

# Recent measurements of azimuthal anisotropy $v_n$ in heavy ion collisions

Takahito Todoroki  
University of Tsukuba

KMI Mini-Workshop 2014

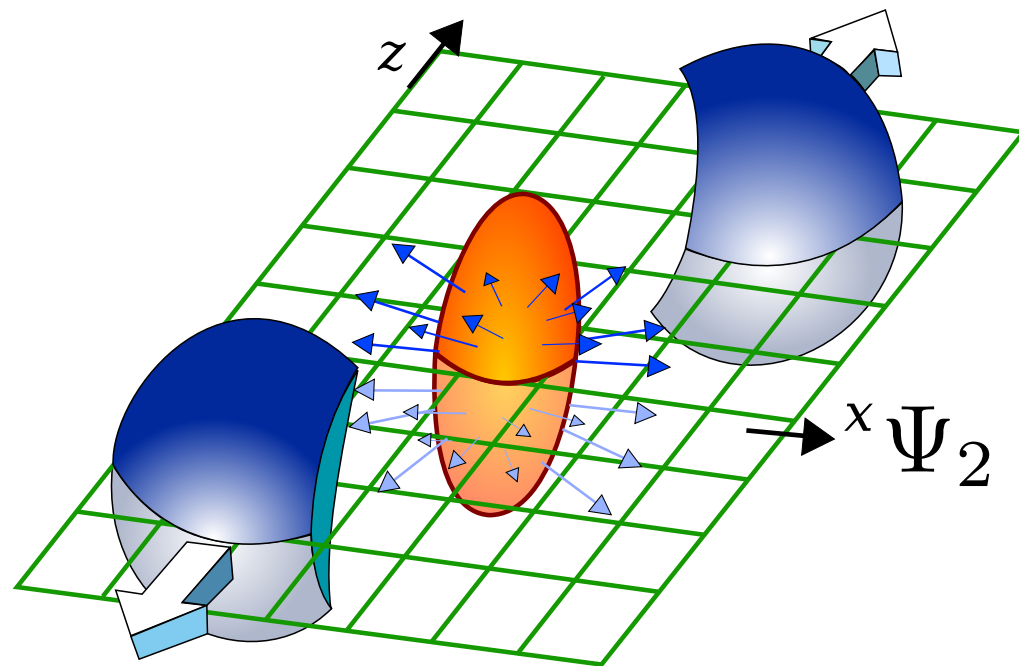
"Fluctuations, collectivity and correlations at RHIC  
and LHC"

October 23, 2014, Nagoya, Japan

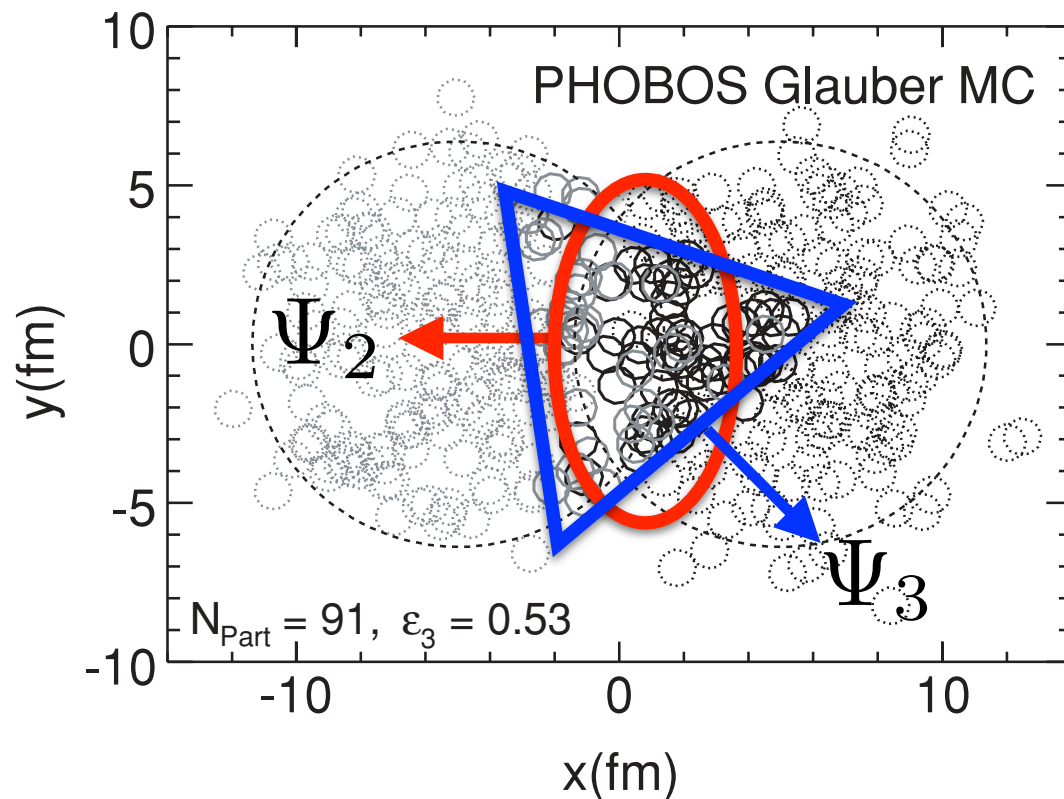
# Outline

- Azimuthal anisotropy in  $p(d)+A$  collisions
- HBT measurements in  $p(d)+A$  collisions
- Event shape control study in  $A+A$  collisions

# Initial Fluctuations



Alver et.al. PRC81.054905



## Simplified Distribution

- Initial spatial anisotropy  $\Rightarrow$  Momentum anisotropy
- Only second-order event-plane

## Ev-by-Ev Fluctuating Distribution

- Higher-order event-planes

$$dN/d\phi \propto 1 + \sum 2v_n \cos n(\phi - \Psi_n)$$

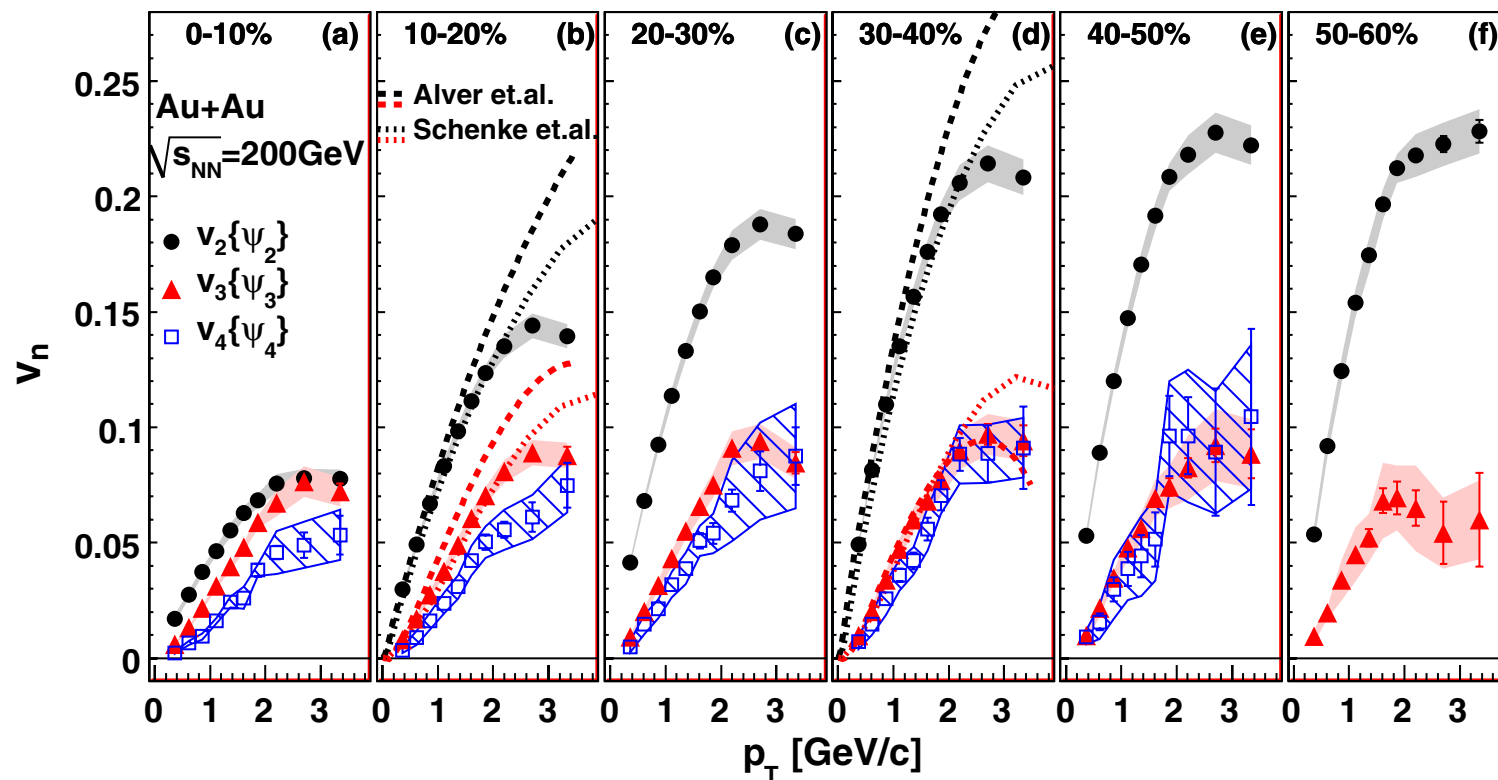
$$\varepsilon_n^{part} = \frac{\sqrt{\langle r^2 \cos n\phi_{part} \rangle^2 + \langle r^2 \sin n\phi_{part} \rangle^2}}{\langle r^2 \rangle},$$

$$\psi_n^{part} = \frac{\text{atan2}(\langle r^2 \cos n\phi_{part} \rangle, \langle r^2 \sin n\phi_{part} \rangle) + \pi}{n}$$

# Differential $v_n$ measurements

**RHIC**

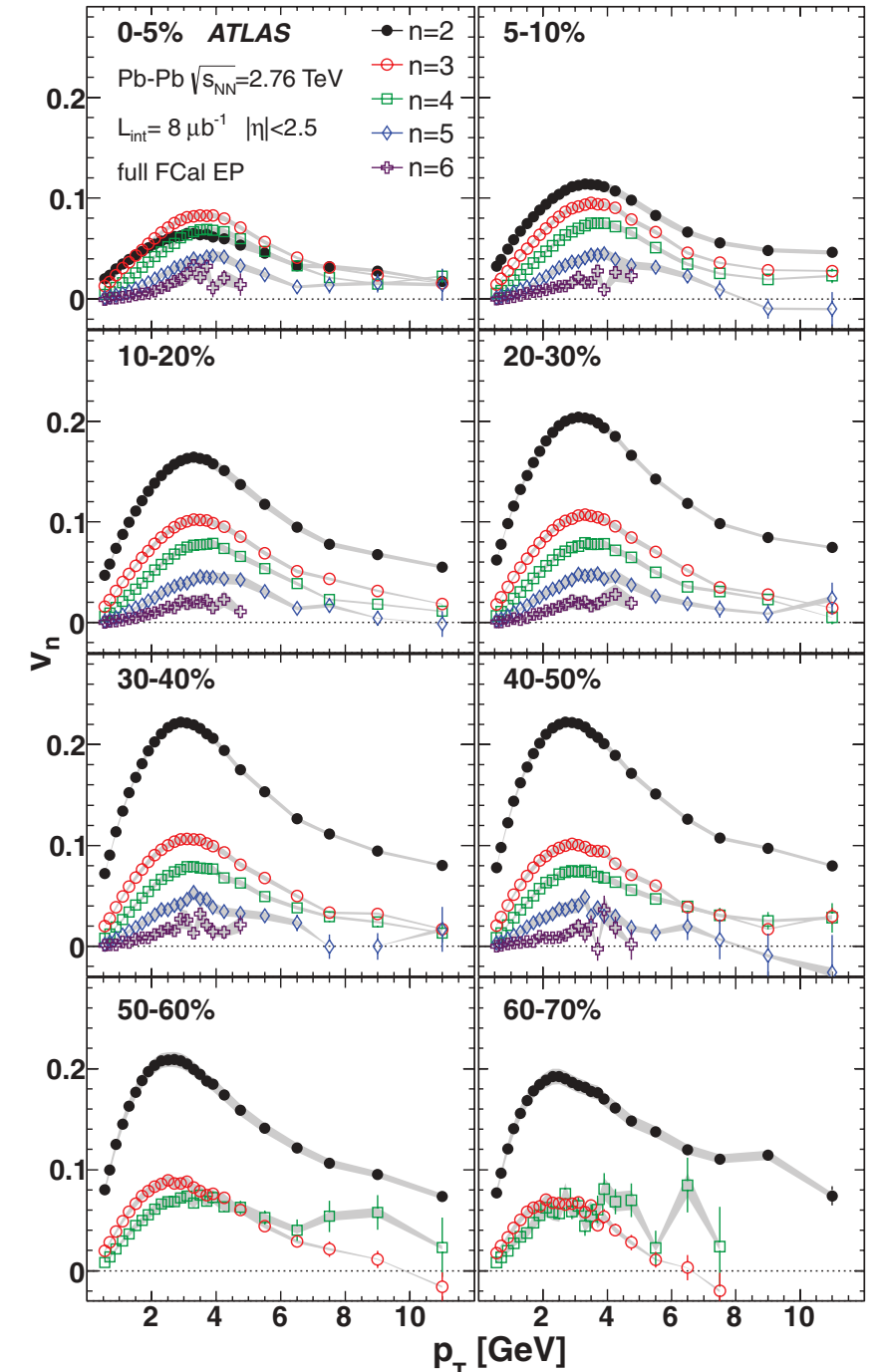
PHENIX PRL107.252301



- Substantial higher order flow harmonics  $v_n$  is observed in both RHIC and LHC energy ranges

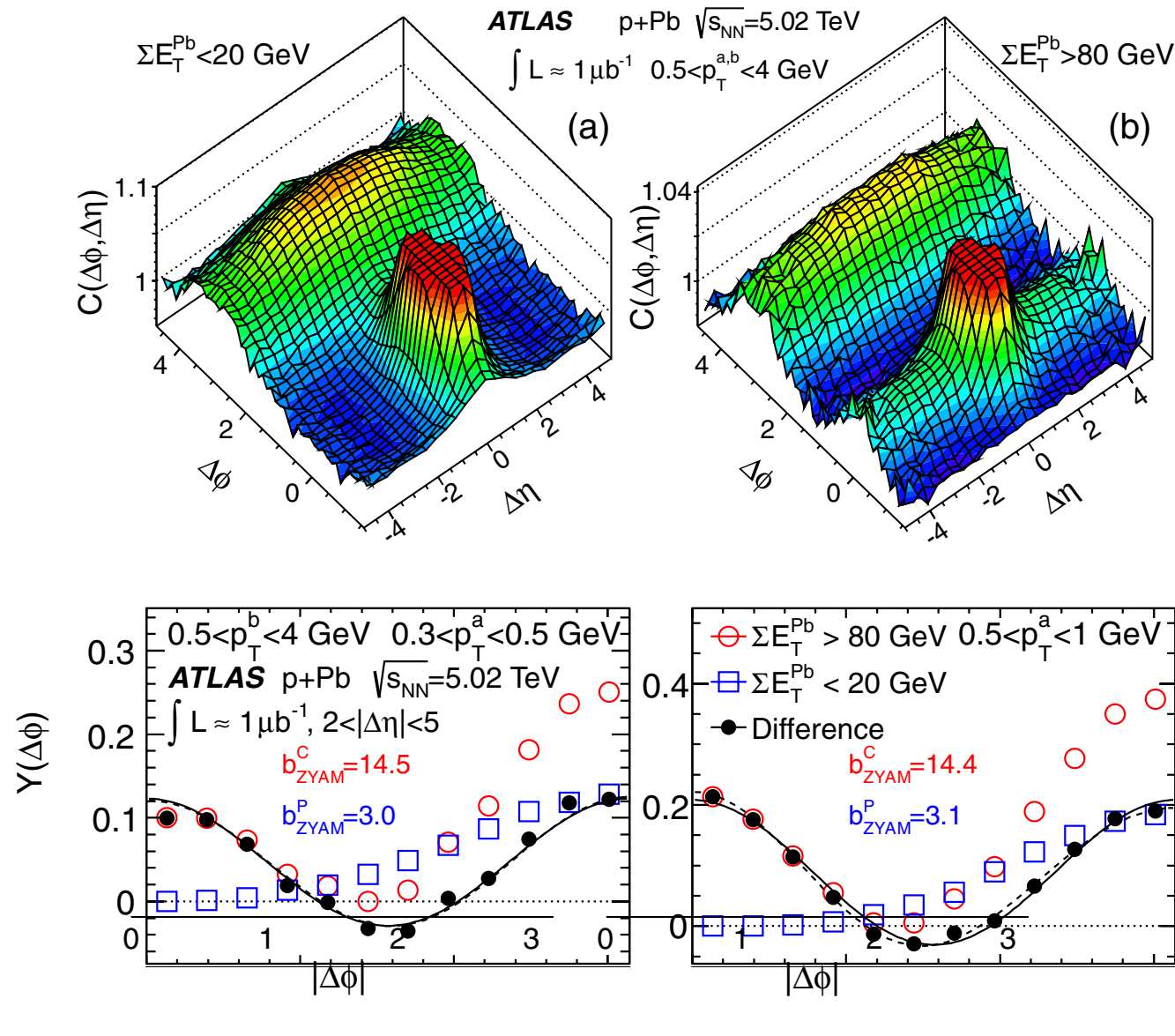
**LHC**

ATLAS PRC86.014907

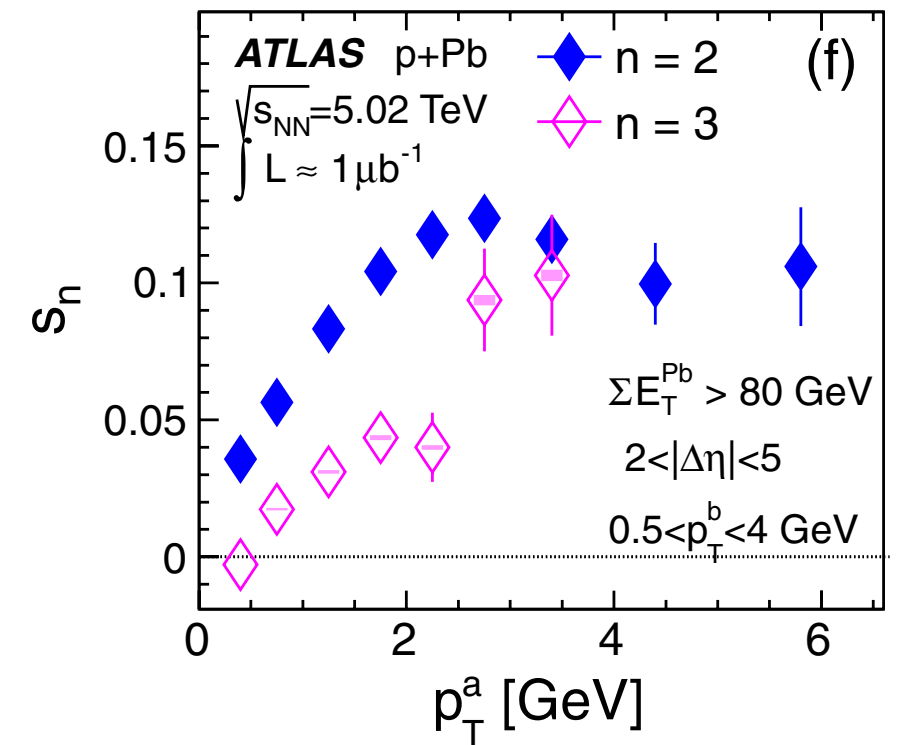




# Ridge & $v_n$ in p+Pb collisions

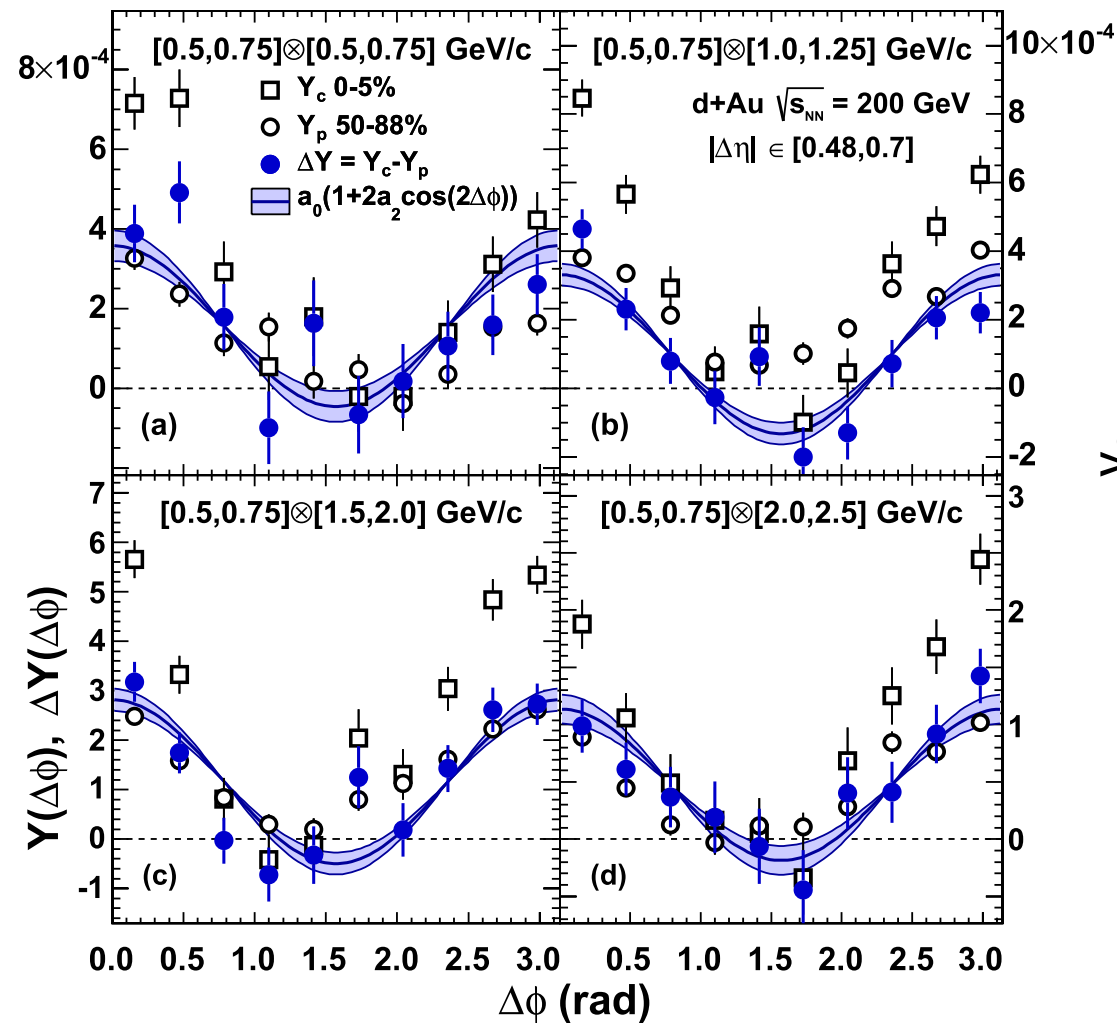


ALICE: Physics Letters B 726 (2013)  
 ATLAS: Phys. Rev. Lett. 110(2013)  
 CMS: Phys. Lett. B 7198(2013)

