

Measurements of 1st, 2nd and 3rd azimuthal anisotropy in $\sqrt{s_{NN}}=200\text{GeV}$ Cu+Au collisions at RHIC-PHENIX

RHIC-PHENIX実験における $\sqrt{s_{NN}}=200\text{GeV}$

銅・金衝突での**1次、2次、3次**方位角異方性の測定

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博士論文本審査 **2016年12月19日**

Outline

✓ Introduction

- Quark Gluon Plasma(QGP)
- Azimuthal anisotropy
- CuAu collisions

✓ Experiment/Analysis

- PHENIX
- centrality, event plane
- Simulation

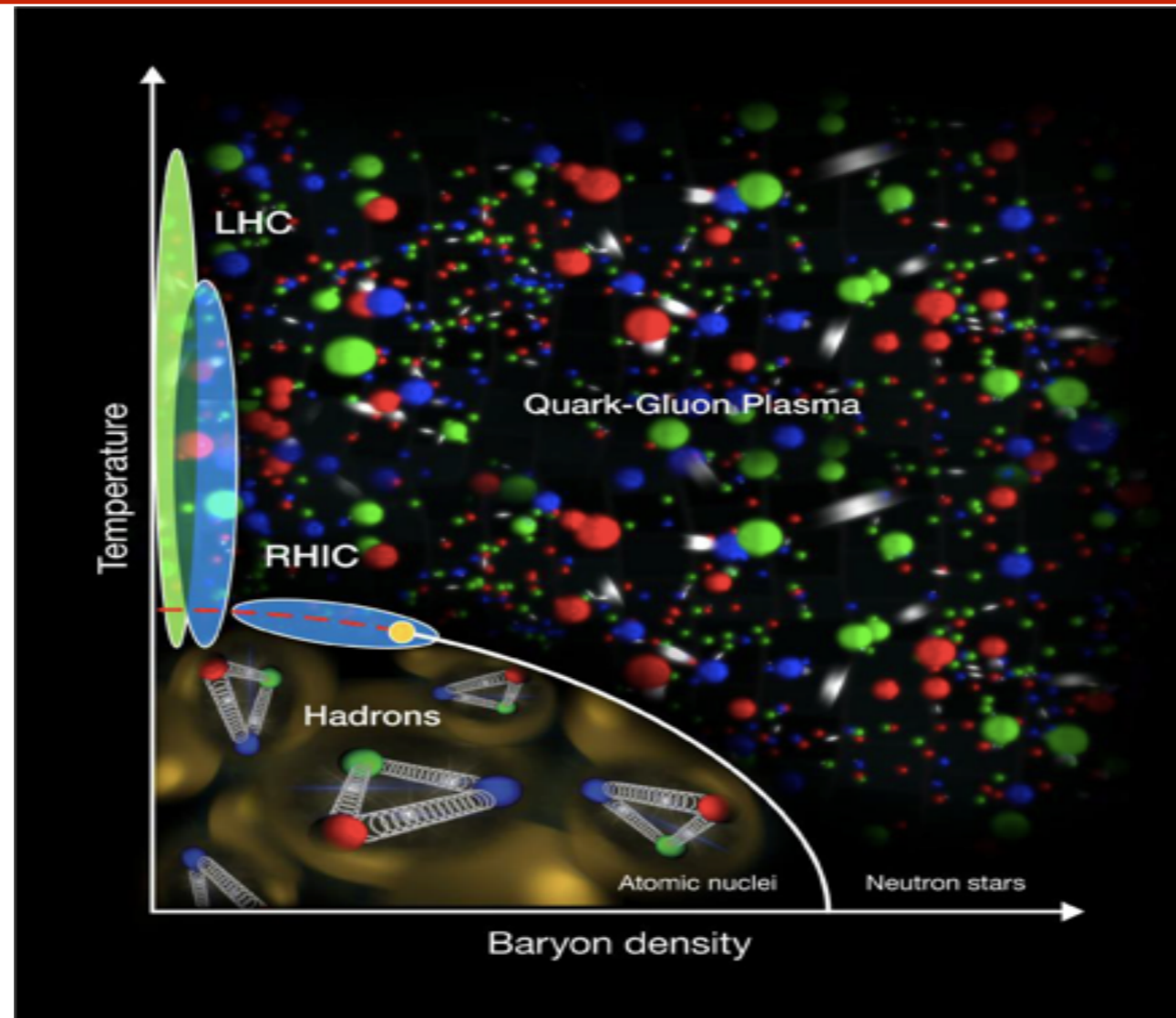
✓ Results/Discussions

- v_n at mid, forward/backward rapidities
- Initial model study

✓ Summary

Introduction

Quark Gluon Plasma(QGP)



QGP is a state of nuclear matter

- extremely high temperature, density
- consist of asymptotic free quarks and gluons
- Almost perfect liquid

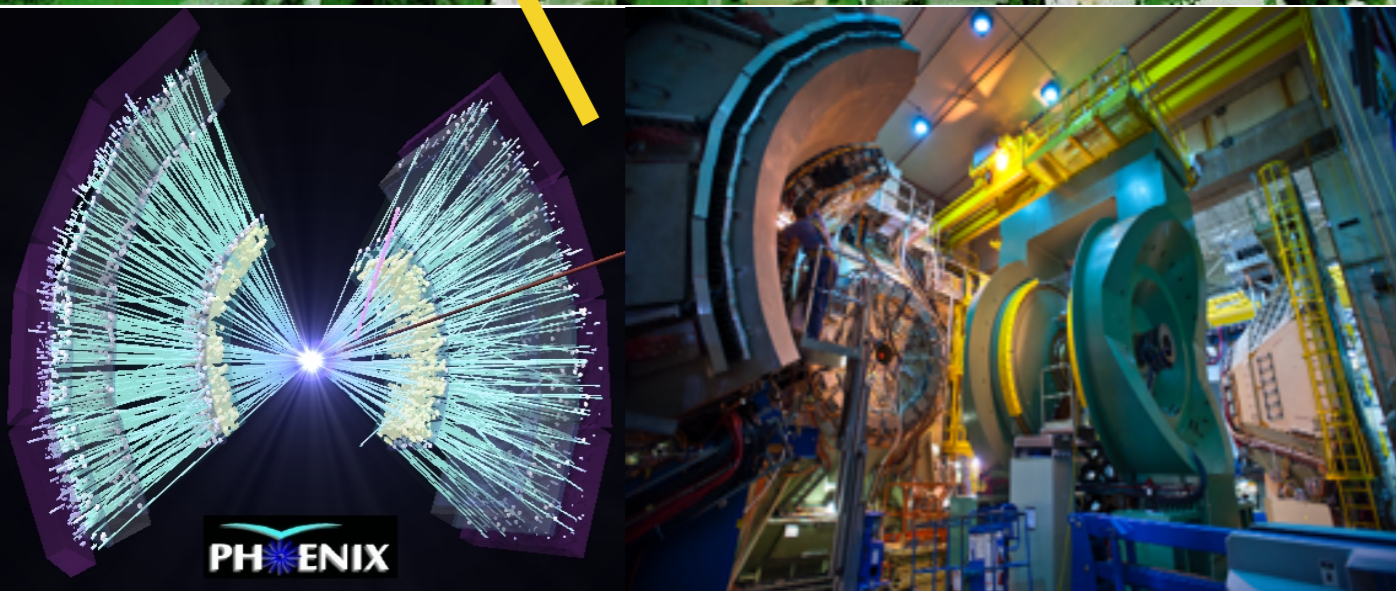
Predicted phase transition ϵ_c and T_c by Lattice QCD calculation

- $T_c \sim 170 \text{ MeV}$
- $\epsilon_c \sim 1 \text{ [GeV/fm}^3\text{]}$

Relativistic Heavy Ion Collider(RHIC)



| Species | Energies |
|--------------|---|
| Au+Au | 200, 130, 62.4 GeV 39, 27, 22.4 GeV 19.6, 14.6, 7.7 GeV |
| Cu+Cu | 200, 62.4, 22.4 GeV |
| U+U | 193 GeV |
| Cu+Au | 200 GeV |
| 3He+Au | 200 GeV |
| d+Au | 200 GeV |
| p+Au | 200 GeV |
| p+Al | 200 GeV |
| p+p | 510, 500, 200 GeV 62.4 GeV |



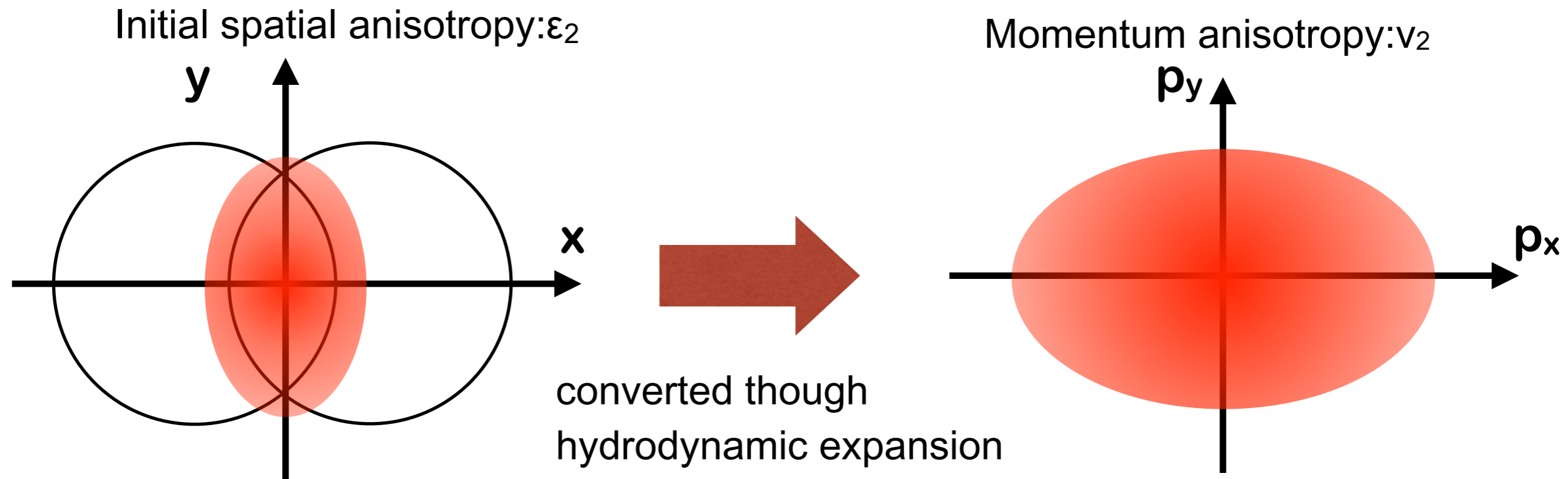
✓ Wide range of species and energies

Relativistic heavy ion collision is
unique tool to form QGP

Au+Au 200 GeV @ RHIC

- $\epsilon_{Bj} \sim 5 \text{ [GeV/fm}^3\text{]} > \epsilon_c$

Azimuthal anisotropy: Elliptic flow



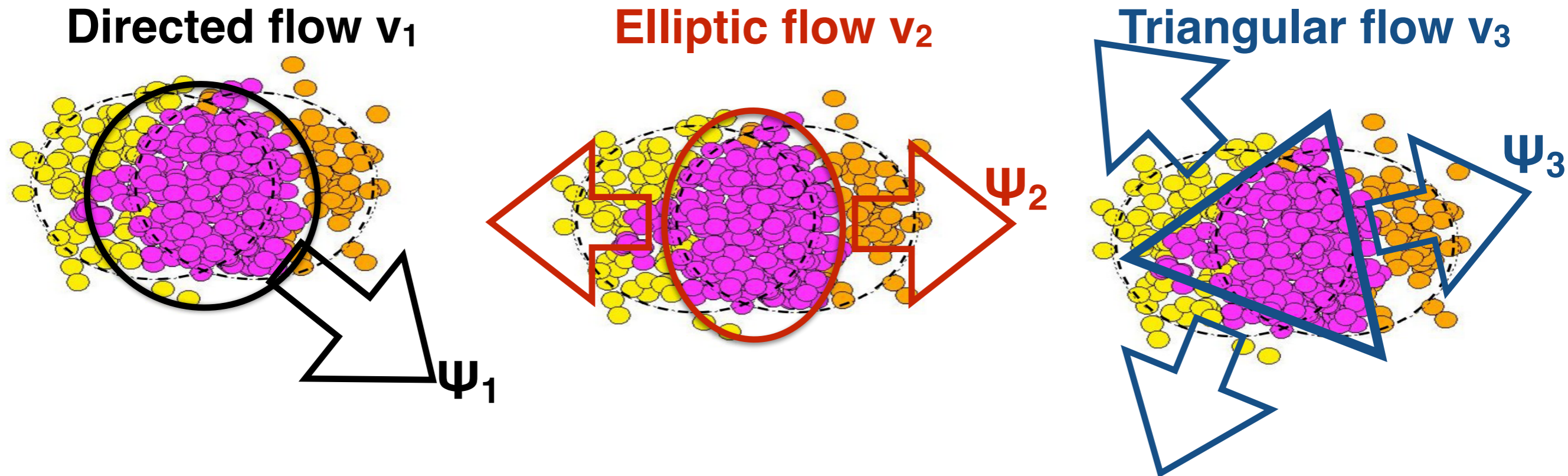
✓ Initial spatial anisotropy ε_2 \rightarrow Final momentum anisotropy v_2

- Non-isotropic pressure gradient
- Larger initial energy density makes larger v_2

✓ Azimuthal anisotropy is strong probe!

- Clear origin \rightarrow initial spatial geometry
- Influenced by hydrodynamic expansion

Azimuthal anisotropy: Directed, Triangular flow



✓ Initial geometry is not smooth picture!

- Event by event, initial participant is fluctuated

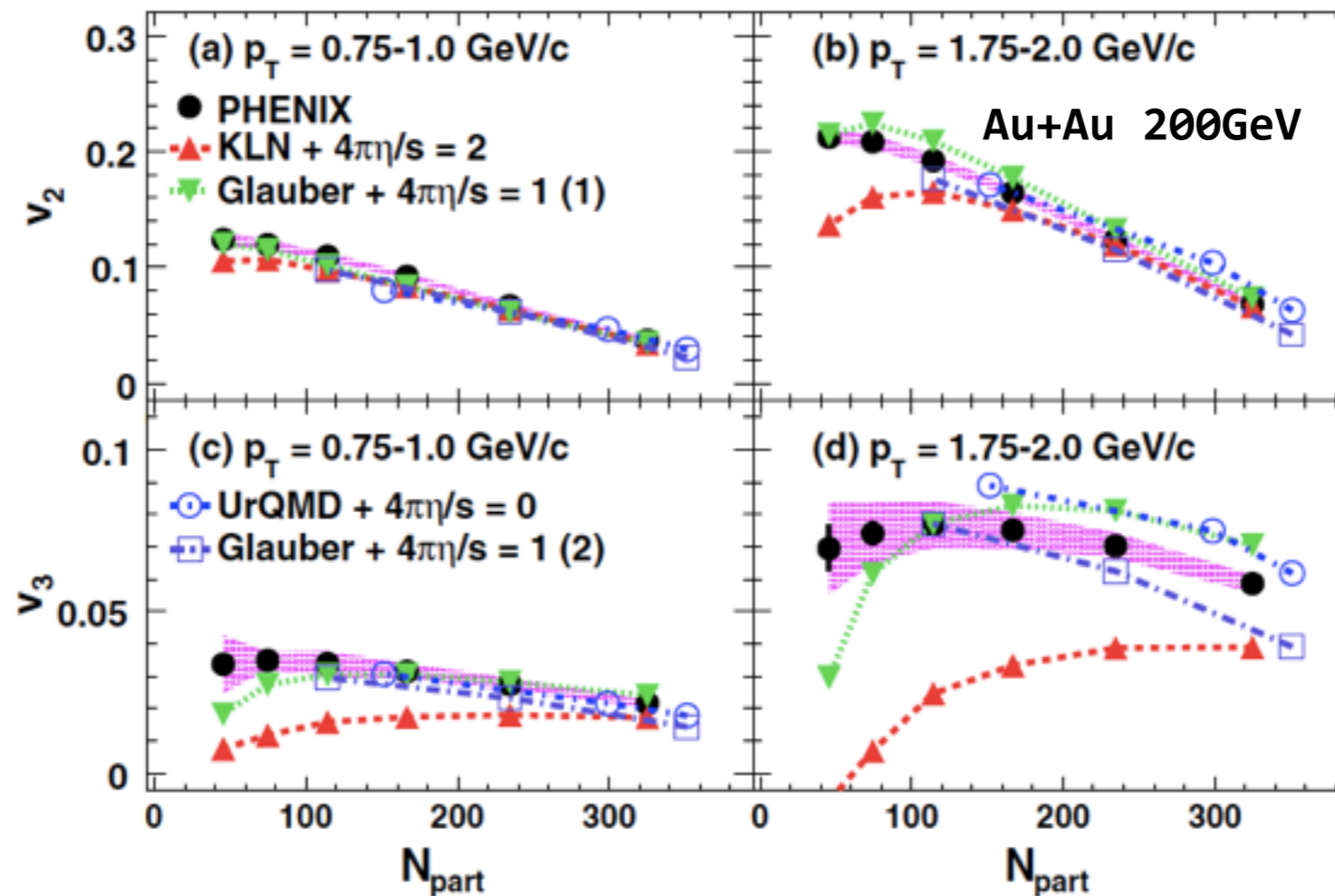
✓ Coefficients in Fourier expansion of particle distribution

