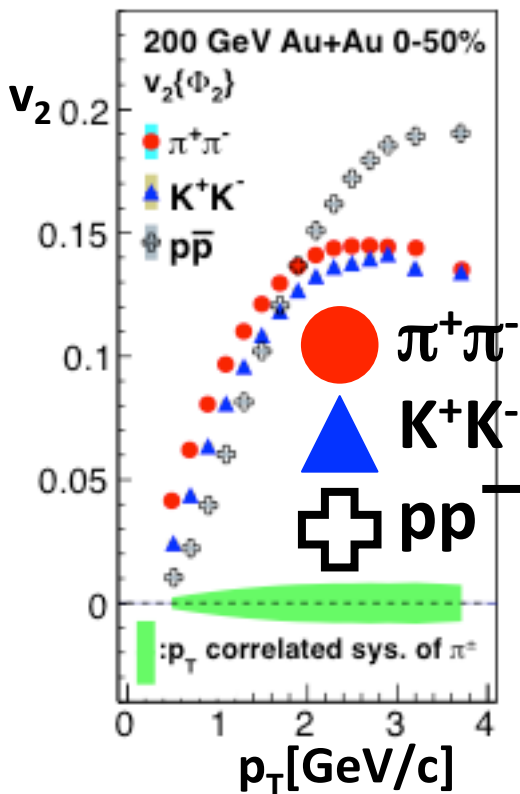
$$\rho(\phi, r) = \rho_0(1 + 2\rho_n \cos(n\phi)) * r$$

$$\alpha_T(\phi, r) = (p_T/T_f) \sinh(\rho(\phi, r))$$

$$\beta_T(\phi, r) = (m_T/T_f) \cosh(\rho(\phi, r))$$

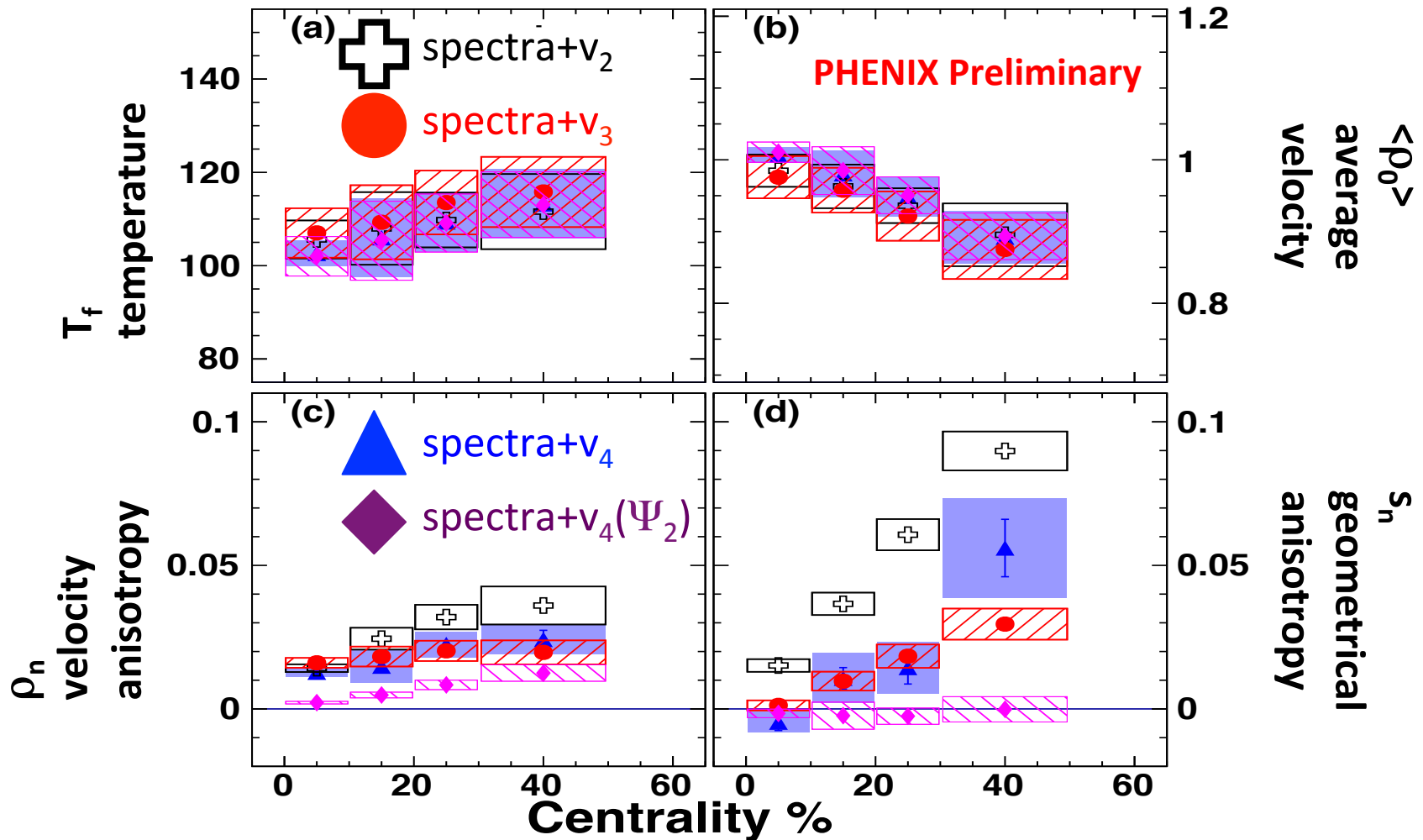
# The number of constituent quark scaling of $v_2$

P.R.L.91, 182301



$v_2$  has mass ordering in low  $p_T$  and meson/baryon dependence higher  $p_T$  region.  
 $v_2(KE_T)$  is well scaled by the number of constituent quarks, less than 1.0[GeV].  
 It is known that hydrodynamic model can describe  $v_2$  in low  $p_T$  region.

# Freeze-out parameters extracted by comparison with BW



$\rho_n$  behavior is similar to centrality dependence of charged particle  $v_n$ .  
 $s_3$  and  $s_4$  are smaller than  $s_2$  but not zero in non-central.



## Summary

$v_2, v_3, v_4, v_4(\Psi_2)$  of charged  $\pi, K, p$  are measured.

It is found that there are mass ordering in low  $p_T$  and meson/baryon dependence larger than 2 [GeV/c] as  $v_2$ .

The number of constituent quarks scaling doesn't work for  $v_n(K_{E_T})_{n>2}$ .

Modified scaling  $v_n(K_{E_T}/n_q)/n_q^{n/2}$  is checked to work well for all harmonics.

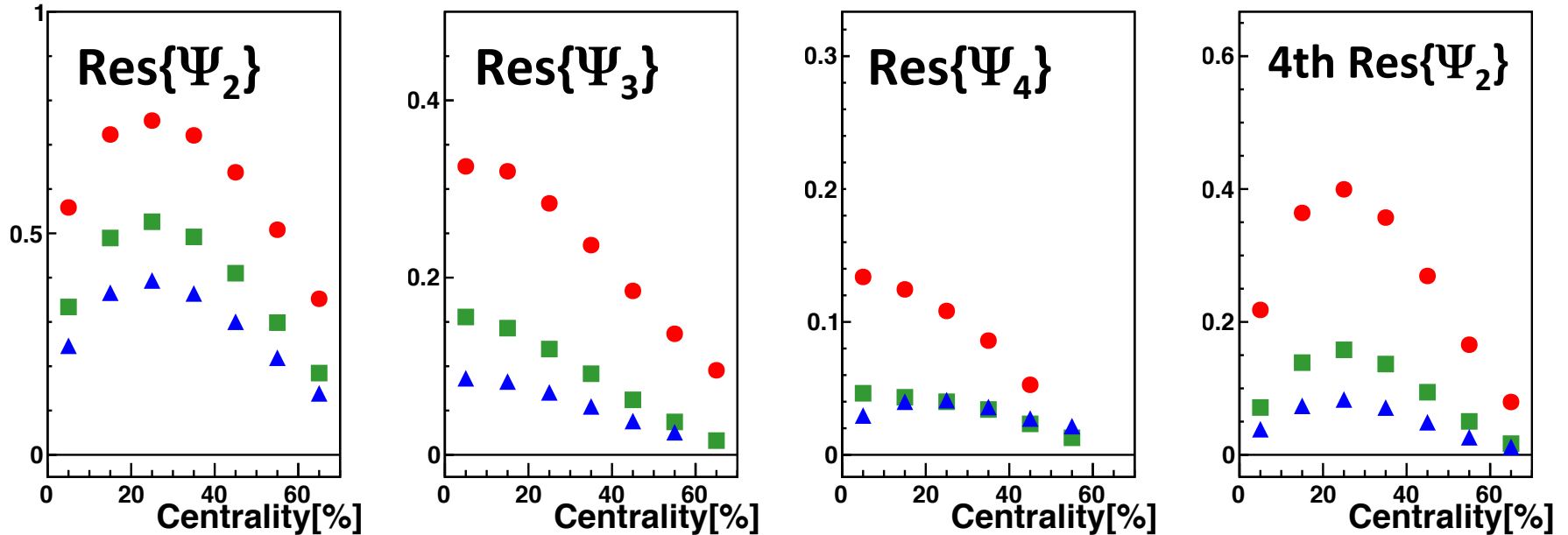
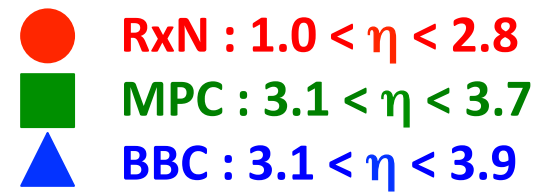
QGP at freeze-out is parameterized by comparison with Blast Wave model.