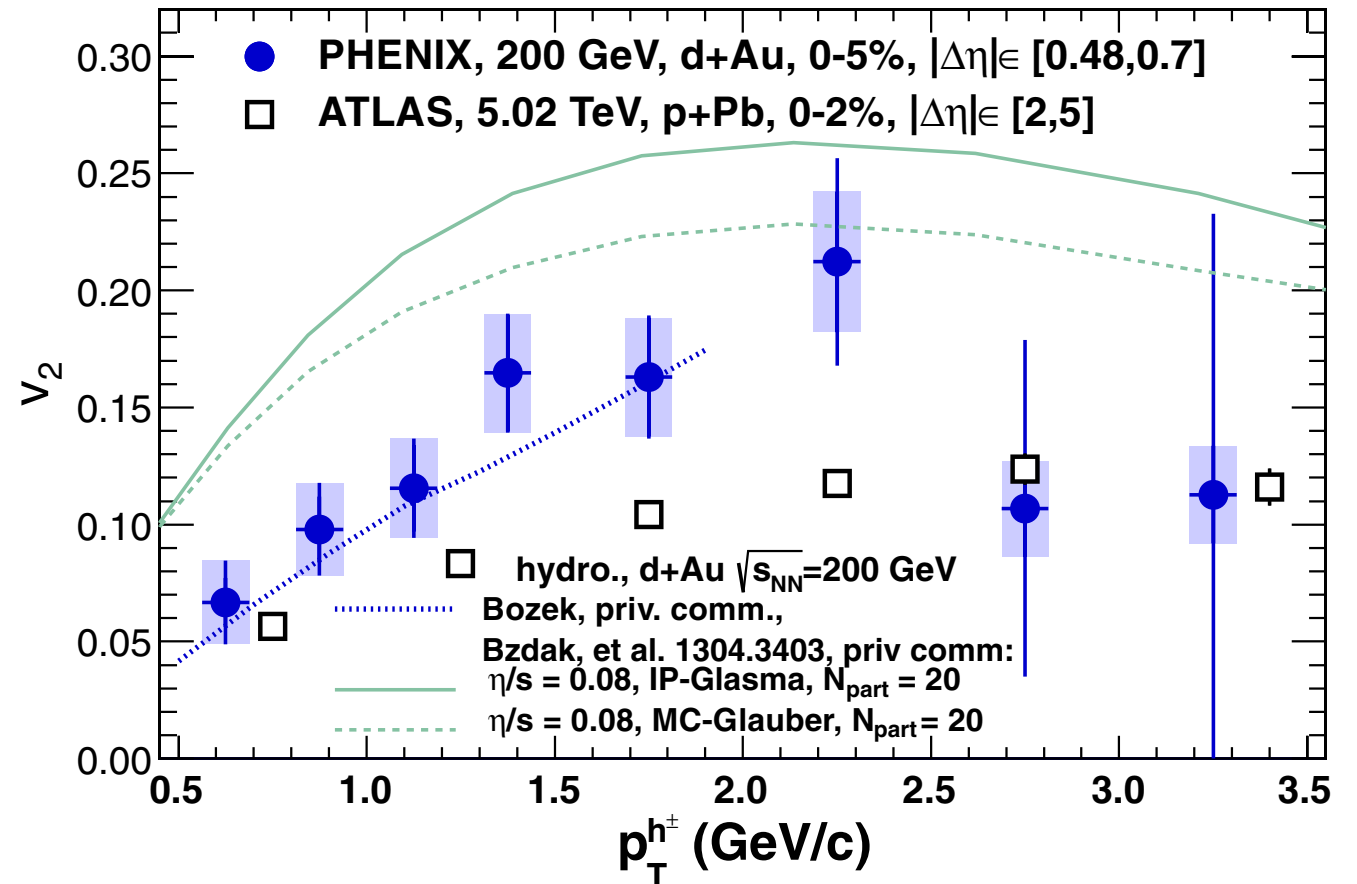


- Ridge and  $v_{2,3}$  are observed in high multiplicity p+Pb collision events

# Ridge and $v_2$ in d+Au collisions

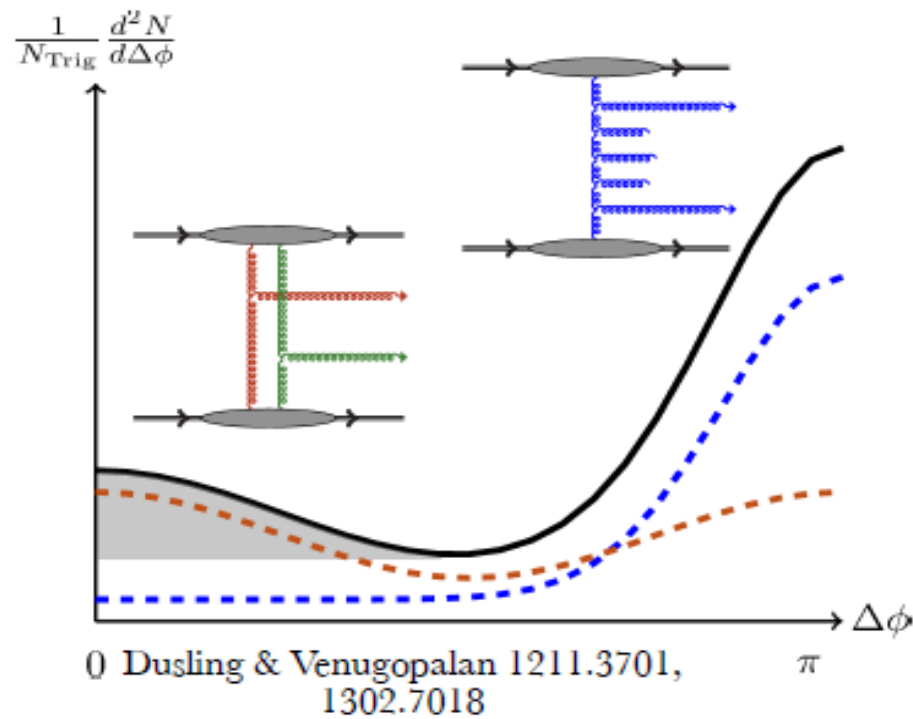


PRL111.212301(2013)

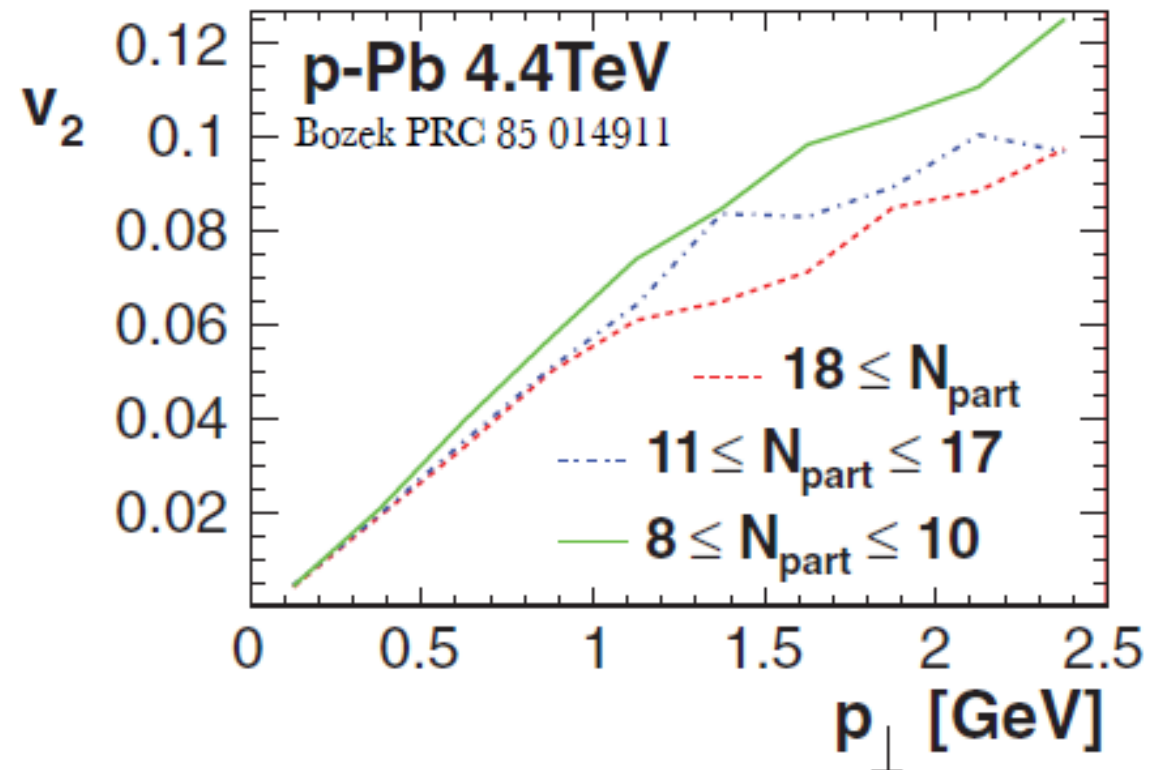


- Peripheral subtraction at  $0.48 < |\Delta\eta| < 0.7$
- None zero  $v_2$  is observed in 0-5% d+Au collisions,
  - Similar  $p_T$  dependence of  $v_2$  in 0-2% p+Pb collisions
  - Consistent with hydrodynamics calculations

# Initial or Final State Effect?



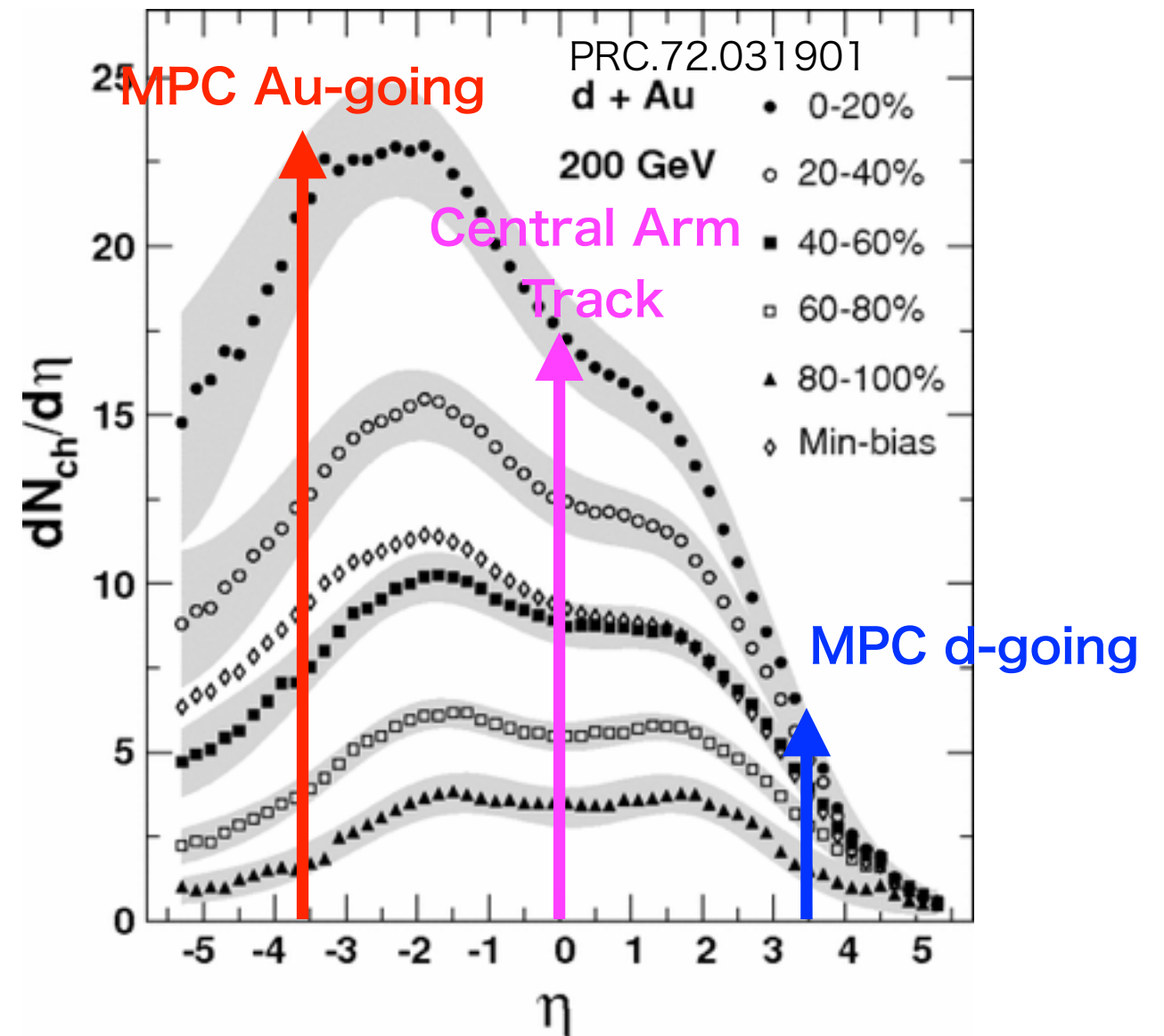
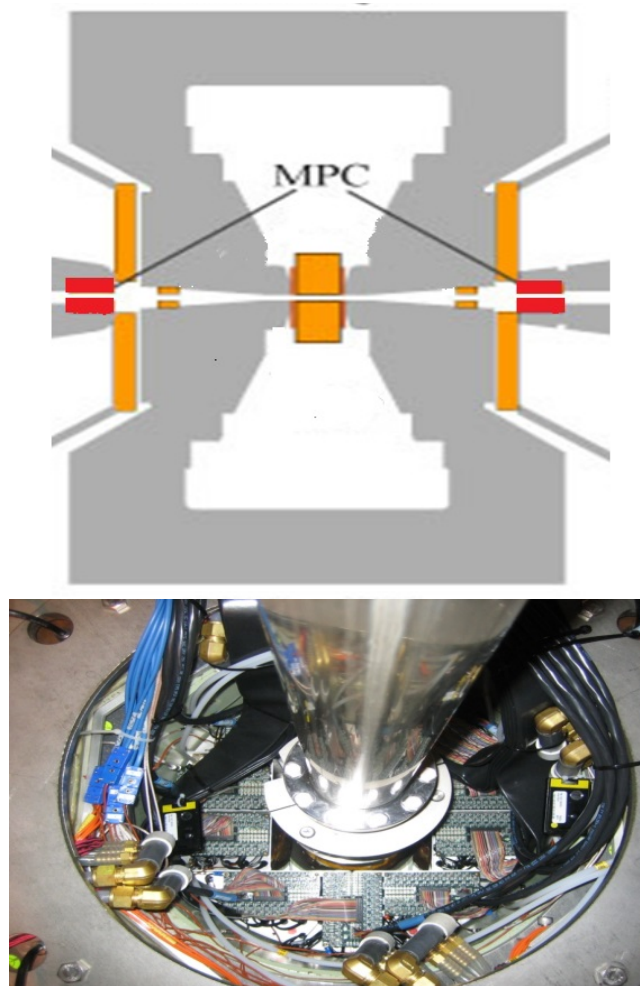
**CGC**



**Hydrodynamics**

- Both initial state (CGC) and final state (hydro) effects can explain  $v_n$  in small collisions systems
- Need more constraints by differential measurements

# Long-range rapidity correlations



- Muon Piston Calorimeter (MPC) : at  $3 < |\eta| < 4$
- Rapidity separation of  $|\Delta\eta| > 2.75$  is achieved by measuring correlations between tracks ( $|\eta| < 0.35$ ) and MPC towers

# Track-tower angular correlations

$$s(\Delta\phi) = \frac{d(\omega_{tower} N_{same}^{track-tower})}{d(\Delta\phi)} : \text{Track-Tower correlations in same events}$$

$$\Delta\phi = \phi_{tower} - \phi_{track}$$

$\omega_{tower}$  : Transverse Energy of each tower  
(Proportional to multiplicity)

$N_{same}^{track-tower}$  : Number of Track-Tower Pairs in same events

$M(\Delta\phi)$  : Track-Tower correlations in mixed events

$$C(\Delta\phi) = \frac{S(\Delta\phi) \int M(\Delta\phi)}{M(\Delta\phi) \int S(\Delta\phi)} : \text{Correlation Function by Event Mixing}$$

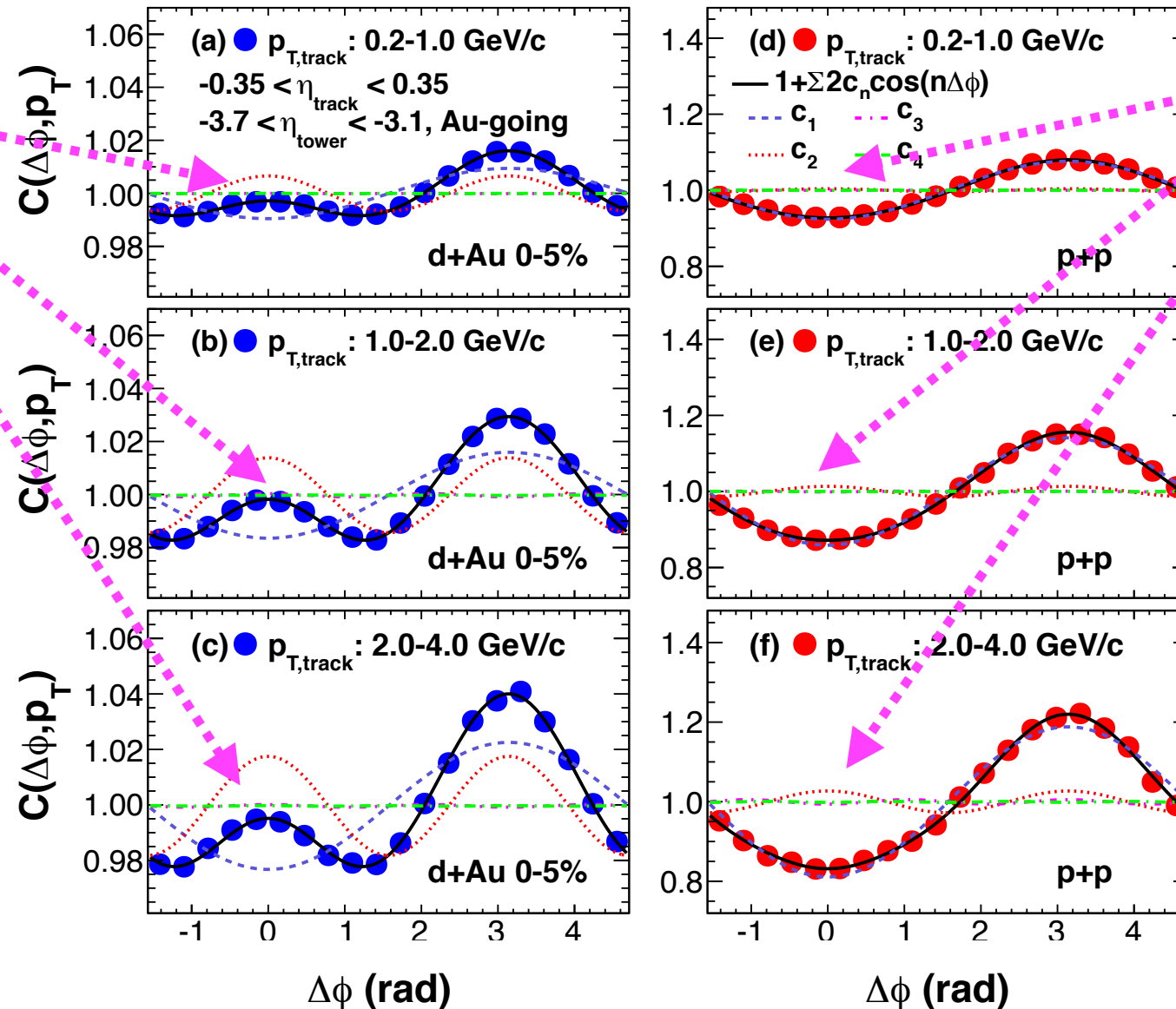


# Correlations in p+p and 0-5% d+Au collisions

arXiv:1404.7461

Ridge

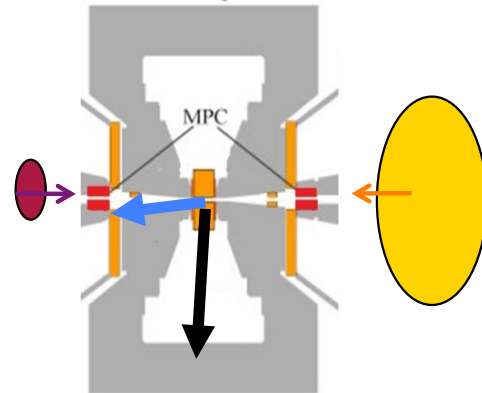
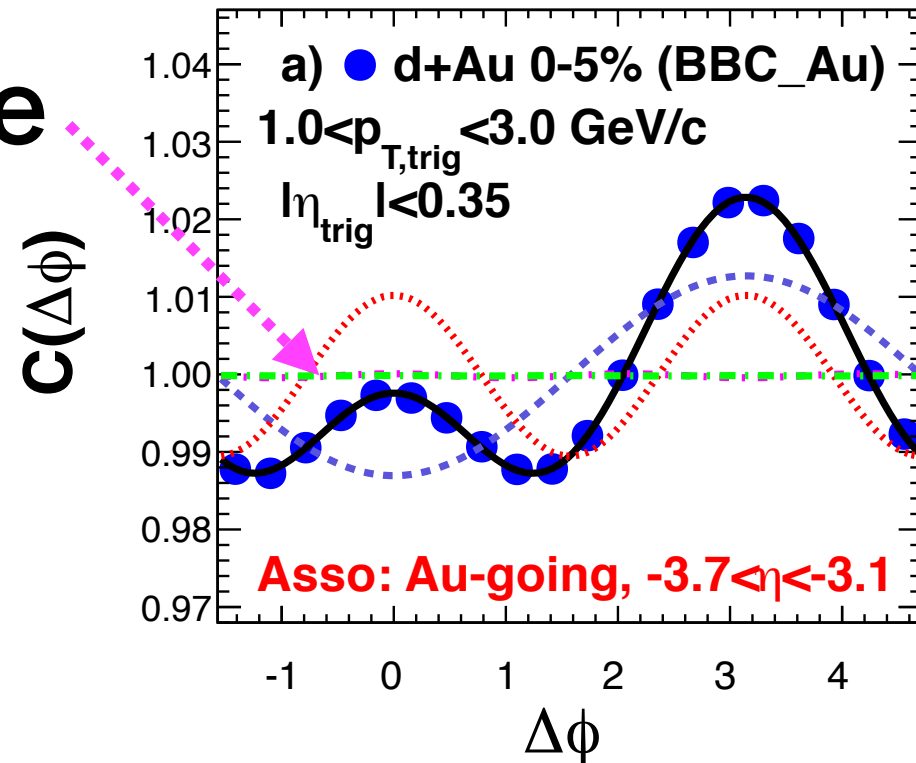
No Ridge



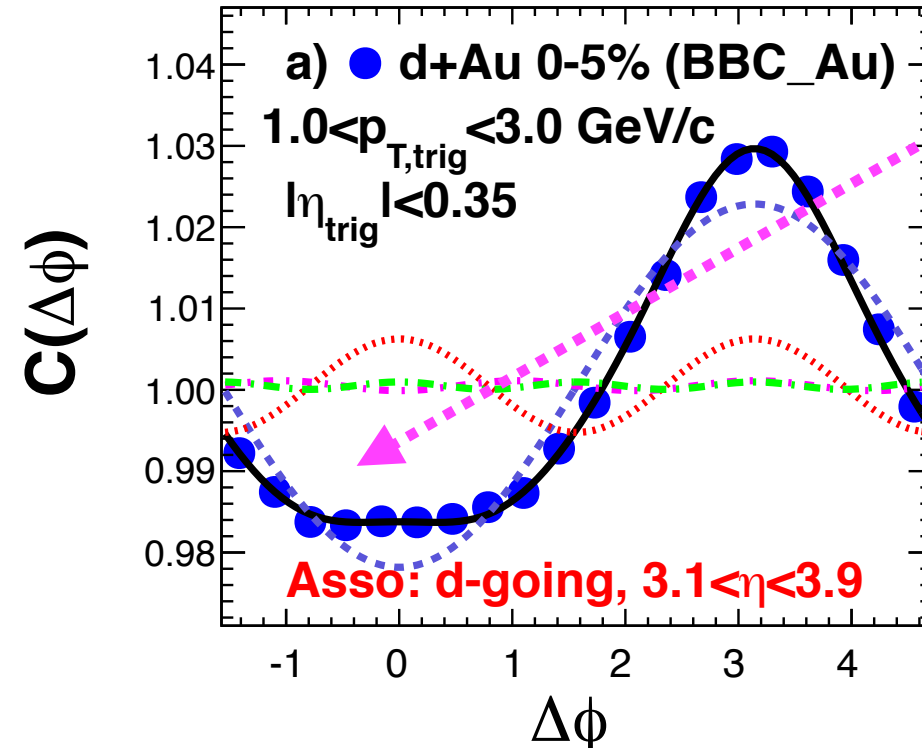
- Ridge is observed in 0-5% d+Au collisions, which is not observed in p+p collisions

# “Au-going” & “d-going”

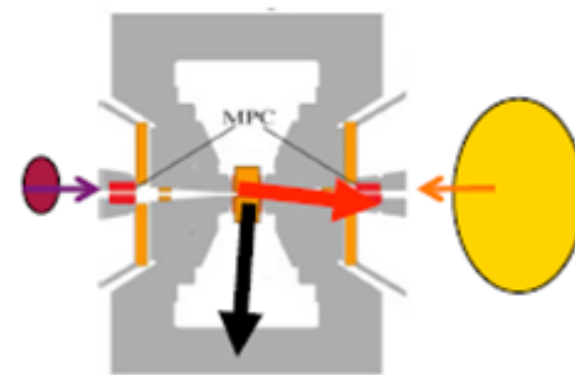
Ridge



arXiv:1404.7461



No Ridge

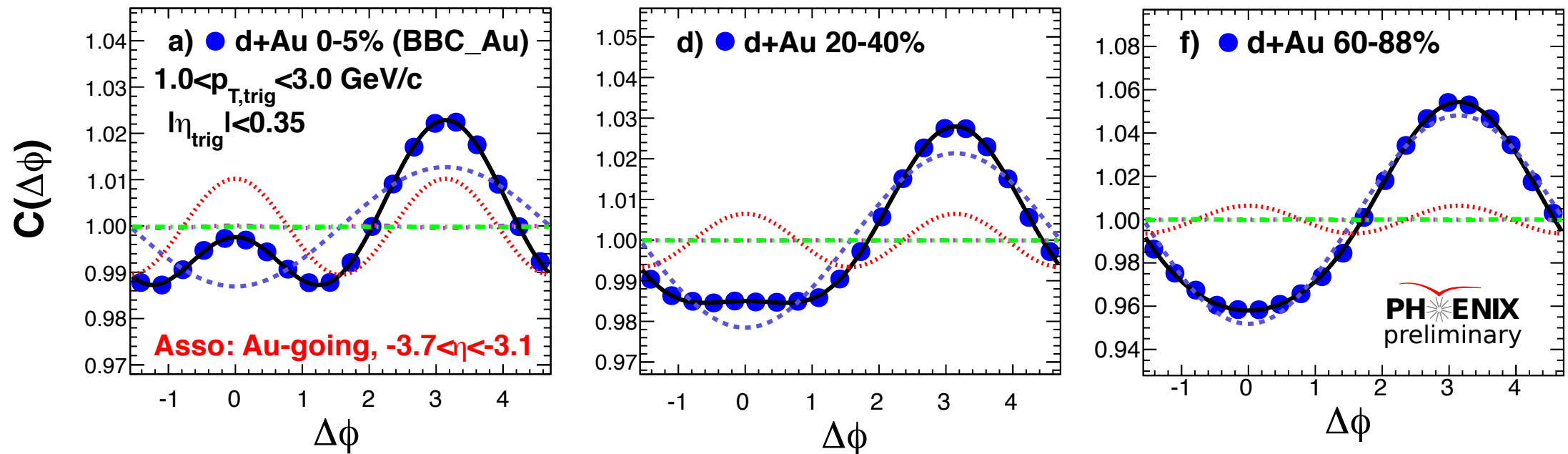


- Ridge is observed in “Au-going” direction
- No ridge is observed in “d-going” direction
- Non-zero  $\cos 2\Delta\phi$  is observed in both directions