$$v_n = \langle \cos[n(\phi - \Psi_n)] \rangle$$

$$\frac{dN}{d\phi} \propto 1 + \sum_{n=1} 2v_n \cos[n(\phi - \Psi_n)]$$

v_n constrain initial condition & viscosity

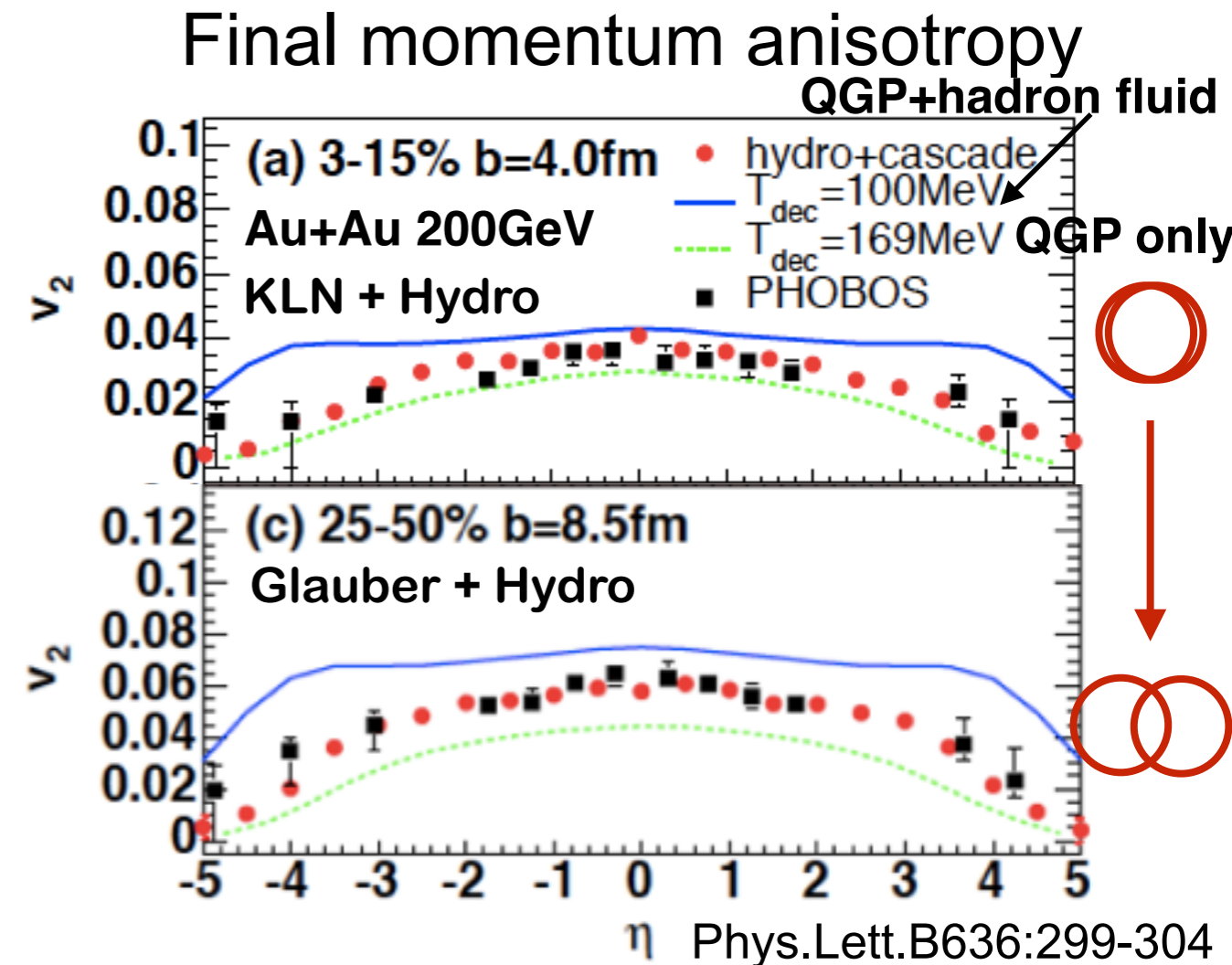
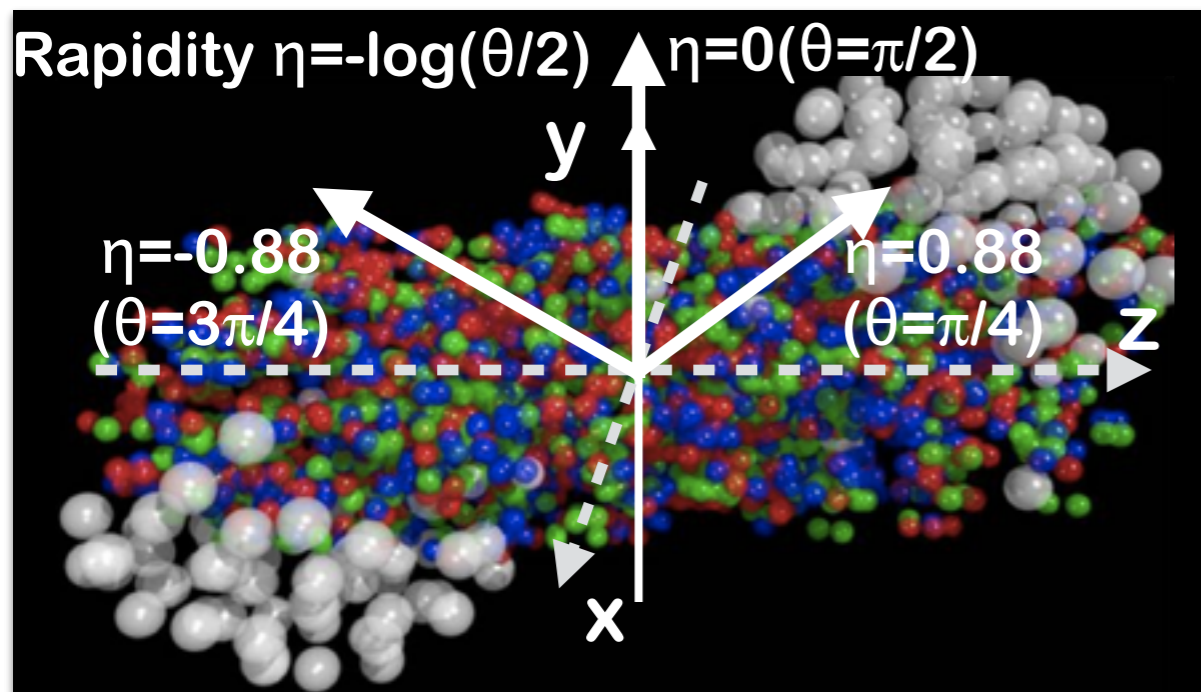
v_2, v_3 theory comparison



- ✓ v_2, v_3 are sensitive to initial condition and viscosity of QGP
- Theoretically, initial condition and viscosity have uncertainty
- ➡ v_n are good constraint of the initial geometry and viscosity

η dependence of v_2

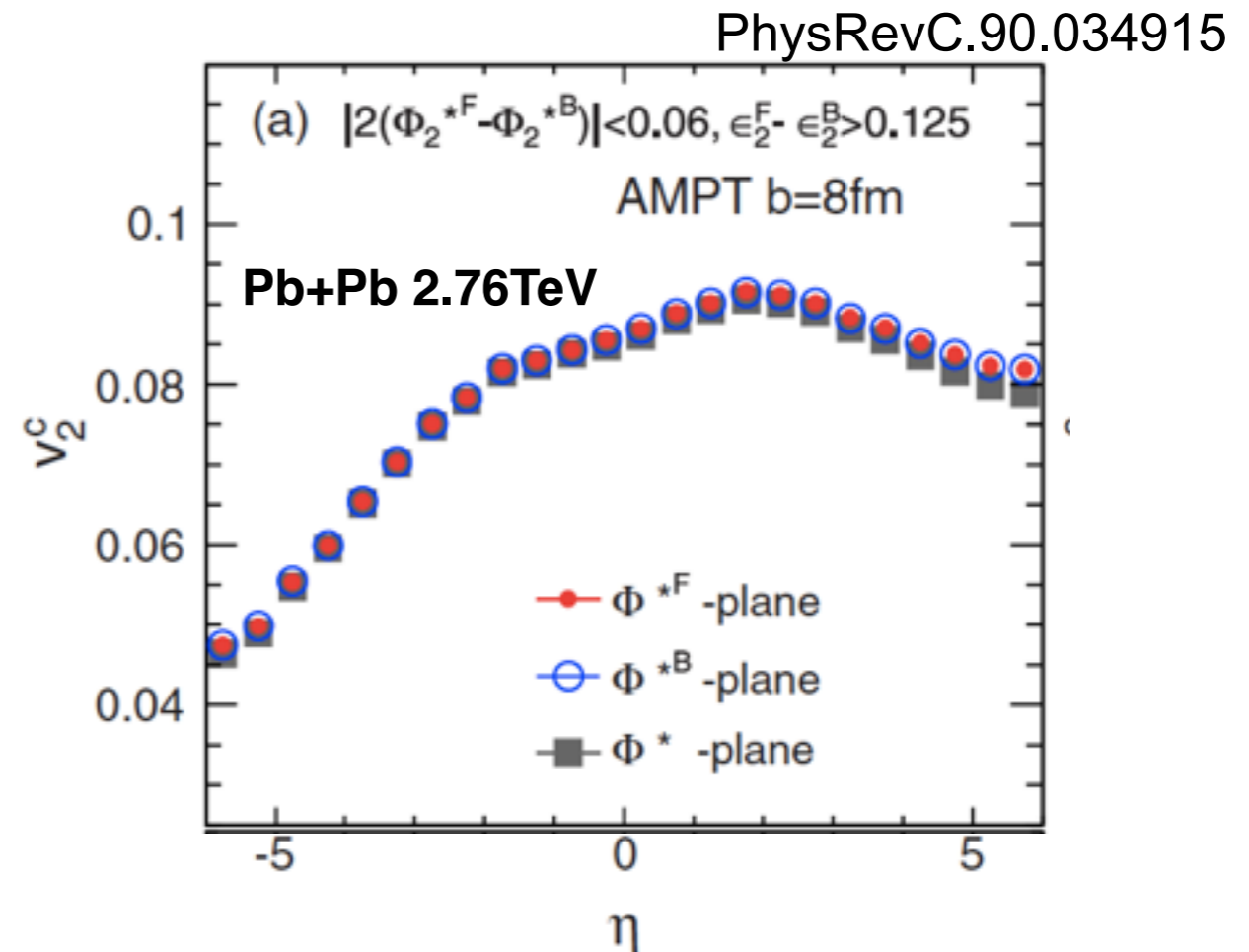
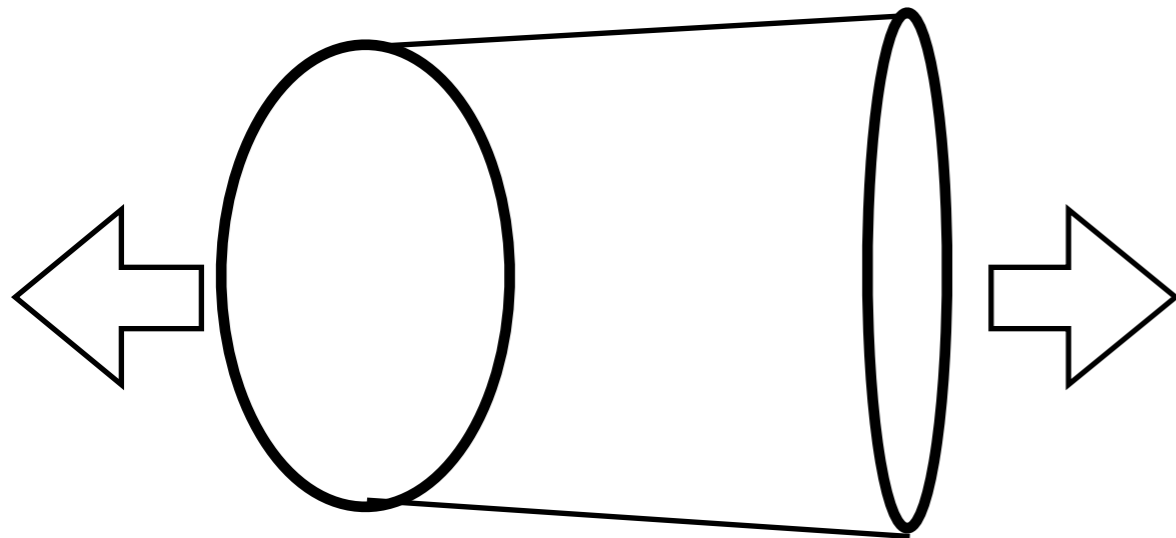
Initial geometry after the collisions



- ✓ At mid- η , v_2 is largest and f/b- η , v_2 becomes small
 - Larger $dN/d\eta$ at mid- η and smaller $dN/d\eta$ at f/b- η
 - Understand η dependence of initial geometry is important
- ✓ $v_2(\eta)$ depends on initial condition
 - Not strong η dependence of initial geometry
 - Mid-central: Glauber, Central: KLN

Rapidity dependence of initial condition

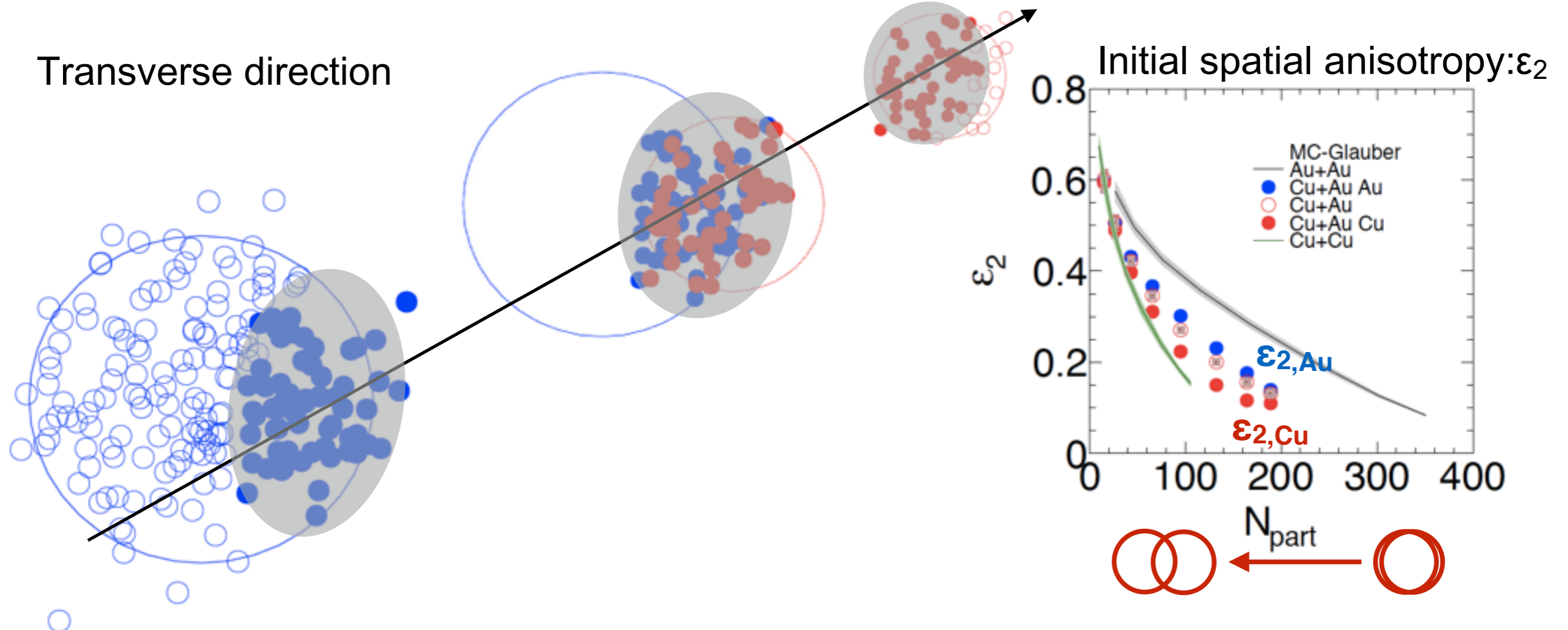
Initial geometry $\epsilon_{2,B} < \epsilon_{2,F}$



- ✓ Initial geometry has been considered to be rapidity independent
- ✓ Event by event, forward/backward v_n might be asymmetric
 - initial participant geometries of the two nuclei would be different
 - $\epsilon_{n,B} < \epsilon_{n,F} \rightarrow v_{n,B} < v_{n,F}$
- ➔ Initial geometry has strong rapidity dependence

Motivation: Why Cu+Au is analyzed ?

Transverse direction



- ✓ First asymmetric Cu+Au collisions were operated in 2012
- ✓ Asymmetric initial condition provides
 - Different left/right pressure gradient $\rightarrow v_1$
 - Different Forward/Backward density and geometry
 - \rightarrow Rapidity asymmetric v_n
- \rightarrow Measurements of v_n in asymmetric system could be good study of initial condition

My activity

M1~M2 (2011~2013)

Repair VTX @BNL

JPS Spring & Fall (Talk)

QM2012 (poster)

ATHIC 2012 (Talk)

Au+Au flow analysis using VTX

D1(2013~2014)

Repair VTX @BNL

Shift taking & detector expert
for Run 13, Run14

Cu+Au flow analysis

D2 (2014~2015)

QM2014(Talk)

JPS-DNP(Talk)

Shift taking & detector expert
for Run 14, Run15

D3(2015~2016)

QM2015(Poster)

TGSW2015 (Talk)

WWND2016(Talk)

D4 (2016~)

Cu+Au flow paper is
accepted by PRC
PRC 94, 054910

Domestic conference

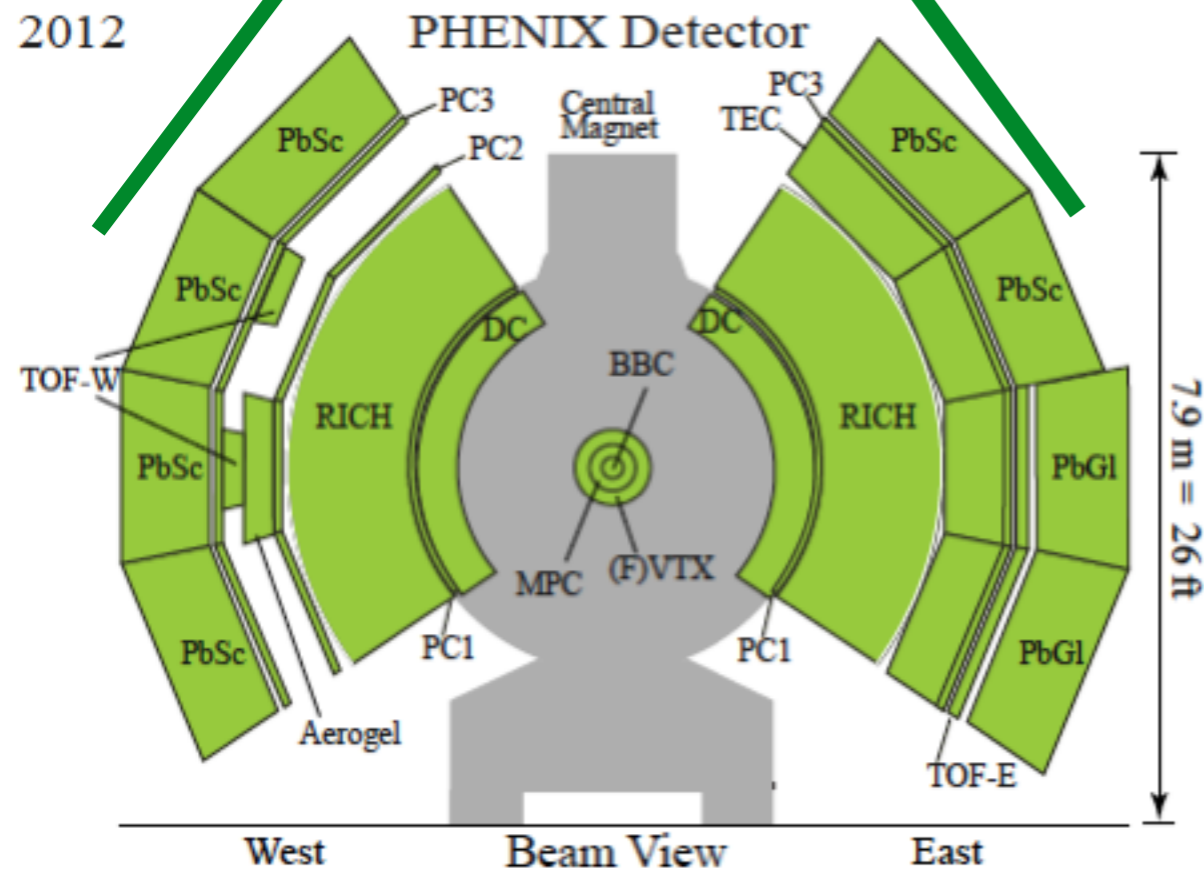
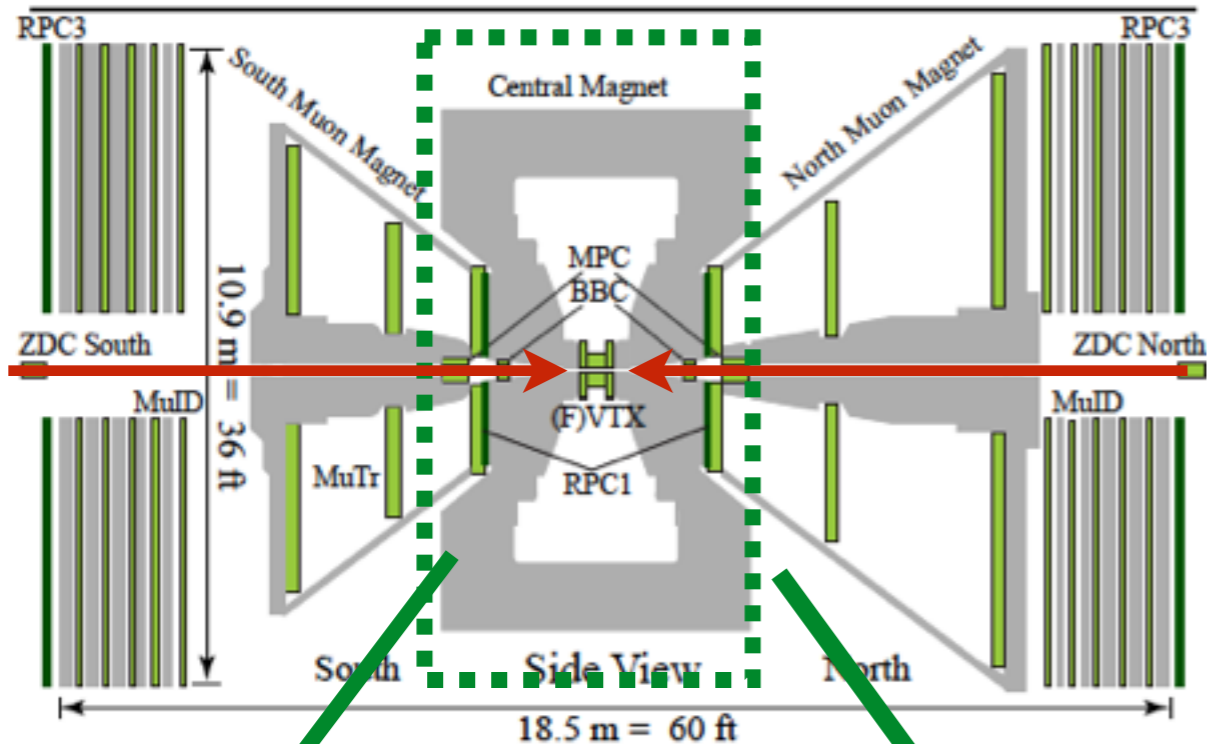
International conference