It is found that  $\rho_n$  (velocity anisotropy) behavior looks like charged particle  $v_n$  behavior.

$s_2$  (Geometry anisotropy) is larger than  $s_3$  and  $s_4$ .

There are geometrical anisotropy at freeze-out.

# Event Plane resolution



$$\nu_{n,true} = \nu_{n,obs} / \text{Res}\{\Psi_n\}$$

$$\text{Res}\{\Psi_n\} = \langle \cos \{n(\Psi_{n,real} - \Psi_{n,obs})\} \rangle$$

Res{Ψ<sub>n</sub>} is estimated from correlation observed Ψ<sub>n</sub>.

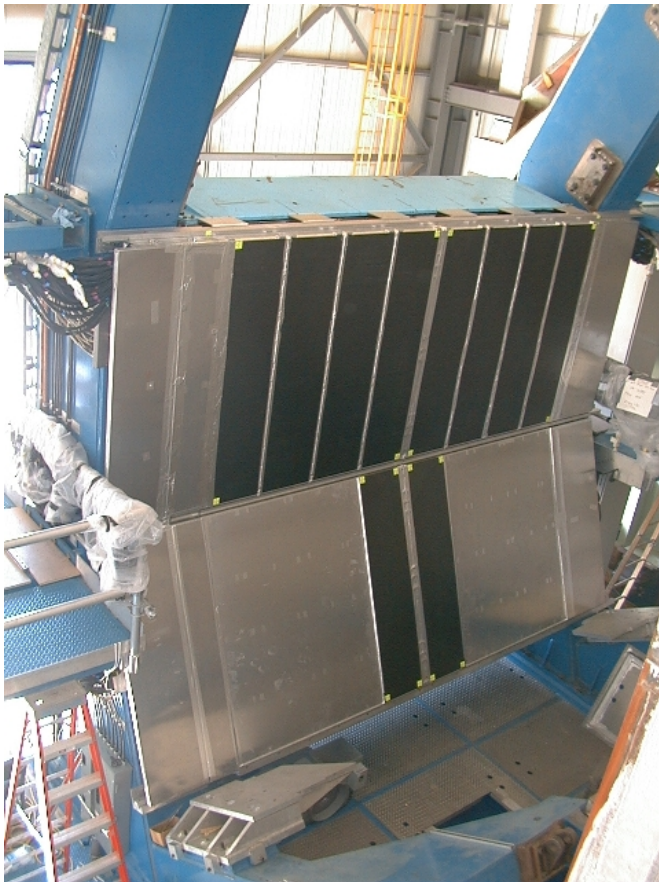
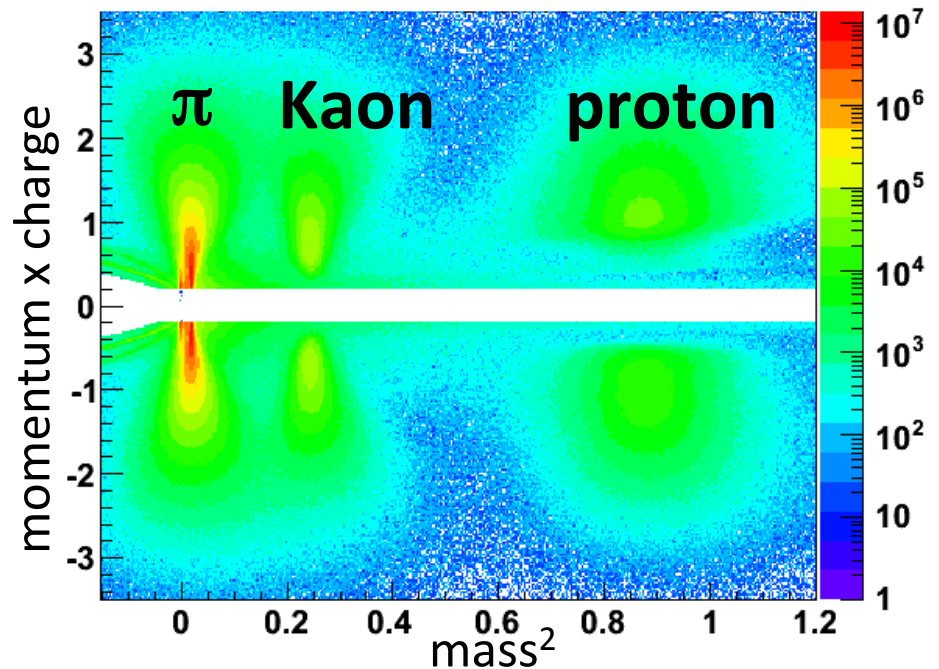
Because RxN has best resolution, Ψ<sub>n</sub> measured by RxN is used in this analysis.

# Time-Of-Flight detector

Particle species are identified by TOF method.  
AGEL and RICH are used to separate them finer.

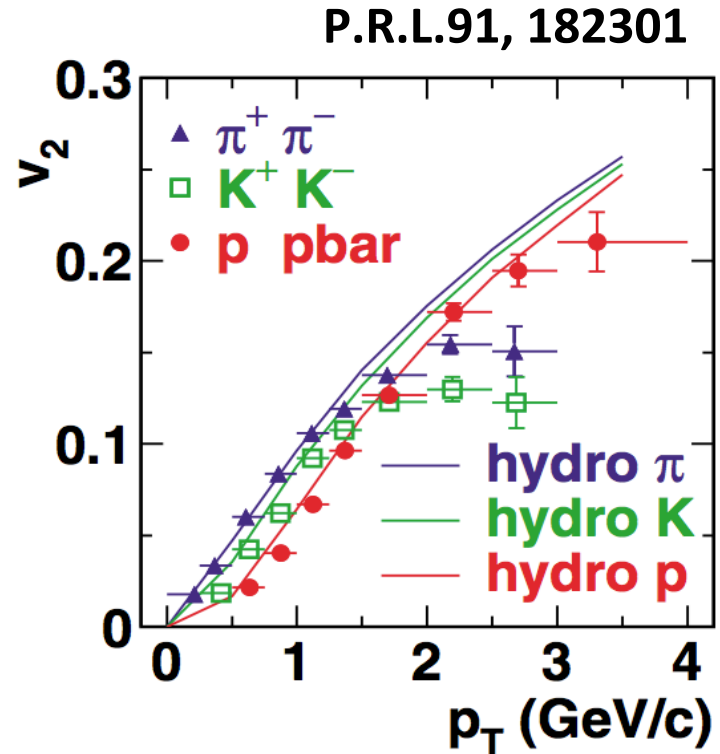
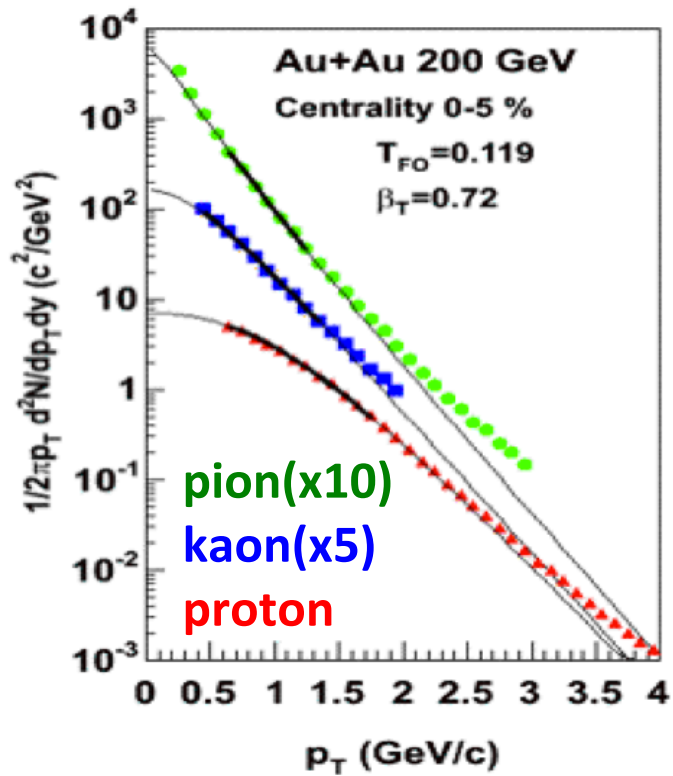
$$m^2 = p^2 \left( \frac{c^2 t^2}{L^2} - 1 \right)$$