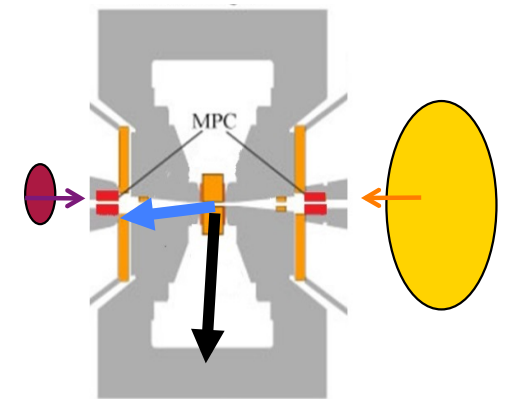


# Centrality dependence in “Au-going” direction

arXiv:1404.7461

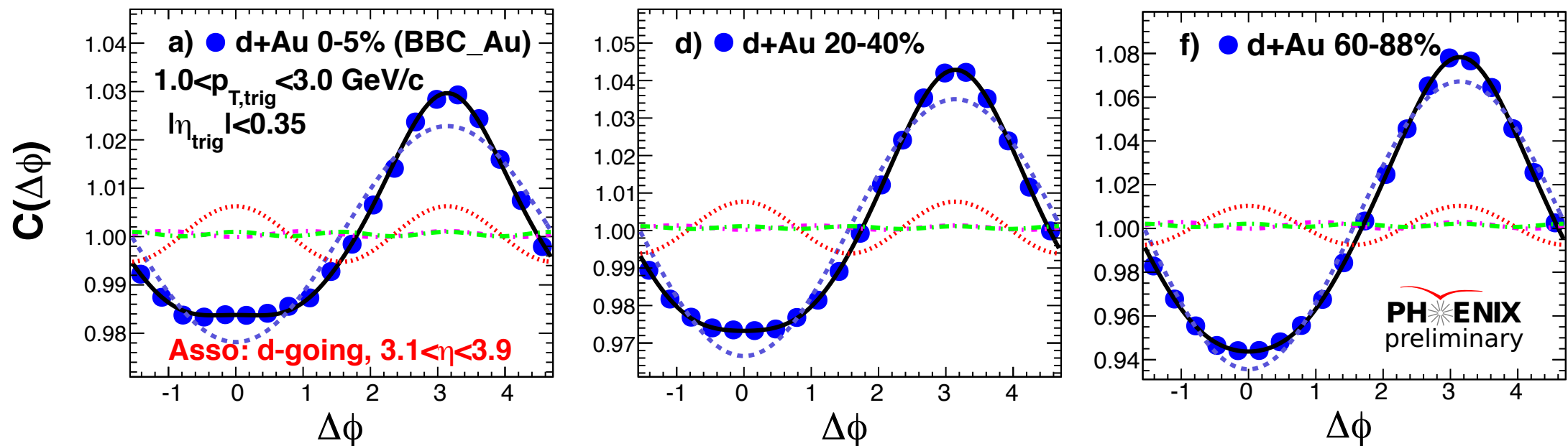


- Ridge is observed only in most-central d+Au collisions
- None-zero  $\cos 2\Delta\phi$  is observed in all centralities

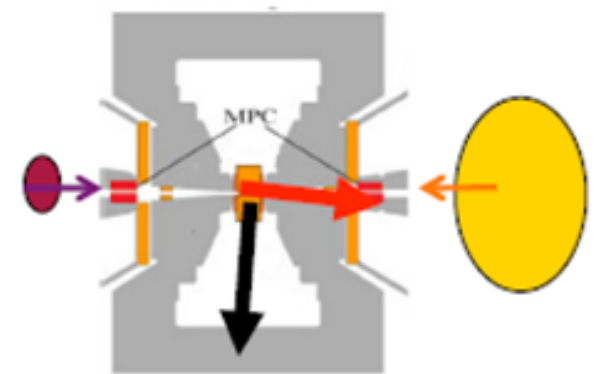


# Centrality dependence in “d-going” direction

arXiv:1404.7461

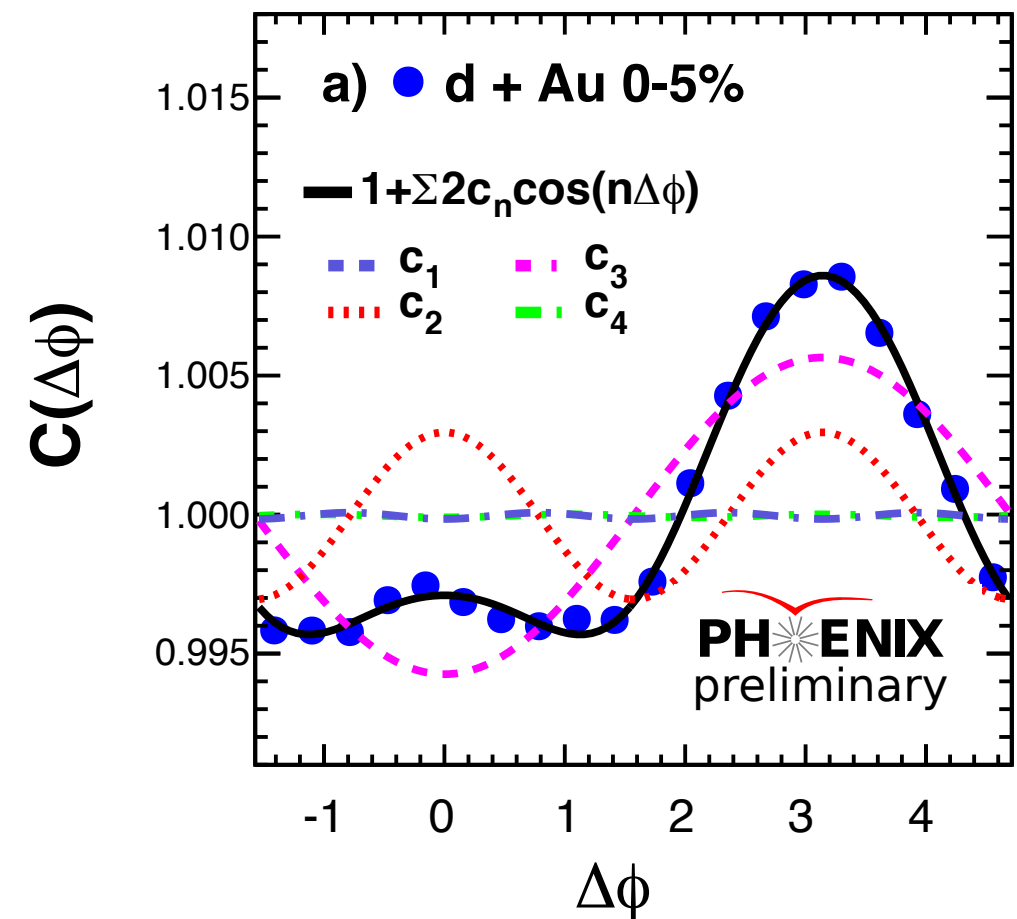
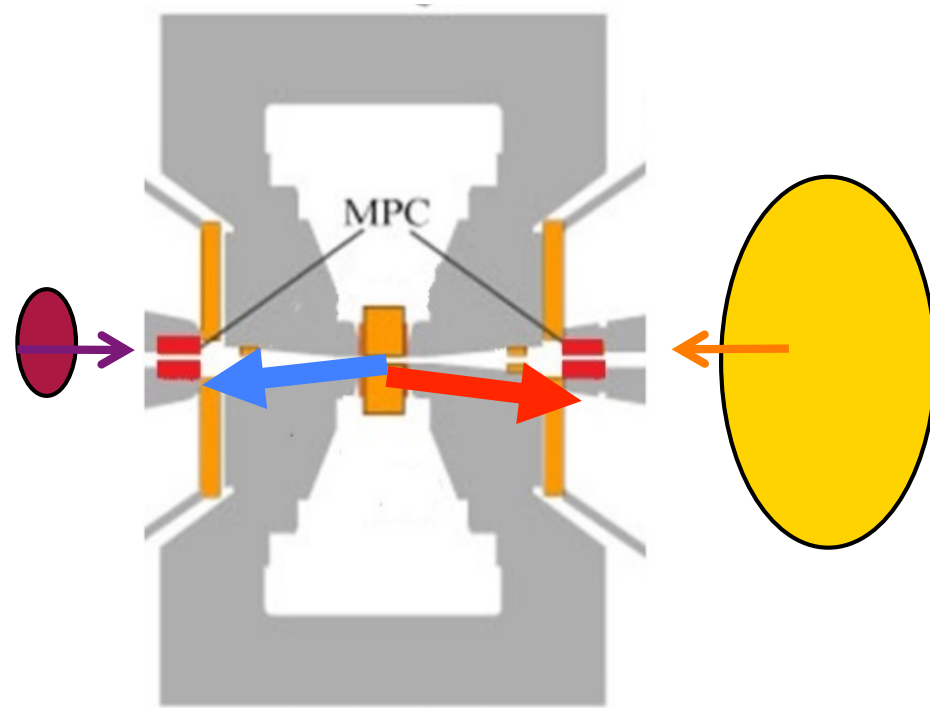


- No ridge is observed even in most-central
- None-zero  $\cos 2\Delta\phi$  is observed in all centralities,  $\cos 2\Delta\phi$  overwhelmed by  $\cos 1\Delta\phi$
- What if peripheral subtraction?
- Subtraction method appears to be important when discussing correlation shapes



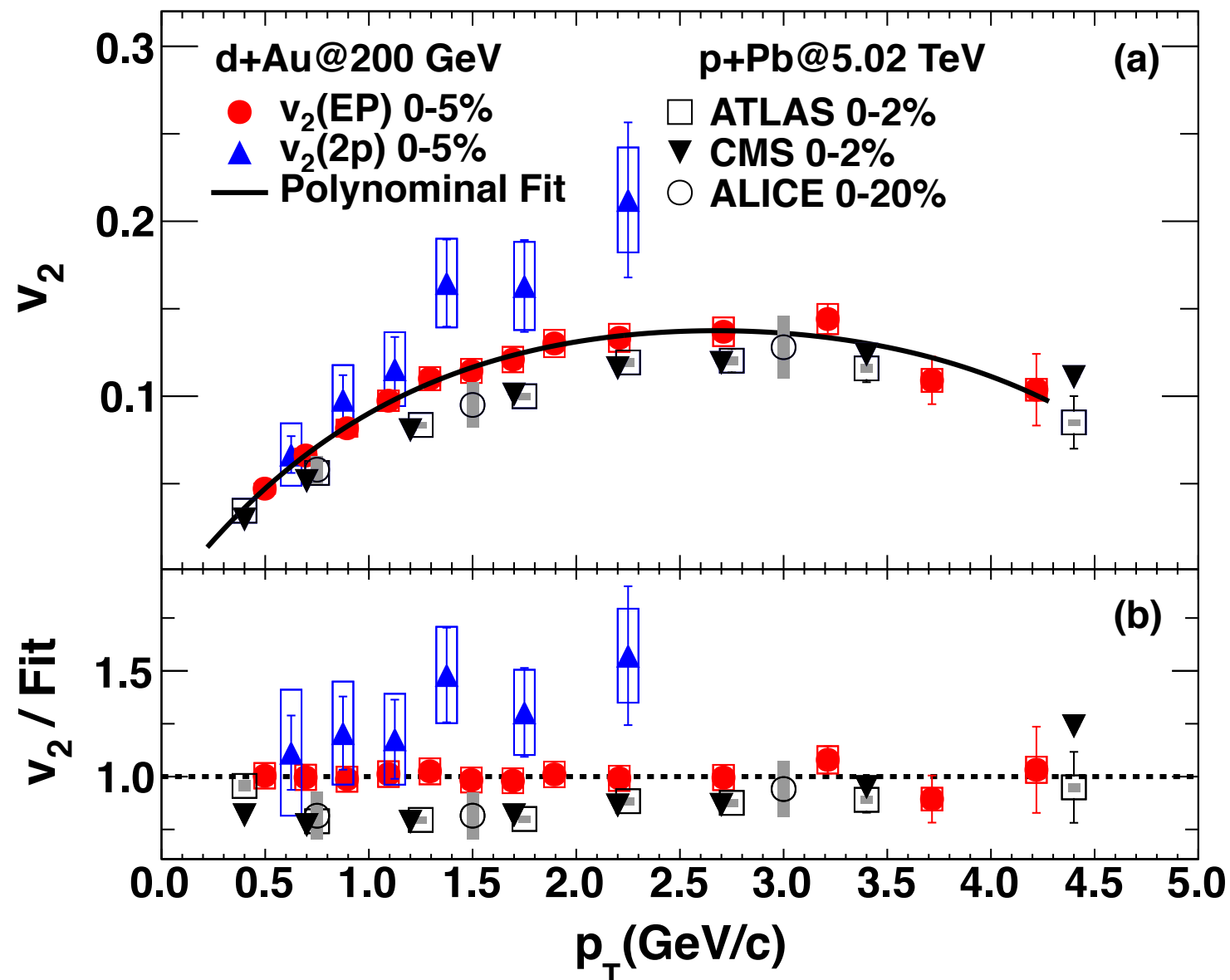
# Ridge across $|\Delta\eta|>6$

arXiv:1404.7461



- $E_T$  integrated tower-tower correlations
- Forward-Backward correlations show a ridge across  $|\Delta\eta|>6$ !!
- Unlike jet effects

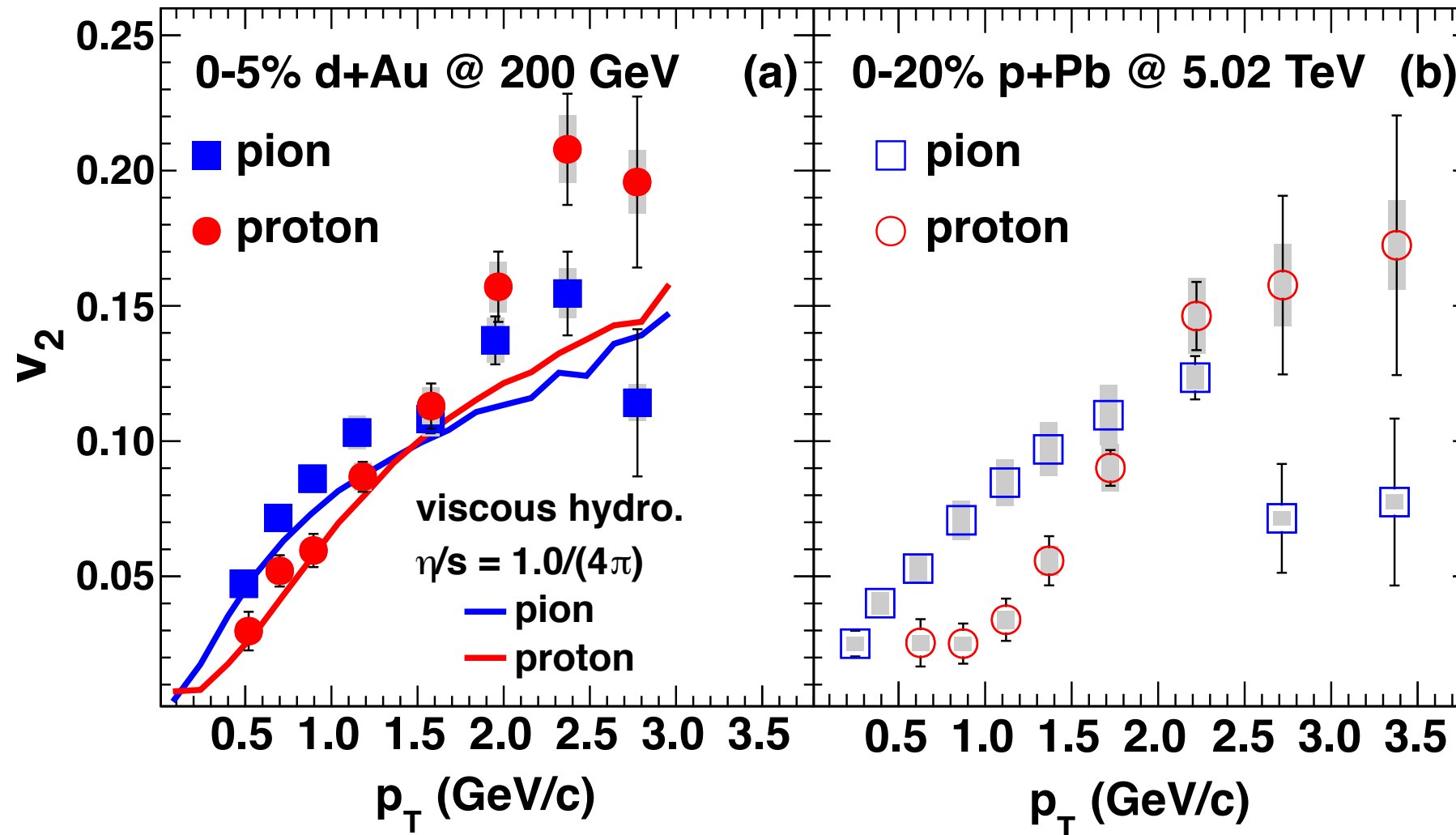
# $v_2$ with more rapidity gap



- EP method using MPC : MPC-CNT rapidity gap  $|\Delta\eta| > 2.75$
- Sizable  $v_2$  observed across large rapidity gap

# PID $v_n$ in $p(d)+A$

PHENIX arXiv:1404.7461v1  
ALICE Phys.Let.B726.164-177

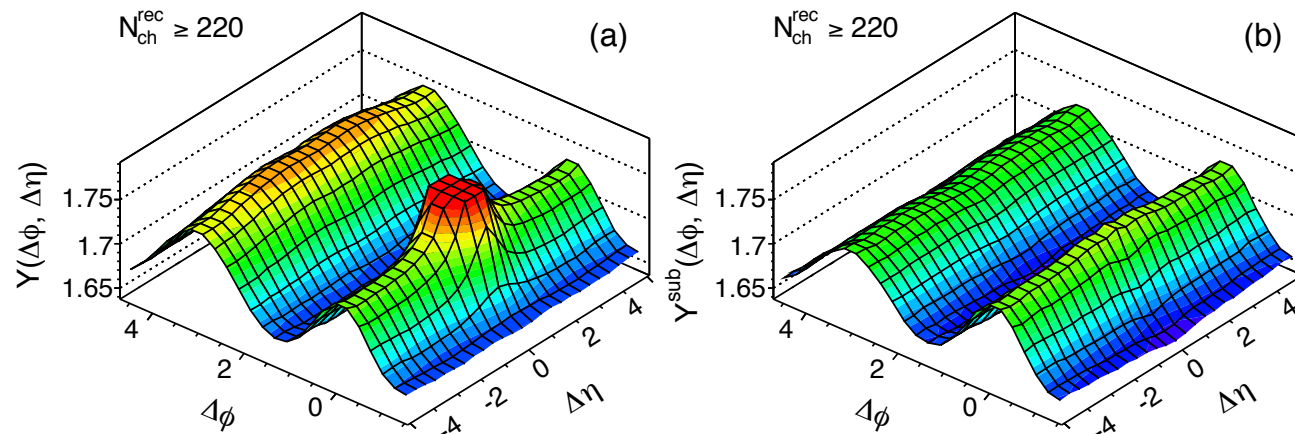


- Mass dependence in low  $p_T$
- Baryon/Meson difference at intermediate  $p_T$
- Qualitatively consistent with hydrodynamics.

# Non-flow effects in p+A collisions

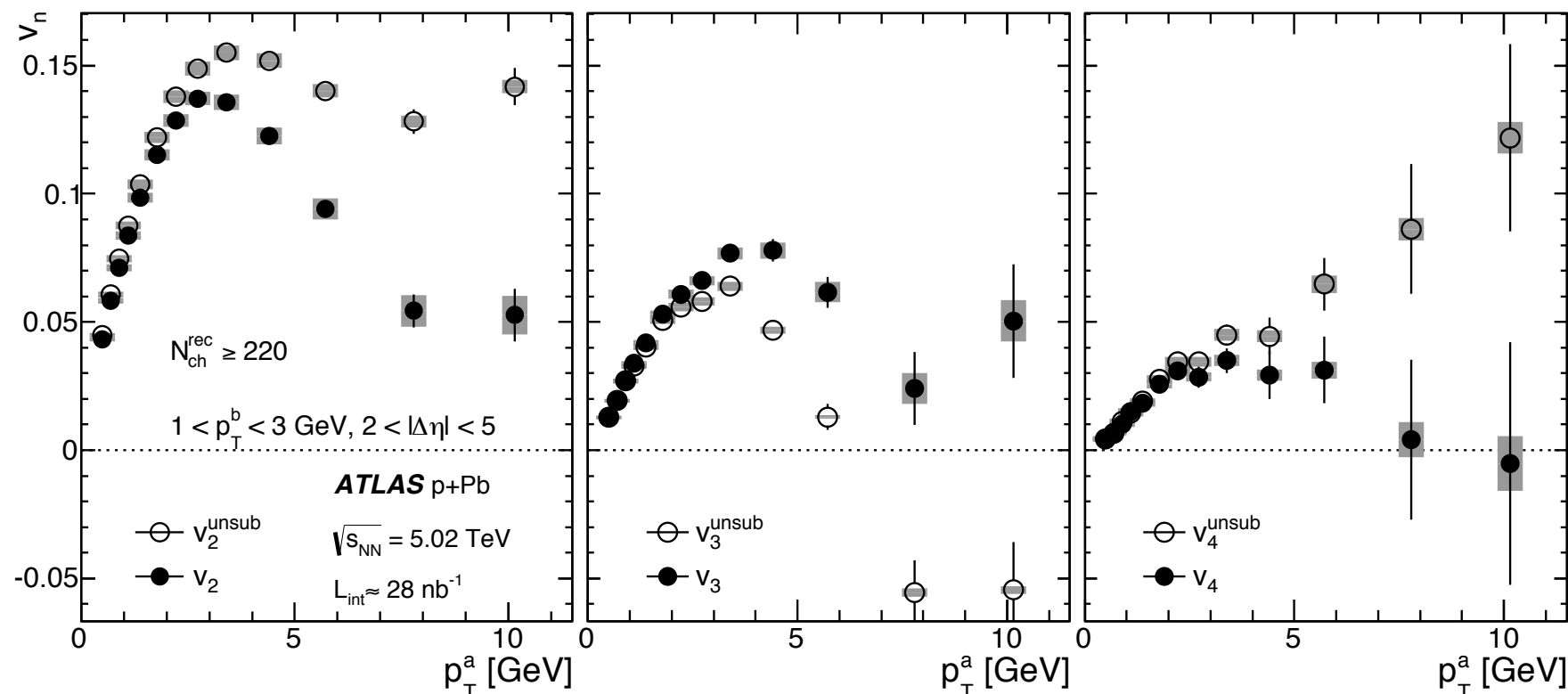
## Recoil Jet Subtraction

ATLAS arXiv:1409.1792v1

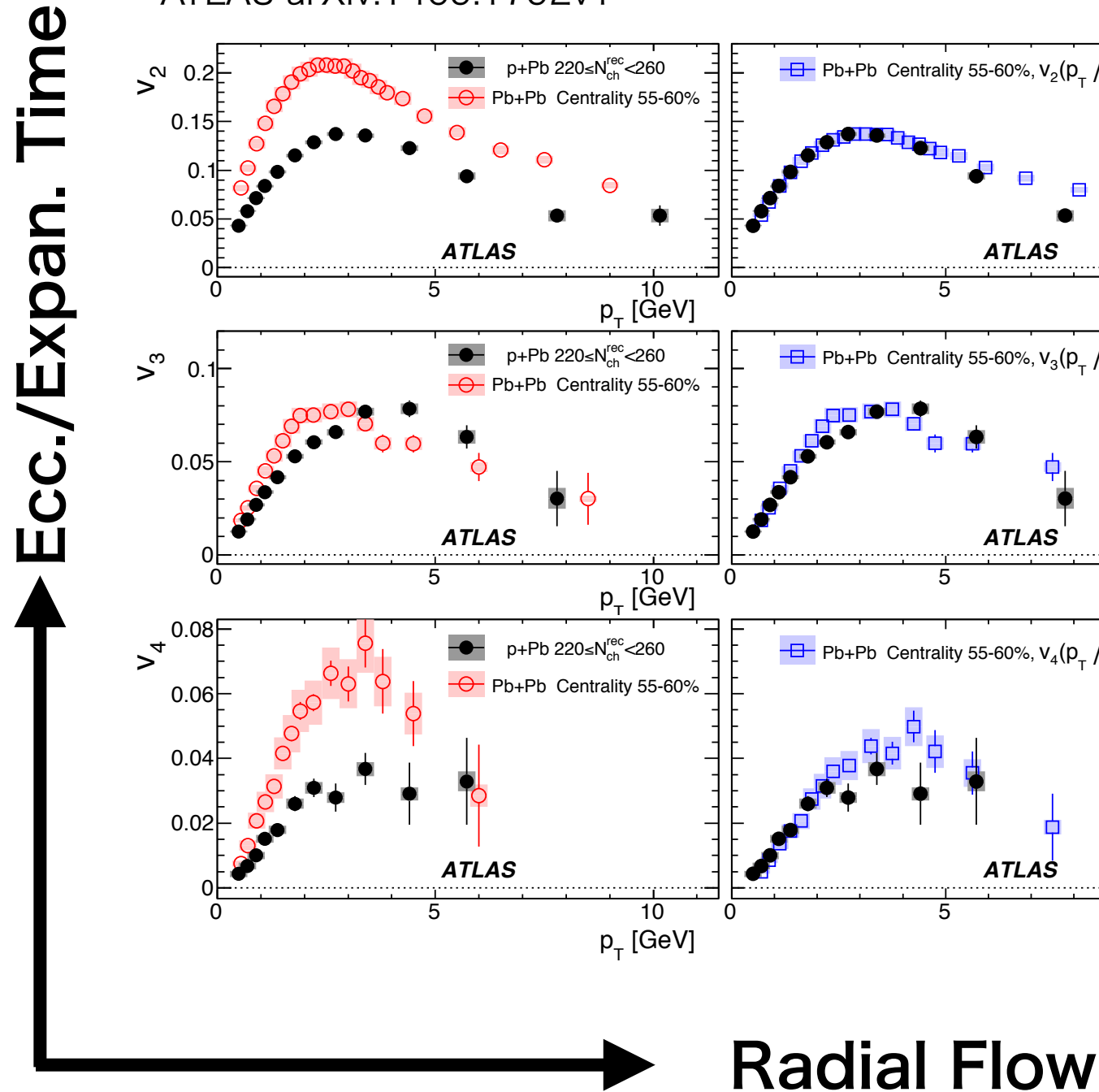


$$Y^{sub}(\Delta\phi) = Y(\Delta\phi) - \alpha Y_{peri}^{corr}(\Delta\phi)$$

- $\alpha$  tuned to completely subtract near-side yield
- Subtraction results in  $v_n=0 \sim 0.05$  at high  $p_T$
- $\sim 10\%$  reduction of  $v_{2,3}$  at 3 GeV/c