Hardware and shift

Analysis

Experiment Analysis

PHENIX detectors



Trigger, centrality, collision vertex
Event plane

-Beam Beam counter(BBC)
($3 < |\eta| < 4$)

Event plane

-Zero degree calorimeter
-Shower max detector

Charged particle Tracking

-Drift Chamber(DC) ($|\eta| < 0.35$)

- Momentum

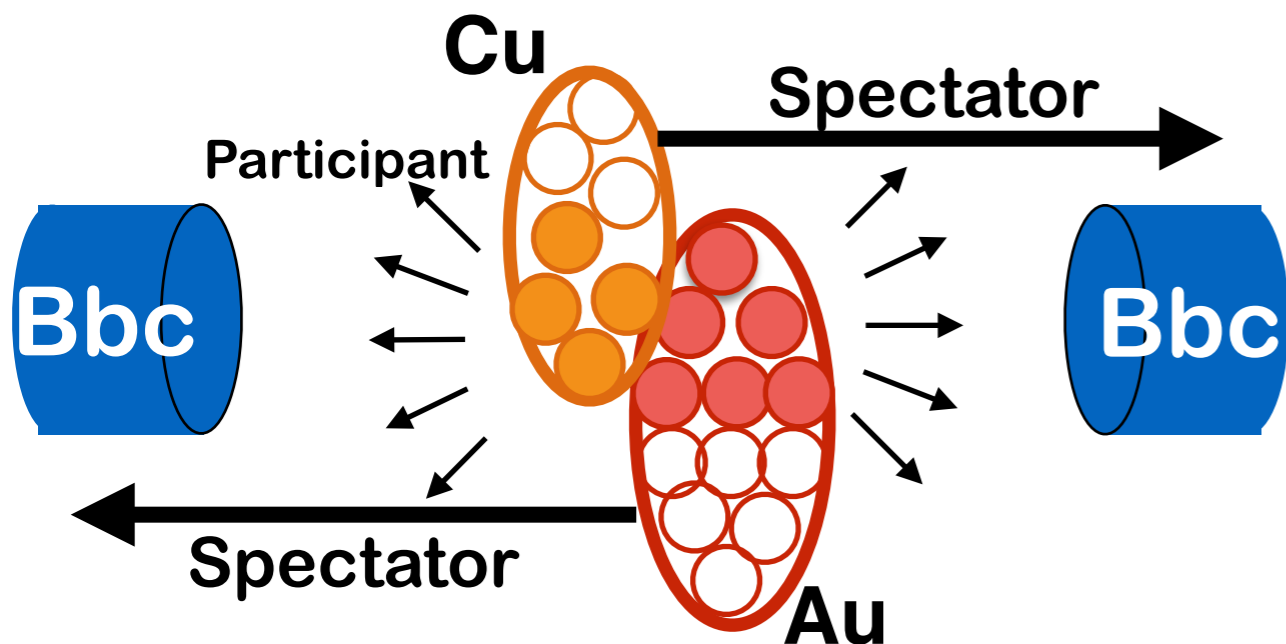
-Pad Chamber(PC) ($|\eta| < 0.35$)

- Hit position

-Electro magnetic
calorimeter(EMC) ($|\eta| < 0.35$)

- Hit position

N_{part} & Centrality

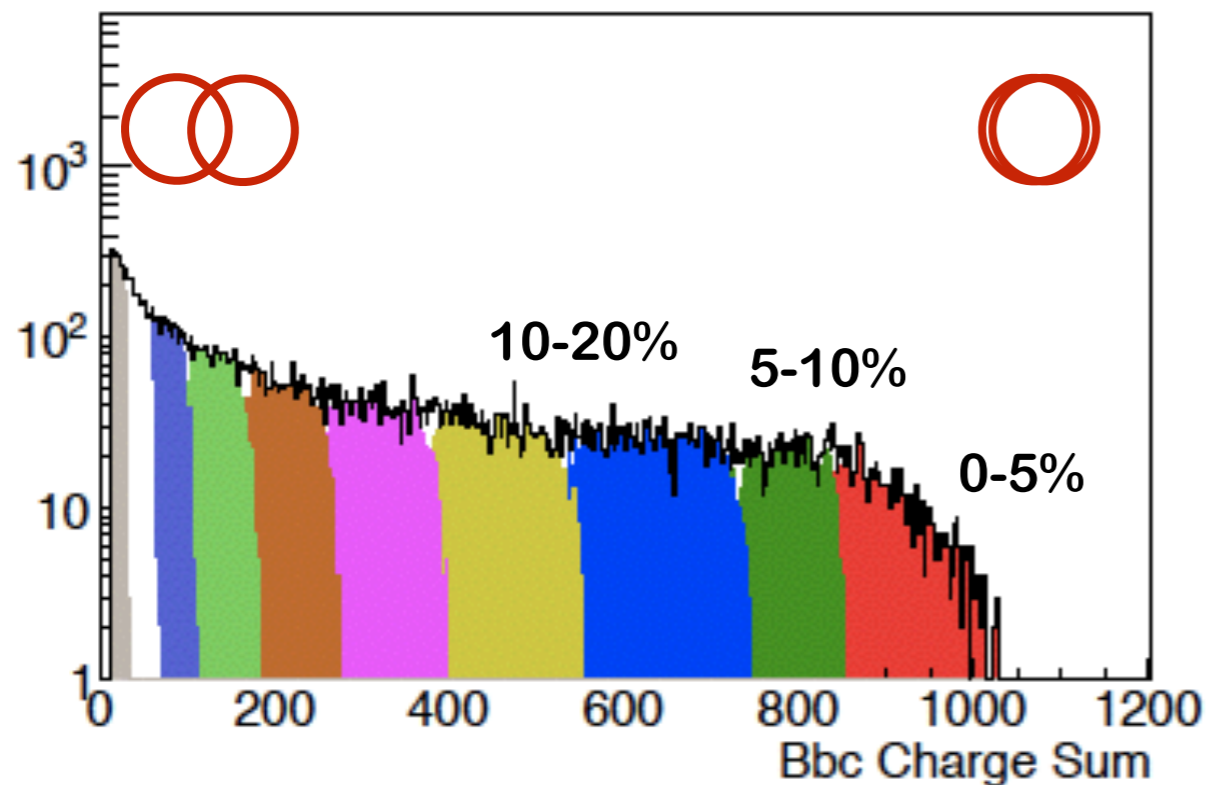


N_{part}

- ✓ Number of participants
 - e.g. Cu 4 , Au 6
- ✓ Estimated by Glauber model
 - nucleon base

Centrality

- ✓ Fraction of events in terms of total geometrical cross section
 - Overlap zone of two nuclei \propto Multiplicity
 - ✓ Experimentally, overlap zone is classified by multiplicity in Bbc
 - Multiplicity in Bbc \propto Overlap zone
- ✓ 0%(central) 100%(peripheral)



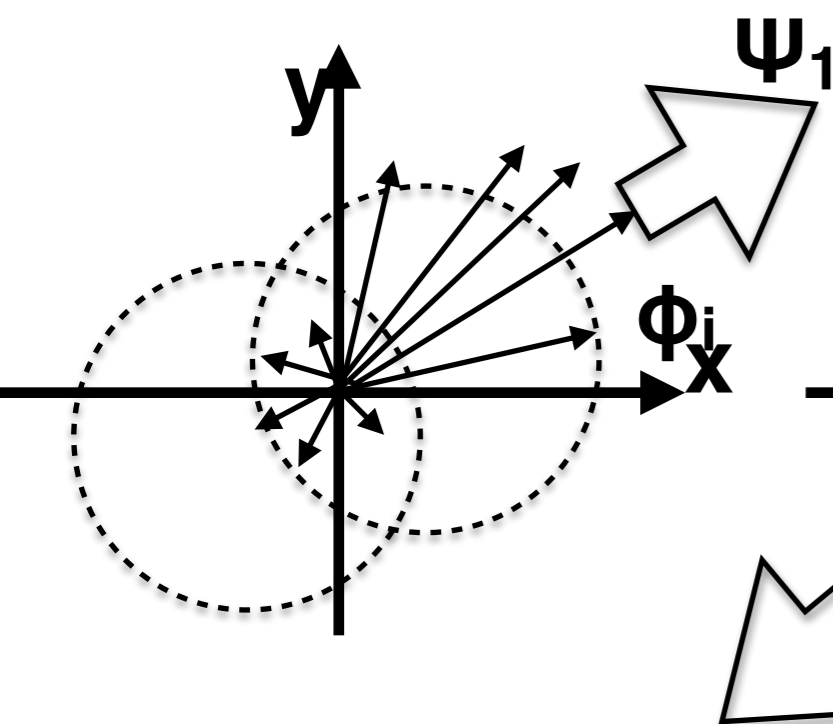
Anisotropy measurement via Event Plane method

Event plane(EP) method

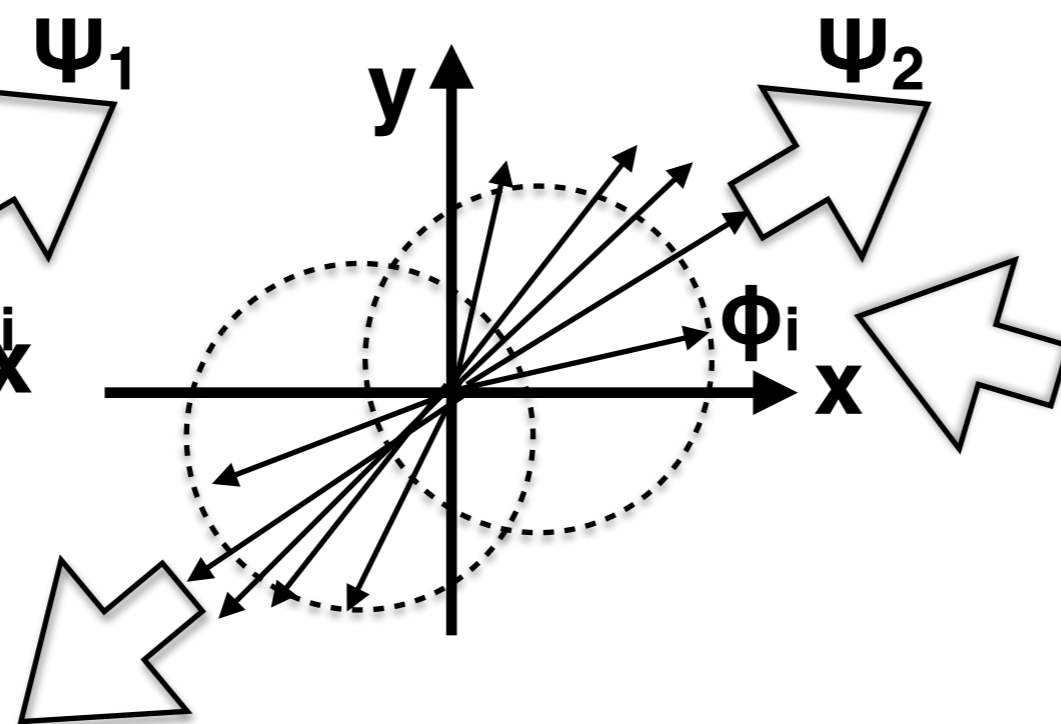
- one of the flow measurement methods
- produced particles are measured with respect to EP
- EP is the azimuthal direction most particles are emitted to
- observed v_n is corrected by EP resolution

$$v_n = \frac{\langle \cos(n[\phi - \Psi_n^{obs}]) \rangle}{\text{Res}\{\Psi_n^{obs}\}}$$