mass<sup>2</sup> distribution via TOF.E



TOF.E detector

# Hydrodynamic model describe identified particle valuable



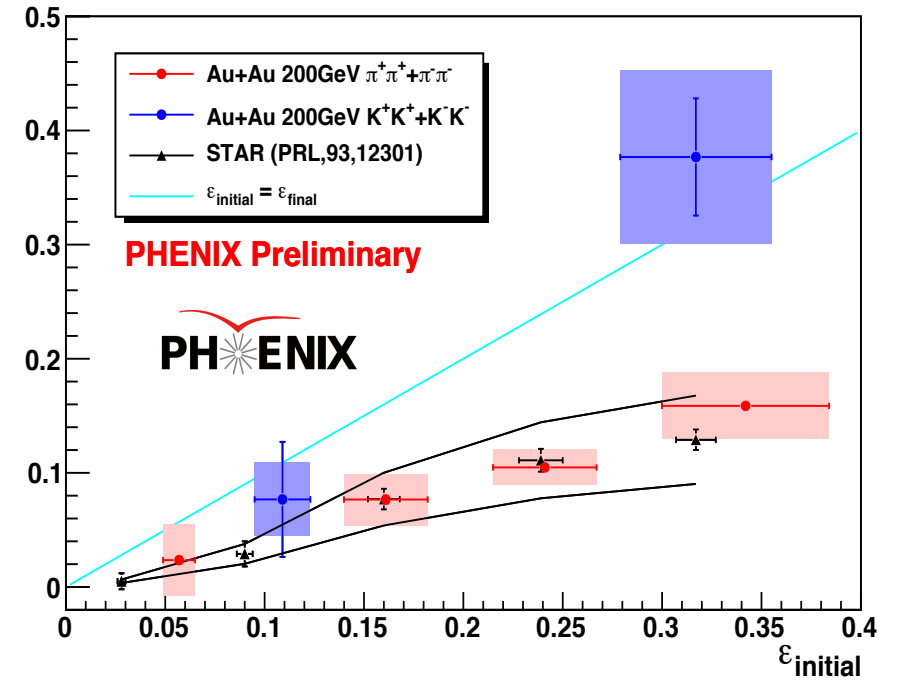
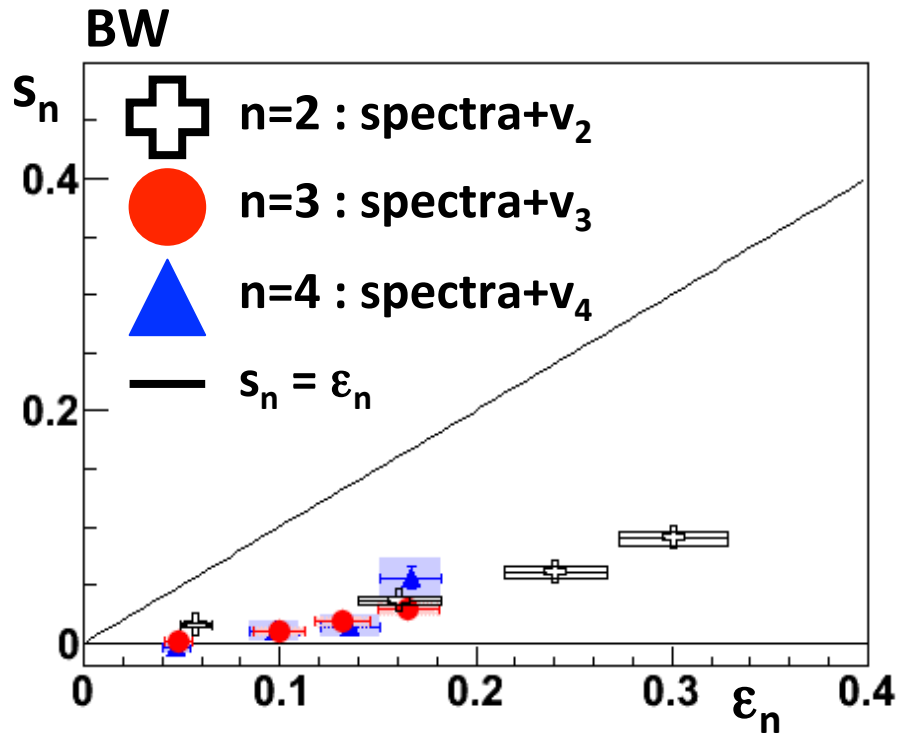
Spectra and PID  $v_2$  have mass ordering in low  $p_T$  region, and they are known that they can be described.

QGP parameters are extracted by comparison with model calculating.

# s<sub>2</sub> behavior is similar with HBT analysis

Takafumi (QM2012)

## HBT (2nd order geometrical anisotropy)



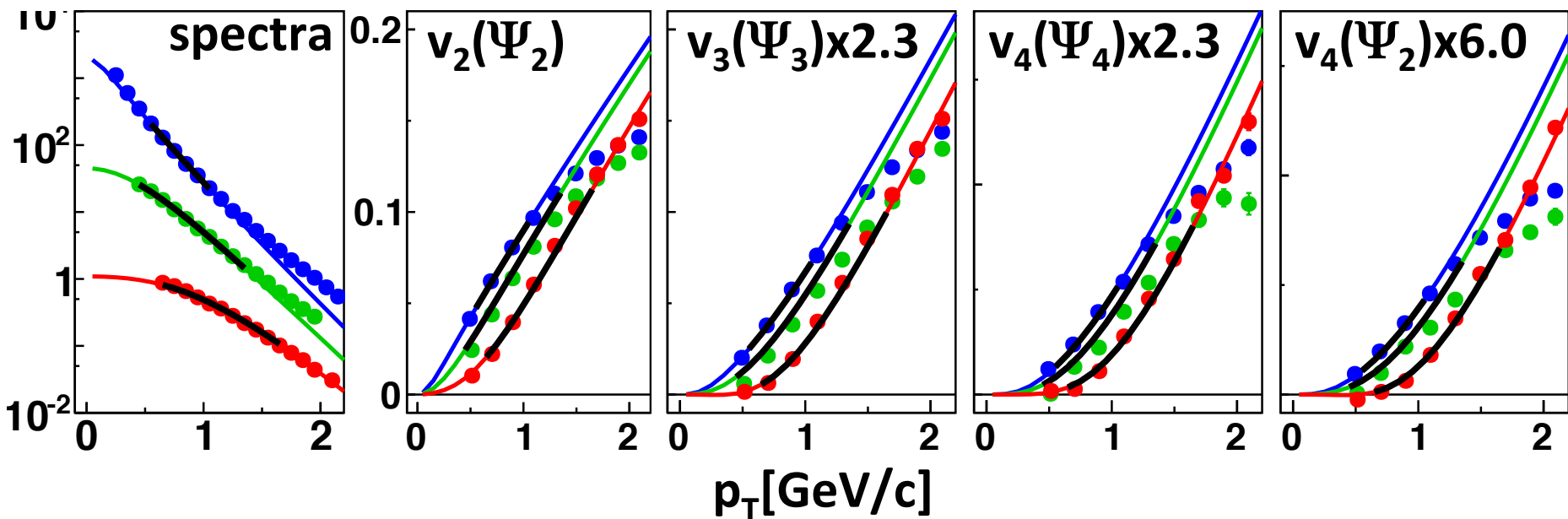
s<sub>2</sub> behavior is similar to HBT result.