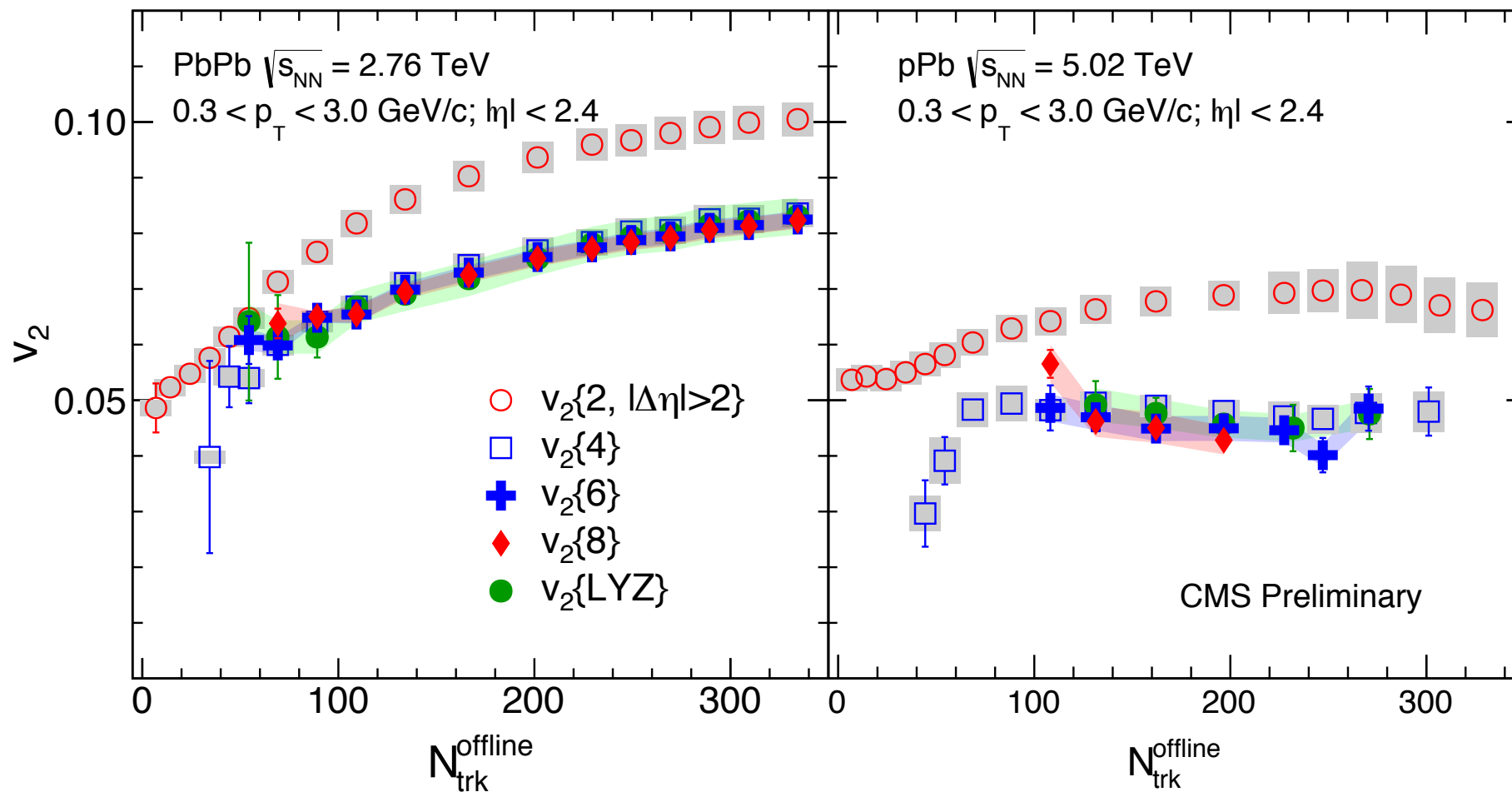
# Scaling among p+A and A+A $v_n$



- Scaled  $v_n$  in A+A collisions match that in p+A collisions
- Suggests similar origin of  $v_n$  in both systems and similar medium response to initial geometry in both systems



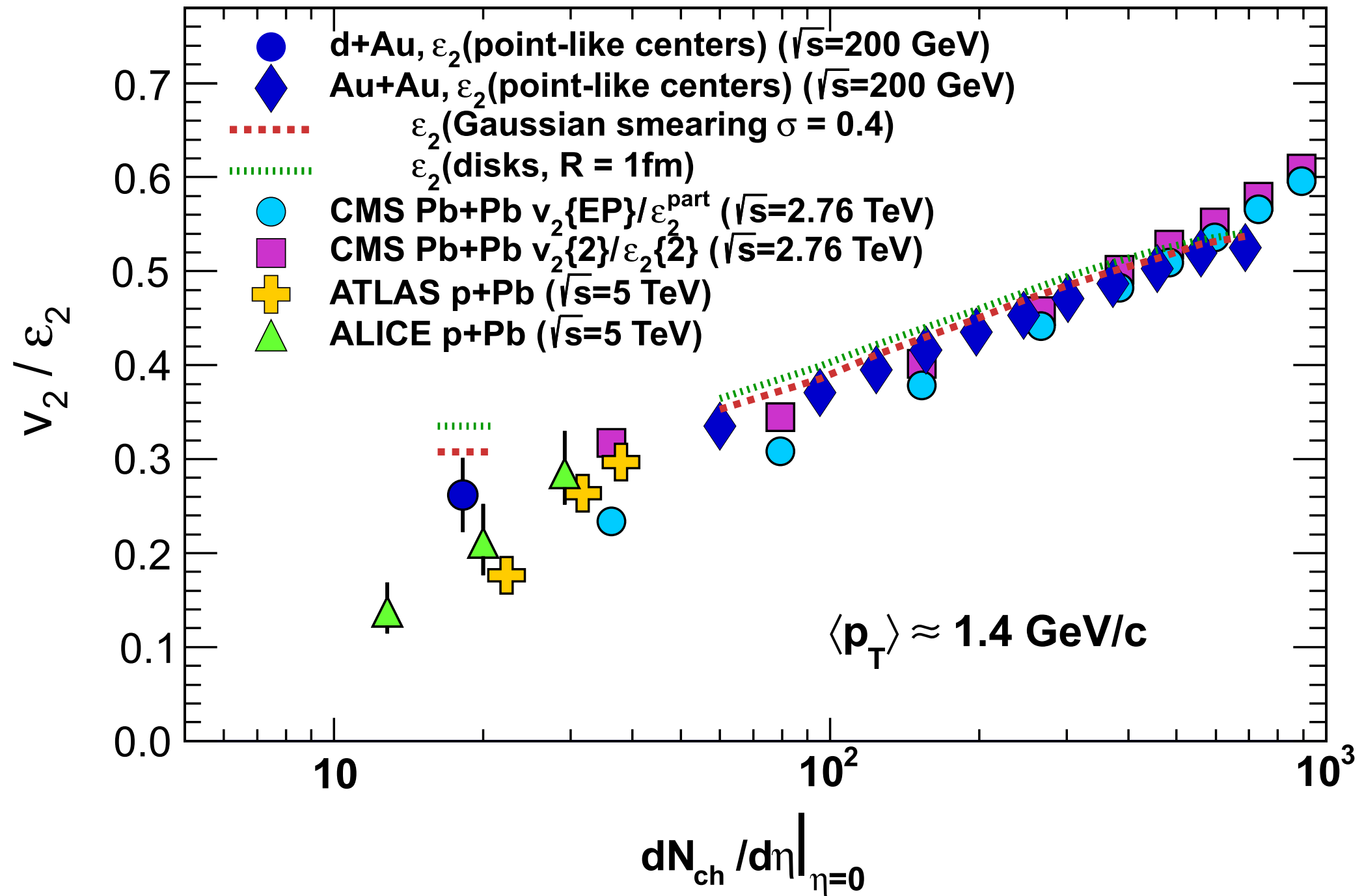
# Multi Particle Cumulants



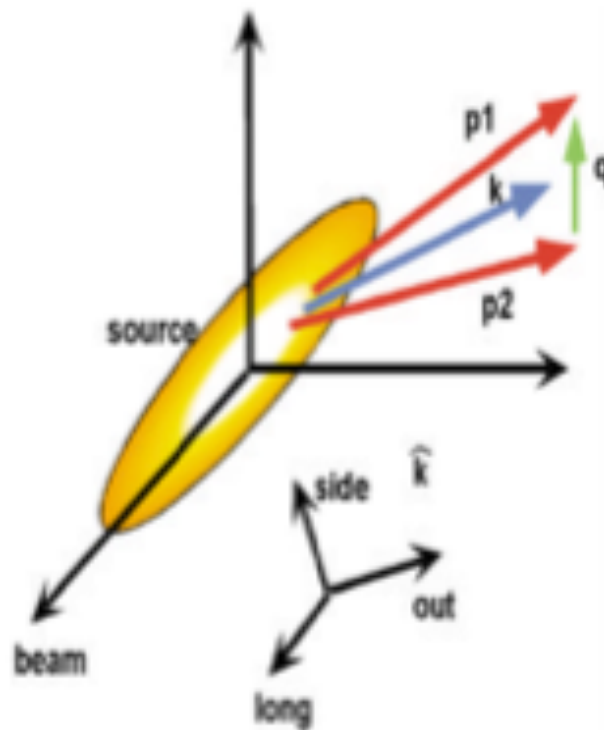
- M.P.C is less sensitive to non-flow than 2-part. cum.
- $\sim 10\%$  reduction of  $v_2$  in both p+A and A+A collisions
- Convergence in  $v_2\{n=4,6,8,\text{LYZ}\}$  in p+A and A+A collisions
- Consistent with hydrodynamics prediction

Bzdak et.al. arXiv:1311.7325

# $v_2/ecc$



# HBT Methodology



LCMS Frame

## Space momentum correlation

$$\begin{aligned}
 C_2 &= P(p_1, p_2) / \{P(p_1)P(p_2)\} \sim 1 + |\rho(q)|^2 \\
 &= C_2^{core} + C_2^{halo} \\
 &= [\lambda(1 + G)F_{coul}] + [1 - \lambda]
 \end{aligned}$$

$$G = \exp(-R_s^2 q_s^2 - R_o^2 q_o^2 - R_L^2 q_L^2 - 2R_{os} q_o q_s)$$

**F<sub>coul</sub>** : coulomb correction factor

**λ** : fraction of pairs in the core

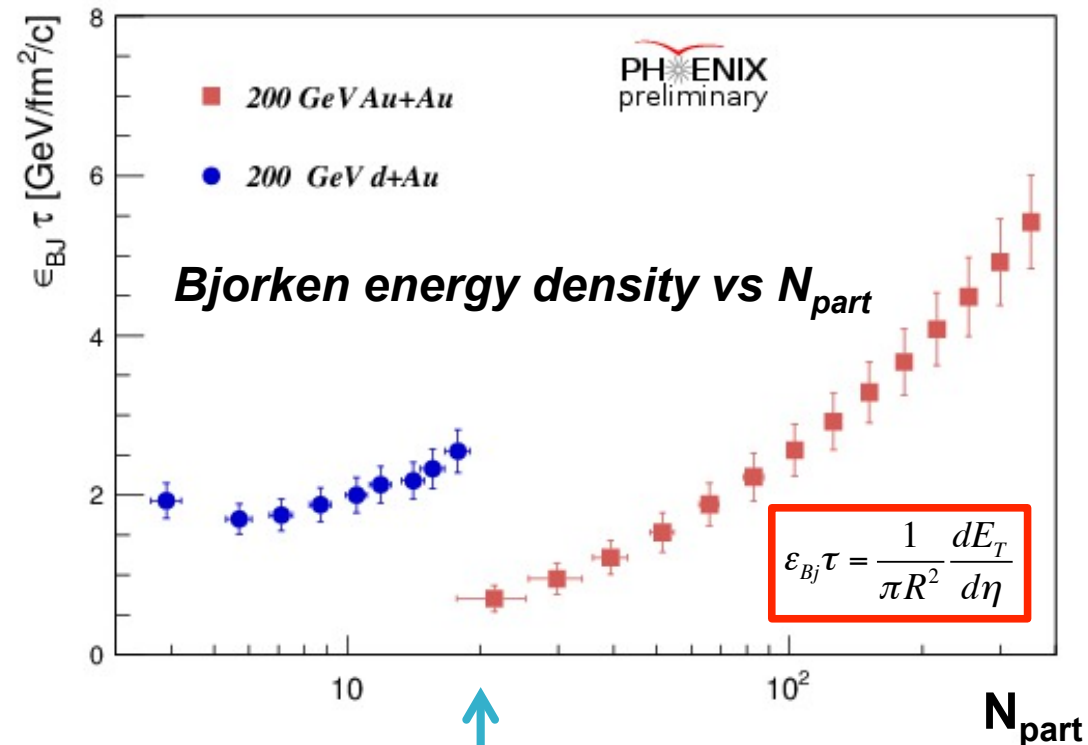
**s** : (sideward) geometrical size

**o** : (outward) geometry and time duration

**L** : (longitudinal) beam direction

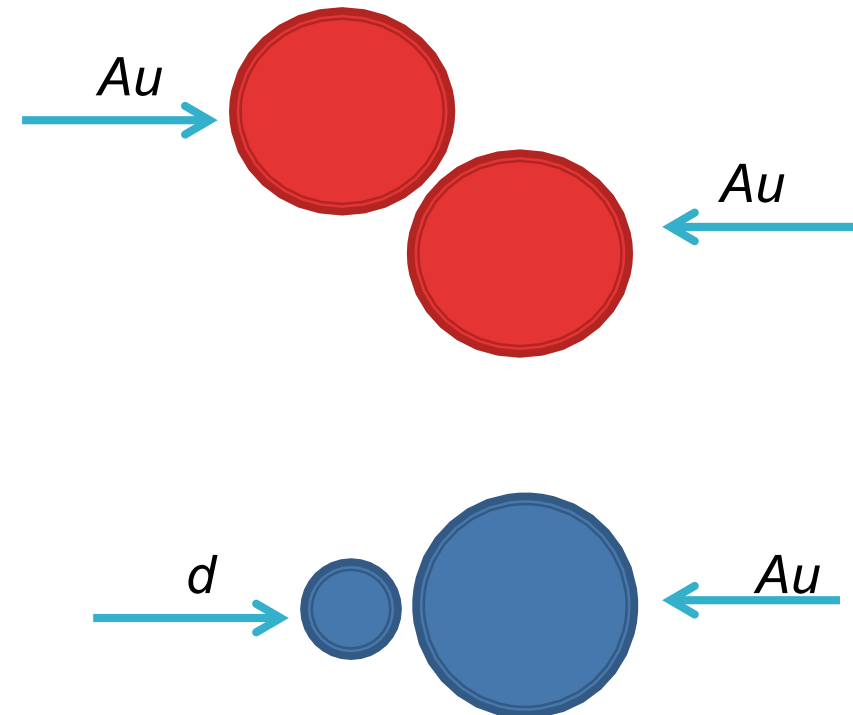
**os** : outward-sideward cross term

# Event selections of d+Au and Au+Au collisions for HBT Analysis

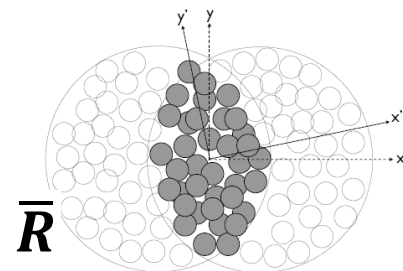


	$N_{part}$	$dE_T / d\eta$	$\bar{R}$	$\epsilon$
Au+Au	$16.7 \pm 1.1$	$19 \pm 1.5$	0.71	0.5
d+Au	$15.7 \pm 1.6$	$22 \pm 1.5$	0.44	2.5

*Initial Parameters for peripheral Au+Au and central d+Au*



**Glauber Model  
initial size**



$$\frac{1}{\bar{R}} = \sqrt{\left( \frac{1}{\sigma_x^2} + \frac{1}{\sigma_y^2} \right)}$$

$\sigma_x$  &  $\sigma_y \rightarrow$  RMS widths  
of density distribution

**Slide from N.Ajit QM'14**

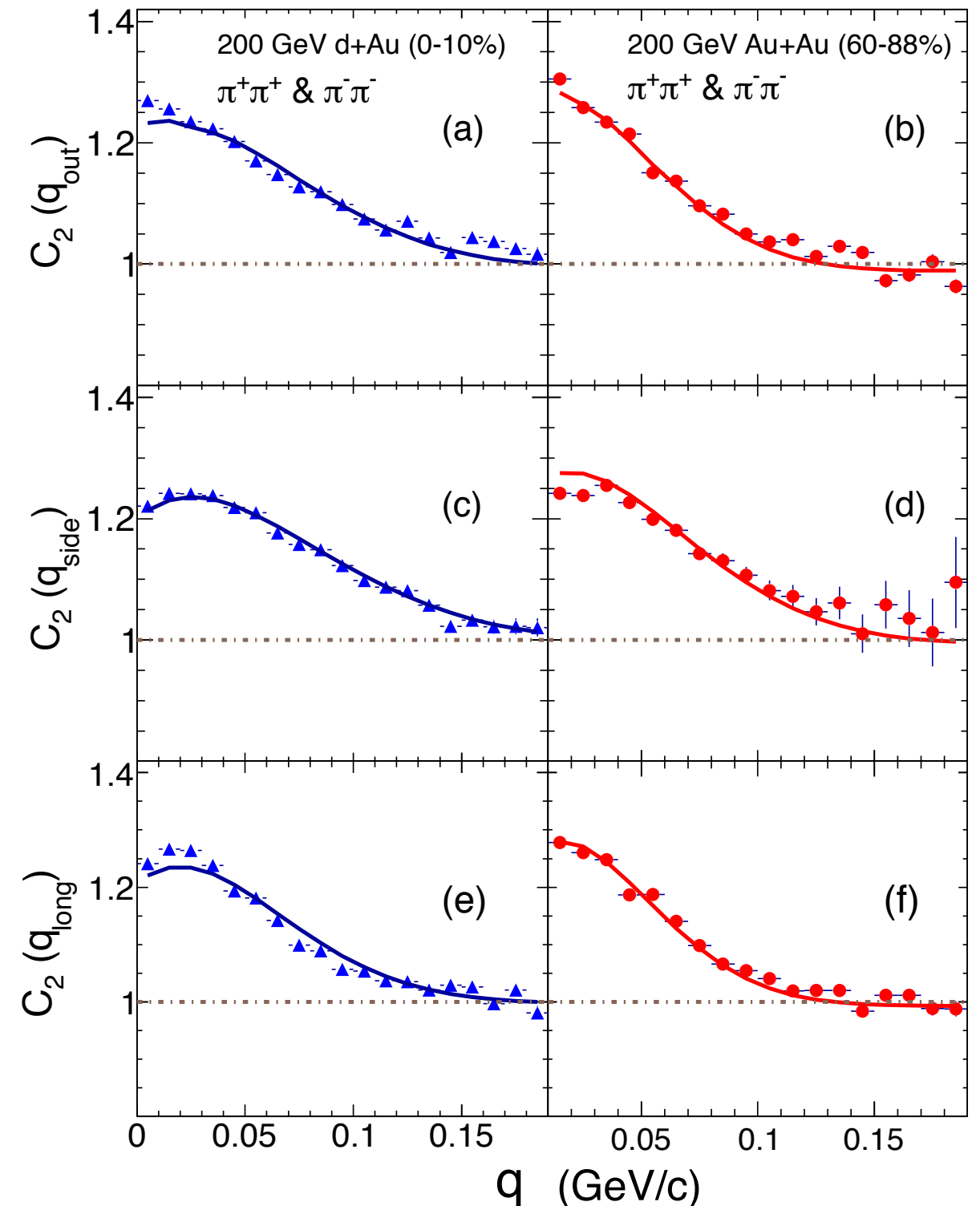
# HBT correlation in d+Au & Au+Au

arXiv:1404.5291

- $\pi^\pm \pi^\pm$  HBT correlations measured at similar  $N_{\text{part}}$  &  $k_T$

	$N_{\text{part}}$	$\langle k_T \rangle$
Au+Au	$16.7 \pm 1.1$	0.39
d+Au	$15.7 \pm 1.6$	0.39

- HBT correlations in d+Au larger than those in Au+Au imply smaller HBT radii



# $m_T$ dependence in d+Au & Au+Au

arXiv:1404.5291

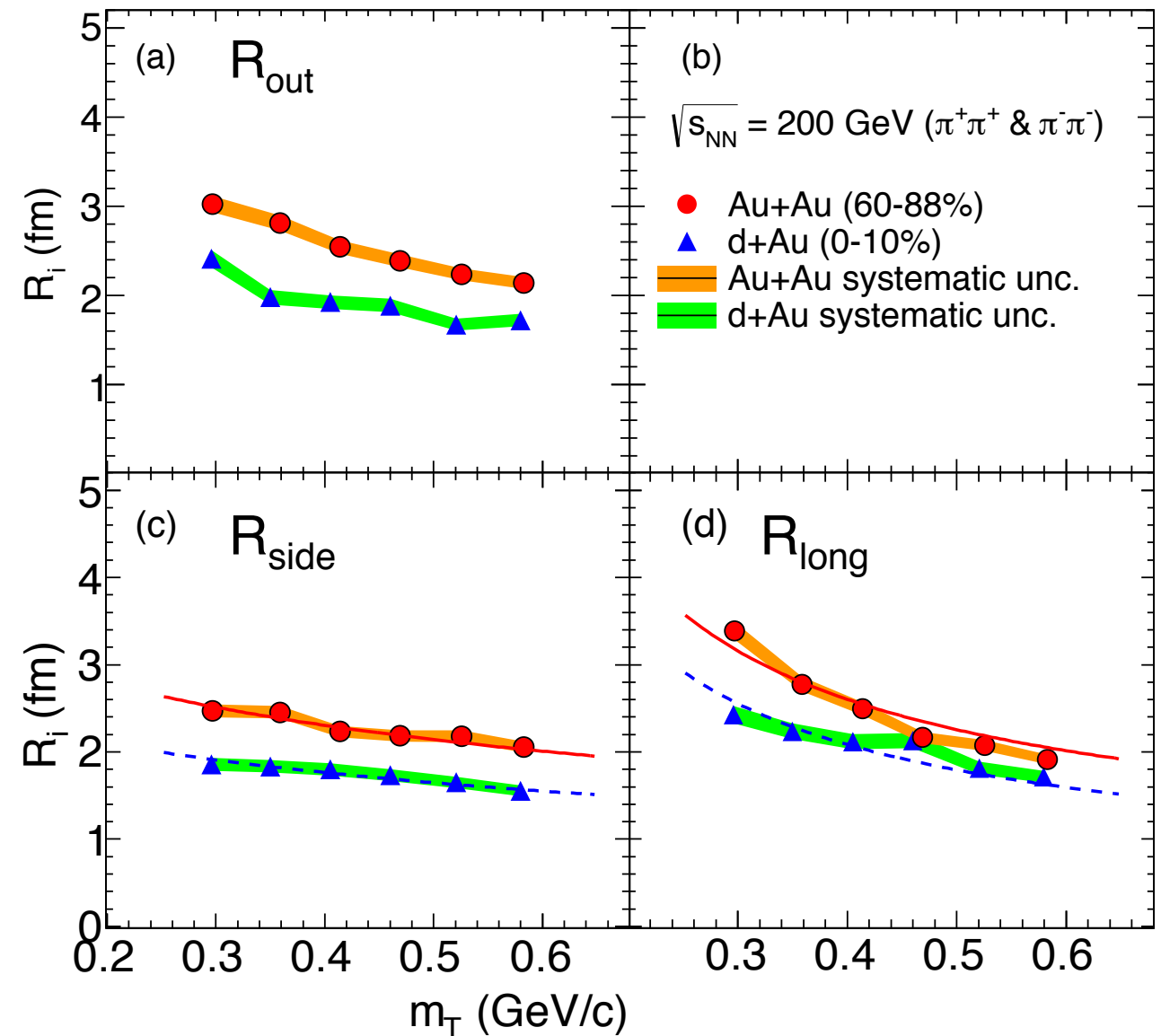
## BW fit function

$$R_{\text{side}} = R_{\text{geom}} / \sqrt{(1 + \beta^2(m_T/T))},$$

$$R_{\text{long}} = \tau_0 \sqrt{(T/m_T)[(K_2(m_T/T))/(K_1(m_T/T))]},$$

TABLE I. Fit parameters

	d+Au	Au+Au
$\tau_0$ (fm/c)	$3.2 \pm 0.04 \pm 0.4$ (syst)	$3.8 \pm 0.04 \pm 0.3$ (syst)
$\chi^2/ndf$	26/5	24/5
$R_{\text{geom}}$ (fm)	$2.2 \pm 0.03 \pm 0.2$ (syst)	$2.8 \pm 0.03 \pm 0.2$ (syst)
$\chi^2/ndf$	6/5	4/5



- Qualitatively similar  $m_T$  dependence in d+Au & Au+Au
  - Similar expansion dynamics?
- Blast-wave fitting defined by expansion velocity & freeze-out temperature works well for  $R_{\text{side}}$