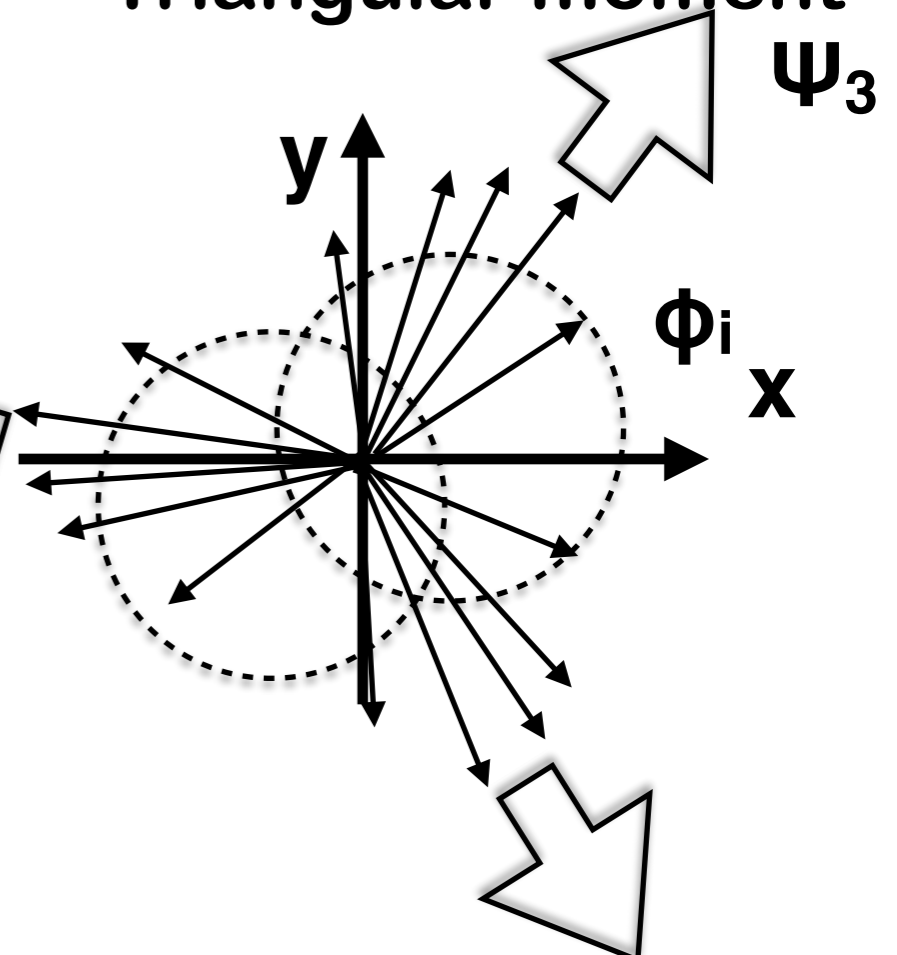
Directed moment



Elliptic moment



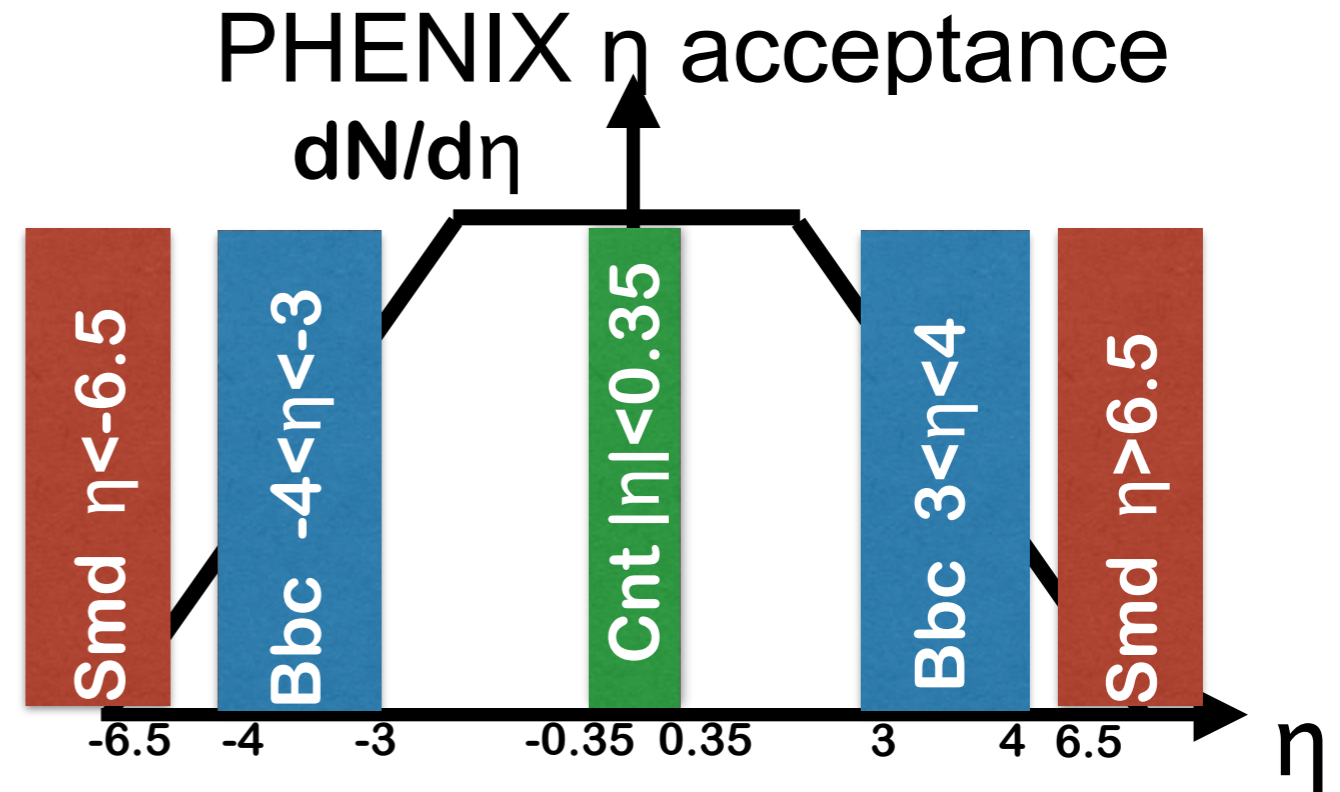
Triangular moment



Event plane detectors and resolutions

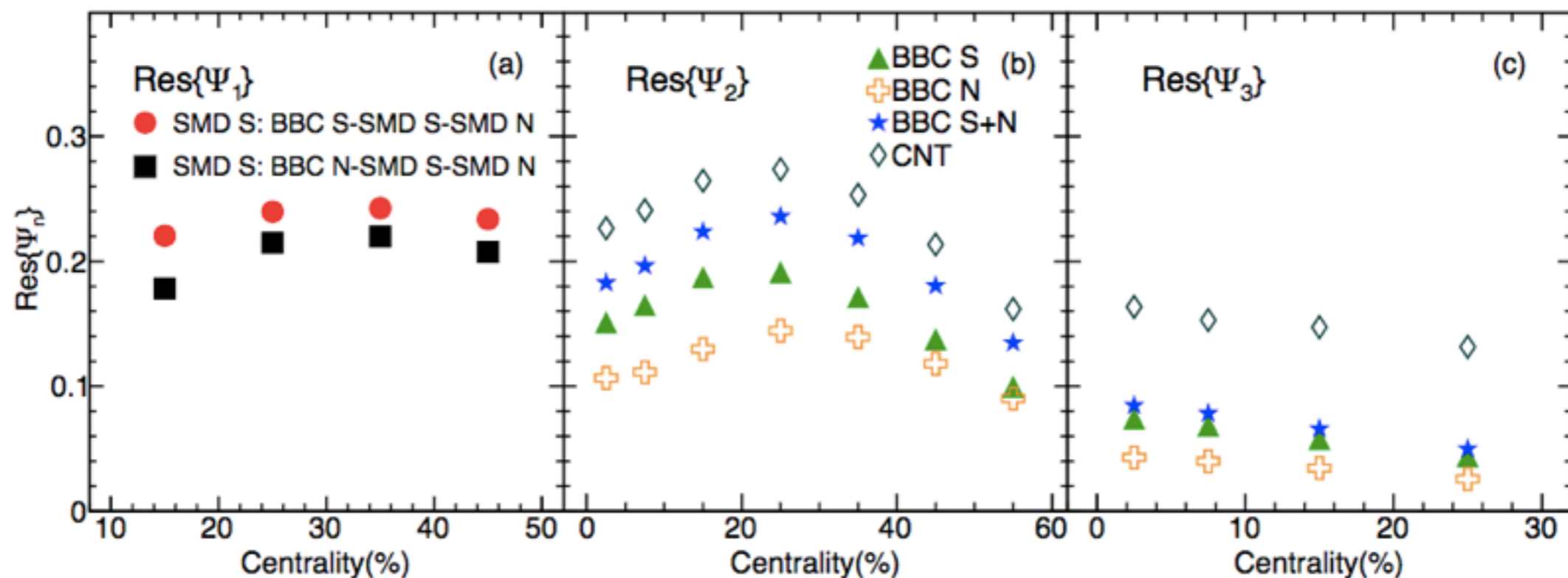
Event Plane detectors

- 2nd, 3rd Event plane
 - Bbc, Cnt
- 1st Event plane
 - Bbc, Smd



Event Plane resolution

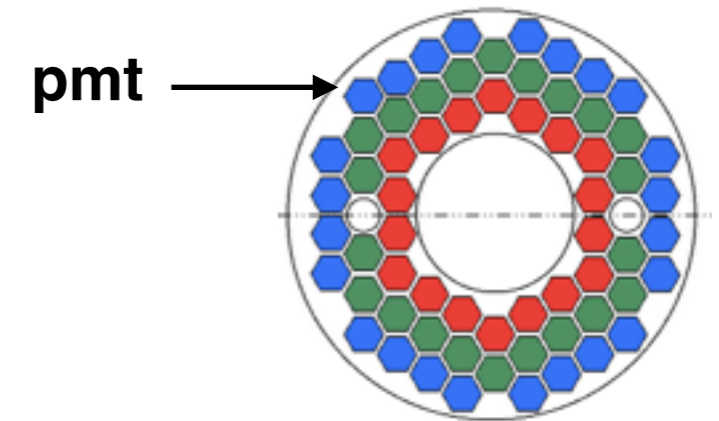
$$\text{Res}\{\Psi_n^{\text{obs}}\} = \langle \cos(n[\Psi_n^{\text{obs}} - \Psi_n^{\text{true}}]) \rangle$$



v_n measurement at Bbc($3 < |\eta| < 4$)

✓ v_n is measured using 64 Bbc pmts

- Bbc can not reconstruct tracks
- Measured v_n include back ground



✓ Full Geant simulation with PHENIX configuration

- Measured $v_n \rightarrow$ True v_n

$$v_n^{\text{true}} = \frac{v_n^{\text{mes}}}{R_n}$$

$$R_n = \frac{v_{n,\text{output}}^{\text{Sim}}}{v_{n,\text{input}}^{\text{Sim}}}$$

$v_{n,\text{input}}^{\text{Sim}}$

Input v_n from particle simulation

$v_{n,\text{output}}^{\text{Sim}}$

Output v_n from Geant simulation

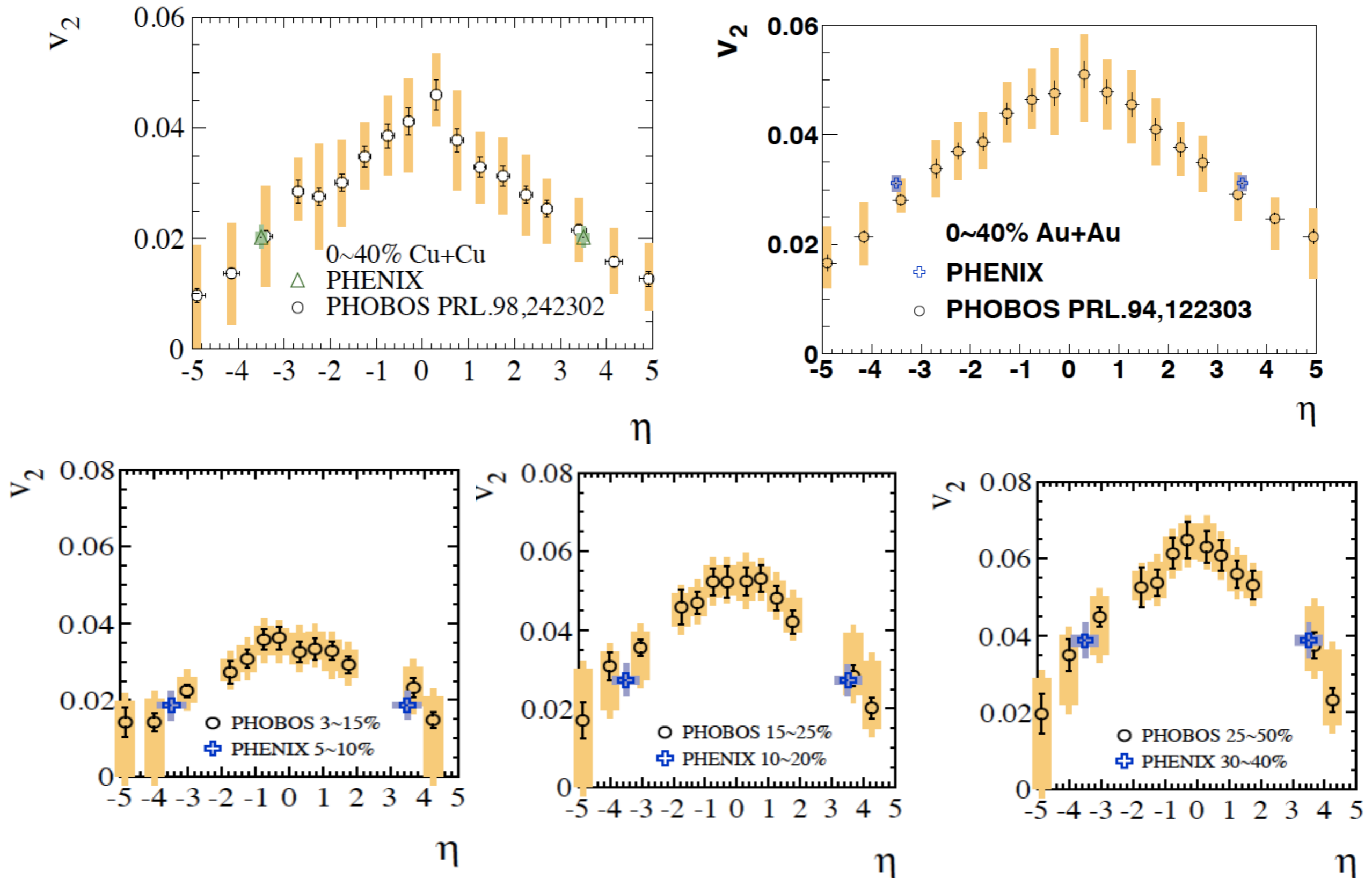
✓ Correction factor R_n

- R_2 : 0.74
- R_3 : 0.66

✓ Systematic study

- $dN/d\eta$
- p_T spectra
- v_n (pt)
- v_n (eta)

Comparison of v_2 to PHOBOS's results



✓ My results are consistent with PHOBOS's results

$dN_{ch}/d\eta$ measurements at Bbc

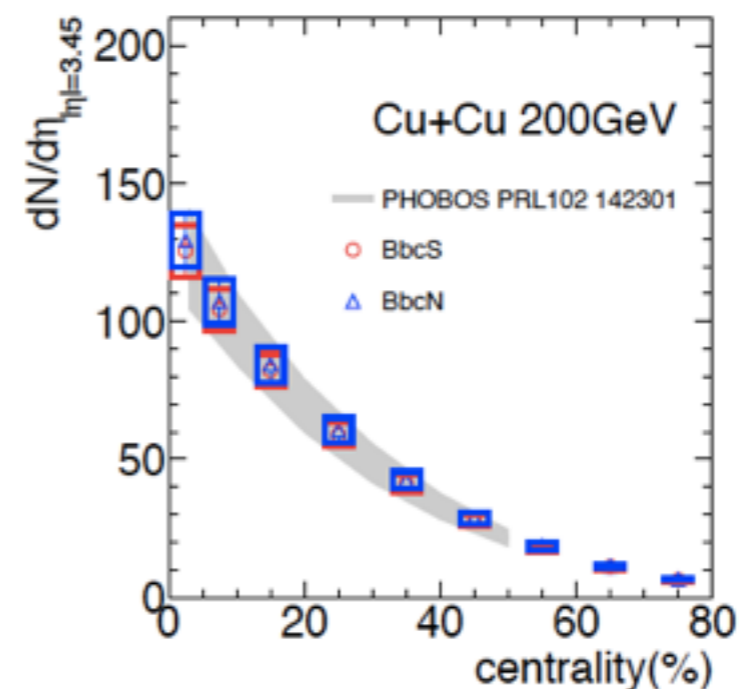
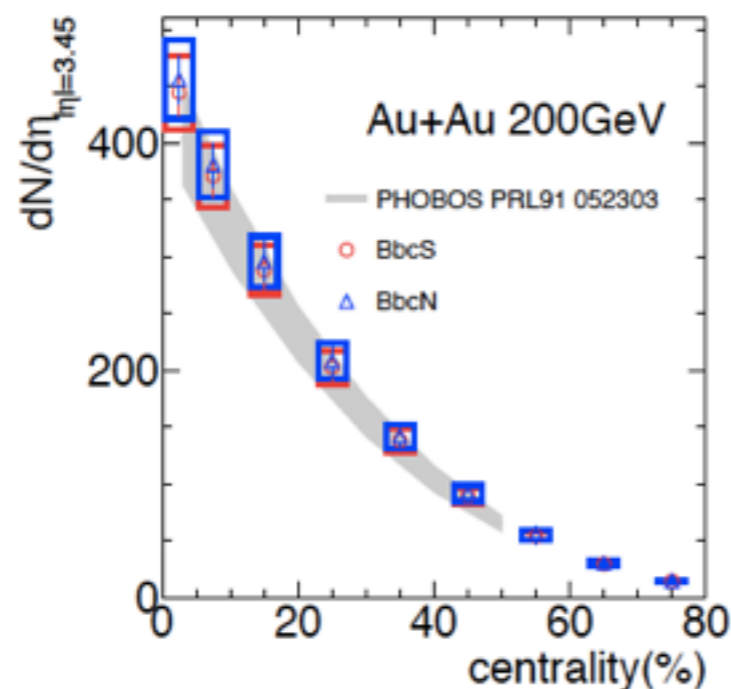
Like v_n measurements, correction factors is estimated from Geant simulation

$$\frac{dN_{ch}}{d\eta} = R * ADC^{obs} \quad 2/3: +- \pi / (+- \pi, \pi 0)$$

$$R = \frac{2}{3} \frac{1}{ADC_{output}^{sim}} \quad ADC_{output}^{sim}$$

➔ $R \sim 0.5$

Comparison to PHOBOS



My results are consistent with PHOBOS's results

Systematic sources

✓ v_n at mid- η

- East and West arm difference
- CNT track cut
- Event Plane difference
- Event Plane resolution difference

✓ v_n at F/B- η

- Event Plane difference
- Geant simulation
- $dN/d\eta$ distribution
- p_T distribution
- p_T dependence of v_n
- η dependence of v_n

✓ $dN/d\eta$ at F/B- η

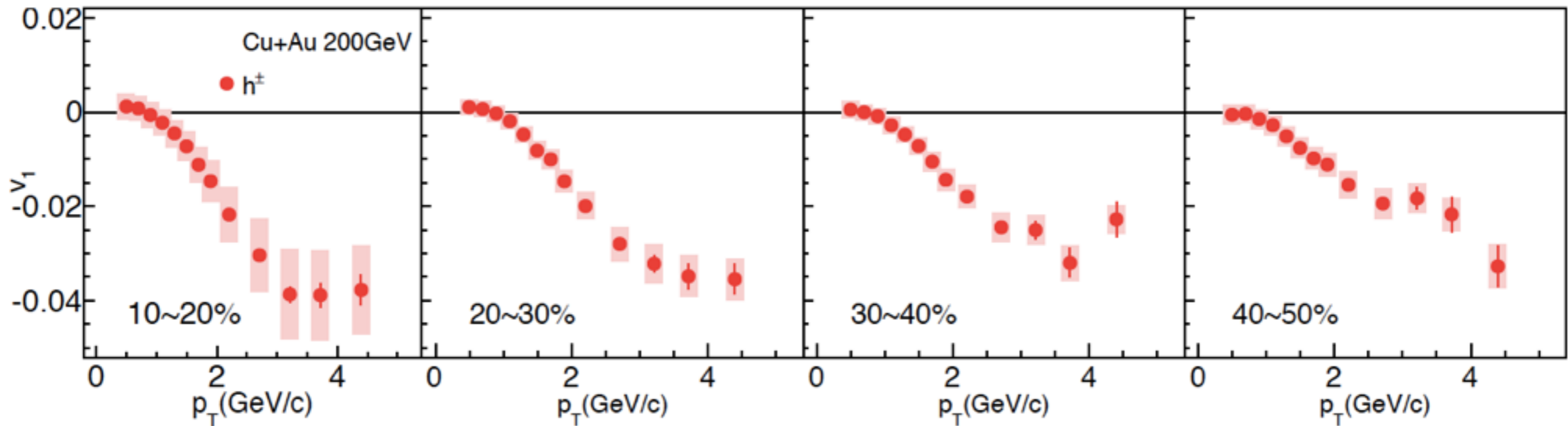
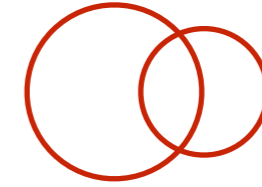
- Geant simulation
- $dN/d\eta$ distribution
- p_T distribution

Results

Discussions

- v_1, v_2, v_3 at mid- η
- Multiplicity at F/B- η
- v_2, v_3 at F/B- η

Charged hadron $v_1(p_T)$ in Cu+Au collisions



✓ v_1 at mid-rapidity is observed with respect to Au spectator for 10-50%

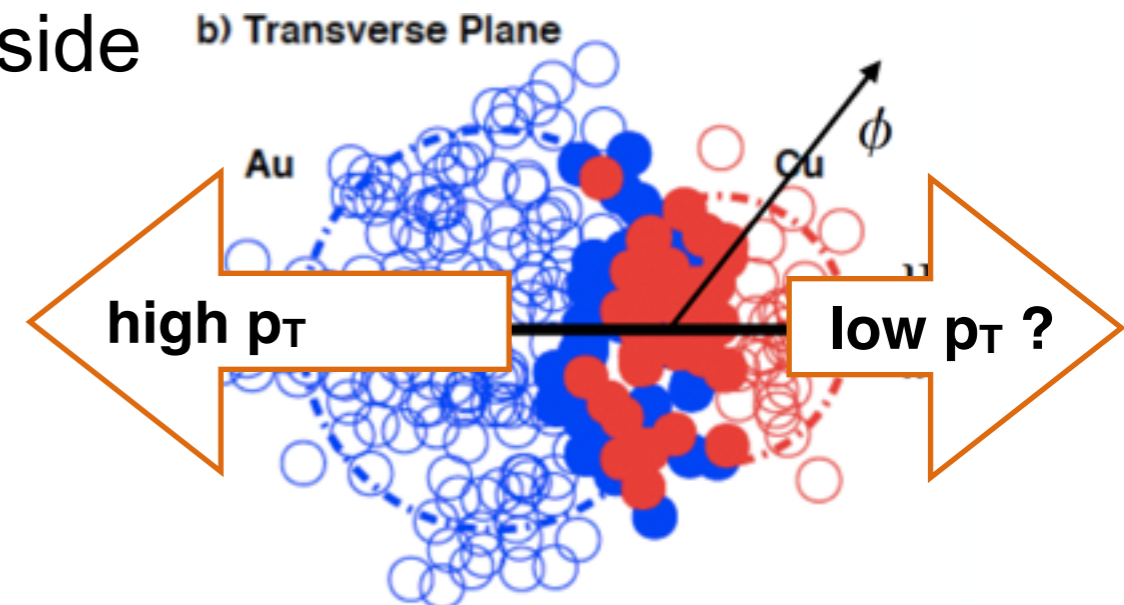
- sign of v_1 is flipped toward Cu nucleus side