# Comparison model

Centrality 0-50%

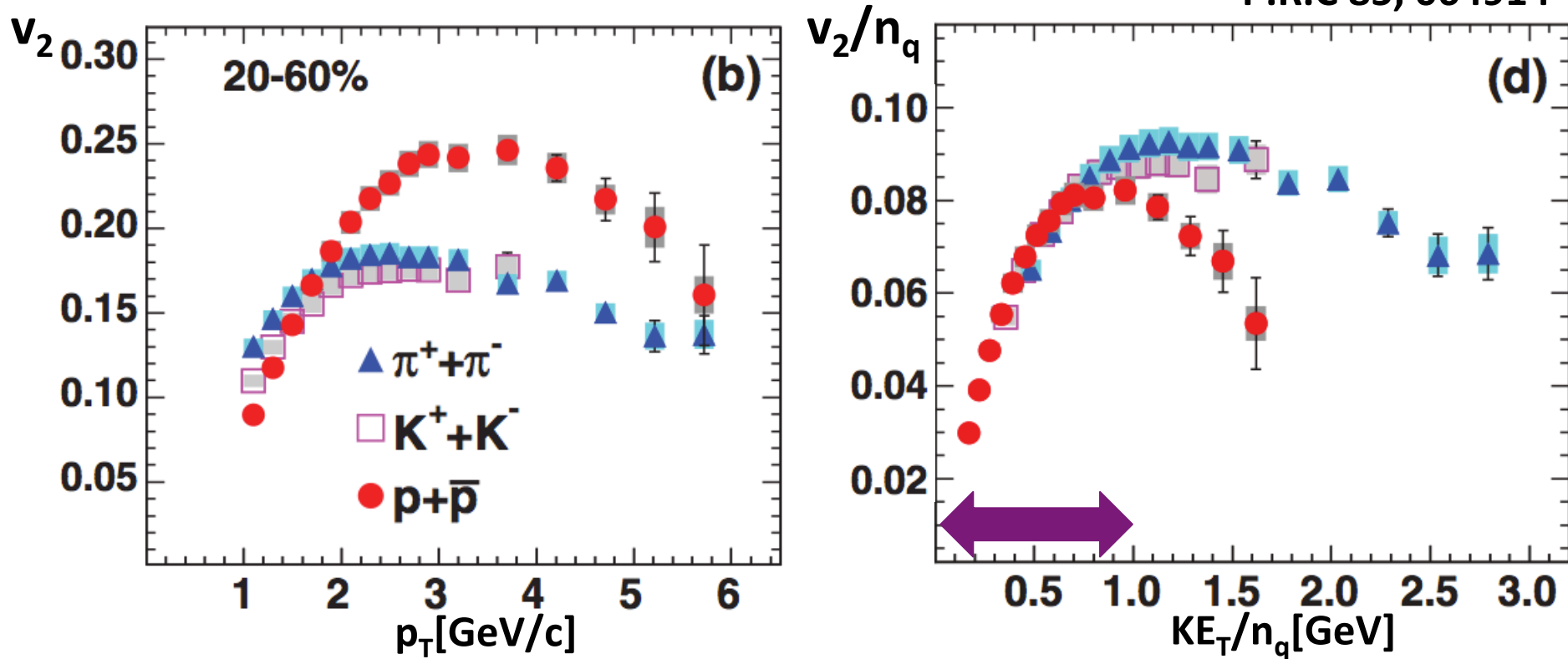
— within fitting range  
— extrapolate range

●  $\pi$  : 0.5 - 1.13[GeV/c]  
● K : 0.4 - 1.40[GeV/c]  
● p : 0.6 - 1.70[GeV/c]



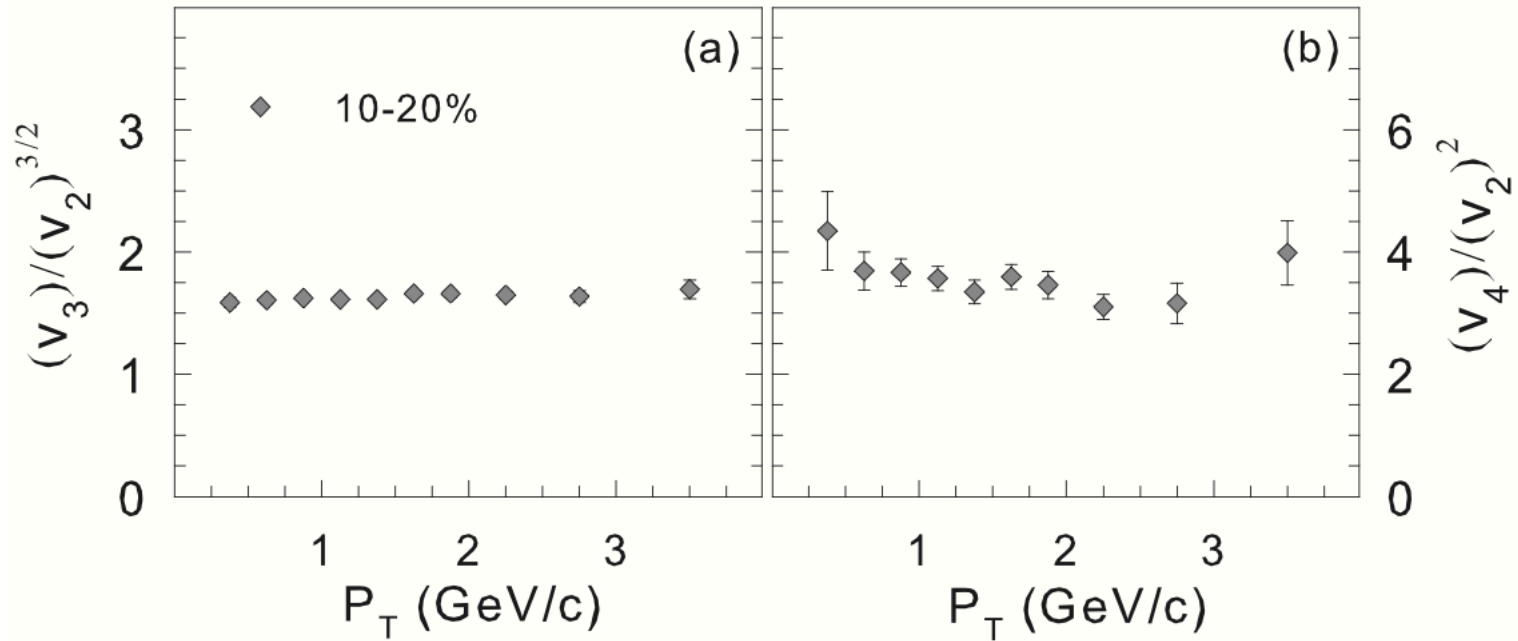
# The number of constituent quark scaling of $v_2$

P.R.C 85, 064914



$v_2$  has mass ordering in low  $p_T$  and meson/baryon dependence higher  $p_T$  region.  
 $v_2(KE_T)$  is well scaled by the number of constituent quarks, less than 1.0[GeV].

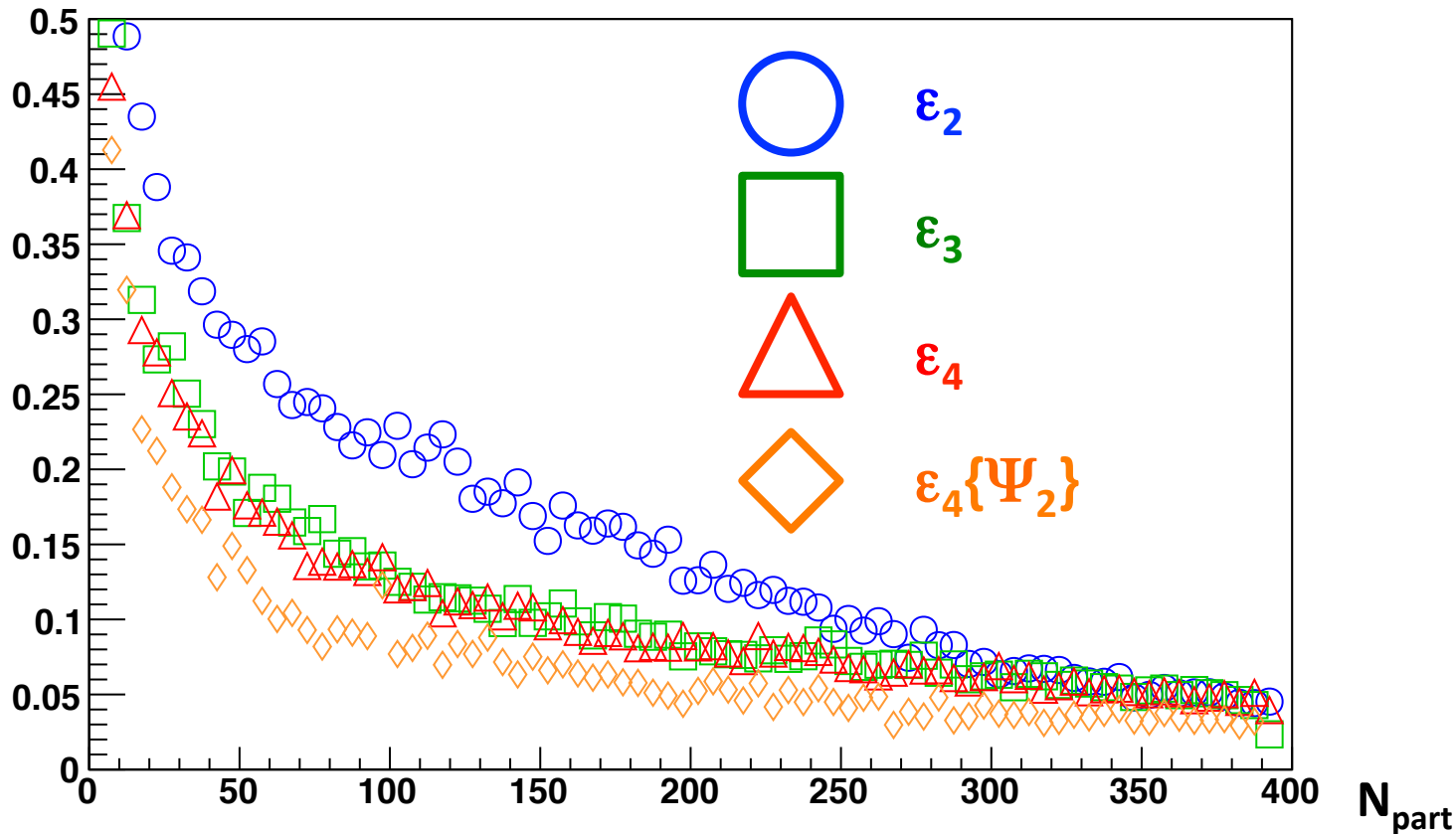
$$KE_T = \sqrt{m_0^2 + p_T^2} - m_0$$



$v_n/v_2^{n/2}$  is scaled.