# Emission duration & freeze-out volume

arXiv:1404.5291

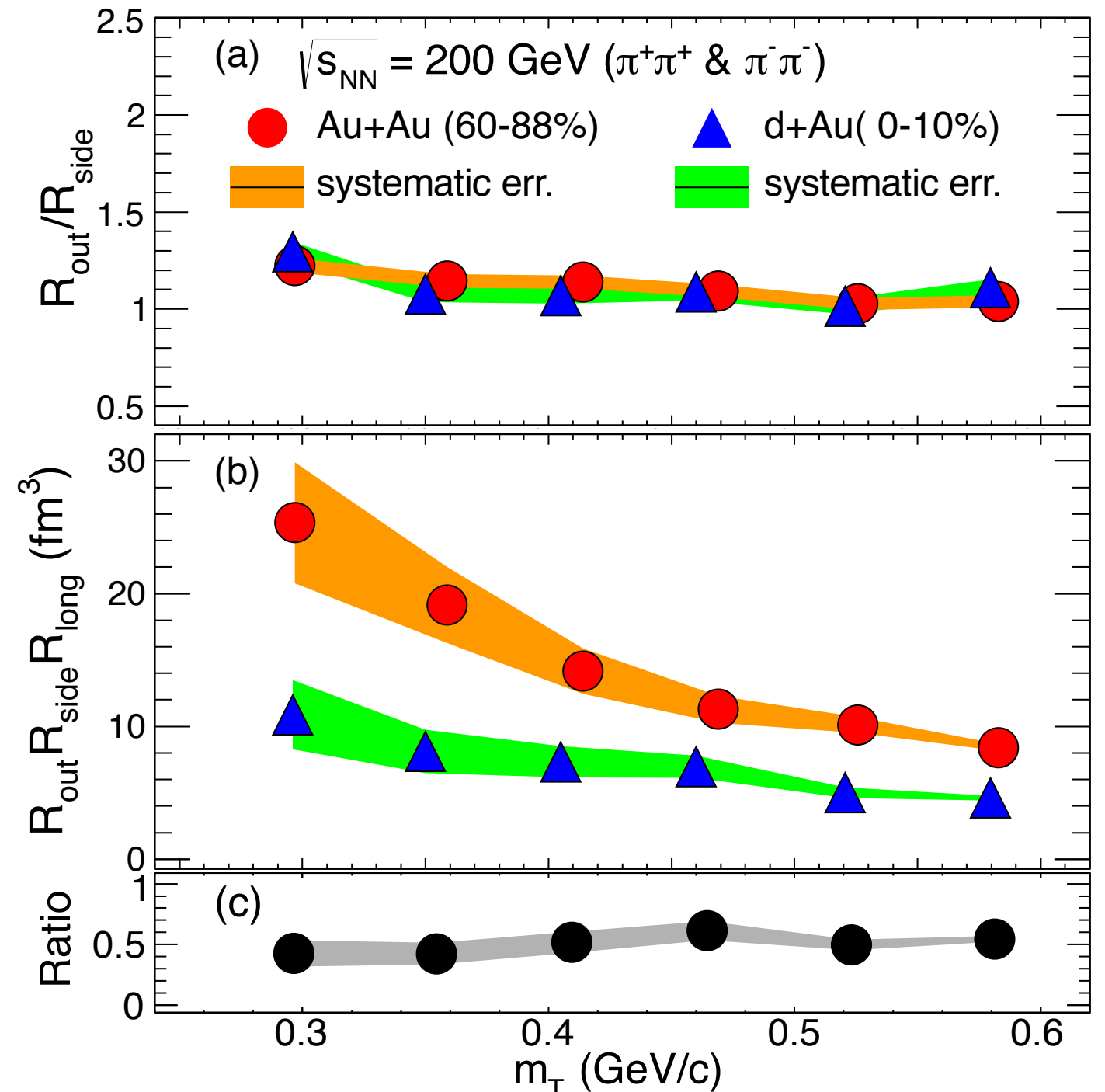
$$R_{\text{out}}/R_{\text{side}} \sim 1$$

Short emission duration

Freeze-out Volume

$$v(\text{dAu}) < v(\text{AuAu})$$

Similar  $m_T$  dependence

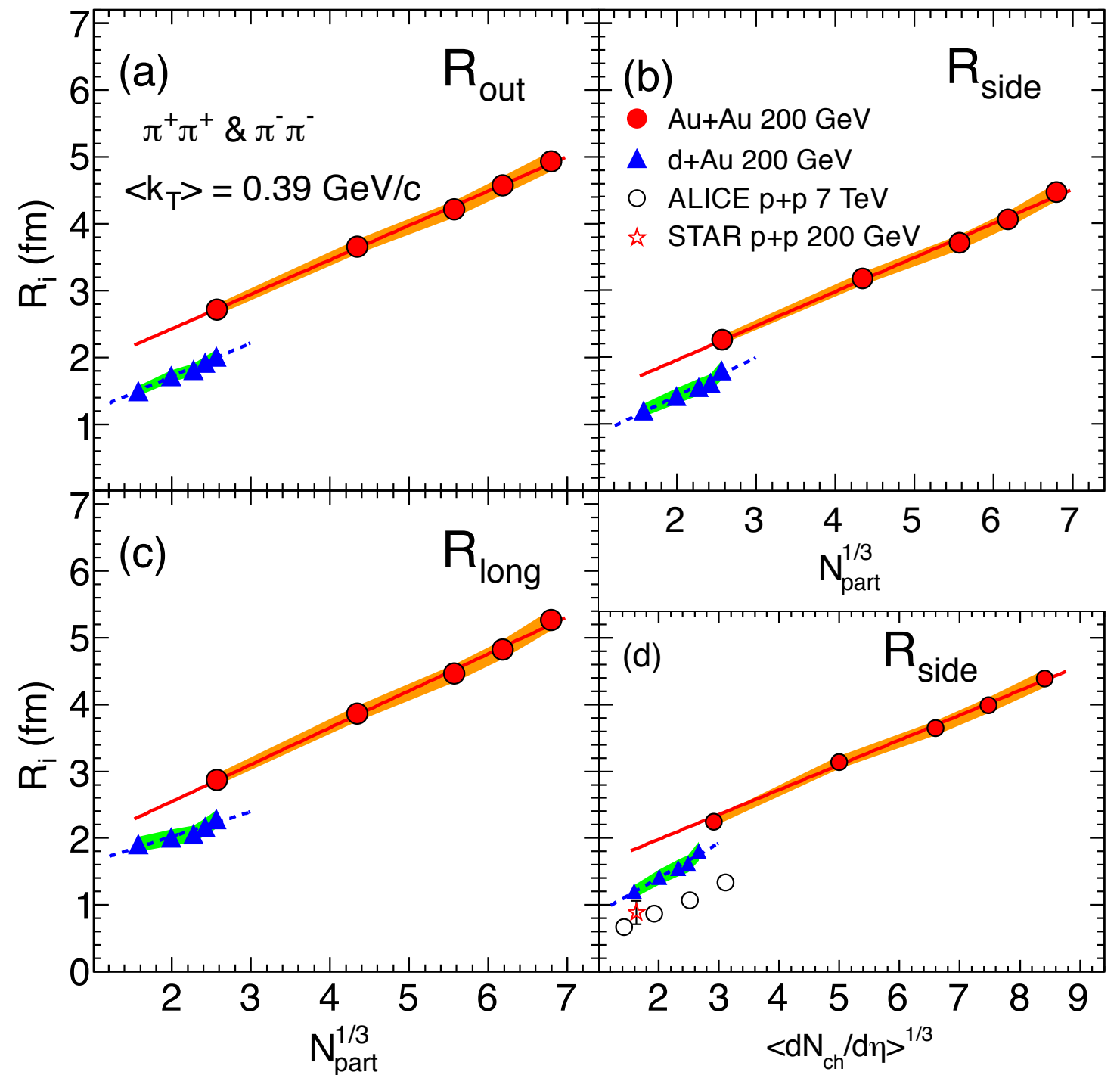




# HBT radii as a function of $N_{\text{part}}^{1/3}$

arXiv:1404.5291

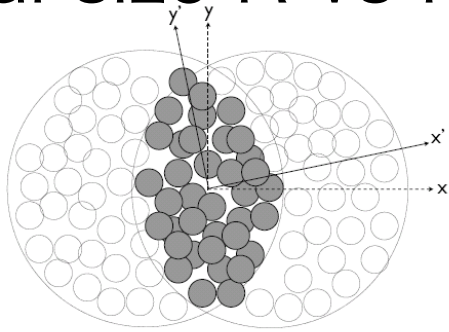
- d+Au & Au+Au HBT radii do not scale together but show a similar linearity
- p+p at 7 TeV also show a linearity with respect to  $\langle dN_{\text{ch}}/\eta \rangle^{1/3}$



# Initial R dependence in p+A & A+A collisions

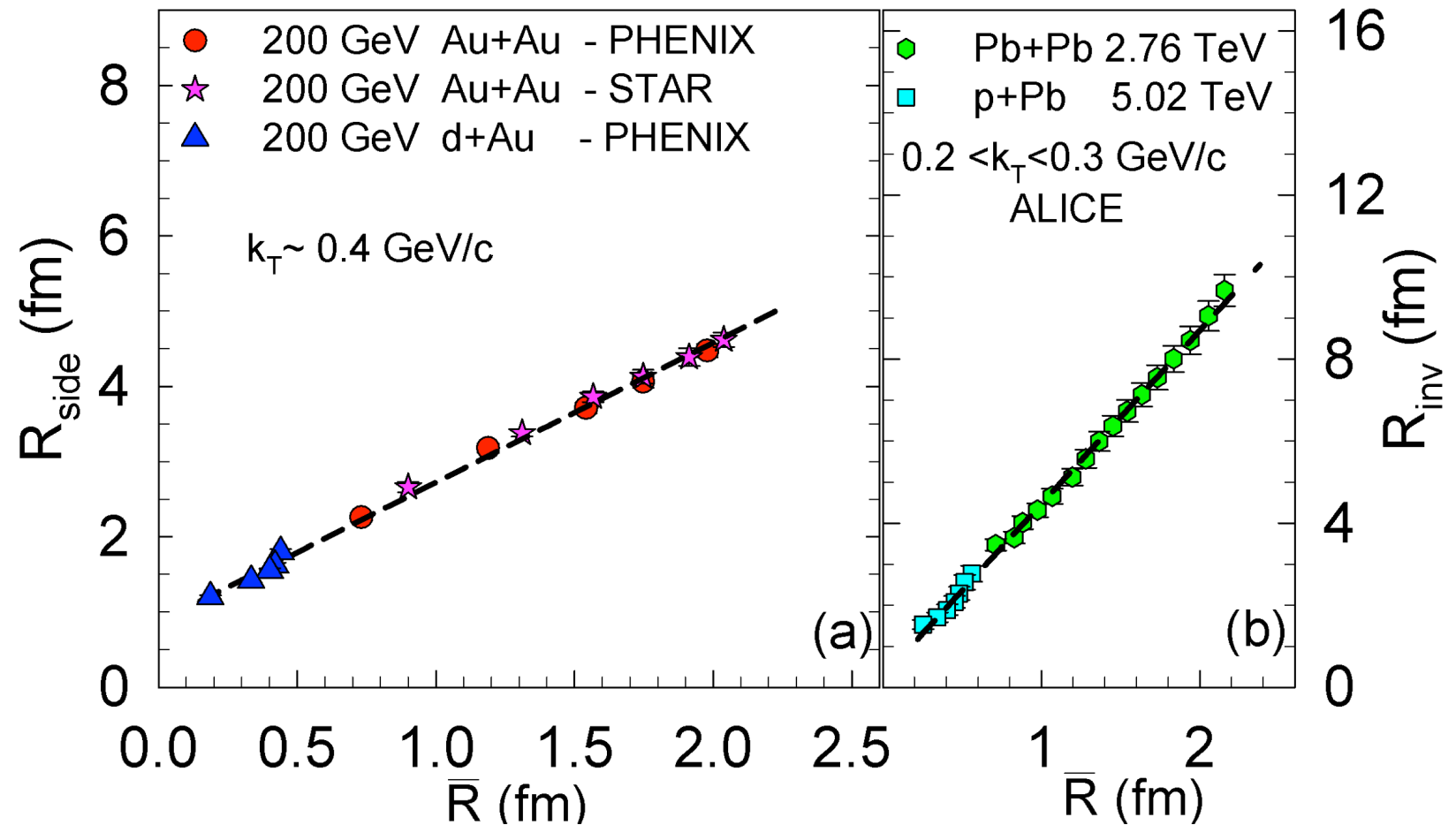
arXiv:1404.5291

Glauber MC to obtain  
initial size  $R$  vs  $N_{\text{part}}$



$$\frac{1}{\bar{R}} = \sqrt{\left(\frac{1}{\sigma_x^2} + \frac{1}{\sigma_y^2}\right)}$$

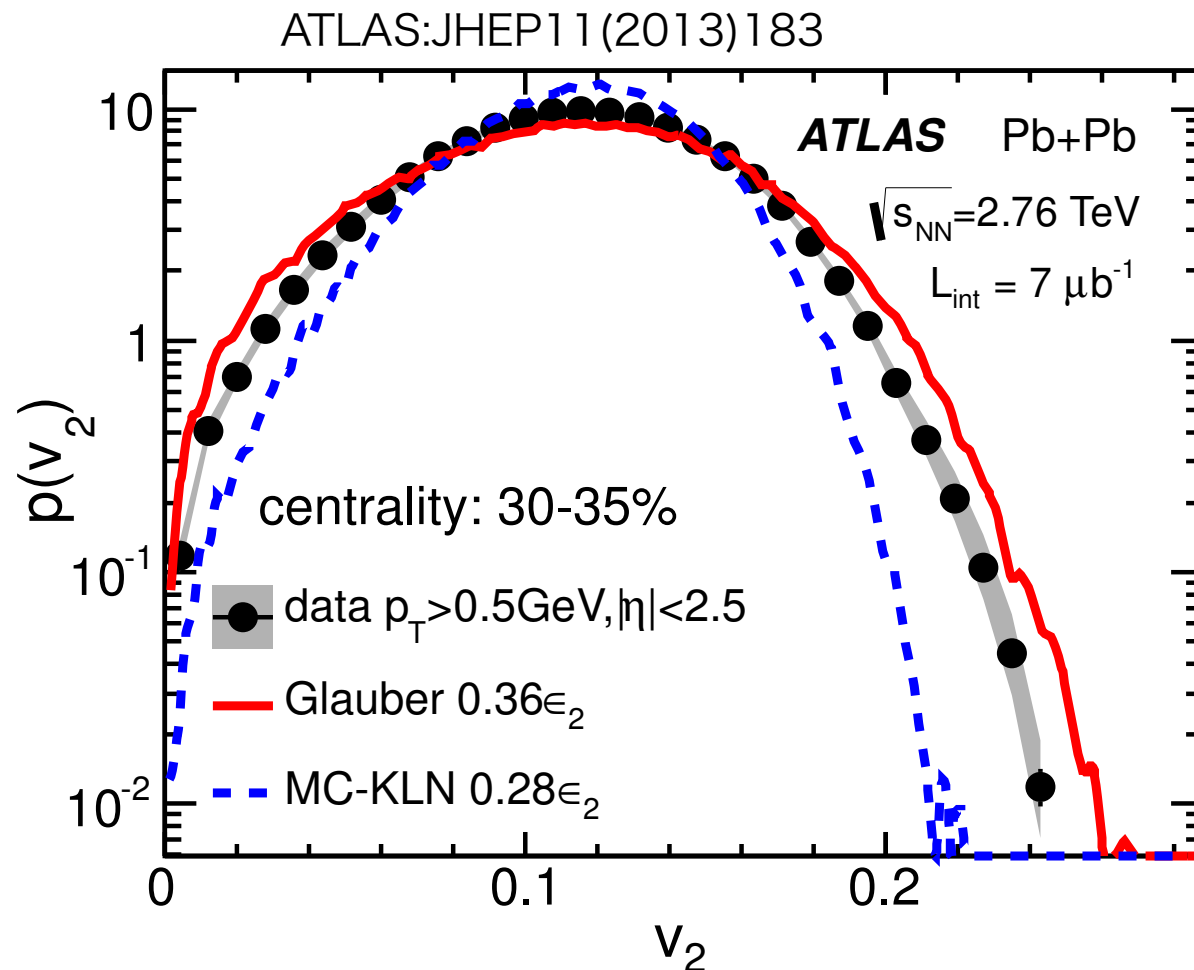
$\sigma_x$   $\sigma_y$ : RMS width of  
density distribution



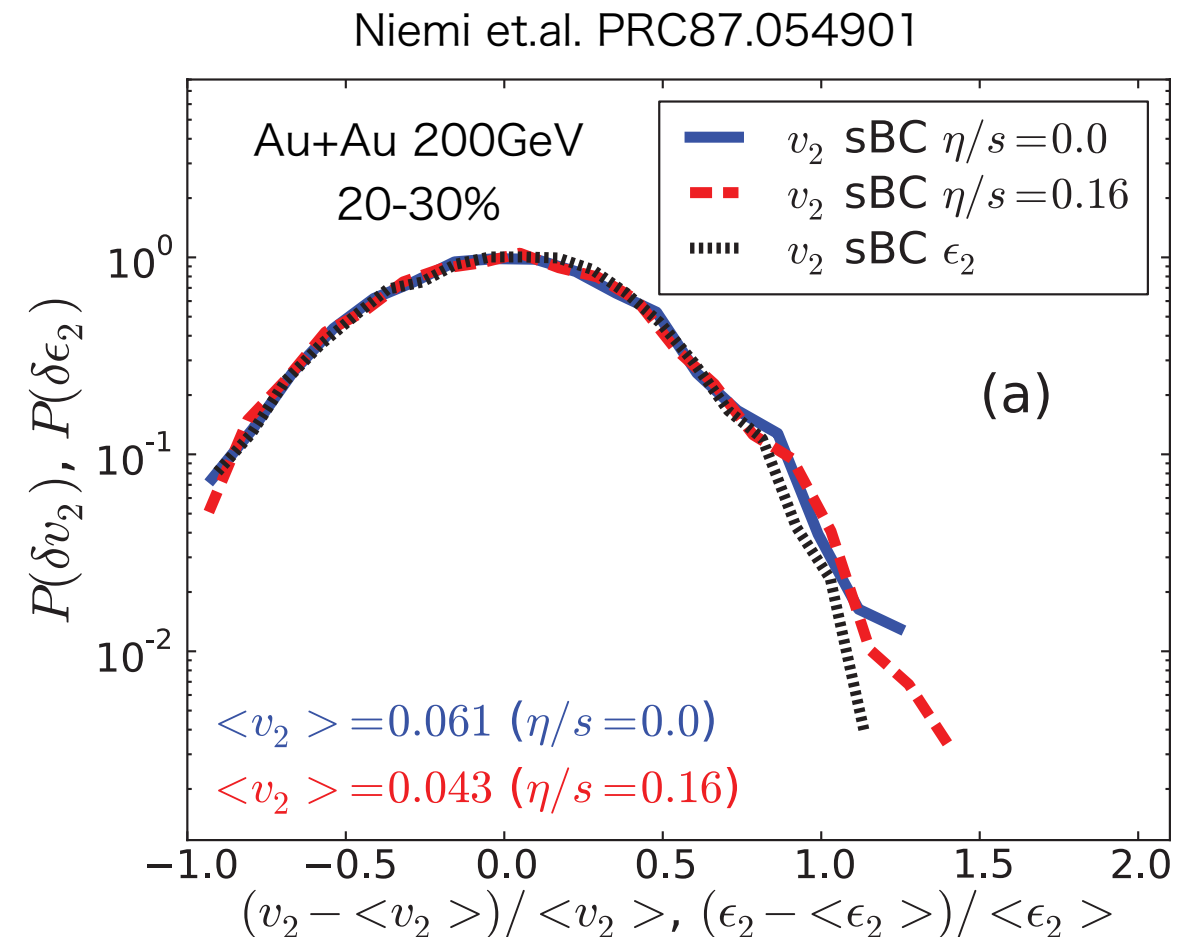
- Linearity and good scaling are seen in p+A and A+A collisions
- Implies possible radial expansion in p+A systems

# Event-by-Event Fluctuations of $v_n$

## LHC Data



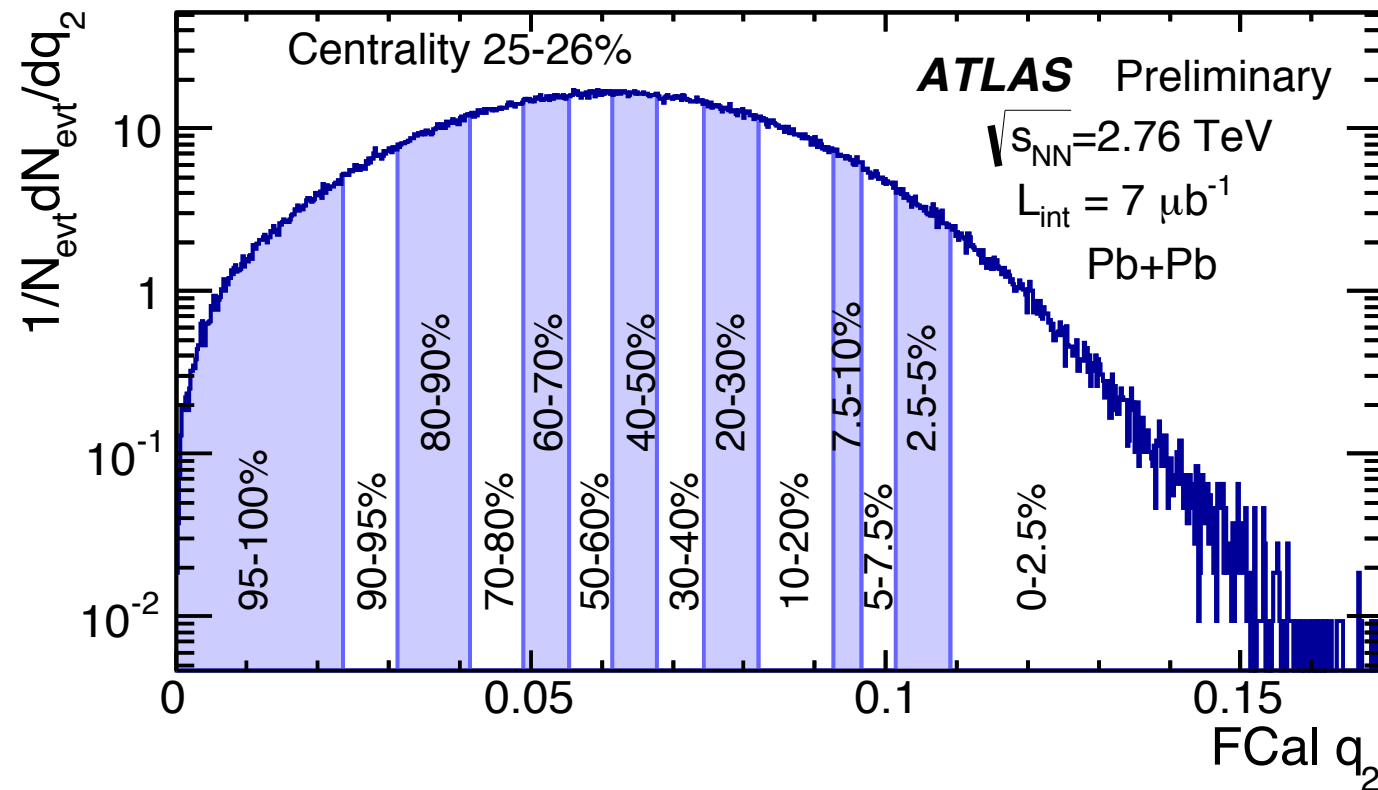
## Hydro Calculation



- Eve-by-Eve fluctuation seems to be independent of shear-viscosity
- Possible probe to access IC