✓ Negative v_1 indicates high p_T particle

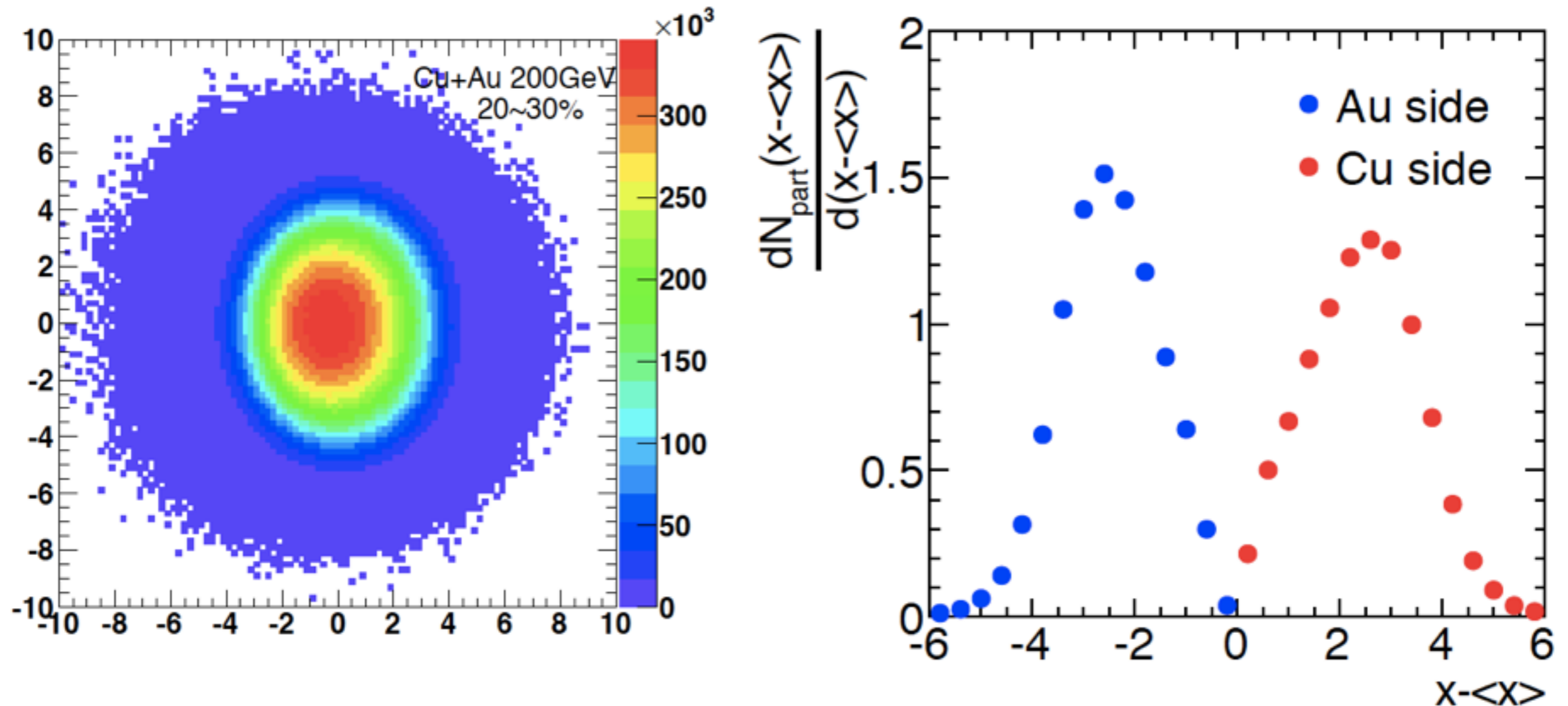
are emitted to Au side

- Magnitude decreases from central to more peripheral events

- In peripheral events, Left/Right path length becomes similar

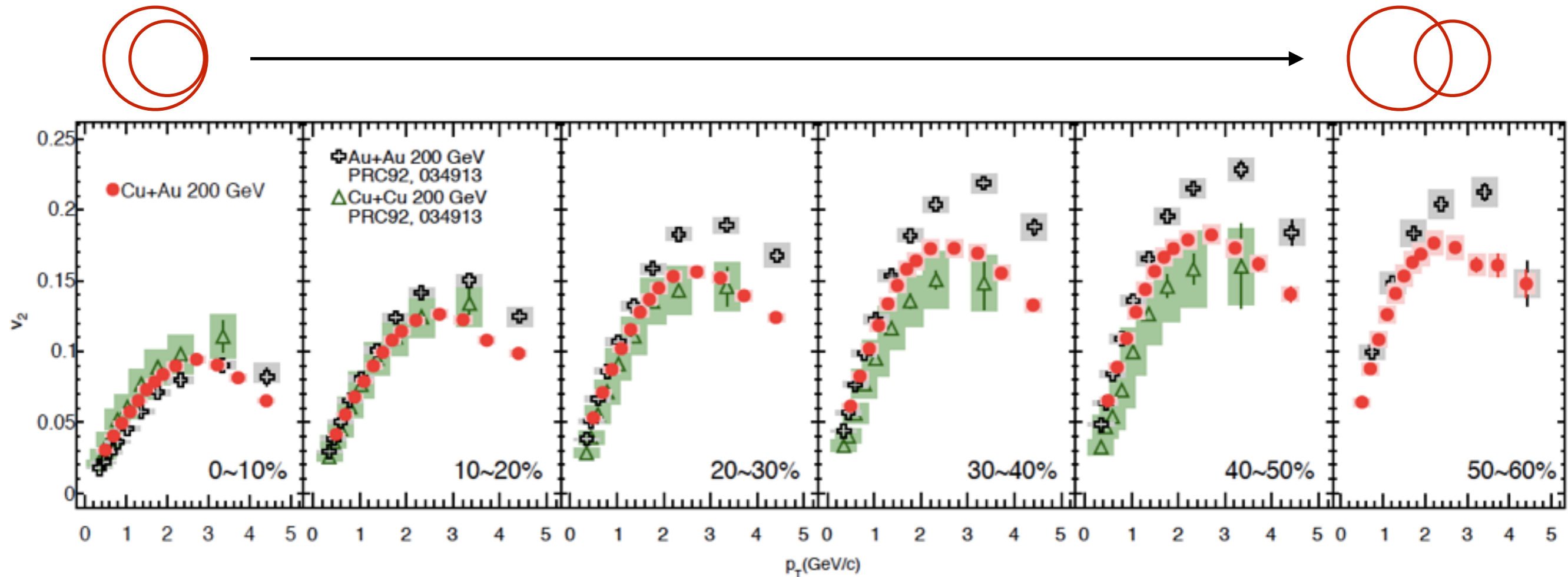


Interpretation of negative $v_1(p_T)$ at higher p_T



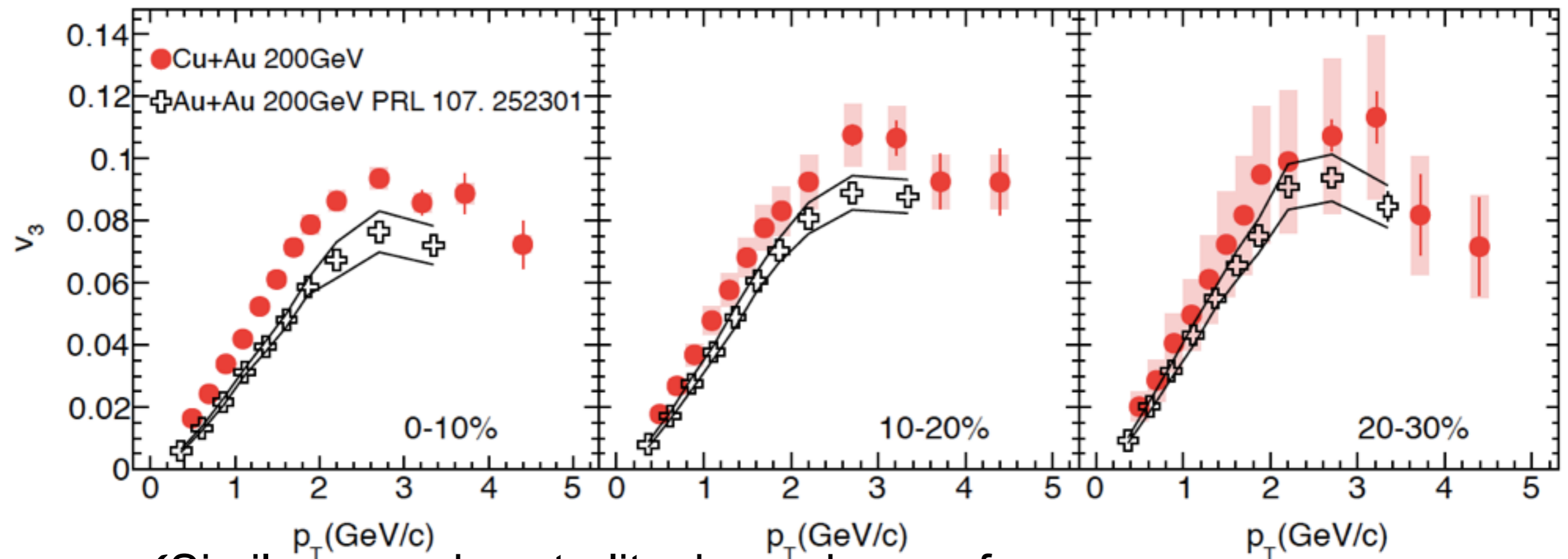
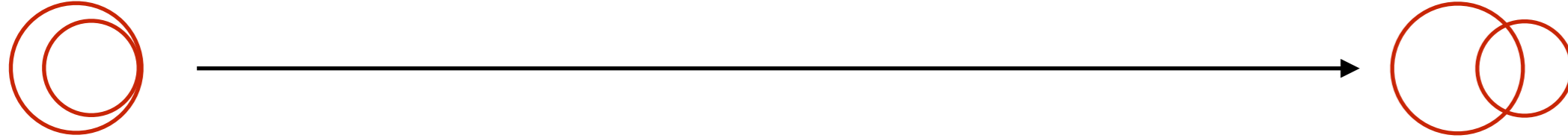
- ✓ Density gradient is larger in Au nucleus side
- ✓ Larger pressure gradient pushes particles to high p_T
 - Density gradient induce pressure gradient
 - Many high p_T particles are emitted toward Au side

Charged hadron $v_2(p_T)$ in Cu+Au collisions



- ✓ Similar p_T and centrality dependence of v_2 as seen in symmetric collisions
 - v_2 is measured with respect to Bbc
 - Strong centrality dependence, magnitude increase from central to peripheral
 - Cu+Au v_2 is between symmetric Au+Au and Cu+Cu collisions

Charged hadron $v_3(p_T)$ in Cu+Au collisions



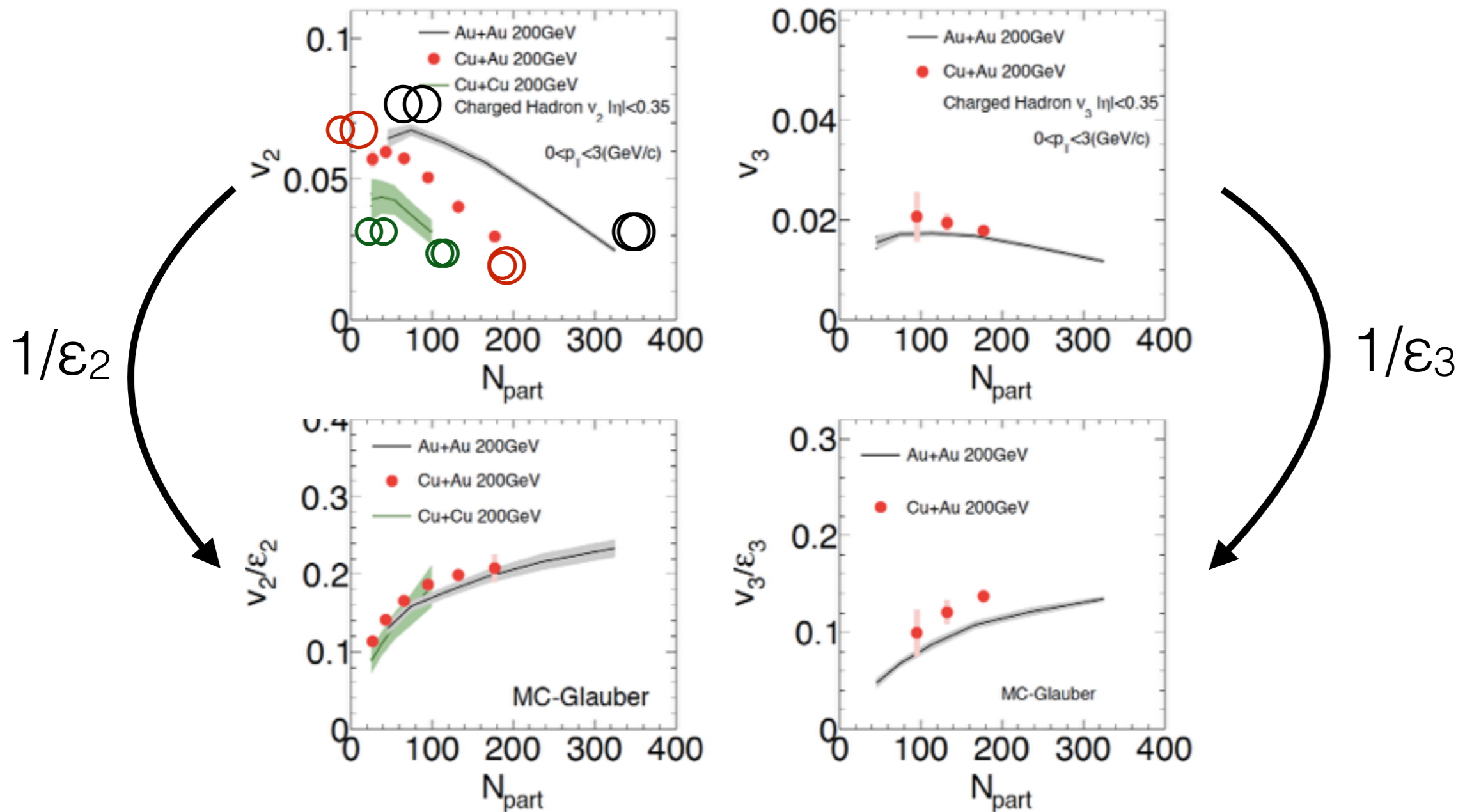
✓ Similar p_T and centrality dependence of v_3 as seen in symmetric collisions

- v_3 is measured with respect to Bbc

- Weak centrality dependence, magnitude slightly increase from central to peripheral

- Cu+Au v_3 shows larger values than Au+Au results

System size dependence of $v_n(N_{\text{part}})$



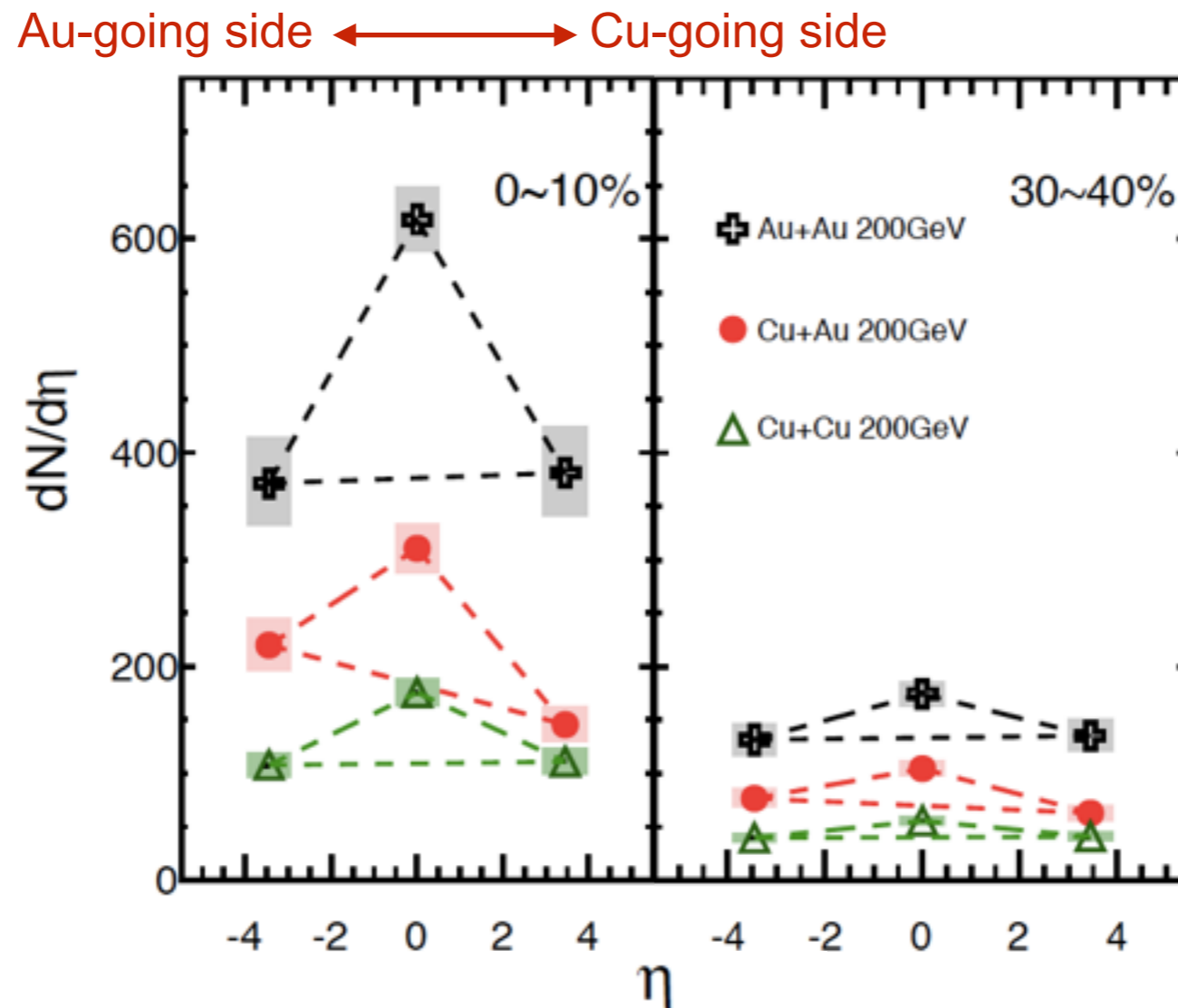
- ✓ Cu+Au v_2/ϵ_2 is consistent with Au+Au and Cu+Cu results
- ✓ Unlike v_2 , Cu+Au v_3 is consistent with Au+Au v_3
- ✓ Cu+Au v_3/ϵ_3 is not consistent with Au+Au results
 - MC-Glauber might not reproduce ϵ_3 correctly