# Comparison initial geometry anisotropy

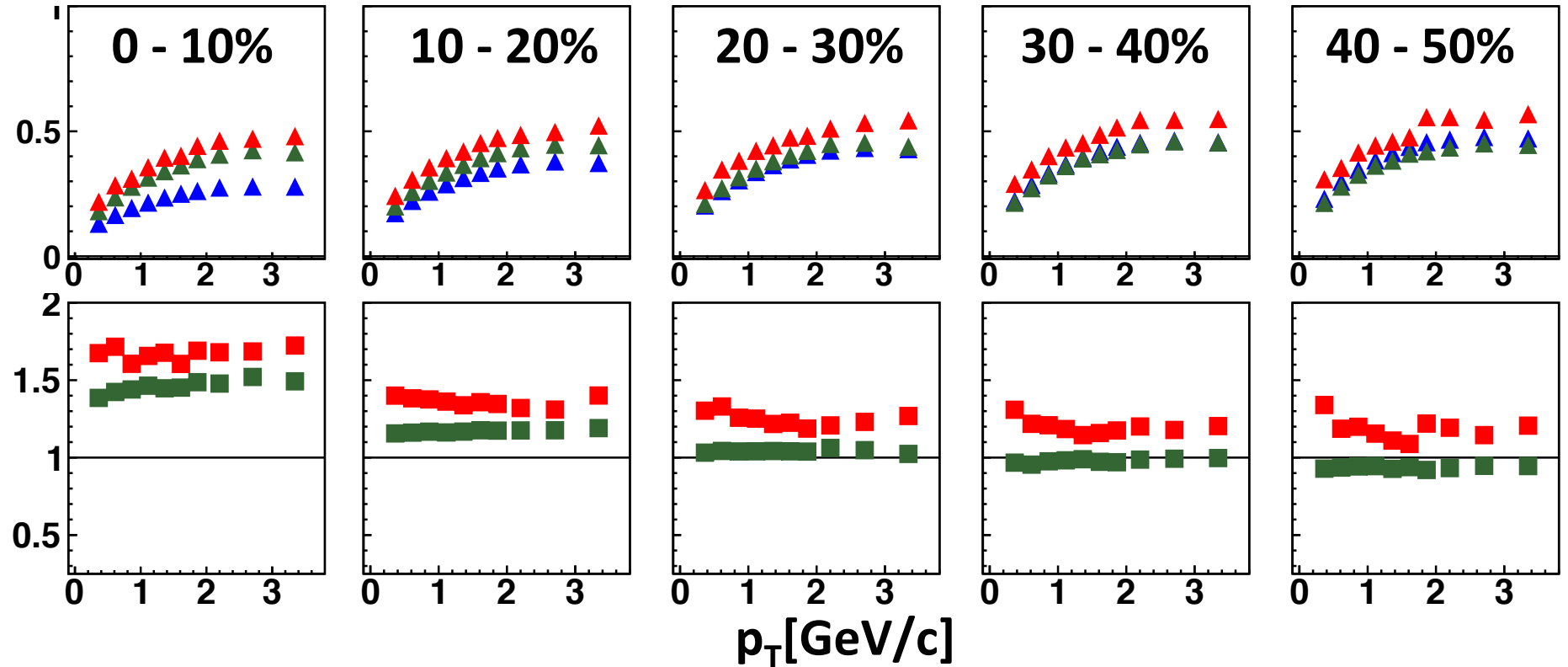
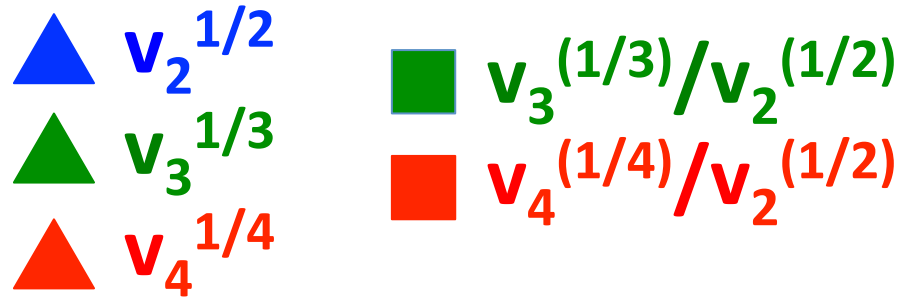


Eccentricity is calculated by Glauber model.

$\epsilon_2$   $N_{\text{part}}$  dependence is larger than higher order.

This dependence resembles  $v_n$  centrality dependence.

# Charged particle scaling



Charged particle are scaled by  $v_n^{1/n}$  beyond harmonics.