# Event-Shape Engineering

Schukraft et.al: arXiv:1208.4563



- $|q_n|$  : Strength of Flow

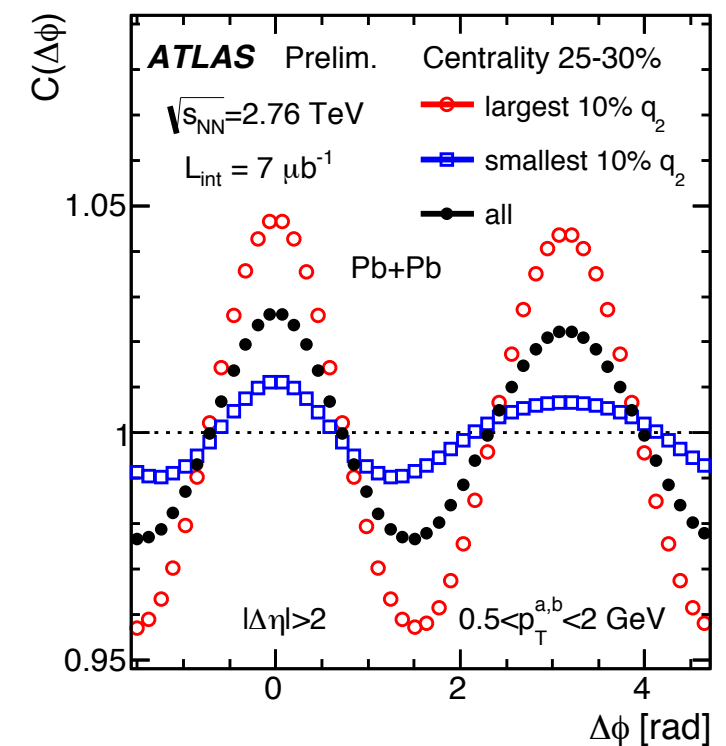
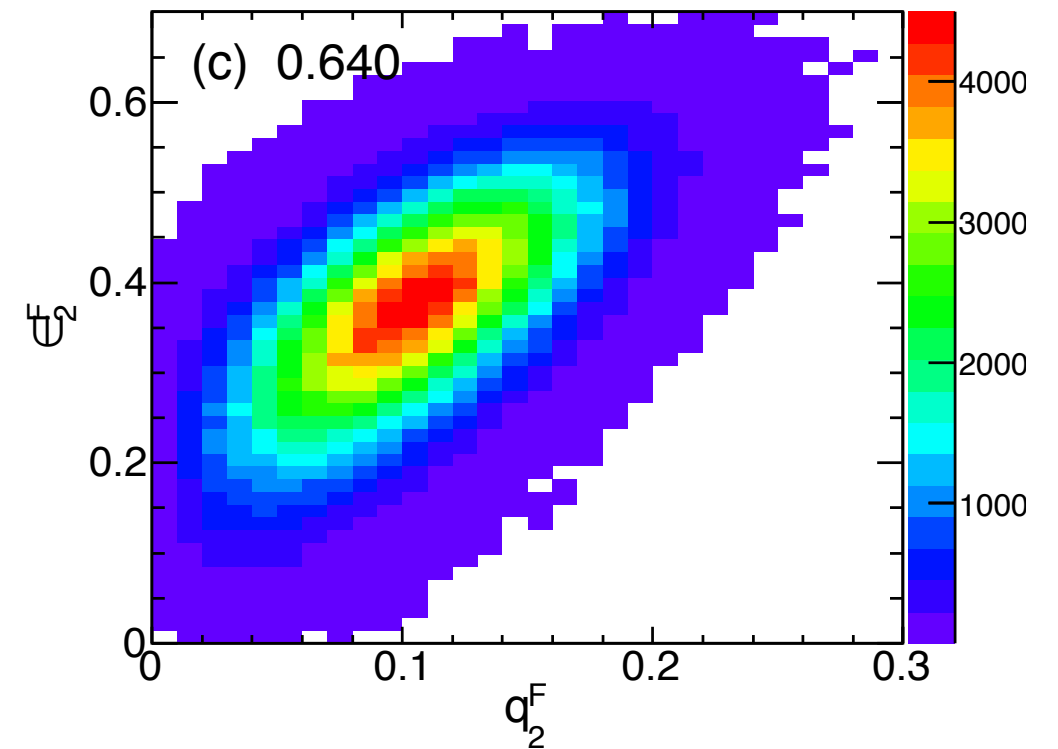
$$(q_n^x, q_n^y) = \frac{1}{\sum_i} \left( \sum_i \cos n\phi_i, \sum_i \sin n\phi_i \right)$$

$$|q_n| = \sqrt{q_n^x{}^2 + q_n^y{}^2}$$

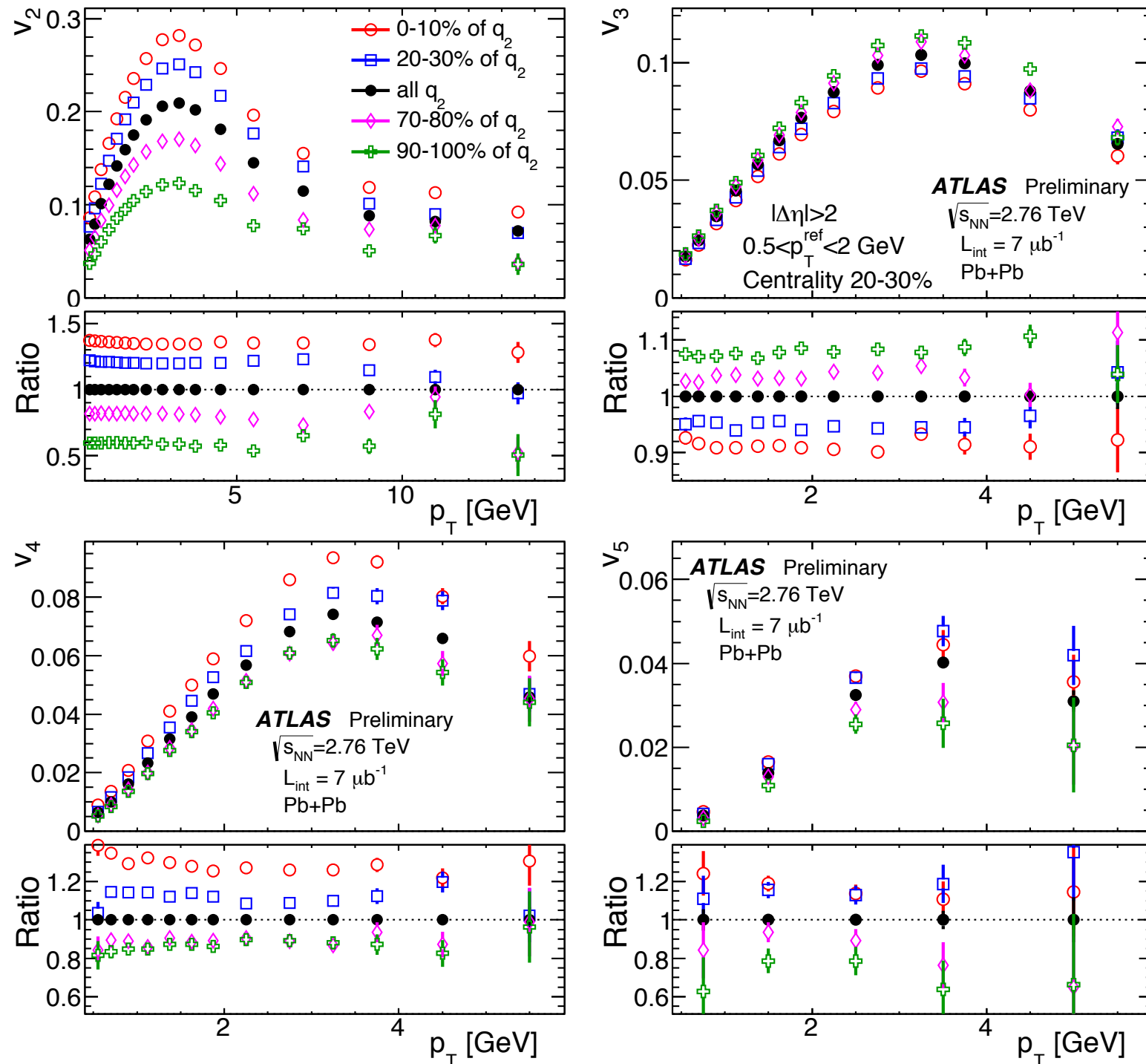
- Possible control of initial geometry

**AMPT**

J.Jia et.al : arXiv:1403.6077

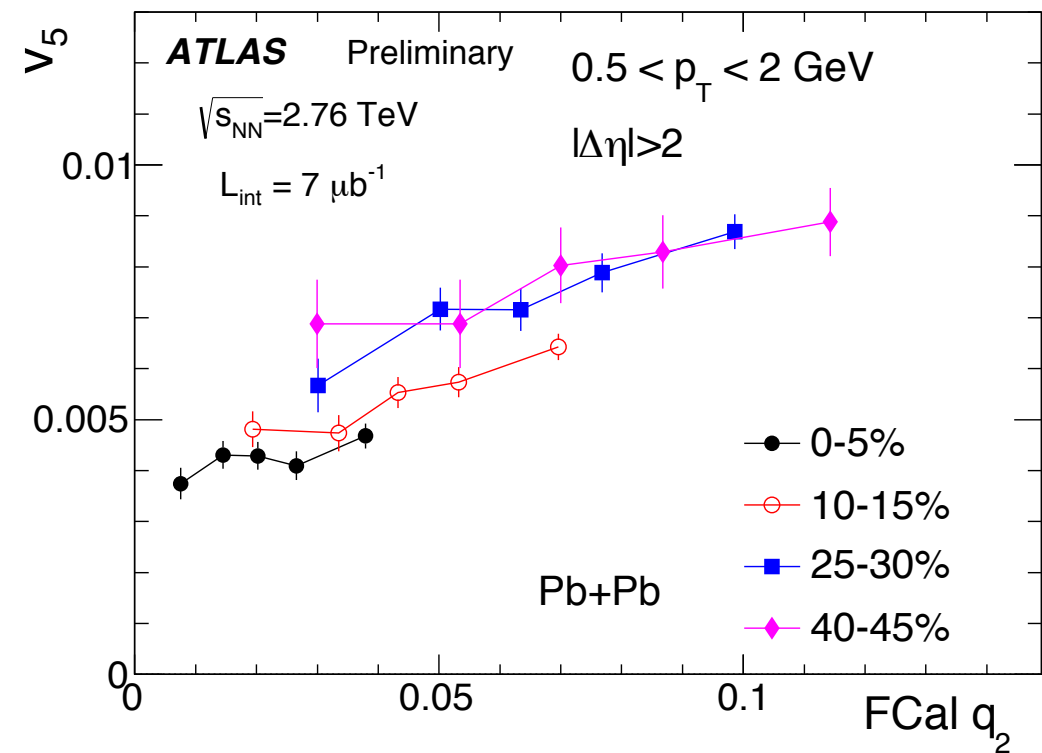
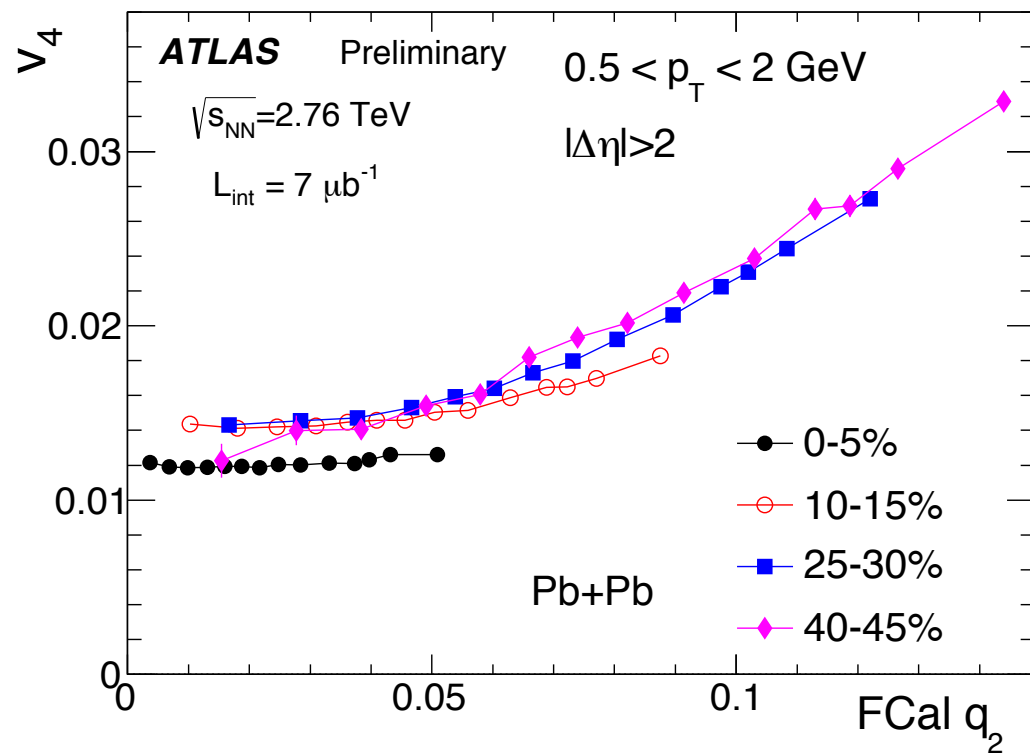
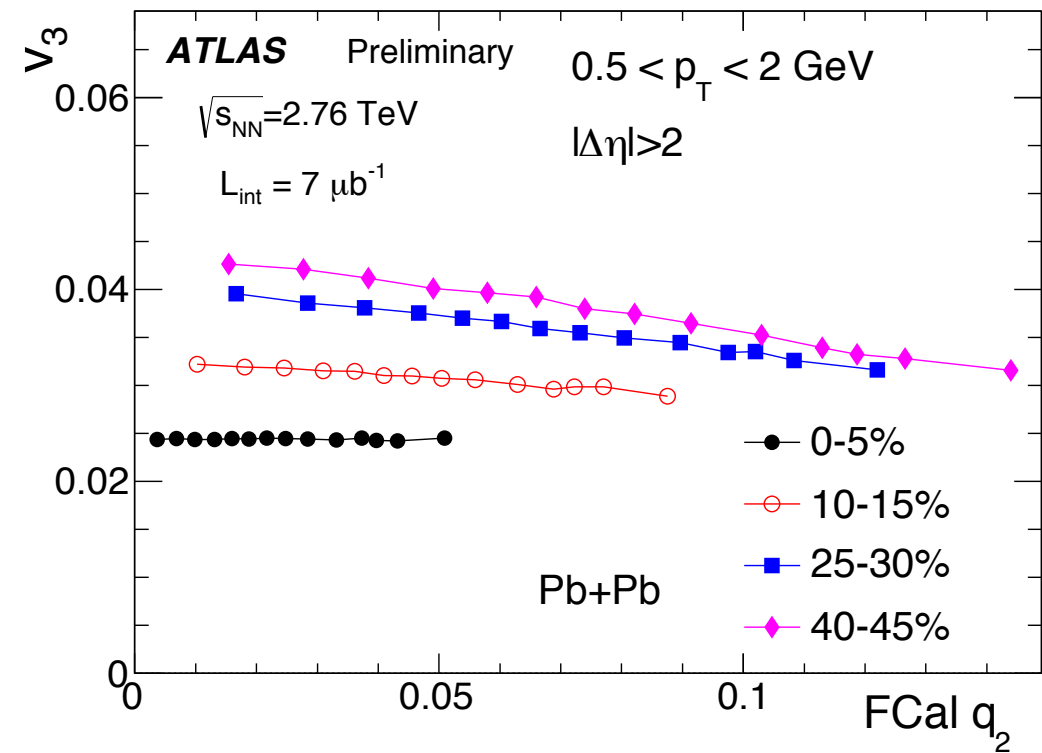
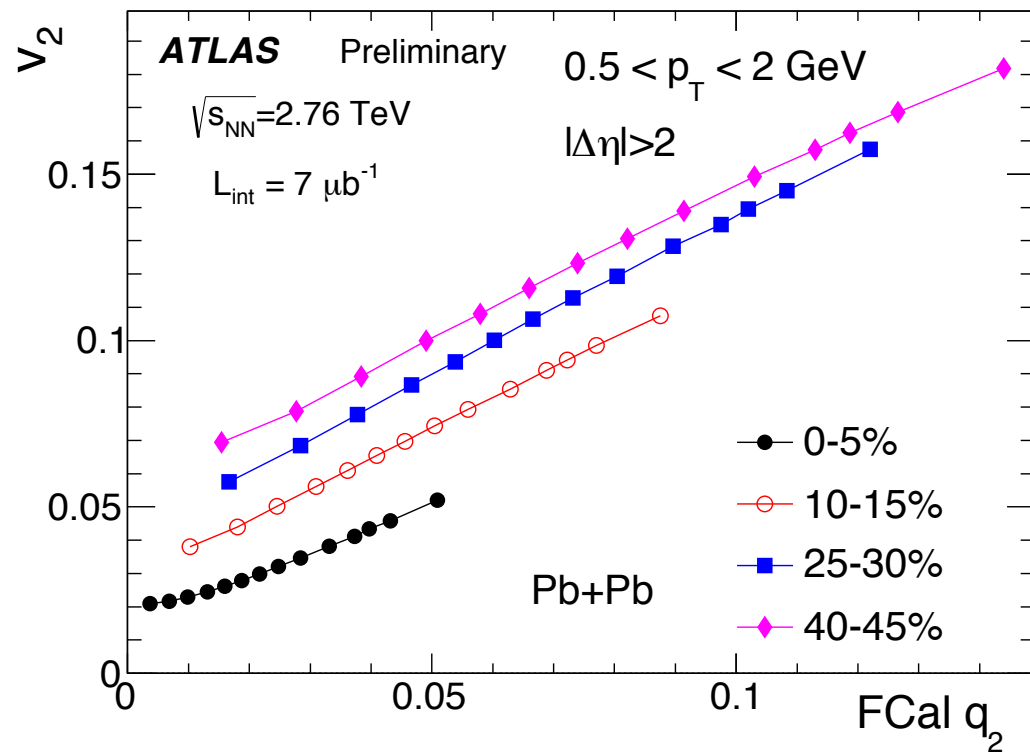


# $v_n(n=2,3,4,5)$ vs $q_2$

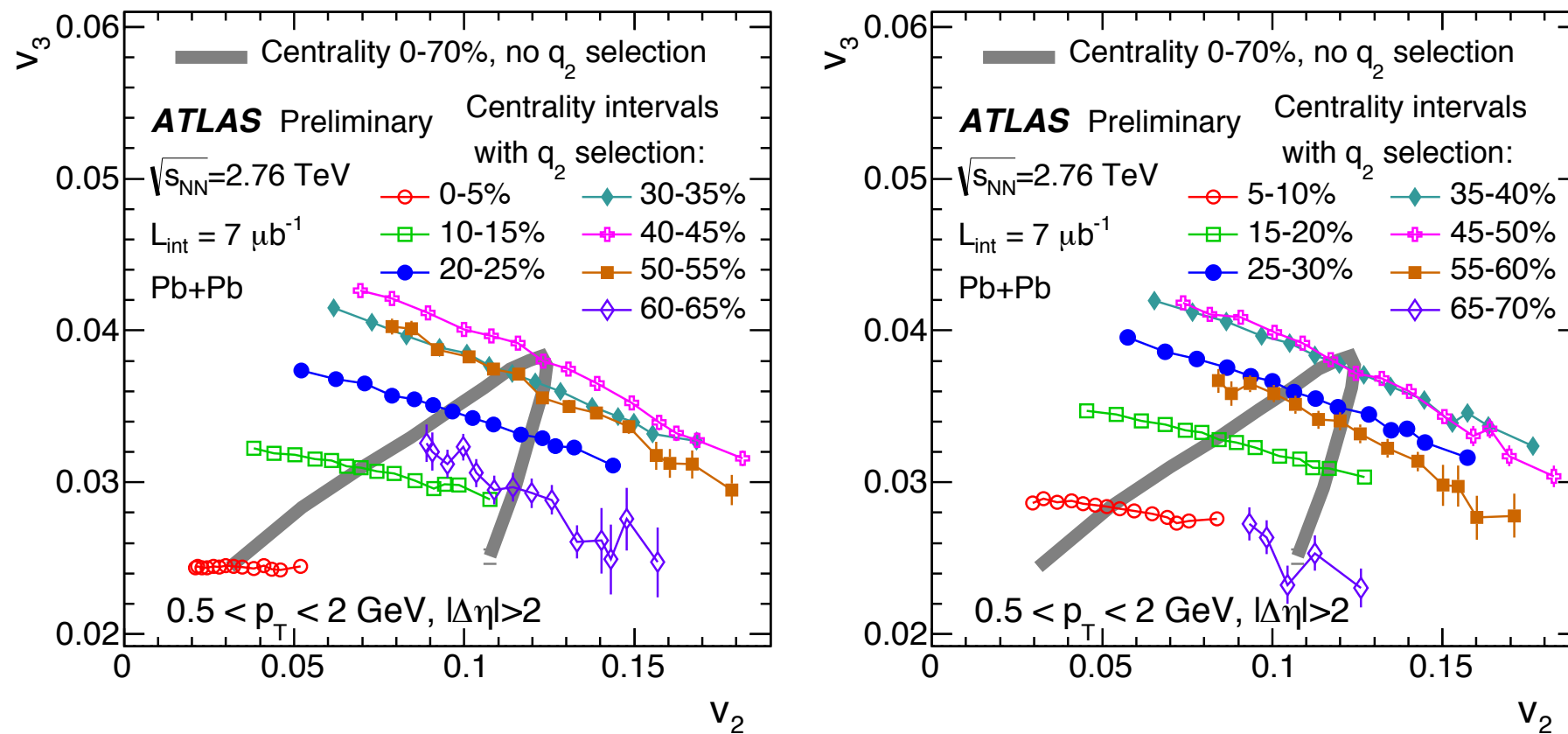


- $q_2$  dependence for  $v_2$
- Weaker, but  $q_2$  dependence also for  $v_n(n=3,4,5)$

# $v_n(n=2,3,4,5)$ vs $q_2$



# $v_2 - v_3$ correlations



- Negative-correlations between  $v_2$  and  $v_3$   $v_3 = c_0 + c_1 v_2$
- Linear response to initial geometry

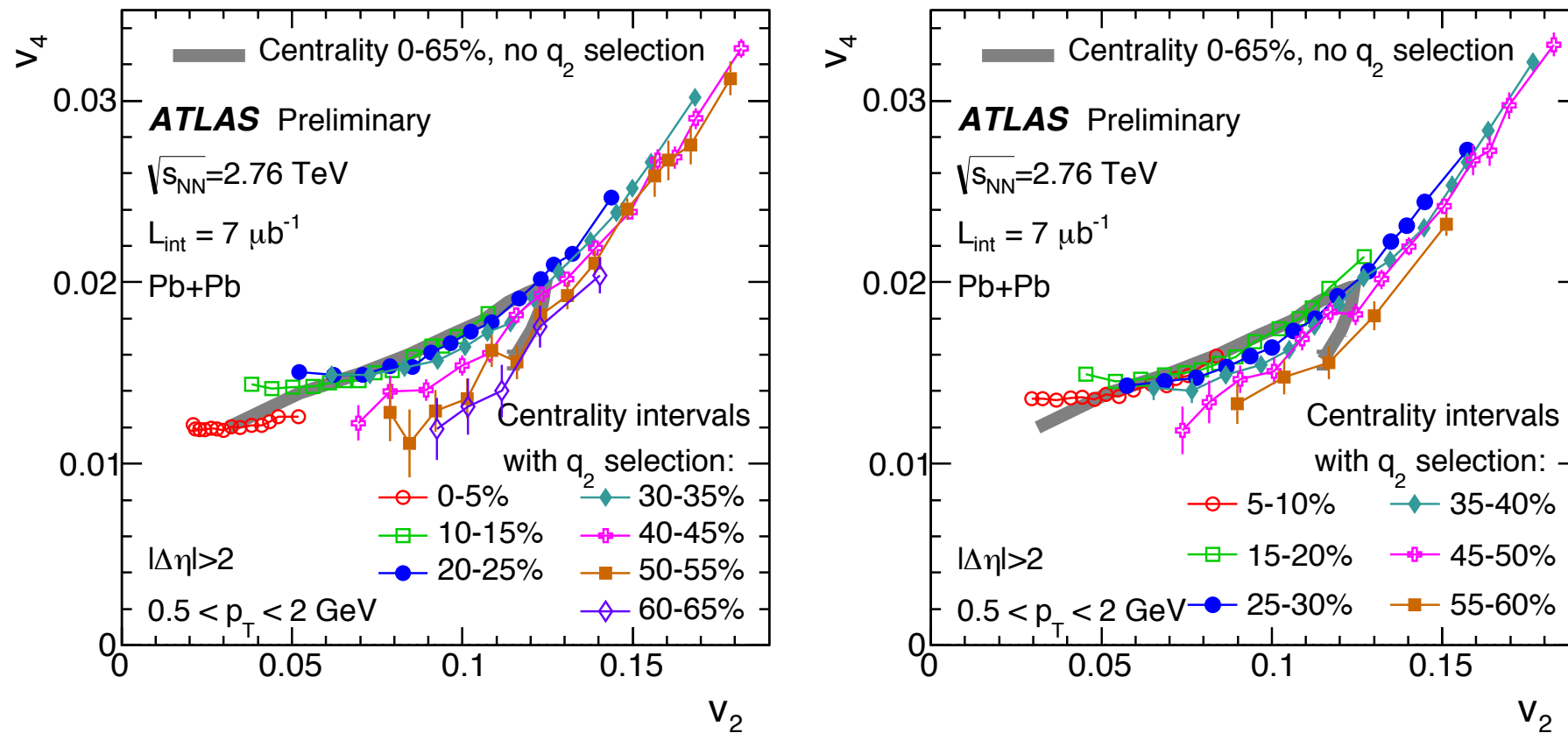
$$v_2 e^{i2\Phi_2} = a_0 \epsilon_2 e^{i2\Phi_2^*}$$

$$v_3 e^{i3\Phi_3} = a_0 \epsilon_3 e^{i3\Phi_3^*}$$

- Anti correlations at initial eccentricities?