Results

Discussions

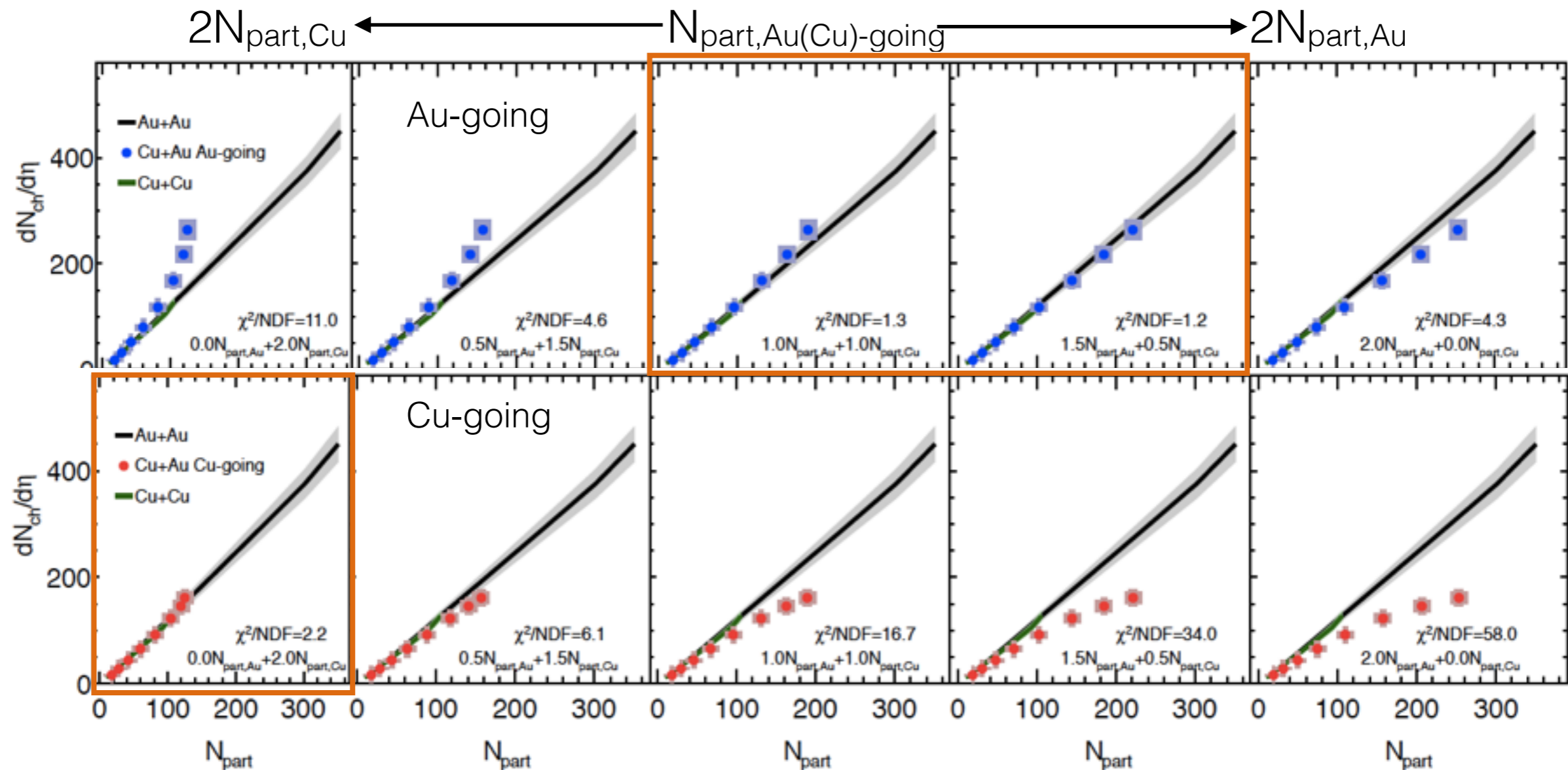
- v_1, v_2, v_3 at mid- η
- Multiplicity at F/B- η
- v_2, v_3 at F/B- η

η dependence of charged particle multiplicity



- ✓ Au-going side $dN/d\eta >$ Cu-going side $dN/d\eta$
 - Number of participants in Au $>$ Number of participants in Cu
- ✓ Larger collision system $dN/d\eta >$ smaller collision system $dN/d\eta$
 - Au+Au $>$ Cu+Au $>$ Cu+Cu

Study of relative contribution from $N_{\text{part,Au}}$ and $N_{\text{part,Cu}}$

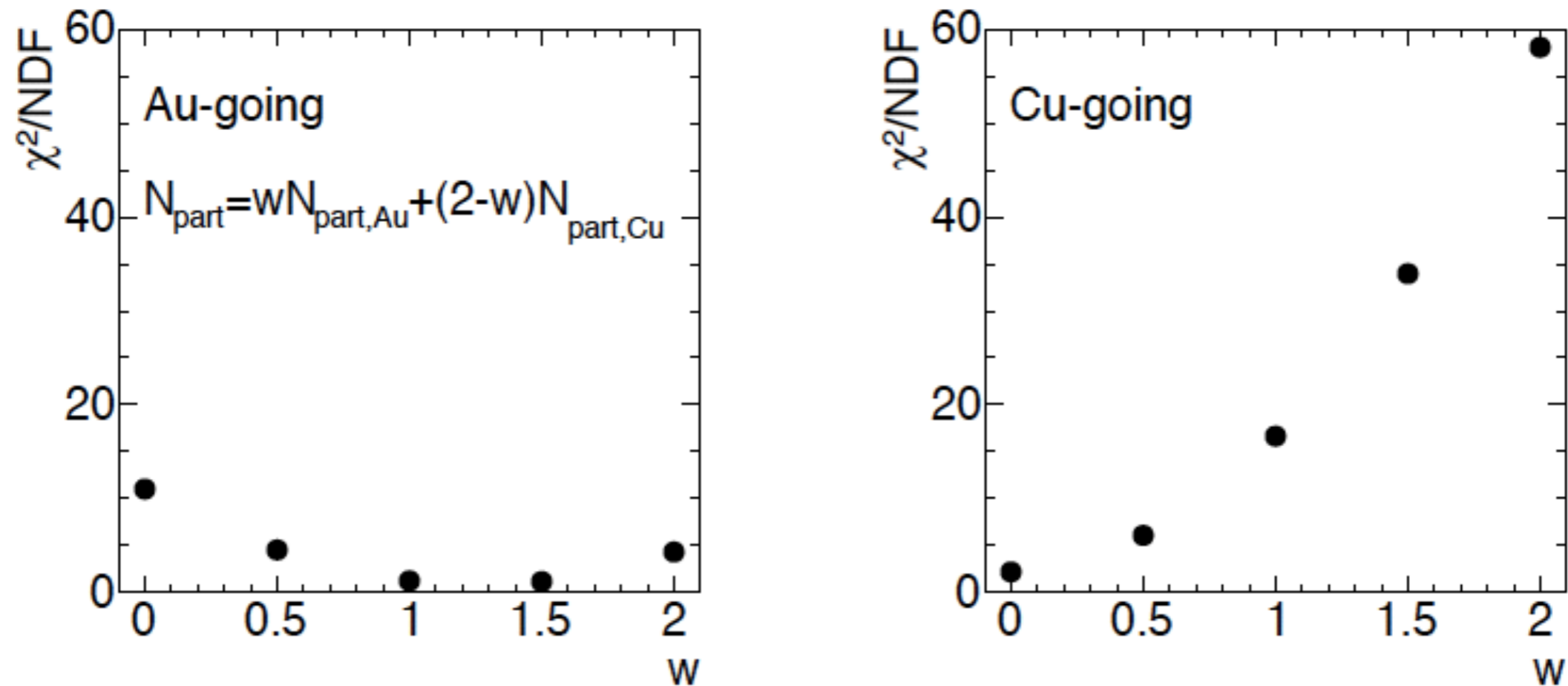


✓ Weighted N_{part} scaling for CuAu $dN/d\eta$

- $N_{\text{part,Au}}$ and $N_{\text{part,Cu}}$ are participants in Au and Cu, respectively
- $N_{\text{part,Au(Cu)-going}} = wN_{\text{part,Au}} + (2-w)N_{\text{part,Cu}}$ ($2N_{\text{part,Cu}} < N_{\text{part,Au(Cu)-going}} < 2N_{\text{part,Au}}$)

✓ Au-going side $\rightarrow N_{\text{part,Au}}$ and $N_{\text{part,Cu}}$, Cu-going side $\rightarrow N_{\text{part,Cu}}$

χ^2/NDF for the difference of $dN_{\text{ch}}/d\eta$ between Cu+Au and Au+Au



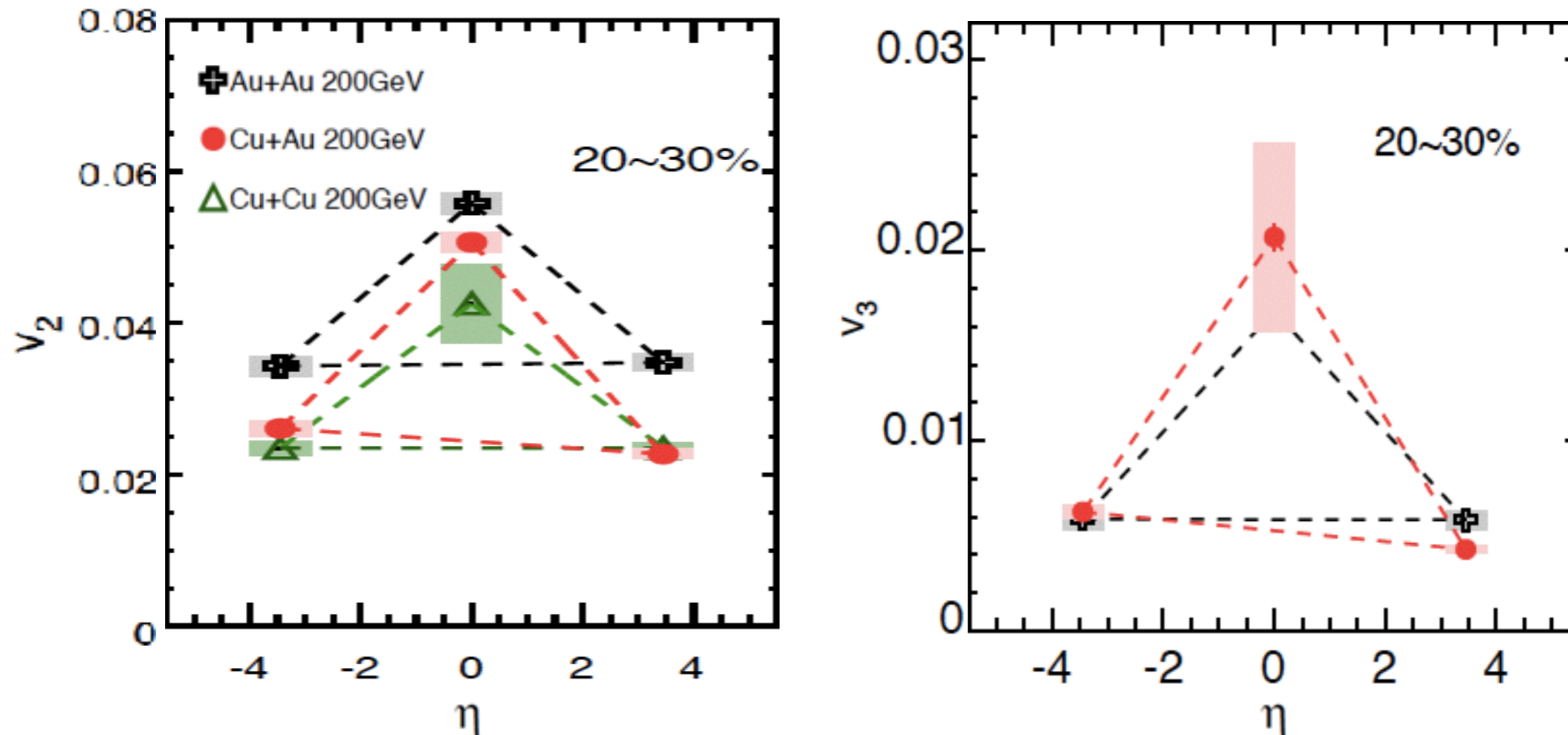
- ✓ Au-going side is determined from $N_{\text{part,Au}}$ and $N_{\text{part,Cu}}$
 - χ^2/NDF become small around $w = 1 \sim 1.5$
- ✓ Cu-going side is determined from mainly $N_{\text{part,Cu}}$
 - χ^2/NDF become small around $w = 0$

Results

Discussions

- v_1, v_2, v_3 at mid- η
- Multiplicity at F/B- η
- v_2, v_3 at F/B- η

Rapidity dependence of v_n in Cu+Au collisions



✓ In Cu+Au collisions, F/B asymmetry of v_n is observed.

- v_n is measured with respect Cnt

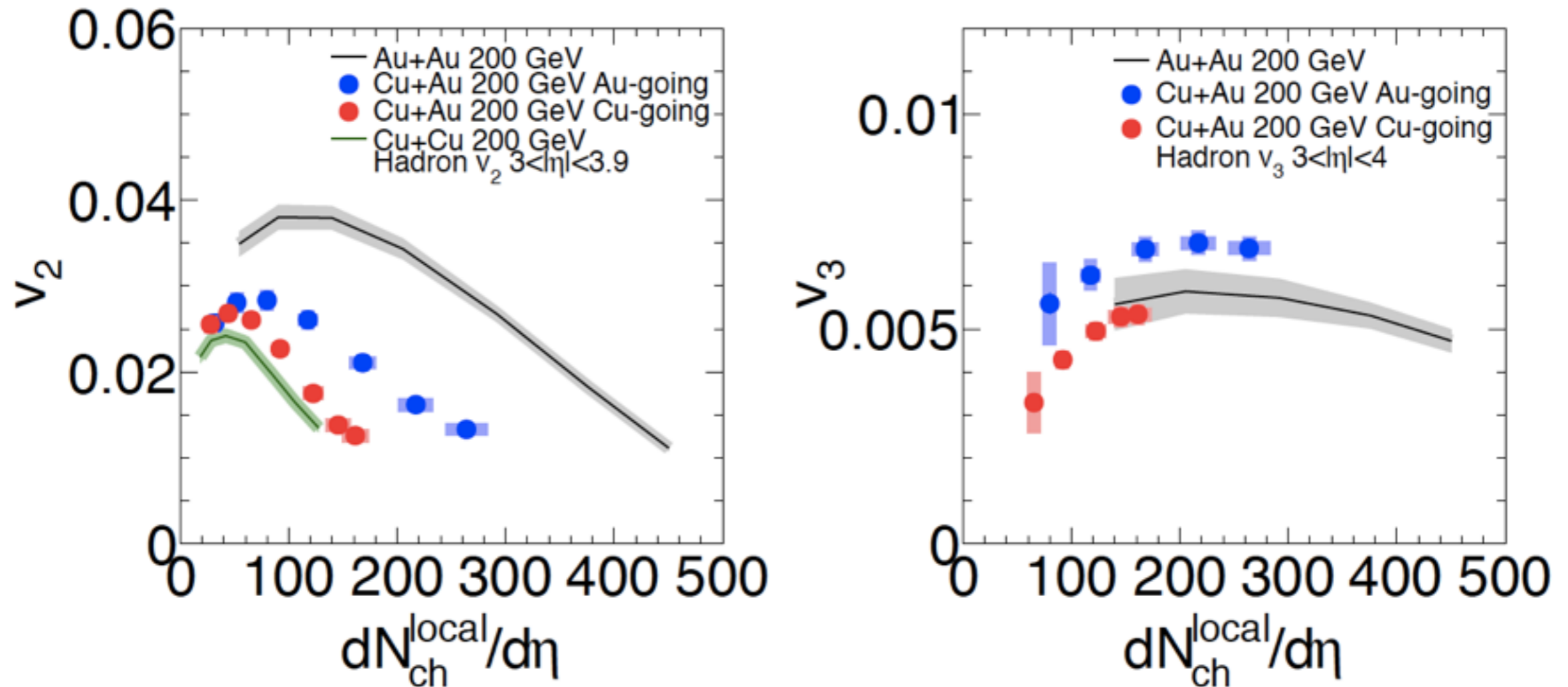
- $v_2(\text{Au-going}) > v_2(\text{Cu-going})$

- $v_3(\text{Au-going}) > v_3(\text{Cu-going})$

-> caused by different initial geometries in Au and Cu ?

✓ Unlike v_2 , Au-going v_3 in Cu+Au show similar values of Au+Au v_3

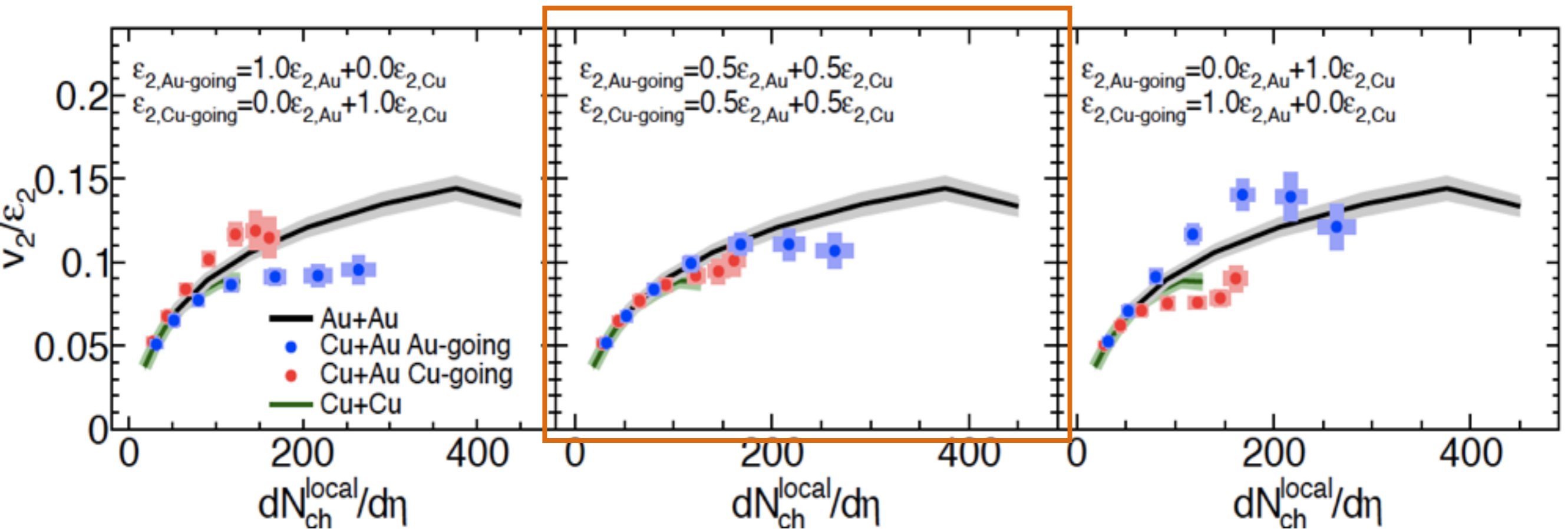
Multiplicity dependence of v_n in Cu+Au collisions



- ✓ In Cu+Au collisions, F/B asymmetry of v_n is observed.
 - plotted as a measured $dN/d\eta$ at F/B-rapidity
 - $v_2(\text{Au-going}) > v_2(\text{Cu-going})$
 - $v_3(\text{Au-going}) > v_3(\text{Cu-going})$
 - > caused by different initial geometries in Au and Cu ?