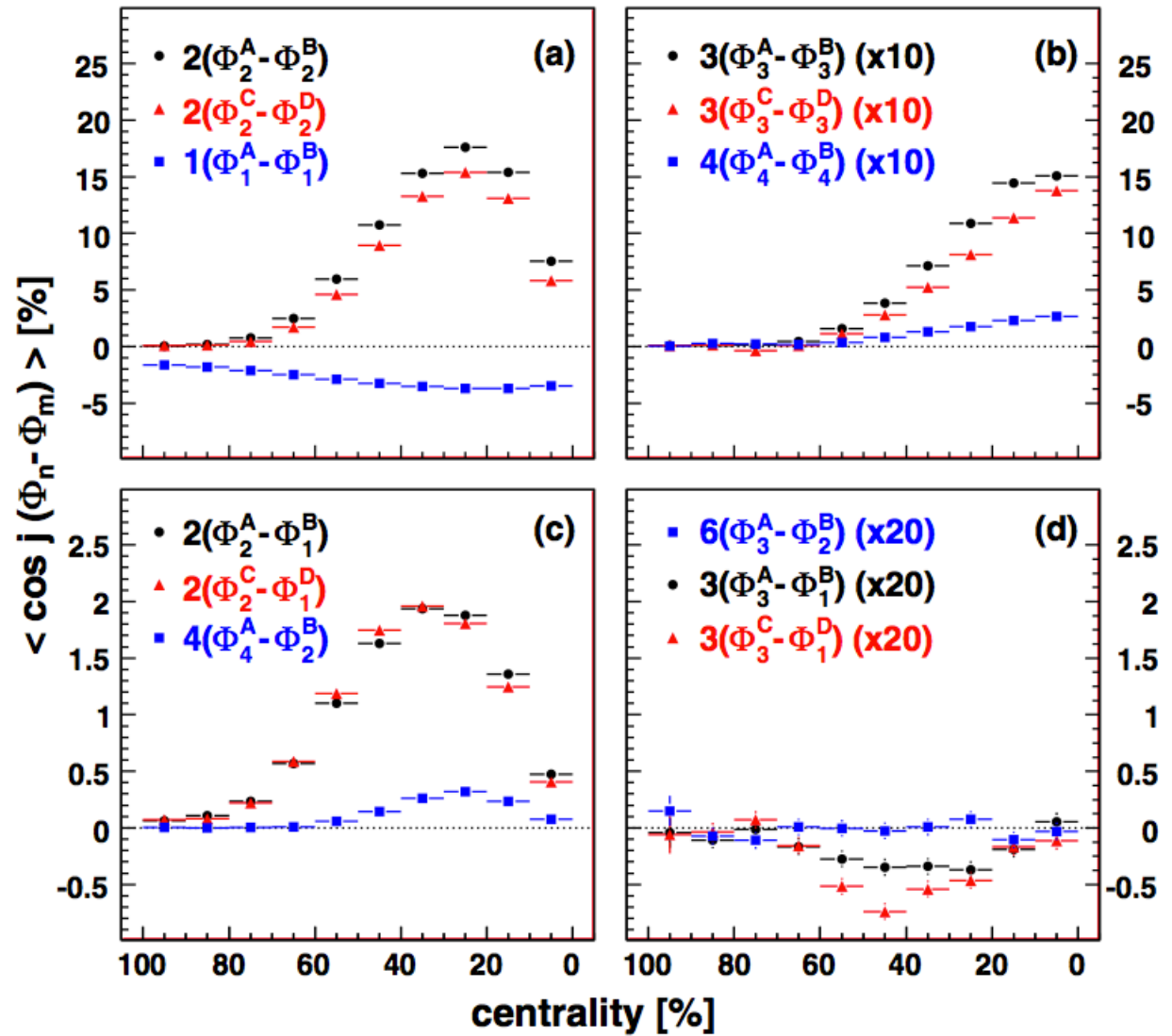
$v_2(K E_T)/n_q$  is scaled

$v_n^{1/n}$  is able to be scaled to  $v_2^{1/2}$

So,  $v_n(K E_T)$  is scaled by  $v_2(K E_T)^{n/2}$

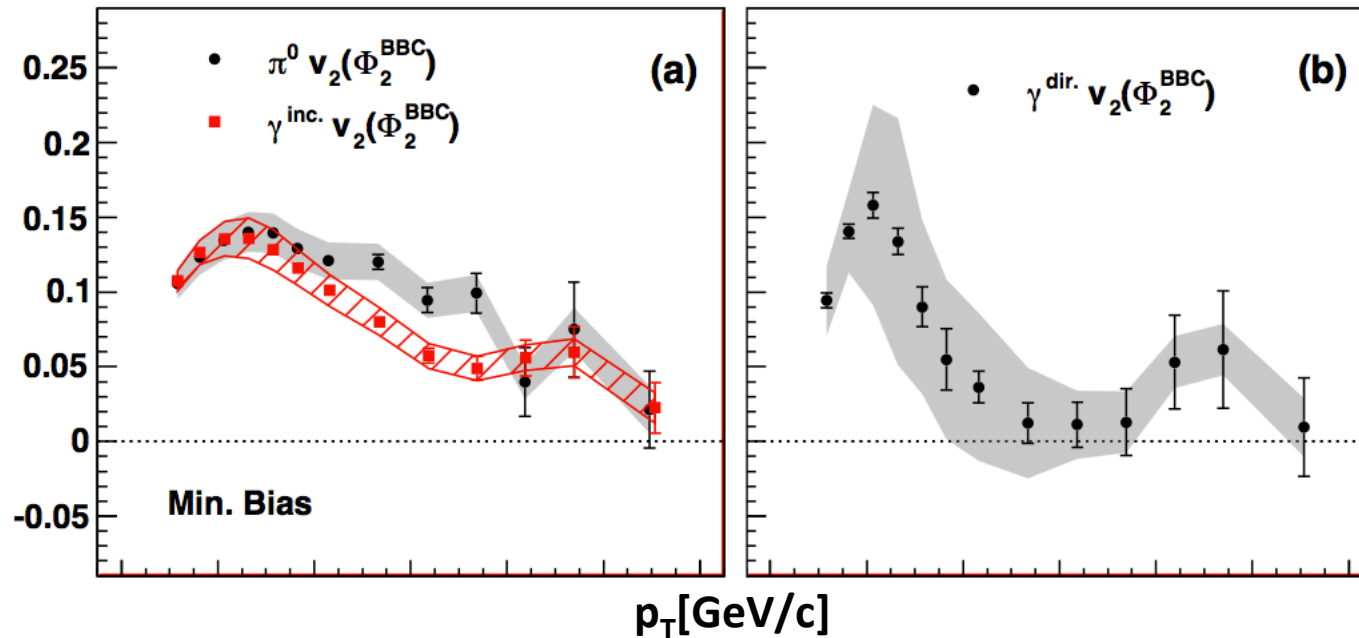
$v_2(K E_T/n_q)/n_q \rightarrow v_2^{n/2}(K E_T/n_q)/n_q^{n/2} \rightarrow v_n(K E_T/n_q)/n_q^{n/2}$

# Event Plane



# $v_2$ of photon result

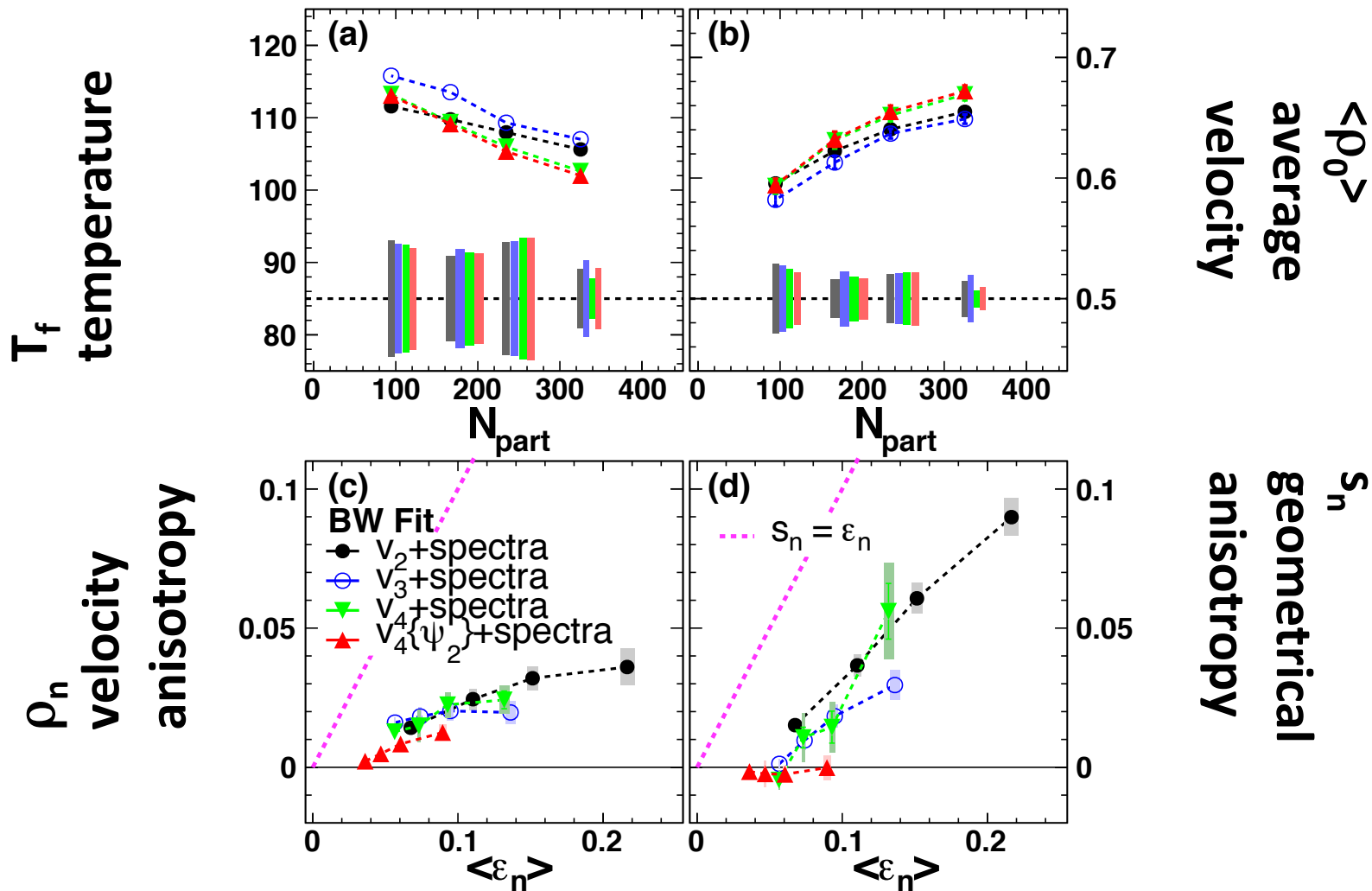
P.R.L. 109, 122302(2012)



Because photon doesn't correlate with QGP, it can provide initial information.  
 $v_2$  of direct photon is as large as ones of hadron in low  $p_T$ .  
What causes?

If it is affected by Magnetic field created by collision,  $v_3$  may have 0.

# Model comparison

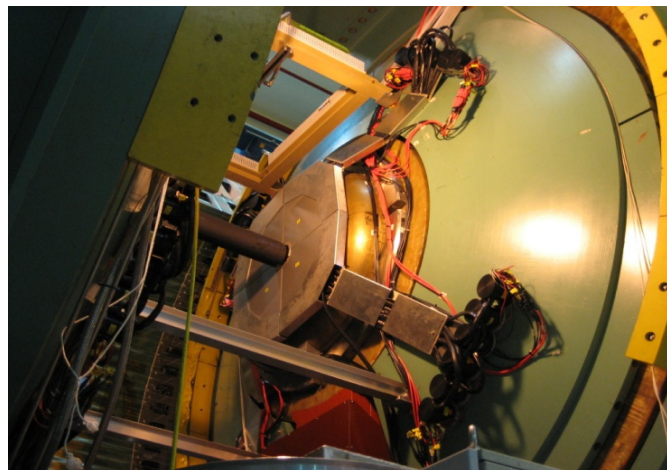


# Event Plane calculation

Event Plane is calculated by three steps.