# $v_2 - v_4$ correlations



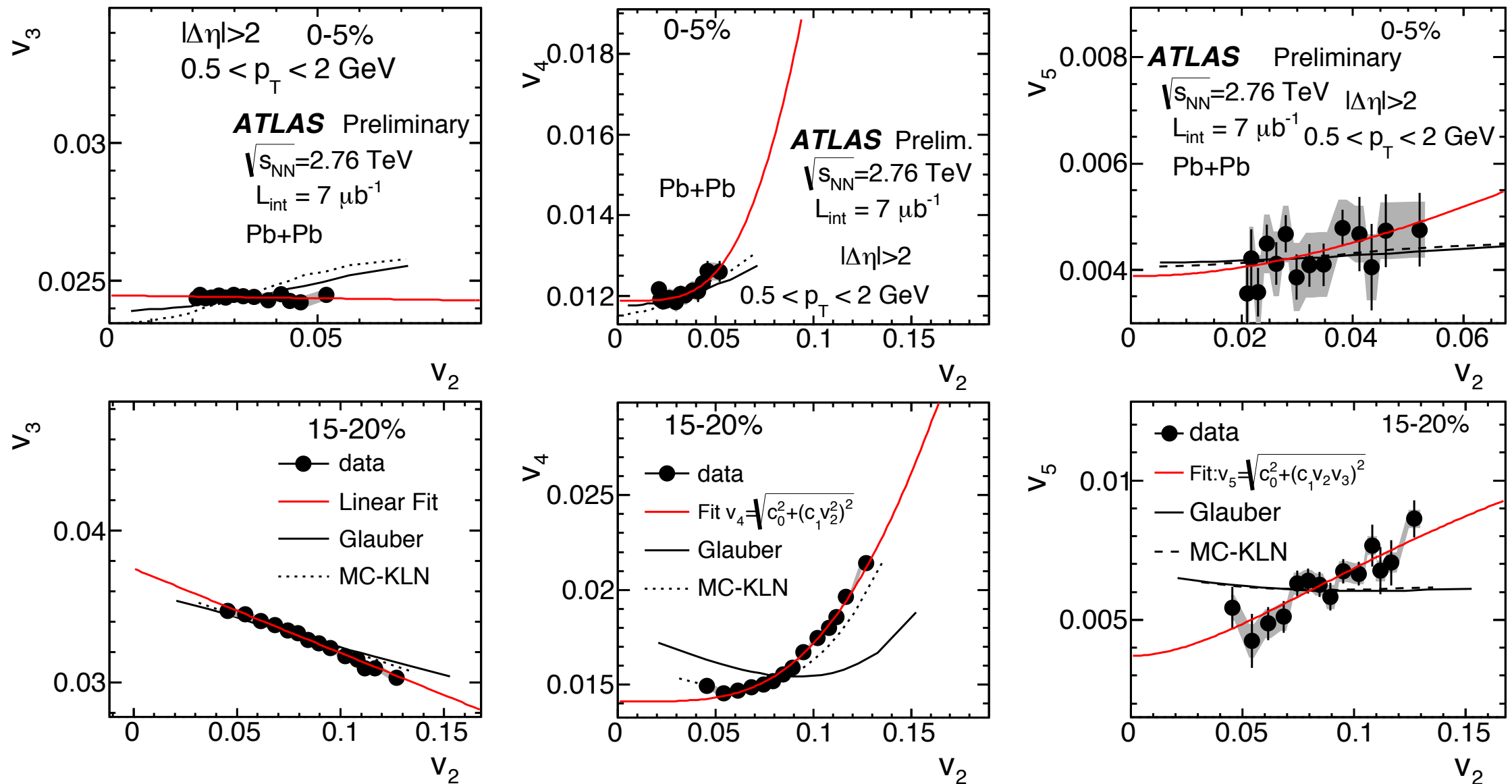
- Linear-term and non-linear term
- Clear non-linear term is seen in data: upward bending

$$v_4 e^{i4\Phi_4} = a_0 \epsilon_4 e^{i4\Phi_4^*} + a_1 (\epsilon_2 e^{i2\Phi_2^*})^2 + \dots$$

$$= c_0 e^{i4\Phi_4^*} + c_1 (v_2 e^{i2\Phi_2^*})^2 + \dots$$

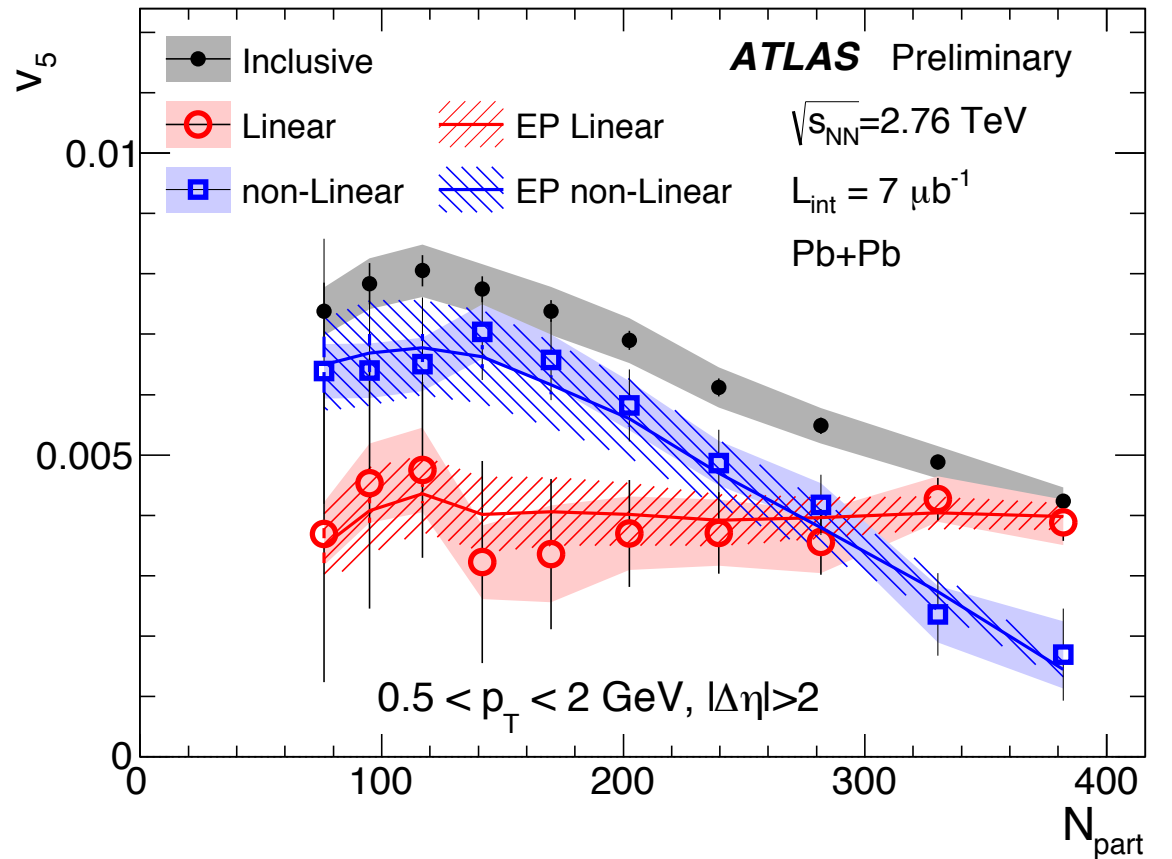
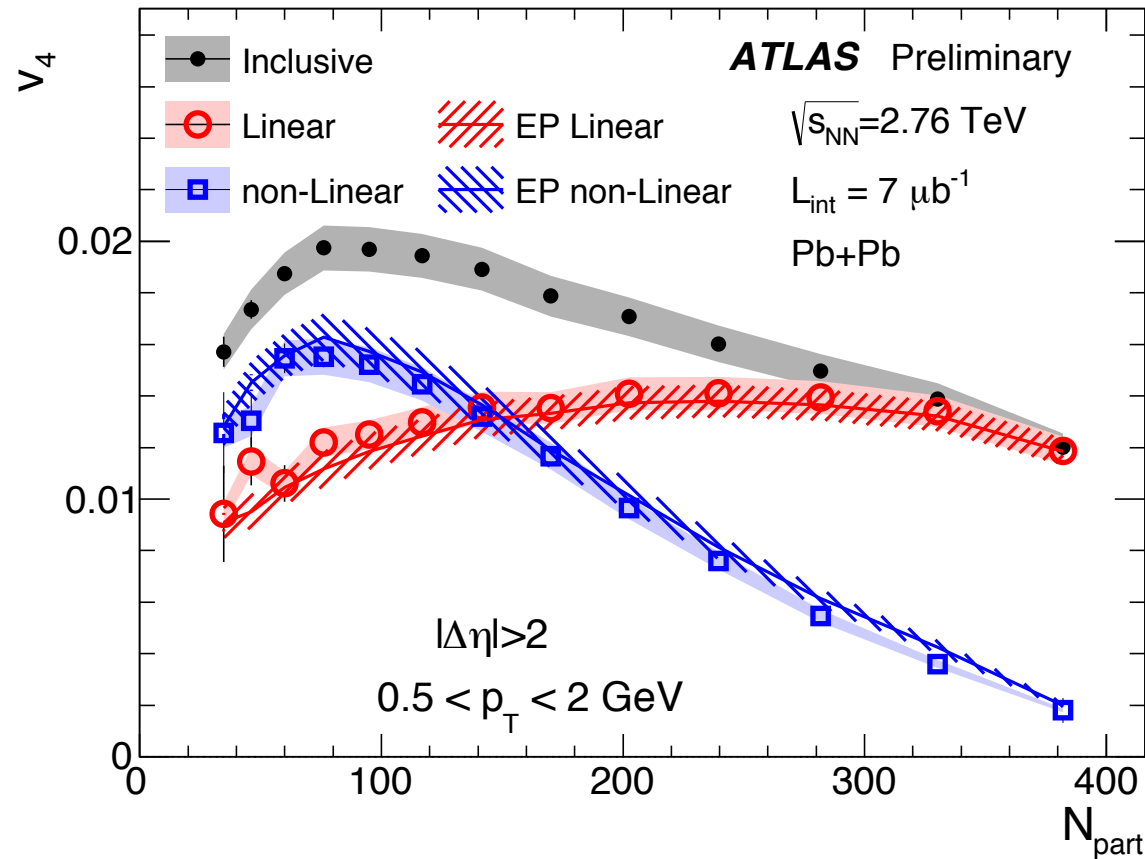
$$v_4 = \sqrt{c_0^2 + c_1^2 v_2^4}$$

# V<sub>2</sub>-V<sub>n</sub> correlations



- Compared with Glauber and MC\_KLN  $\varepsilon_2$ - $\varepsilon_n$  correlations
- Access to IC if a unique hydro response to a given initial correlation

# Linear/non-Linear terms



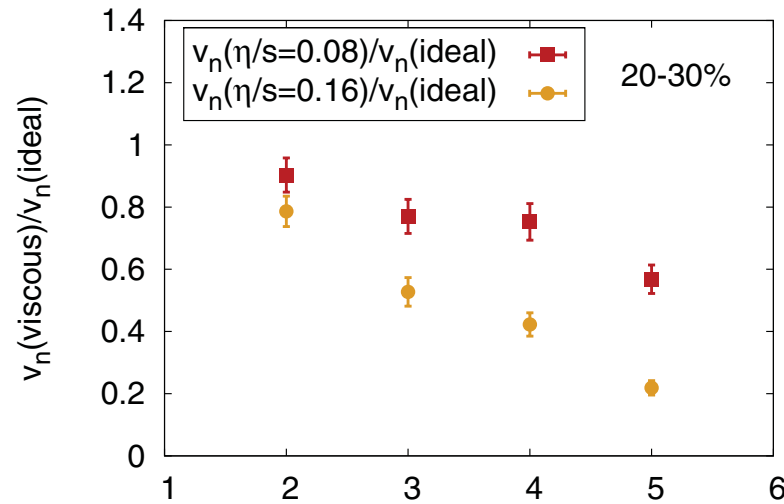
$$v_4^L = c_0, v_4^{NL} = \sqrt{v_4^2 - v_4^L{}^2} \quad v_5^L = c_0, v_5^{NL} = \sqrt{v_5^2 - v_5^L{}^2}$$

- Most-central :  $v_4$  is almost independent of  $v_2$
- NL term increases with centrality
- Similar trends in  $v_5$

# Viscous dumping

- Viscous dumping of  $v_n$  with “n”

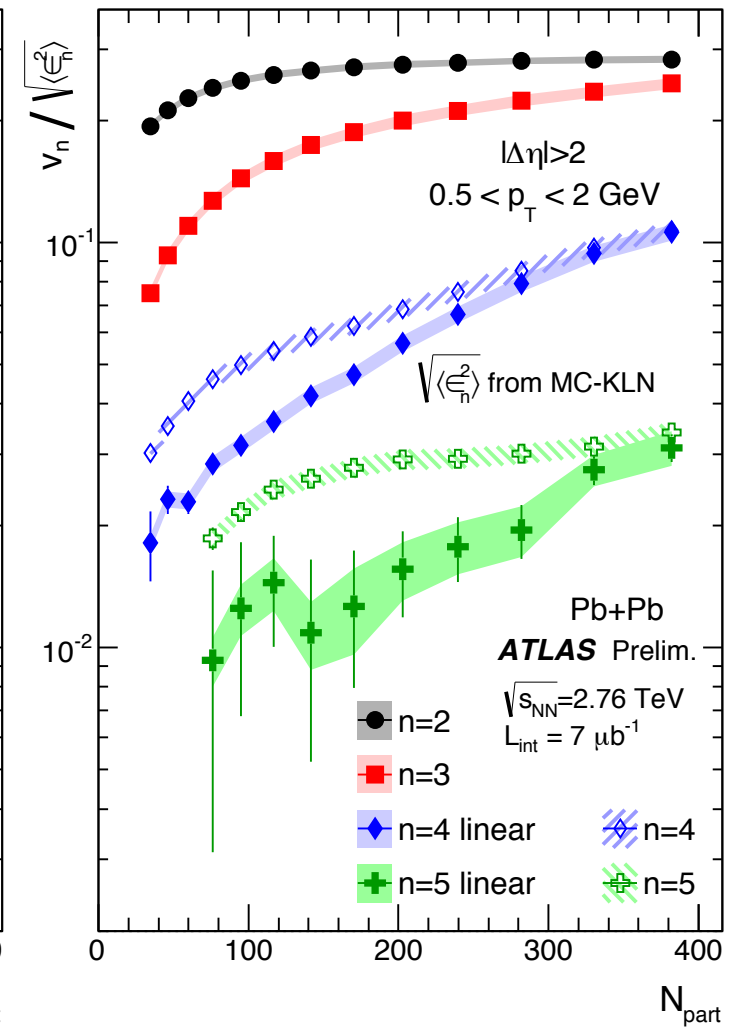
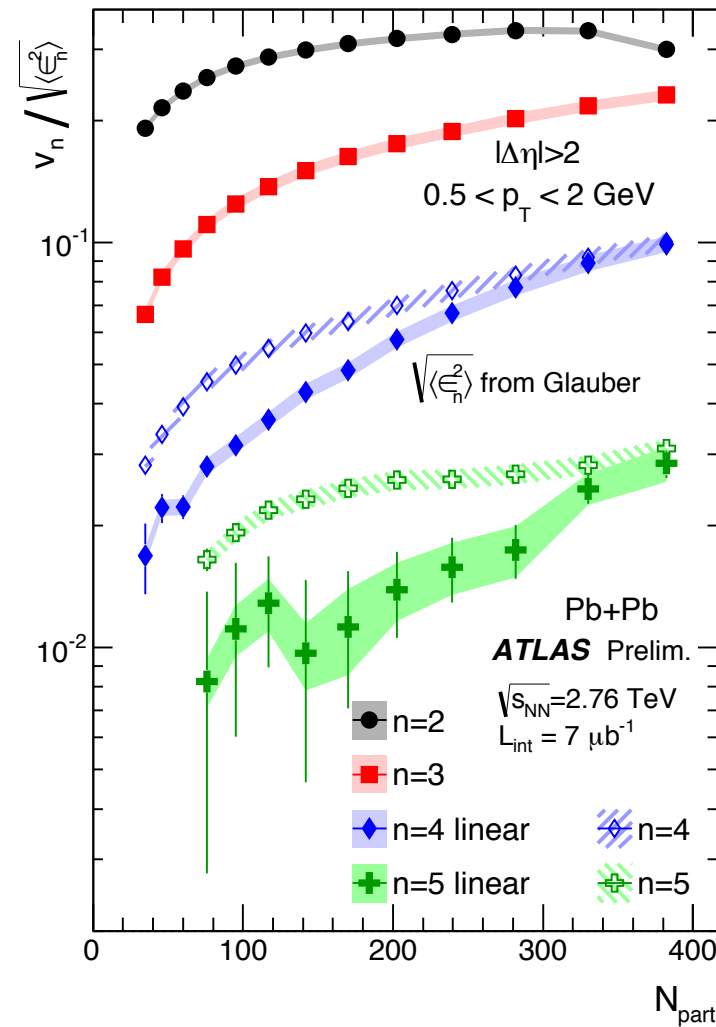
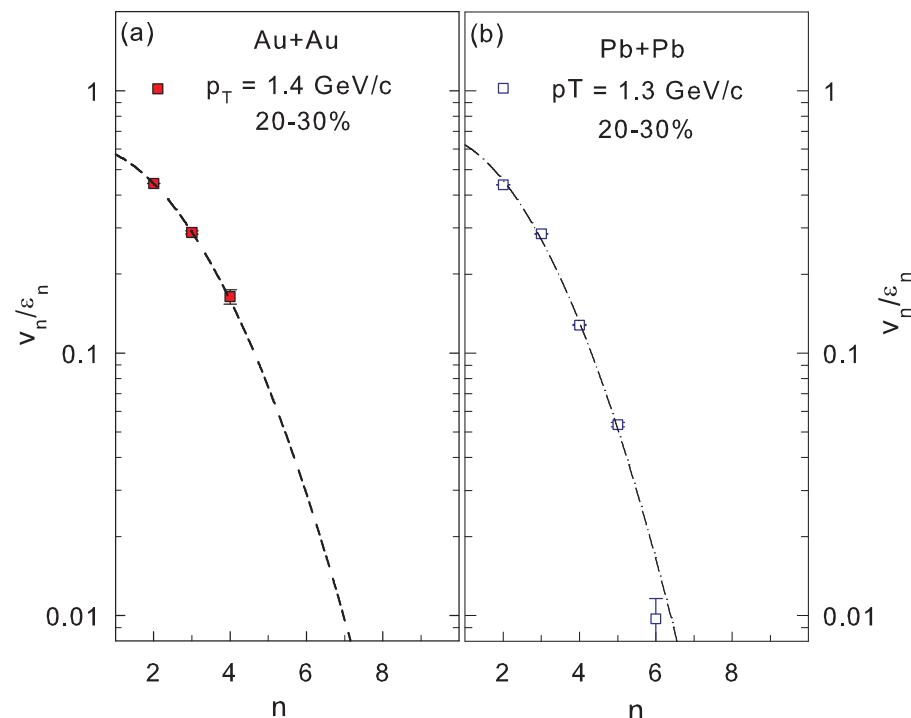
PRC85.024901



- Acoustic viscous dumping

$$\delta T_{\mu\nu}(n,t) = \exp(-\beta' n^2) \delta T_{\mu\nu}(n,0), \quad \beta' = \frac{2\eta}{3s} \frac{1}{\bar{R}^2 T} t$$

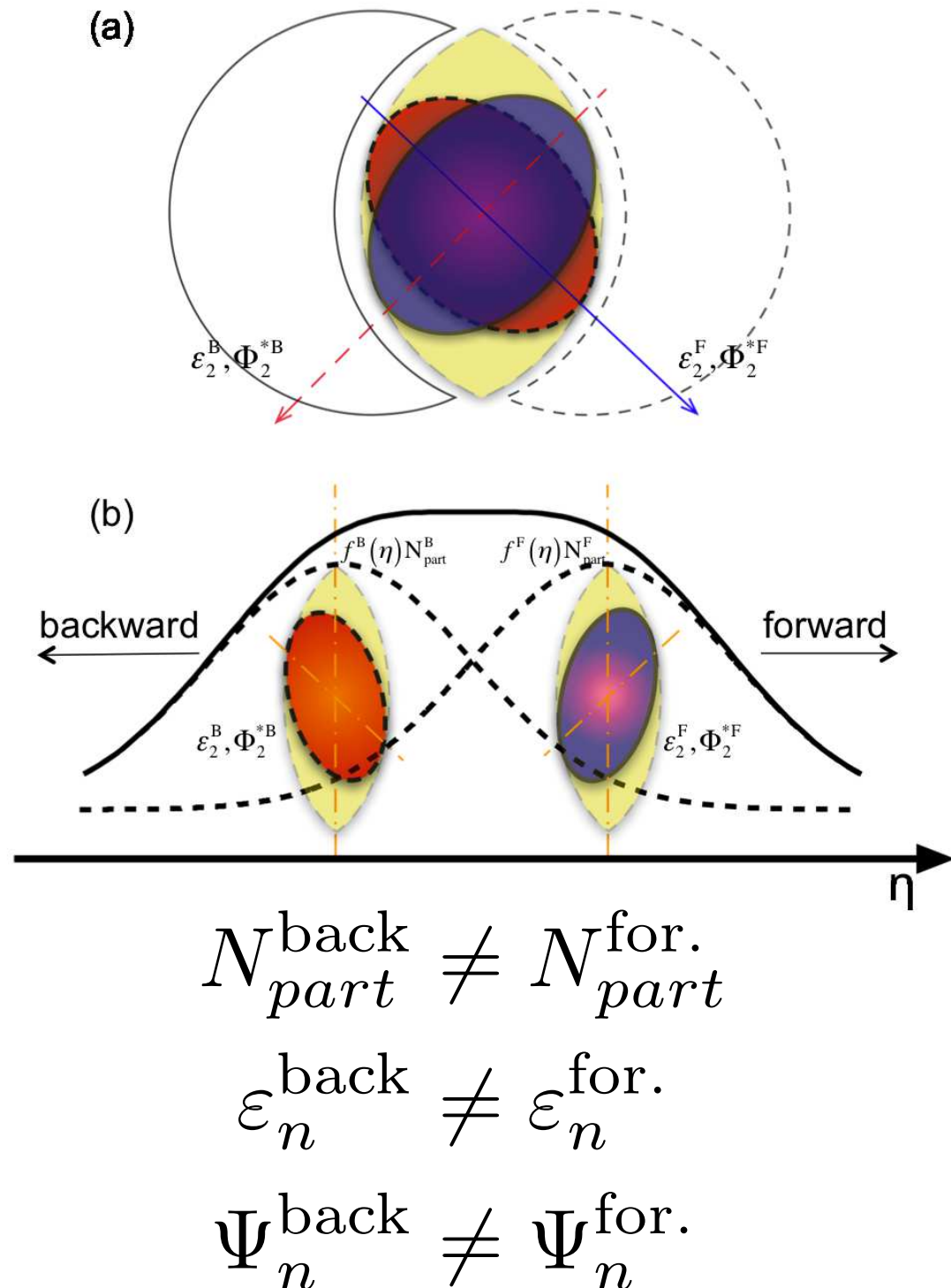
Lacey et.al. 1105.3782, Staig et. al. PRC84.034908



- Dumping pattern may be determine by the data

# Twist Effect

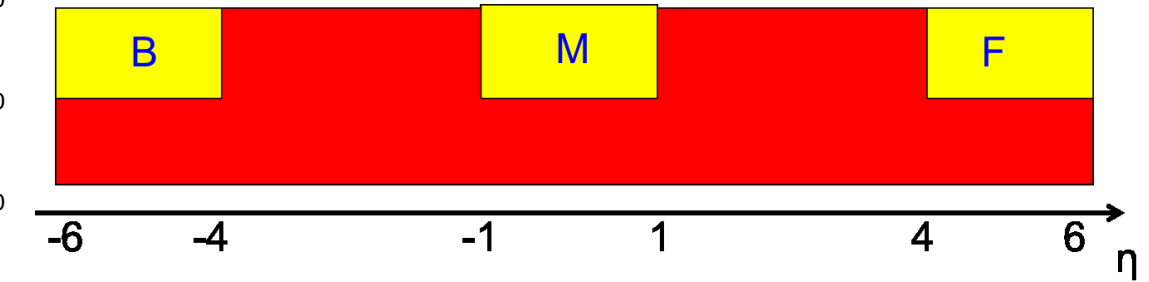
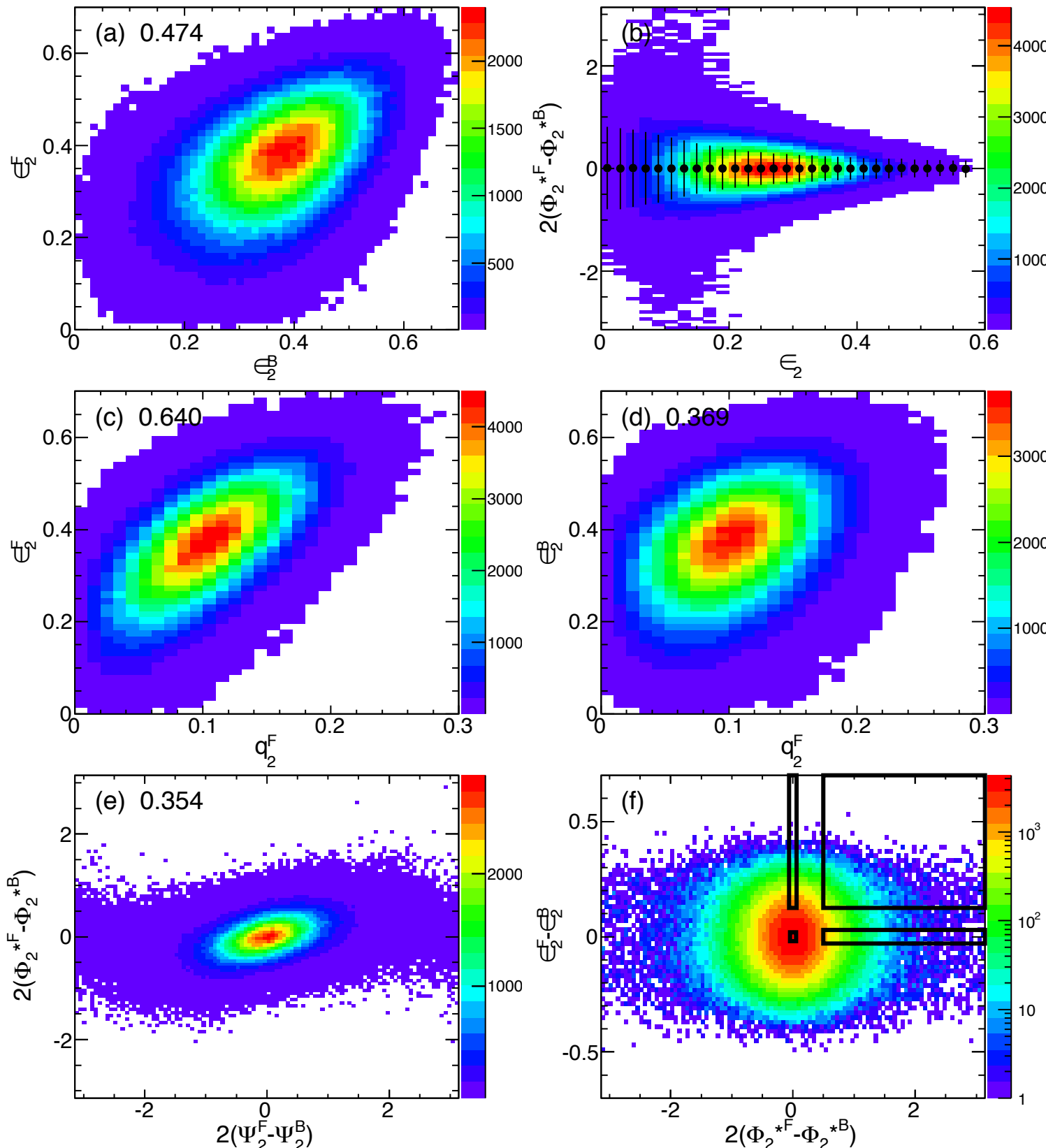
Jia et. al. arXiv:1403.6077