Study of ε_2 in Cu+Au collisions at F/B-rapidity

$$\begin{array}{l} \varepsilon_{2,Au} \longleftarrow \varepsilon_{2,Au\text{-going}} \longrightarrow \varepsilon_{2,Cu} \\ \varepsilon_{2,Cu} \longleftarrow \varepsilon_{2,Cu\text{-going}} \longrightarrow \varepsilon_{2,Au} \end{array}$$



✓ Weighted ε_2 scaling of v_2 ($dN/d\eta$) at ($3 < |\eta| < 3.9$)

- $\varepsilon_{2,Au}$ and $\varepsilon_{2,Cu}$ are given by Au and Cu, respectively

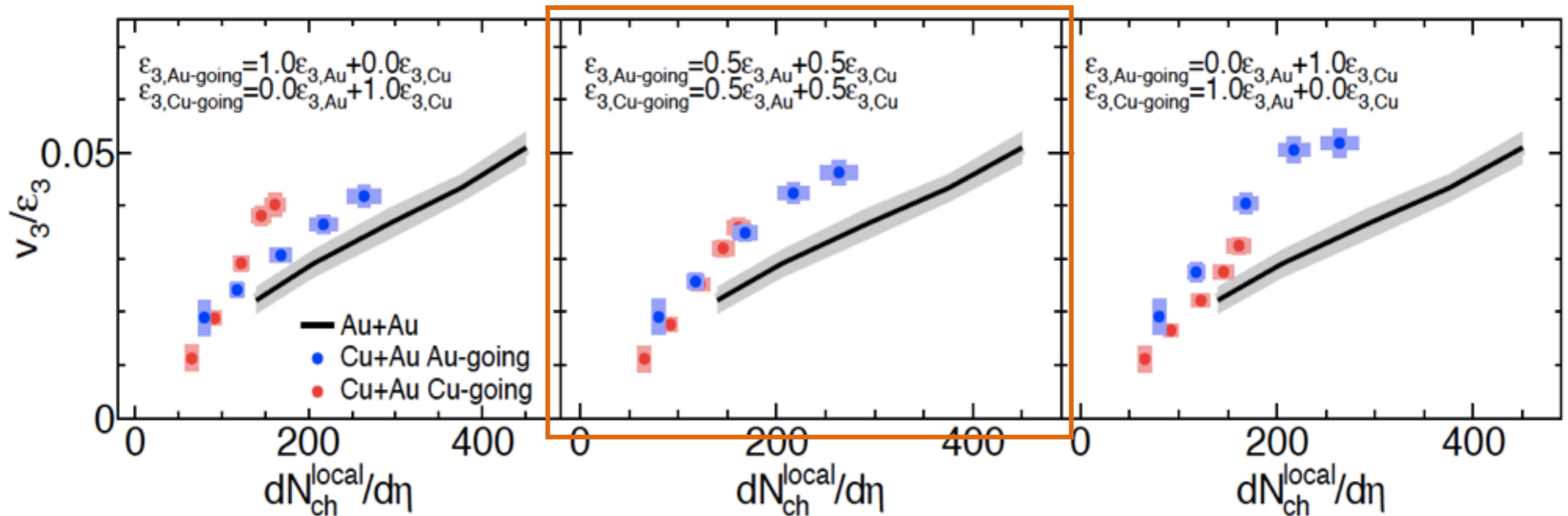
- $\varepsilon_{2,Au(Cu)\text{-going}} = W_{Au(Cu)\text{-going}}\varepsilon_{2,Au} + (1 - W_{Au(Cu)\text{-going}})\varepsilon_{2,Cu}$

($\varepsilon_{2,Cu} < \varepsilon_{2,Au(Cu)\text{-going}} < \varepsilon_{2,Au}$)

➡ common $\varepsilon_{2,Au\text{-going}} = \varepsilon_{2,Cu\text{-going}}$ is favored

Study of ε_3 in Cu+Au collisions at F/B-rapidity

$$\begin{array}{l} \varepsilon_{3,Au} \longleftarrow \varepsilon_{3,Au\text{-going}} \longrightarrow \varepsilon_{3,Cu} \\ \varepsilon_{3,Cu} \longleftarrow \varepsilon_{3,Cu\text{-going}} \longrightarrow \varepsilon_{3,Au} \end{array}$$



Weighted ε_3 scaling of v_3 ($dN/d\eta$) at ($3 < |\eta| < 3.9$)

- $\varepsilon_{3,Au}$ and $\varepsilon_{3,Cu}$ are given by Au and Cu, respectively

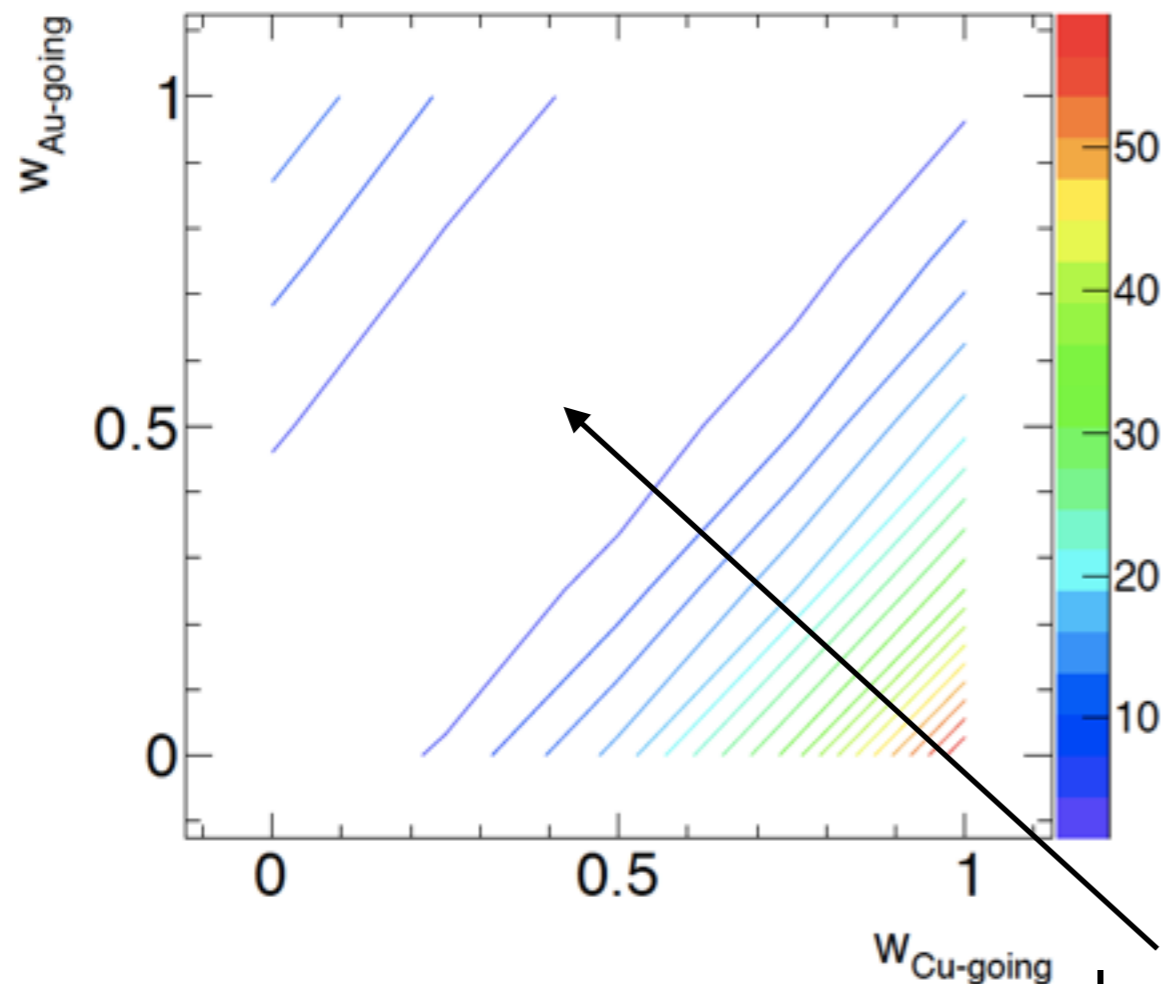
- $\rightarrow \varepsilon_{3,Au(Cu)\text{-going}} = W_{Au(Cu)\text{-going}}\varepsilon_{3,Au} + (1 - W_{Au(Cu)\text{-going}})\varepsilon_{3,Cu}$ ($\varepsilon_{3,Cu} < \varepsilon_{3,Au(Cu)\text{-going}} < \varepsilon_{3,Au}$)

✓ Like mid-rapidity v_3 , MC-Glauber can not describe system size dependence?

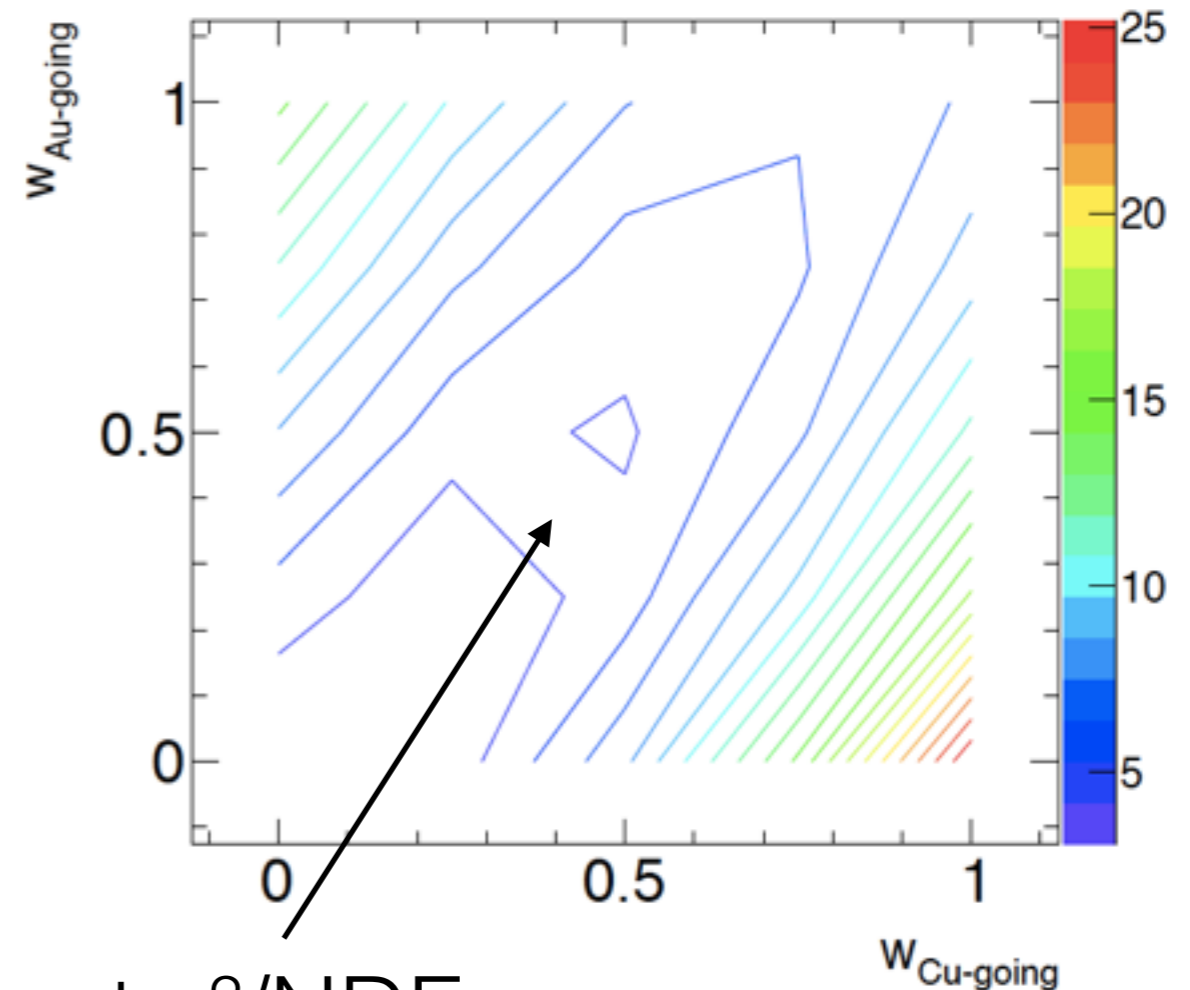
✓ common $\varepsilon_{3,Au\text{-going}} = \varepsilon_{3,Cu\text{-going}}$ is favored

χ^2/NDF for the difference of v_n/ϵ_n between Au-going and Cu-going

2nd order harmonics



3rd order harmonics



lowest χ^2/NDF

✓ χ^2/NDF for $W_{\text{Au-going}}$ VS $W_{\text{Cu-going}}$

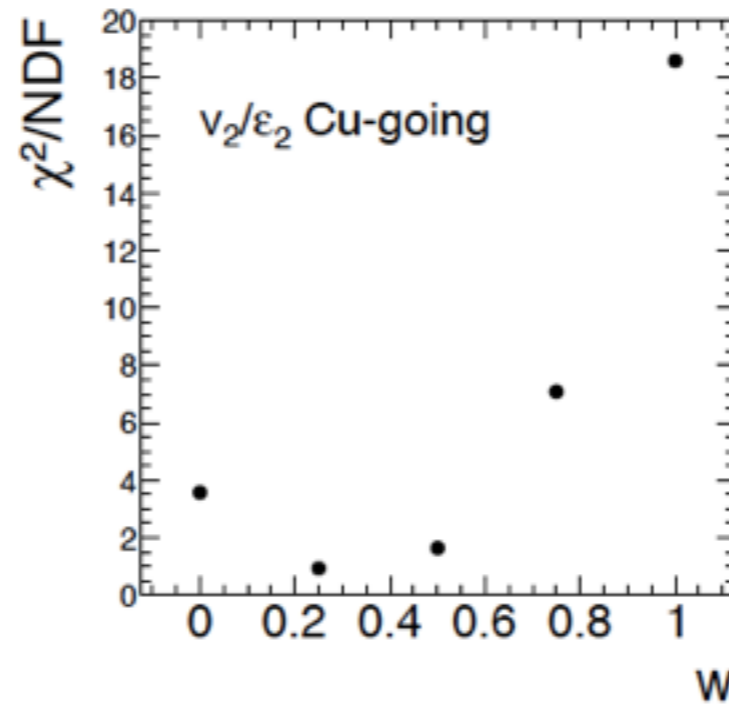
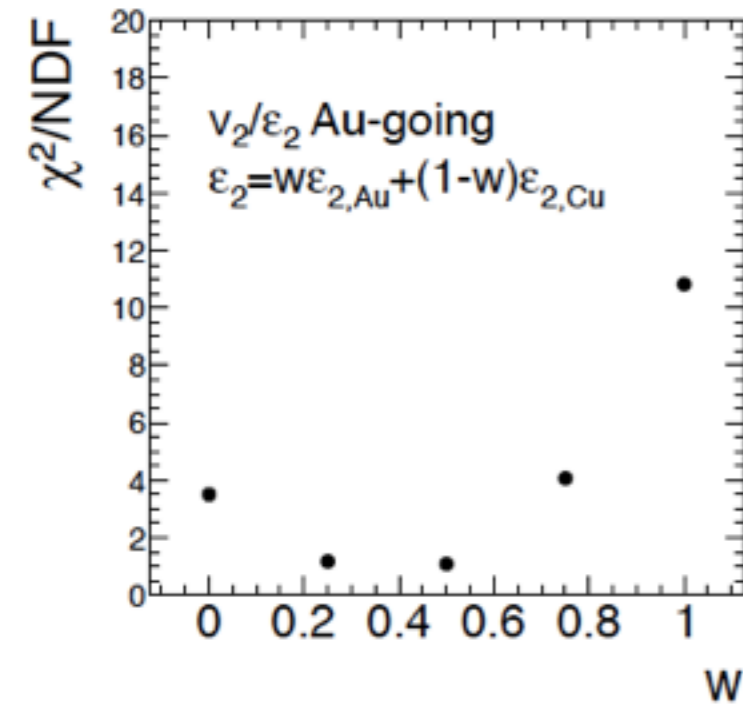
$$-\epsilon_{n,\text{Au}(\text{Cu})\text{-going}} = W_{\text{Au}(\text{Cu})\text{-going}}\epsilon_{n,\text{Au}} + (1 - W_{\text{Au}(\text{Cu})\text{-going}})\epsilon_{n,\text{Cu}}$$

✓ Common $\epsilon_{n,\text{Au-going}} \sim \epsilon_{n,\text{Cu-going}}$ is favored by v_2 and v_3

$$-W_{\text{Au-going}} \sim W_{\text{Cu-going}}$$

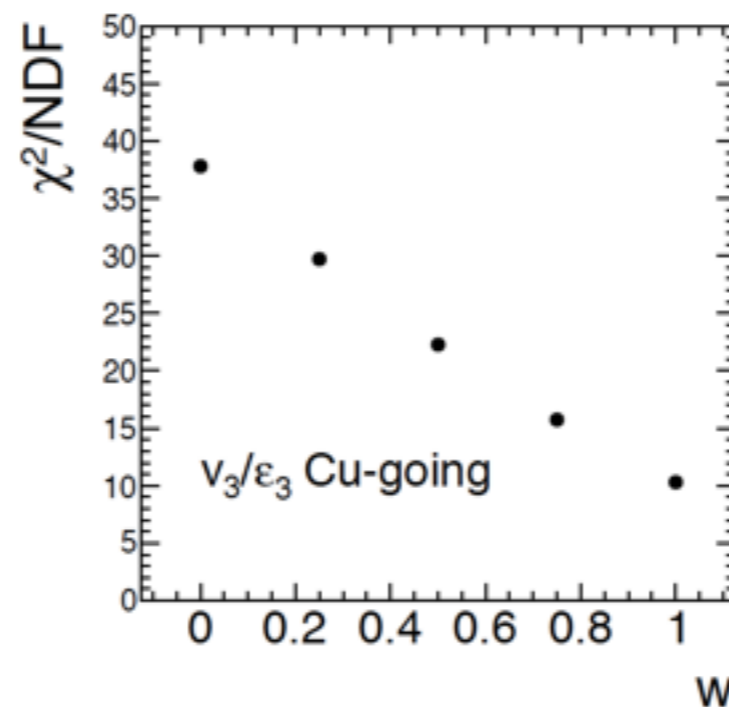
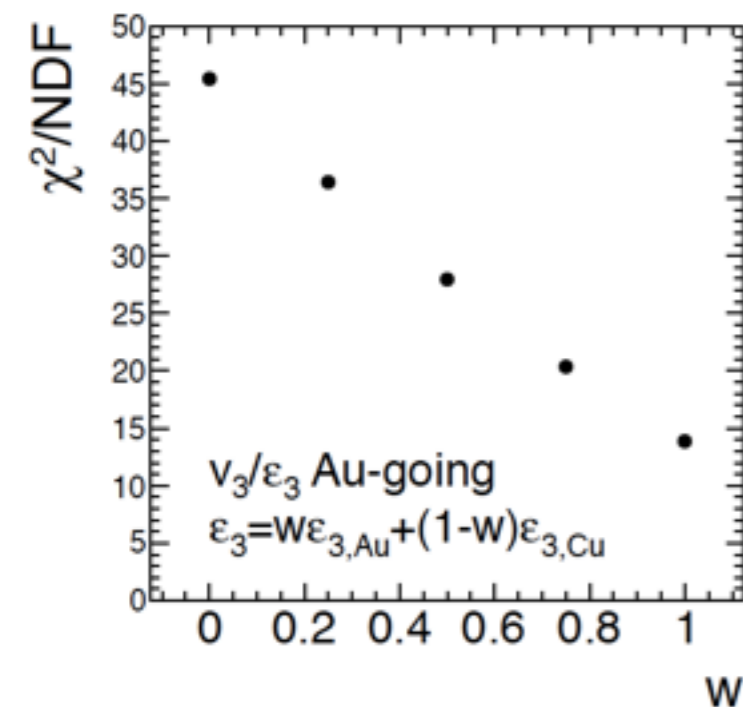
χ^2/NDF for the difference of v_n/ε_n between Cu+Au and Au+Au

2nd order harmonics



- ✓ $\varepsilon_{2,\text{Au-going}} \sim \varepsilon_{2,\text{Cu-going}}$
- $\varepsilon_{2,\text{Au}}$ and $\varepsilon_{2,\text{Cu}}$ are similar contribution
- Both χ^2/NDF become small around $w = 0.2 \sim 0.5$

3rd order harmonics



- ✓ Glauber does not describe ε_3
- Compared to v_2/ε_2 , χ^2/NDF is large
- Both χ^2/NDF become small around $w = 1$

Summary 1 : Mid-rapidity

✓ First order flow harmonic

- High p_T particles are emitted to Au side
- Magnitude decrease from central to peripheral
- Larger density gradient in Au nucleus side push particle to high p_T

✓ Second order flow harmonics

- Similar centrality and p_T dependence as seen in symmetric collisions
- Glauber model well described initial geometry

✓ Third order flow harmonics

- Similar centrality and p_T dependence as seen in symmetric collisions
- Glauber model is not favored by the third order initial geometry

Summary 2 : Forward/Backward rapidity

✓Charged particle multiplicity

- Au-going side is higher than Cu-going side
- Au-going side is determined by both of $N_{\text{part,Au}}$ and $N_{\text{part,Cu}}$
- Cu-going side is determined by mainly $N_{\text{part,Cu}}$

✓Second order flow harmonics

- Au-going side is higher than Cu-going side for mid central
- Au-going side is close to Cu-going side for central and peripheral
- Au-going and Cu-going side are scaled well by common eccentricity

✓Third order flow harmonics

- Au-going side is higher than Cu-going side for central and mid central
- Like v_2 Au-going and Cu-going side are scaled well by common eccentricity
- Like mid-rapidity v_3 , Glauber model does not describe initial geometry in Au+Au and Cu+Au.