1. gain correction
2. re-centering
3. flattening

$$\nu_{n,real} = \nu_{n,obs} / \text{Res}\{\Psi_n\}$$

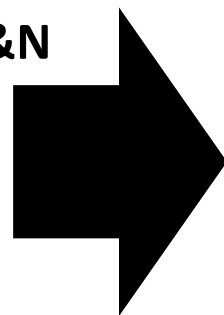
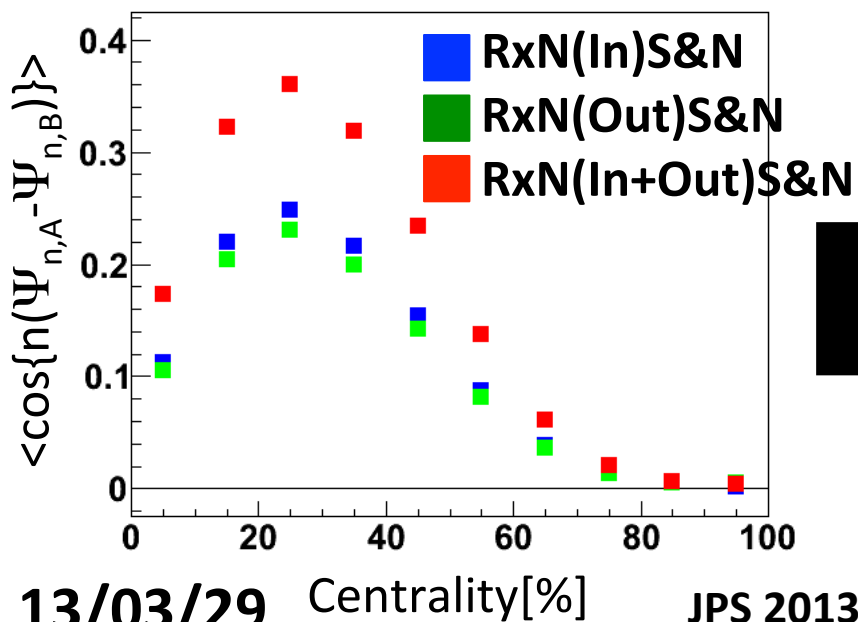


Reaction Plane detector(RxN)