- Twisted medium between forward and backward directions emerging from participant fluctuations
- Correlation length of initial fluctuations in rapidity directions
- Possible underestimate of  $v_n$  i.e. overestimate of shear-viscosity due to neglecting decorrelated term

# AMPT : Twist Effect

Jia et. al. arXiv:1403.6077



- Event-Plane & Ecc &  $q_{2,3}$  determination

$$F : +4 < \eta < +6$$

$$M : -1 < \eta < +1$$

$$B : -6 < \eta < +4$$

- Correlations among EP, ECC,  $q_{2,3}$  etc.
- Final twist probes initial twist

# AMPT : Twist Effect

Jia et. al. arXiv:1403.6077

## Event Selection

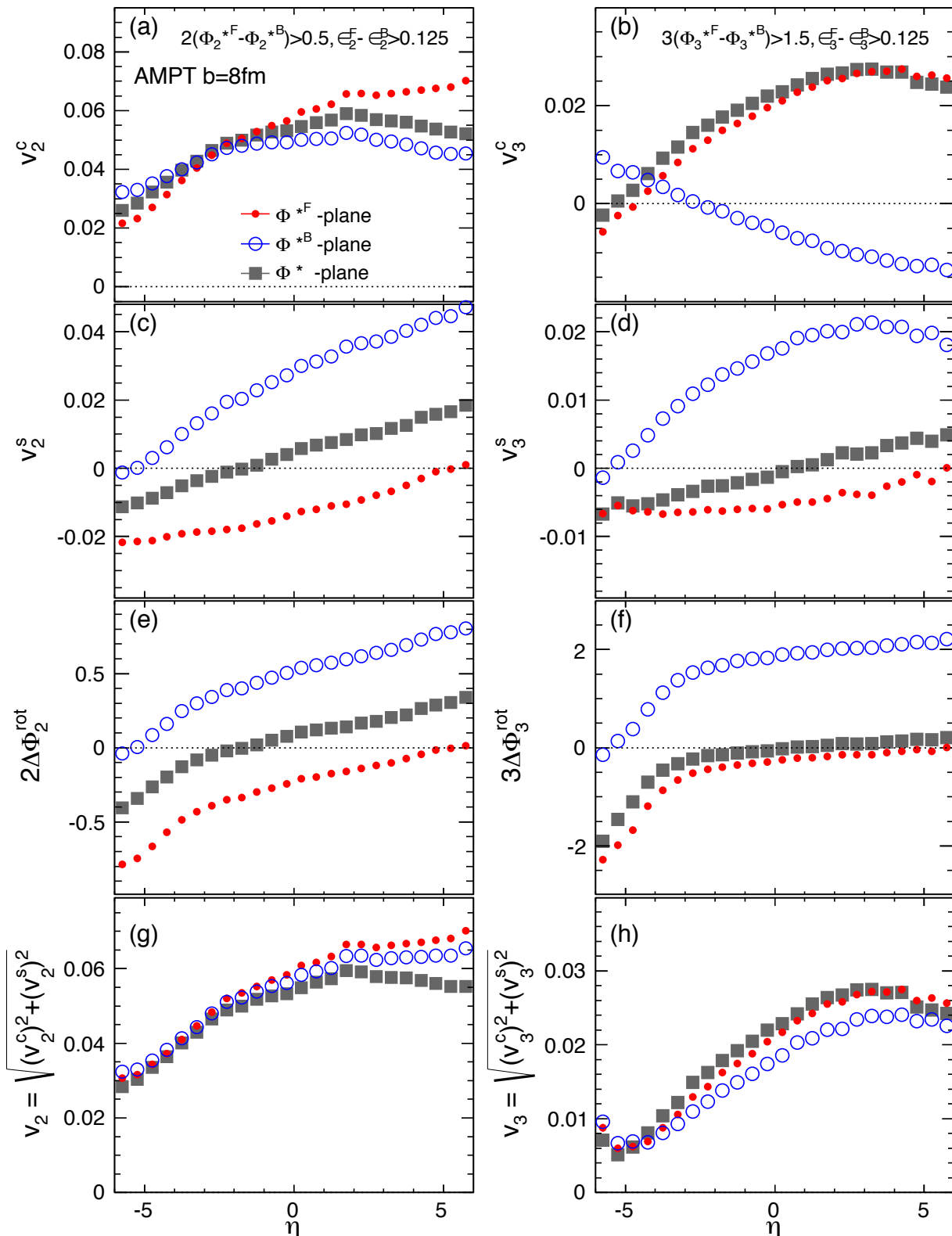
$$2(\Psi_2^F - \Psi_2^B) > 0.5 \quad \varepsilon_2^{\text{back}} < \varepsilon_2^{\text{for.}}$$

$$3(\Psi_3^F - \Psi_3^B) > 1.5 \quad \varepsilon_3^{\text{back}} < \varepsilon_3^{\text{for.}}$$

$$v_n^c = \langle \cos n(\phi - \Psi_n) \rangle / \text{Res} \{n\Psi_n\}$$

$$v_n^s = \langle \sin n(\phi - \Psi_n) \rangle / \text{Res} \{n\Psi_n\}$$

- Twisted term  $v_n^s$  observed  
i.e. underestimate of  $v_n$
- This study should be done  
for experimental data





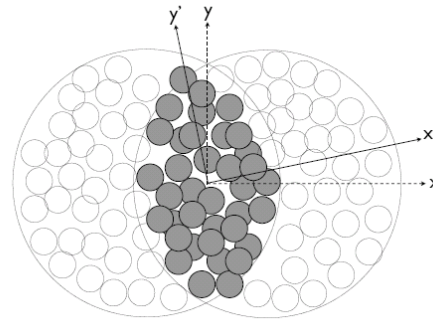
# Summary

- Similar trends among  $p(d)+A$  and  $A+A$  collisions in  $v_n$  and HBT measurements
- Observables in  $p(d)+A$  collisions are qualitatively consistent with final state effects
- Hadron mass dependence of CGC?
- Event Shape Control Study is a promising method to address initial geometry of heavy ion collisions
- Possible access to initial state model

# Auxiliary Slides

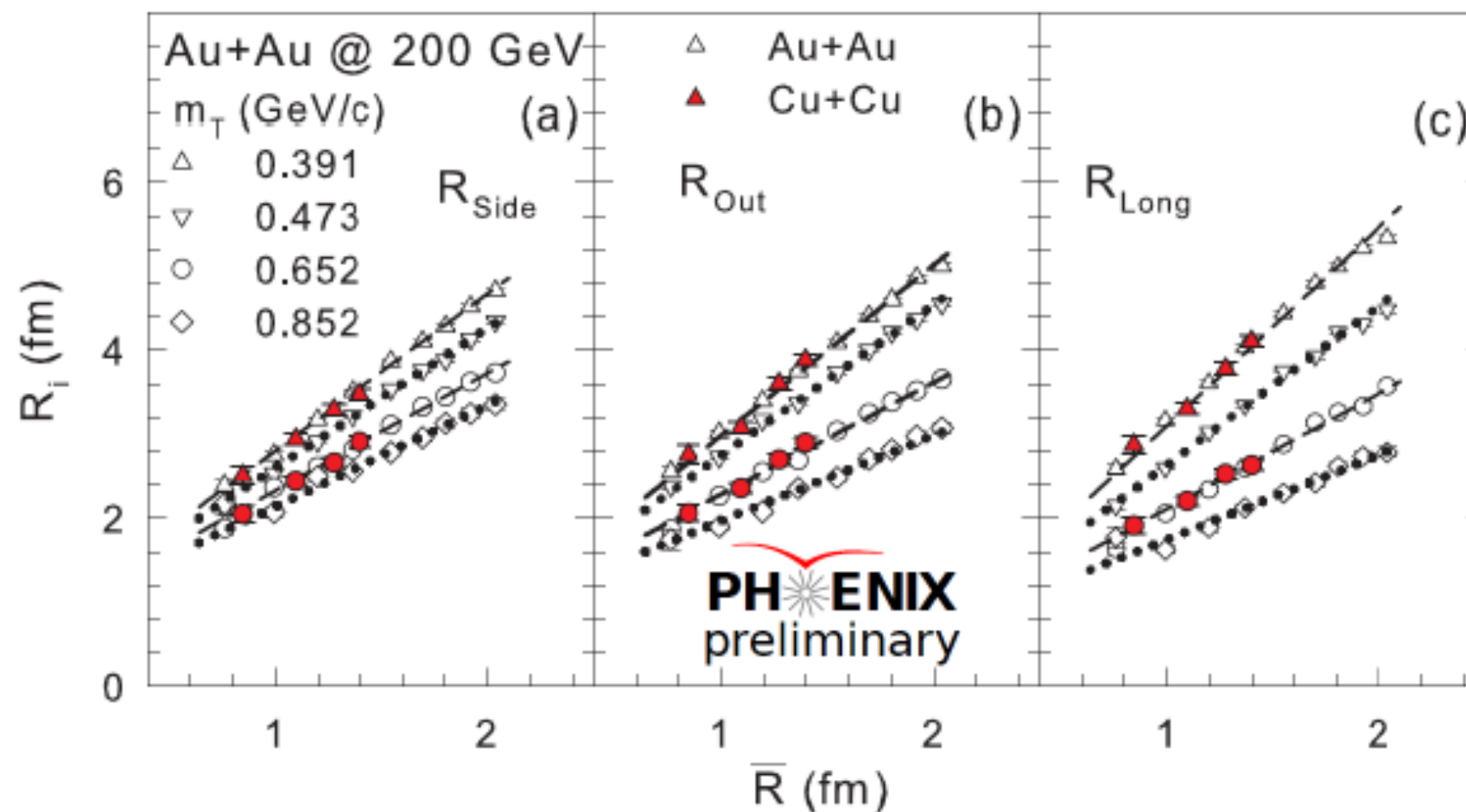
Hydro models associate a larger expansion time with a larger initial size  $\bar{R}$  Does it make a good scaling parameter ?

Use Glauber model to get  $N_{part}^{1/3}$  vs initial size  $\bar{R}$



$$\frac{1}{\bar{R}} = \sqrt{\left(\frac{1}{\sigma_x^2} + \frac{1}{\sigma_y^2}\right)}$$

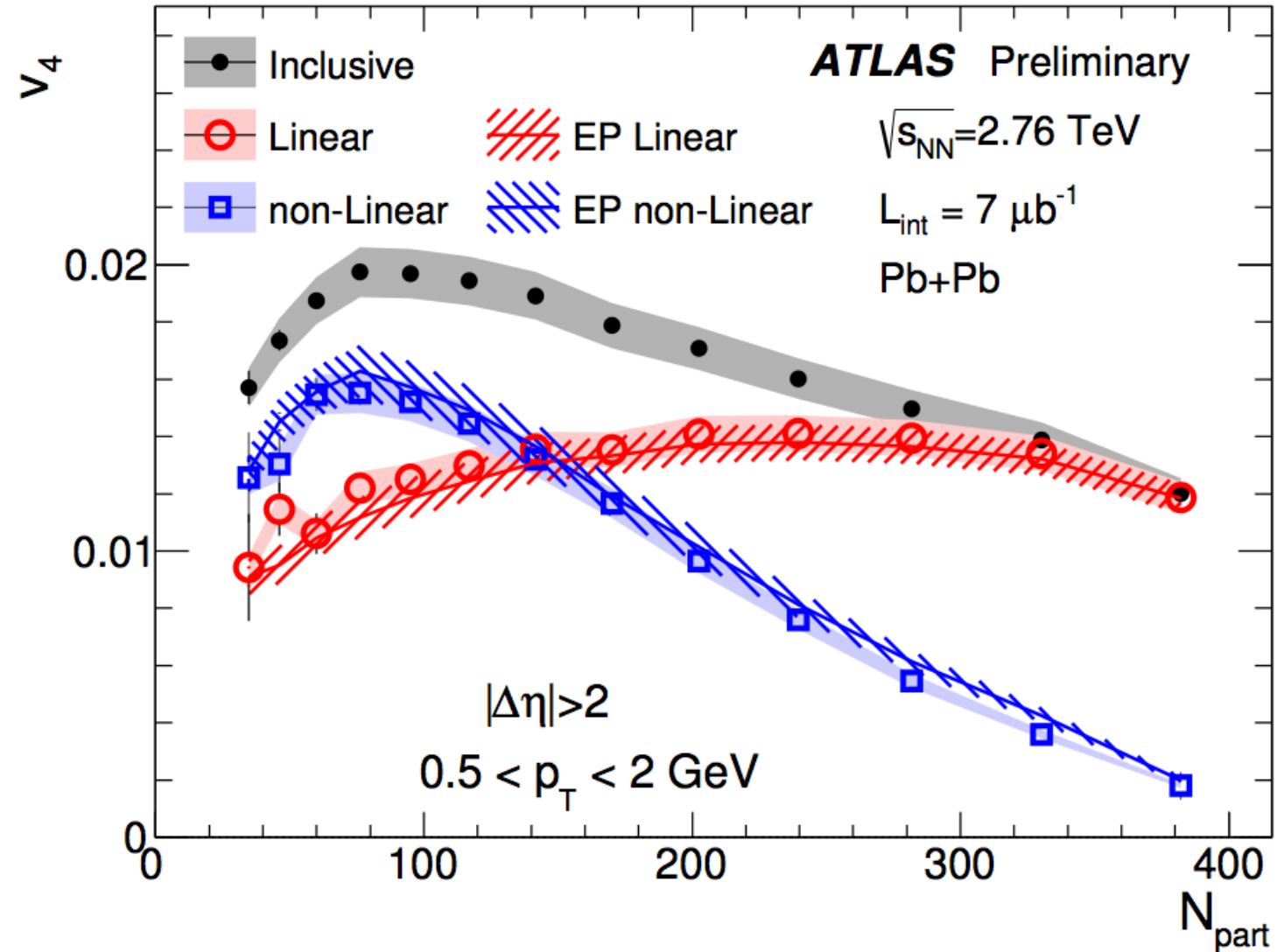
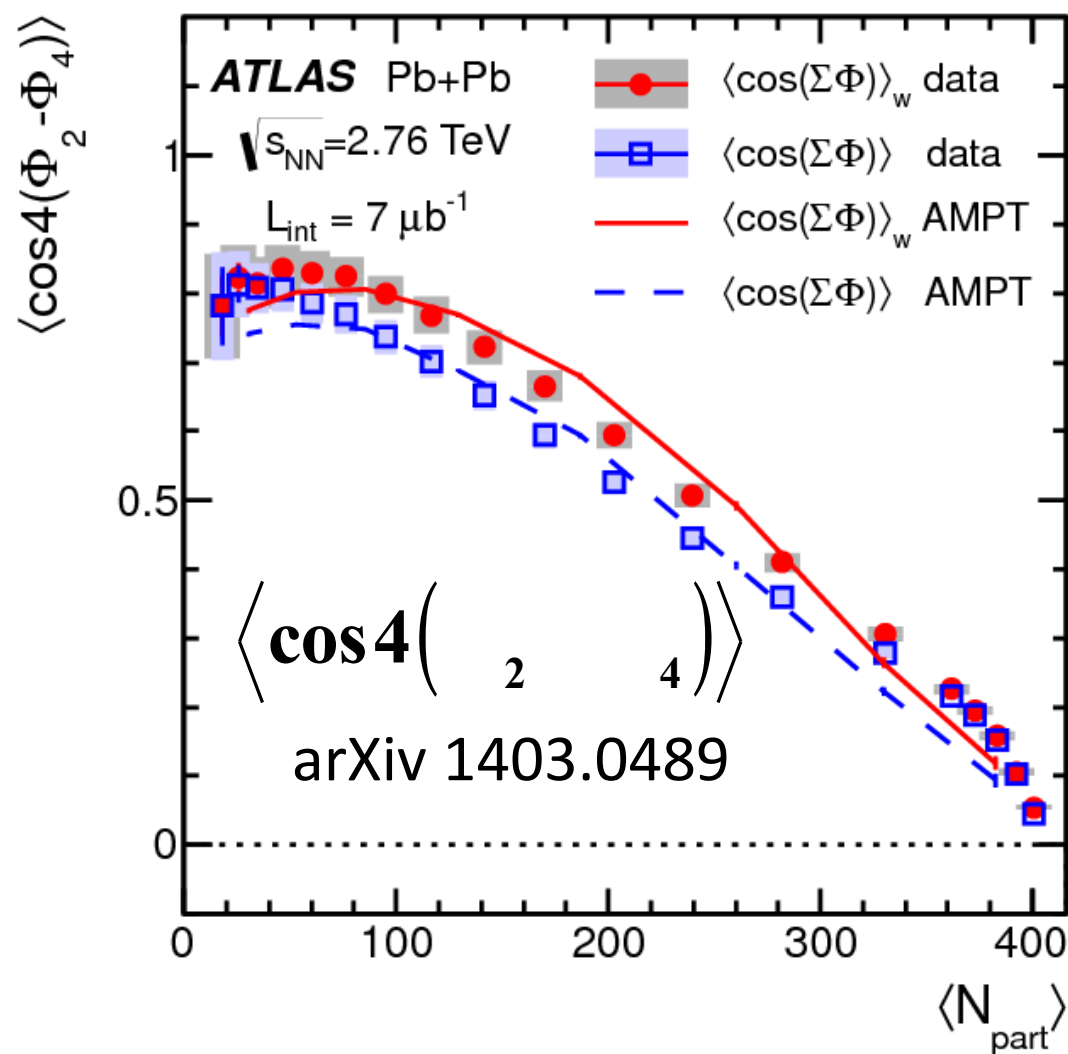
$\sigma_x$  &  $\sigma_y \rightarrow$  RMS widths of density distribution



Pion HBT radii scale with  $\bar{R}$

Linear dependence of transverse expansion on initial geometry

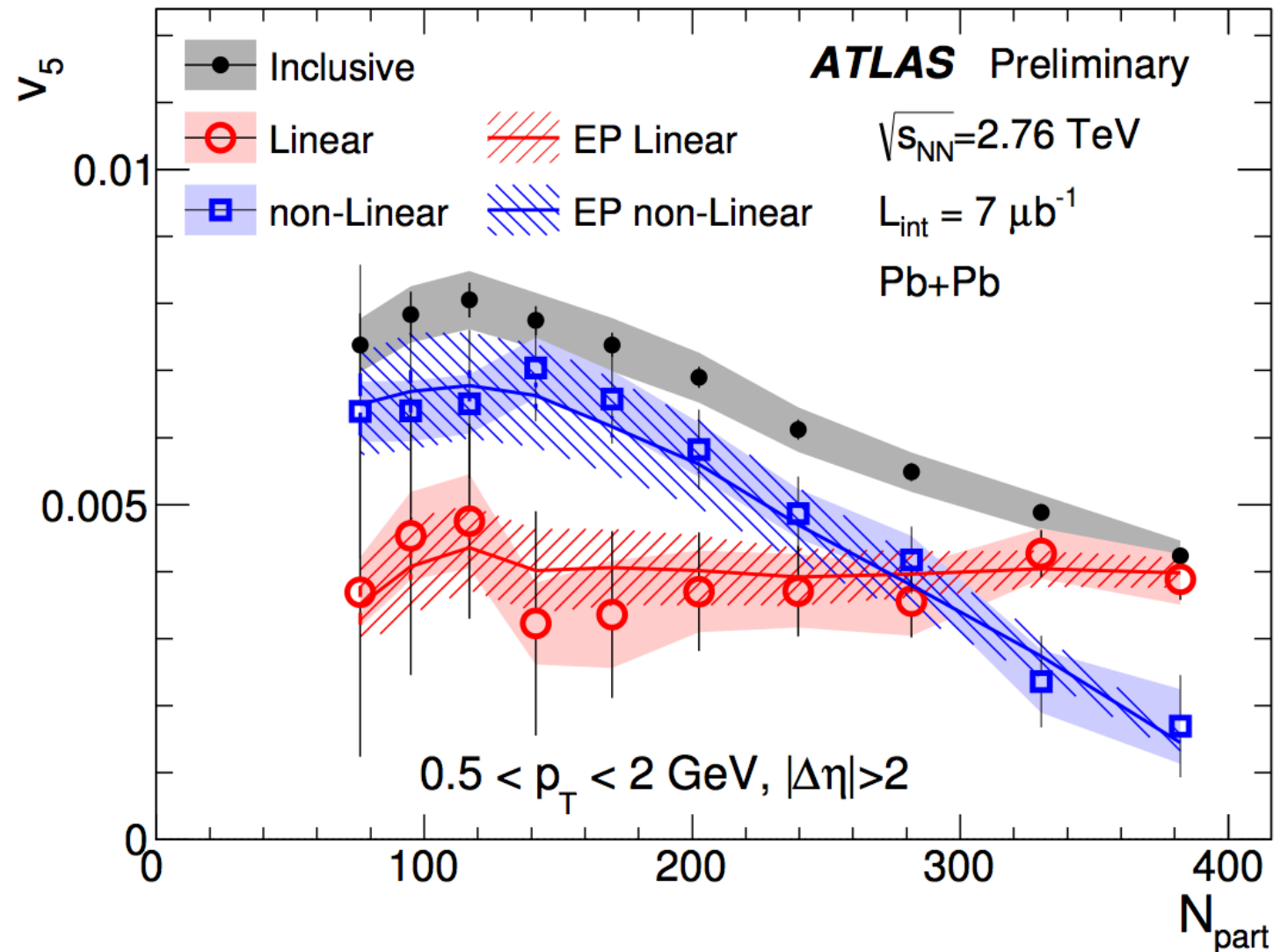
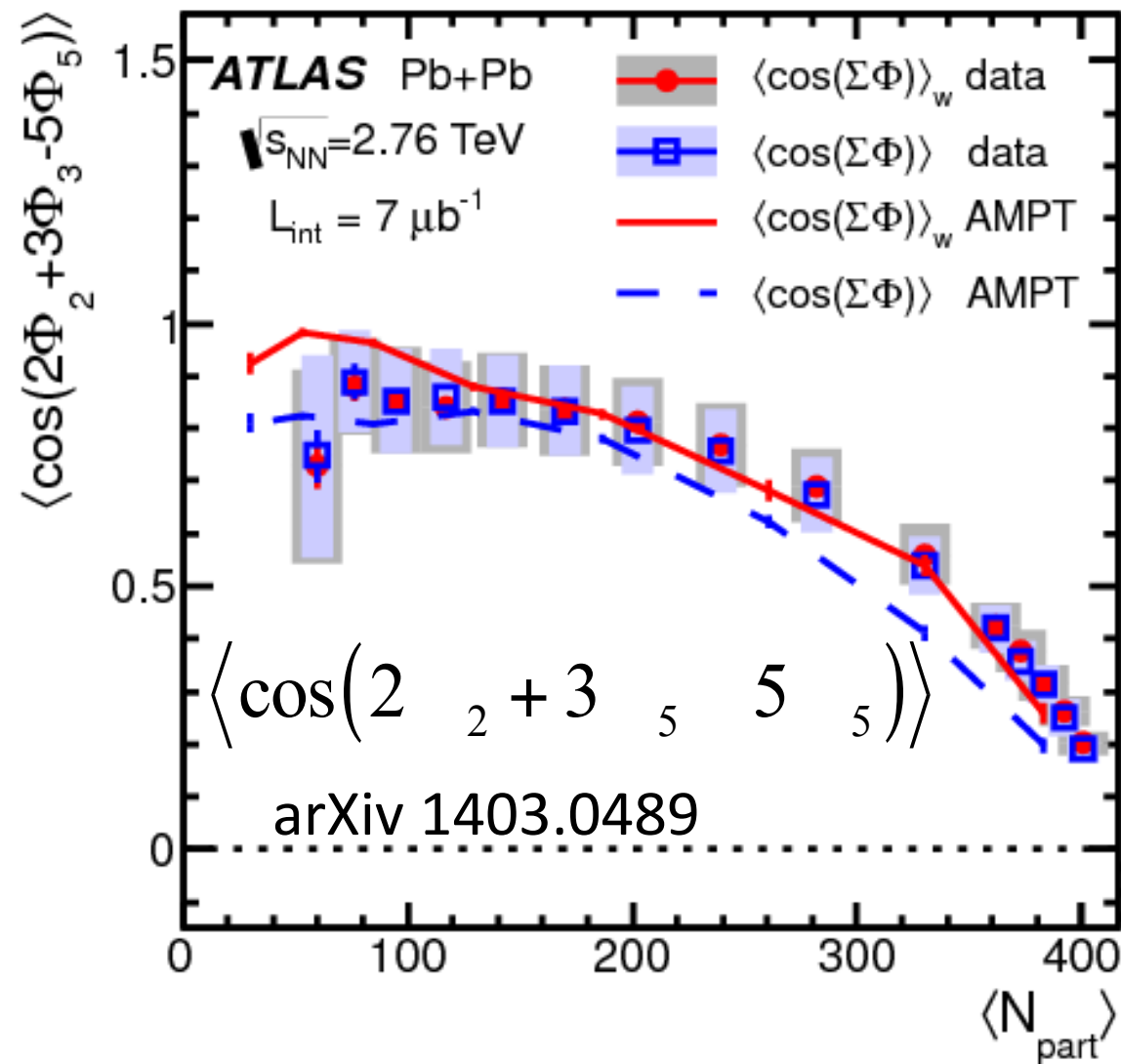
Slide from N.Ajit QM'14



- The non-linear & linear components from EP correlations are obtained as:

$$v_4^{NL} = v_4 \langle \cos 4(\Phi_2 - \Phi_4) \rangle, \quad v_4^L = \sqrt{v_4^2 - (v_4^{NL})^2}$$

- The results from the two procedures compare quite well
- In most central cases almost all  $v_4$  is uncorrelated with  $v_2$
- Correlated component gradually increases and overtakes linear component as  $N_{part} \sim 120$



- Compare linear & non-linear components from this analysis to EP correlation results
- The non-linear & linear components from EP correlations are obtained as:

$$v_5^{NL} = v_5 \langle \cos(2\Phi_2 + 3\Phi_3 - 5\Phi_5) \rangle, \quad v_5^L = \sqrt{v_5^2 - (v_5^{NL})^2}$$