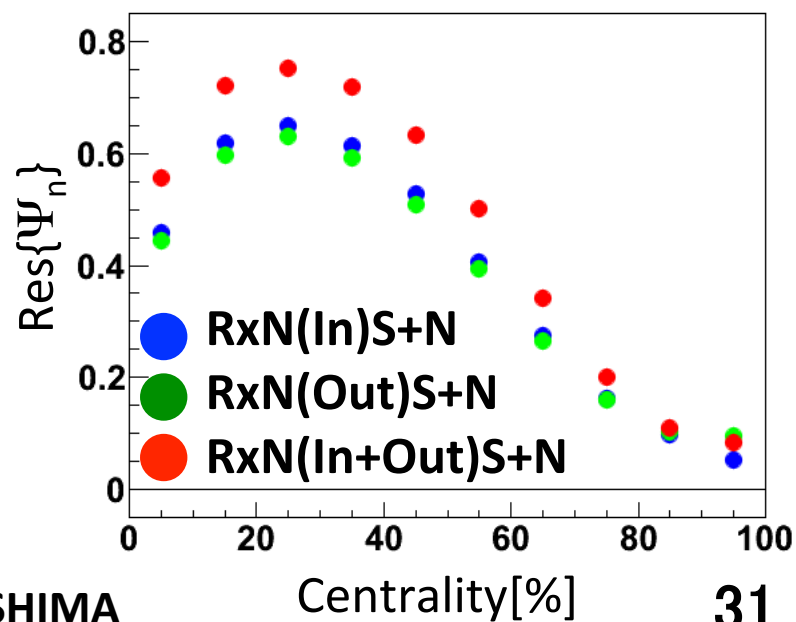
Inner :  $1.5 < |\eta| < 2.8$

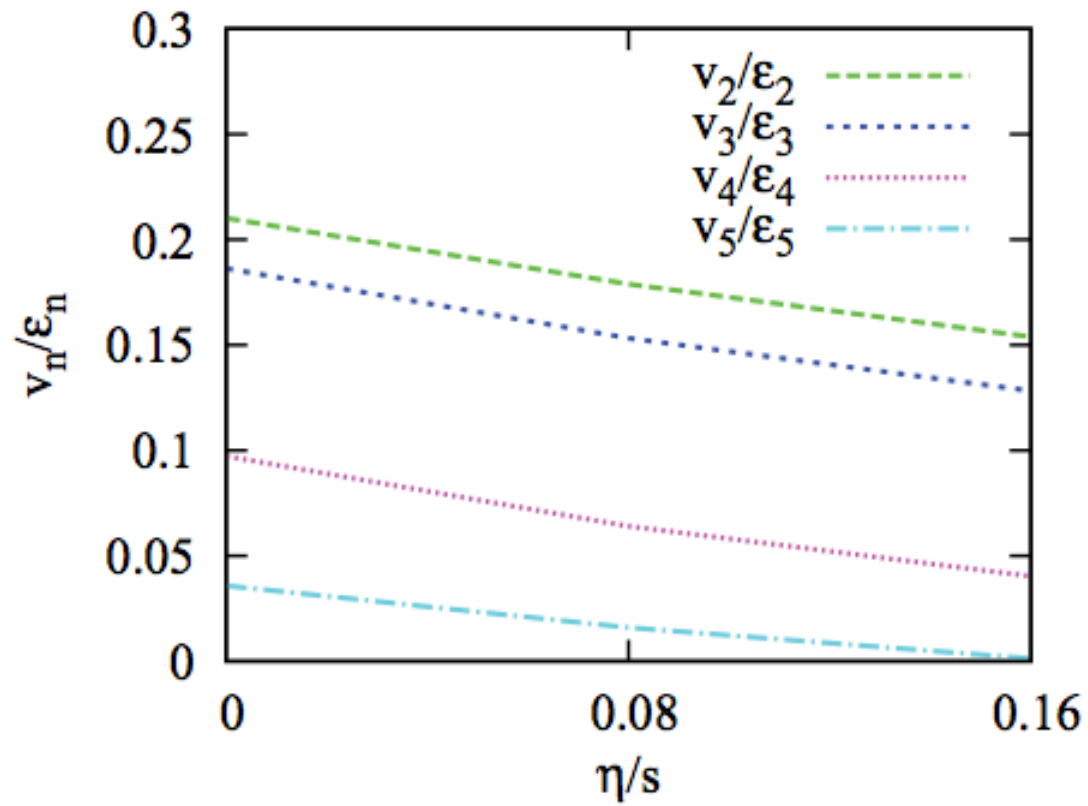
Outer :  $1.0 < |\eta| < 1.5$

2nd Event Plane correlation



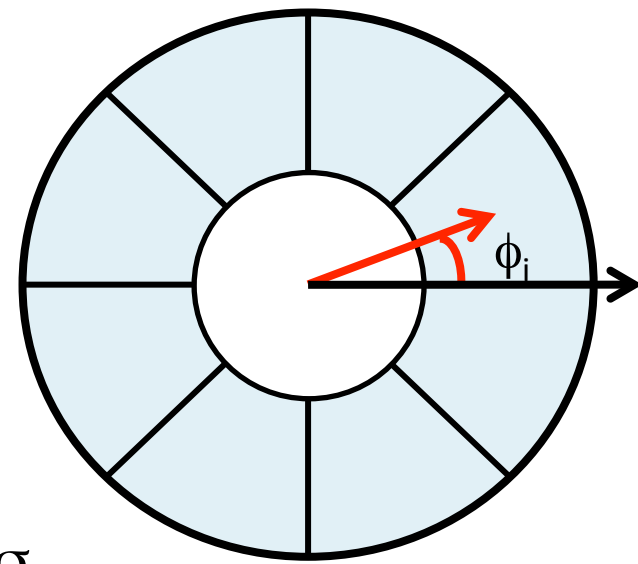
2nd Event Plane resolution







# Event Plane Calculation



## 1. Gain correction

$$w_i = \text{adc}_i / \langle \text{adc} \rangle$$

$$Q_{x,n} = \sum w_i \cos(n\phi_i), \quad Q_{y,n} = \sum w_i \sin(n\phi_i)$$

$$\Phi_n = \text{atan2}(Q_{x,n}, Q_{y,n}) / n$$

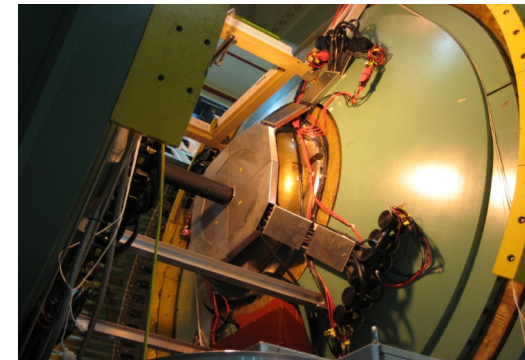
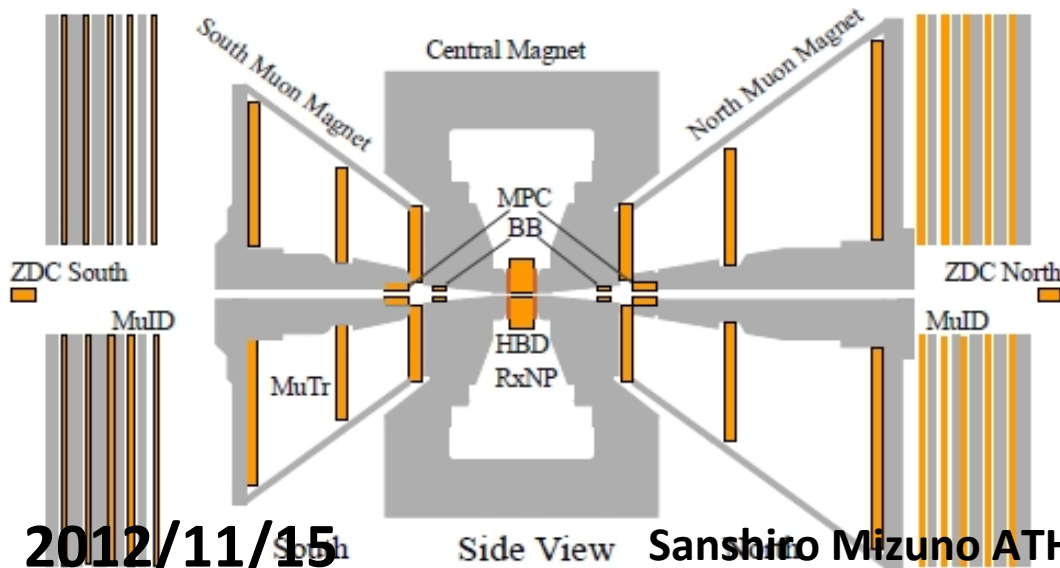
## 2. Re-centering

$$Q'_{x,n} = (Q_{x,n} - \langle Q_{x,n} \rangle) / \sigma_{Q_{x,n}}, \quad Q'_{y,n} = (Q_{y,n} - \langle Q_{y,n} \rangle) / \sigma_{Q_{y,n}}$$

$$\Phi'_n = \text{atan2}(Q'_{x,n}, Q'_{y,n}) / n$$

## 3. Flattening

$$n\Phi''_n = n\Phi'_n + \sum 2/i \{ -\langle \sin(in\Phi'_n) \rangle \cos(in\Phi'_n) + \langle \cos(in\Phi'_n) \rangle \sin(in\Phi'_n) \}$$



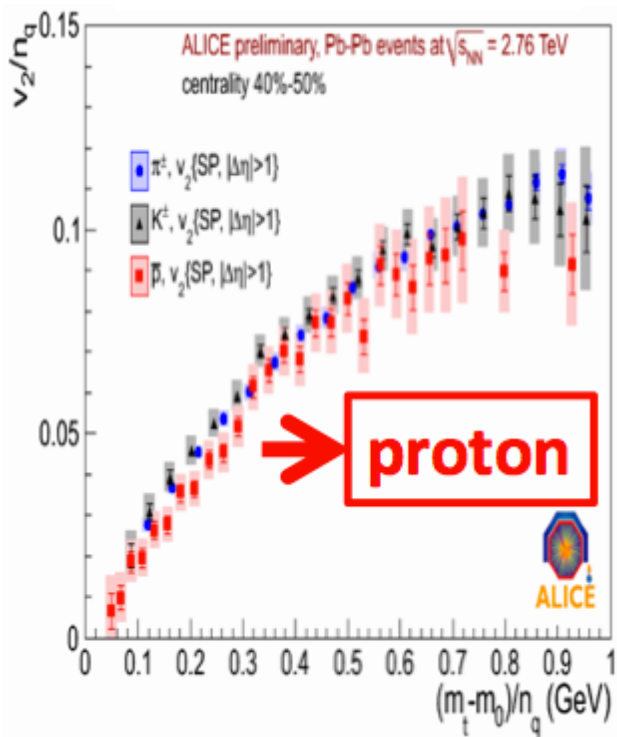
reaction plane detector(RxN)

inner  $1.5 < |\eta| < 2.8$

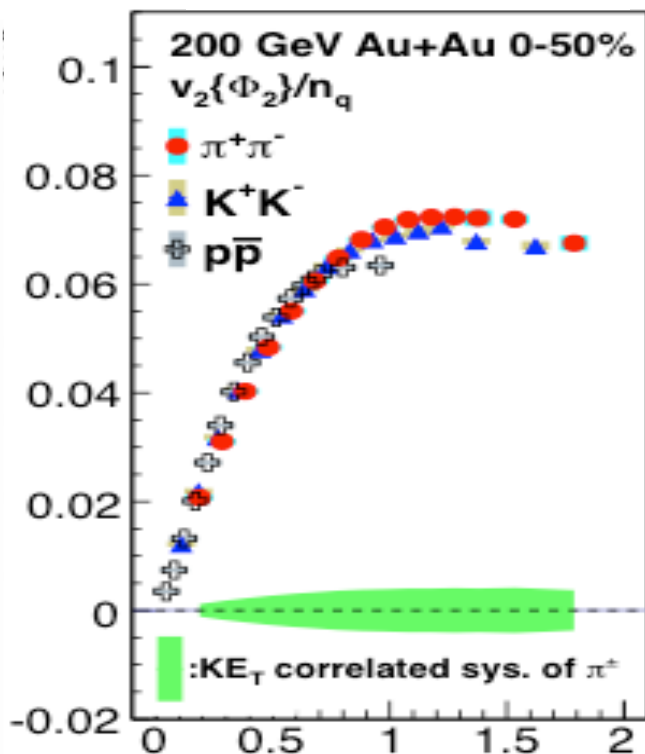
outer  $1.0 < |\eta| < 1.5$

# Comparison scaling among different energy

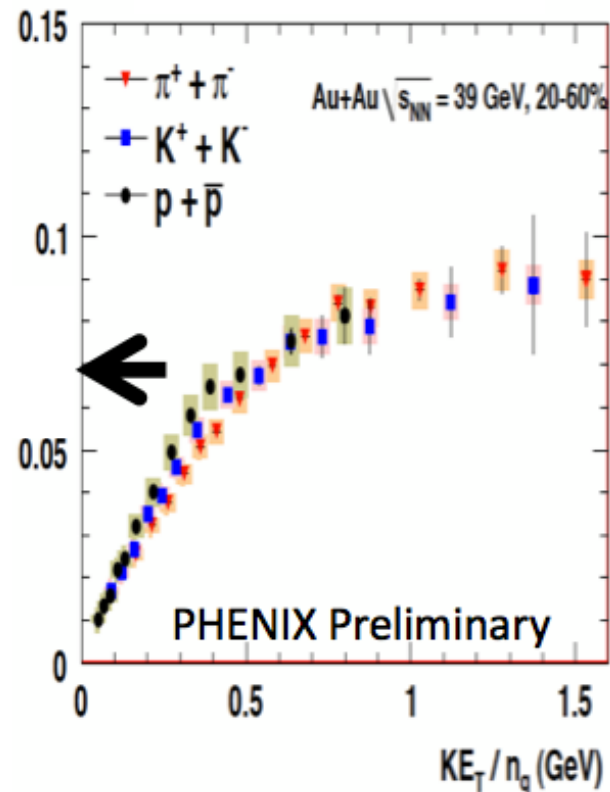
Pb+Pb 2760GeV



Au+Au 200GeV

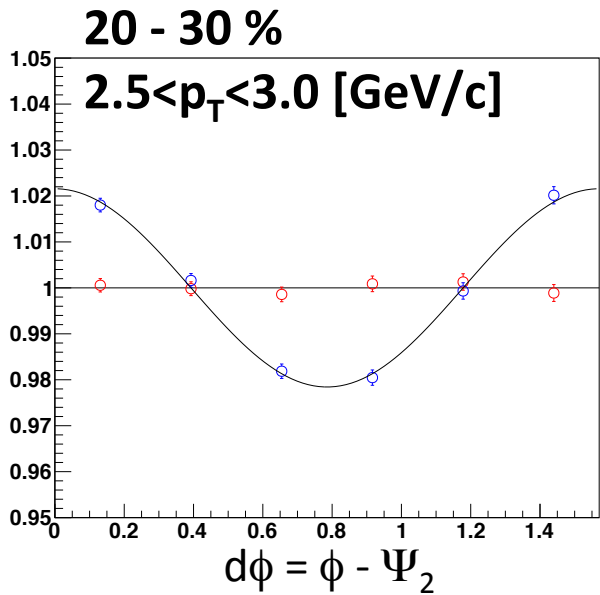


Au+Au 39GeV



- Proton is shifted  
Is the strength of radius expansion related?

# Fit function dependence w.r.t. $v_2$



data /  $N_0[1+2v_2\cos\{2d\phi\}+2v_4\cos\{4d\phi\}]$   
 data /  $N_0[1+2v_2\cos\{2d\phi\}]$   
 Black line is  $1+2v_4\cos\{4d\phi\}$

These  $v_2$  are consistent within 3%.