Conclusion

By studying azimuthal anisotropy and particle multiplicity in Cu+Au collisions,

✓ Initial geometry

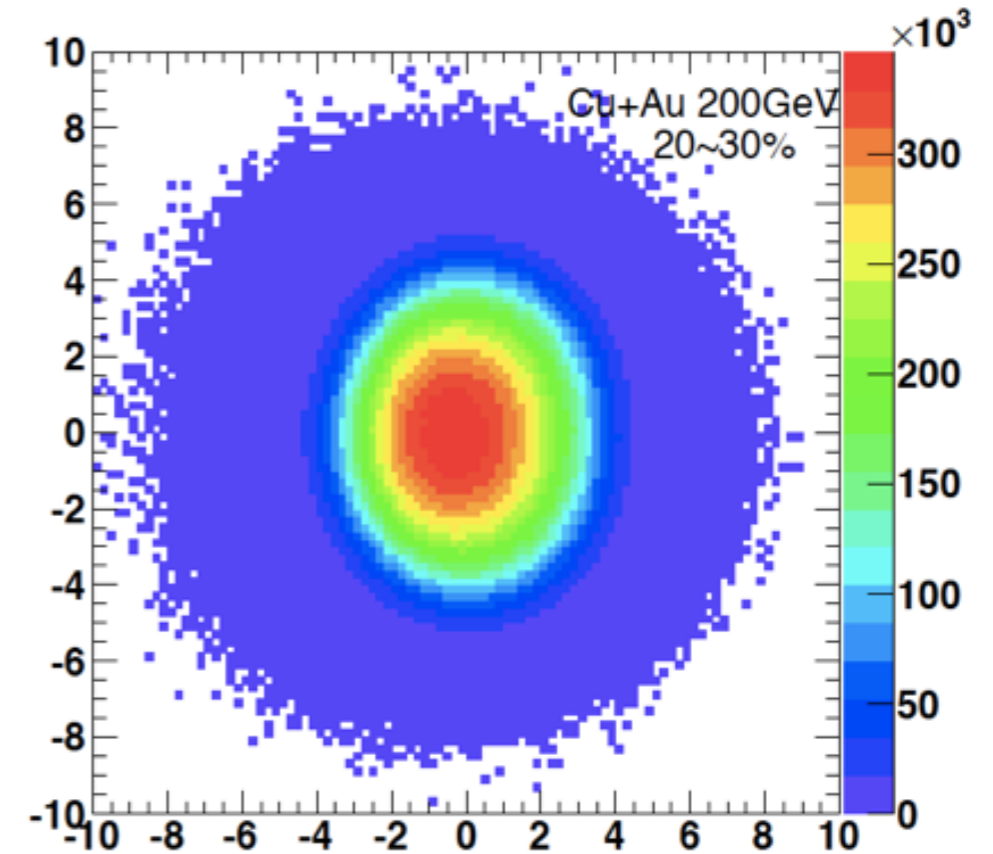
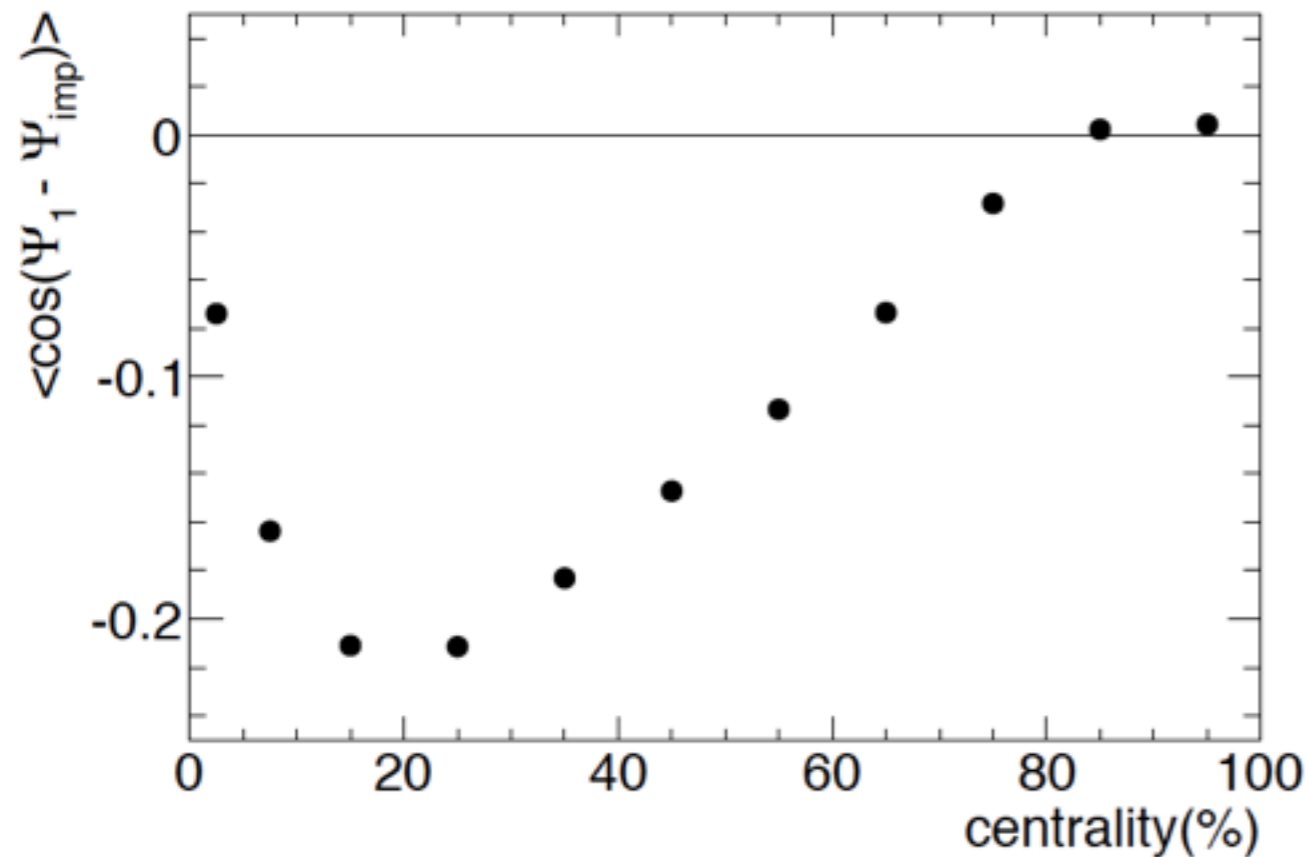
- Left / Right asymmetry in transverse direction
- Initial geometry at Forward/Backward is common

✓ Initial energy density

- Au-going side is determined by both of $N_{\text{part,Au}}$ and $N_{\text{part,Cu}}$
- Cu-going side is determined by mainly $N_{\text{part,Cu}}$

Back Up

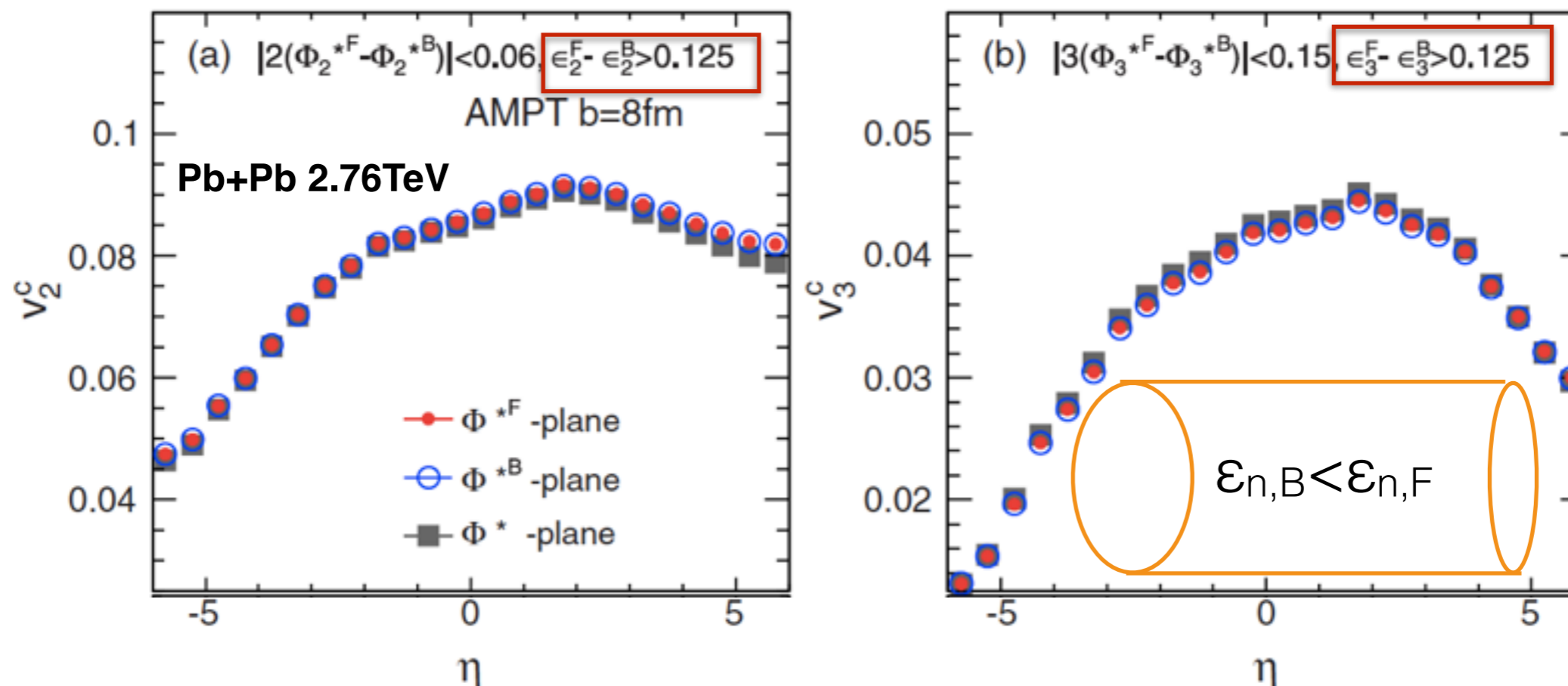
Interpretation of negative $v_1(p_T)$ at higher p_T



✓ Density gradient is larger in Au nucleus side

Rapidity dependence of initial condition

PhysRevC.90.034915



✓ initial geometry has been considered to be

rapidity independent

✓ Initial conditions on target and projectile nuclei are not same event

$$\epsilon_n(+\eta) > \epsilon_n(-\eta)$$



$$v_n(+\eta) > v_n(-\eta)$$

✓ Initial geometry has strong rapidity dependence



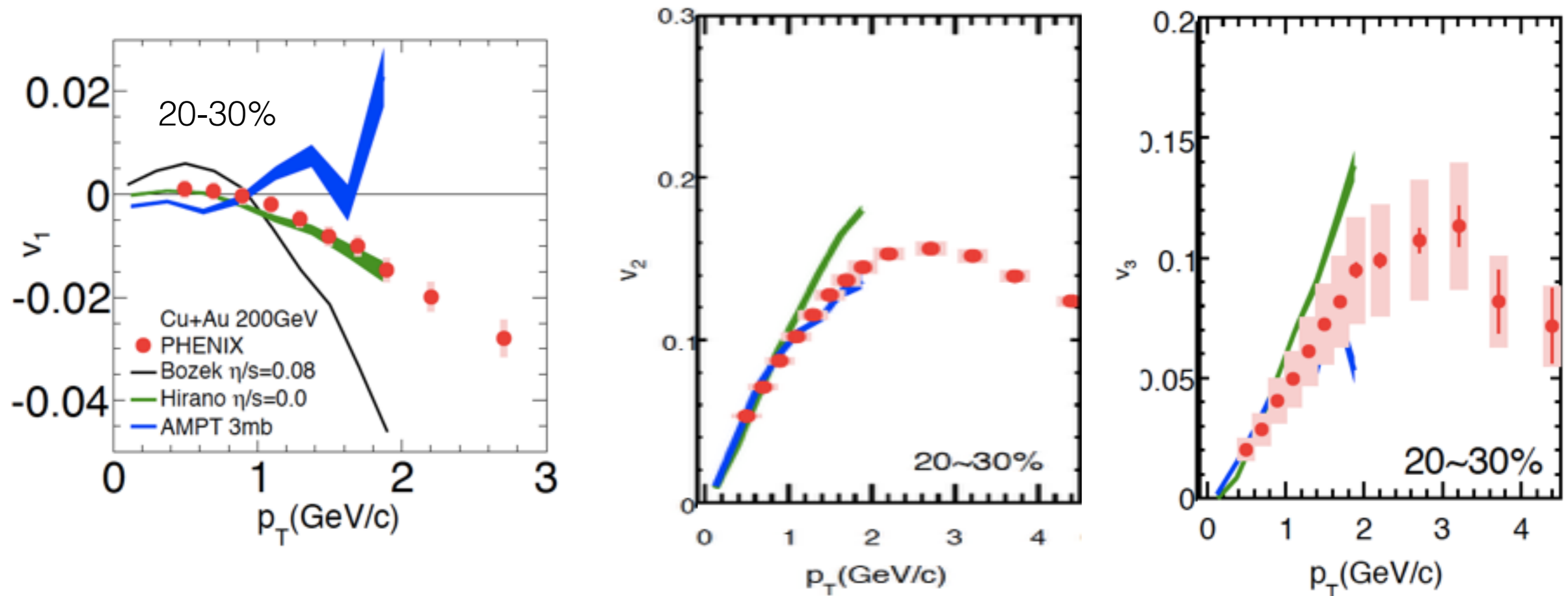
$$\epsilon_n(\eta) = \alpha\epsilon_n(+\eta) + \beta\epsilon_n(-\eta)$$

Results

Discussions

- v_1, v_2, v_3 at mid- η
- v_2, v_3 at F/B- η
- Initial condition study
- **v_1, v_2, v_3 theory comparison**

Parton cascade and hydro $v_n(p_T)$

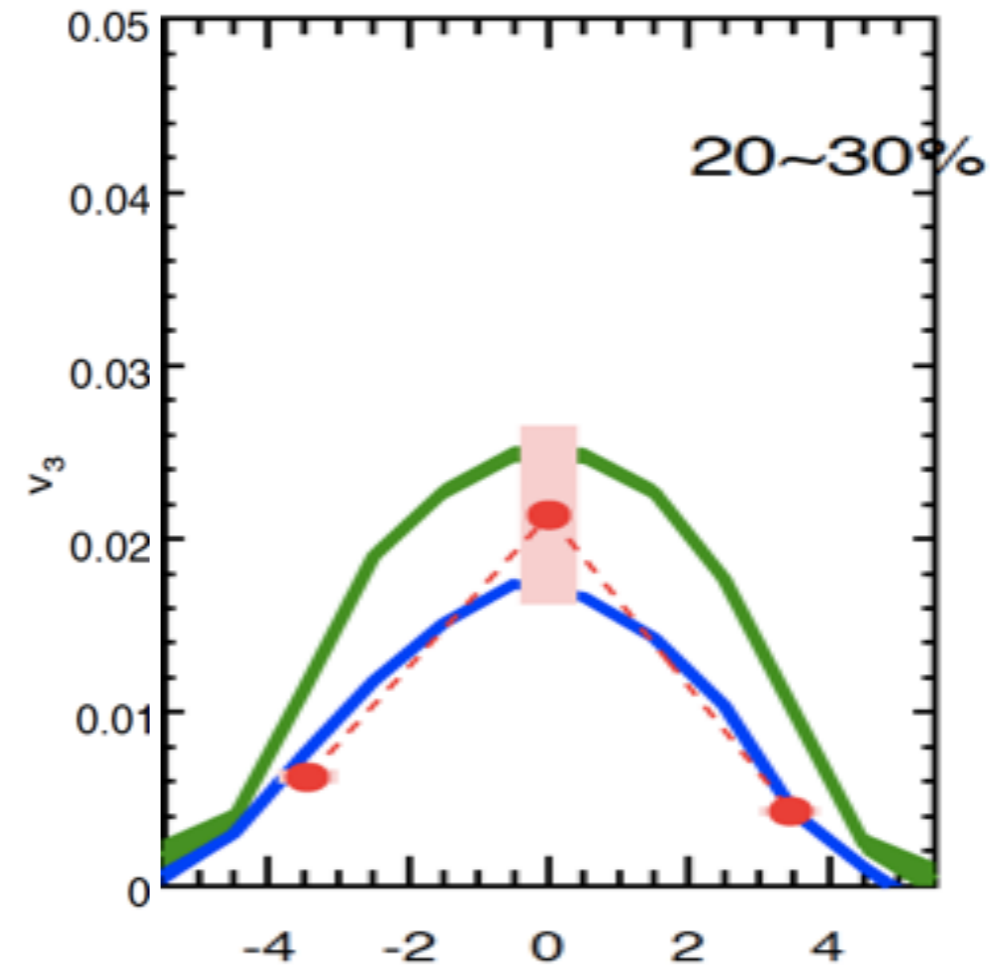
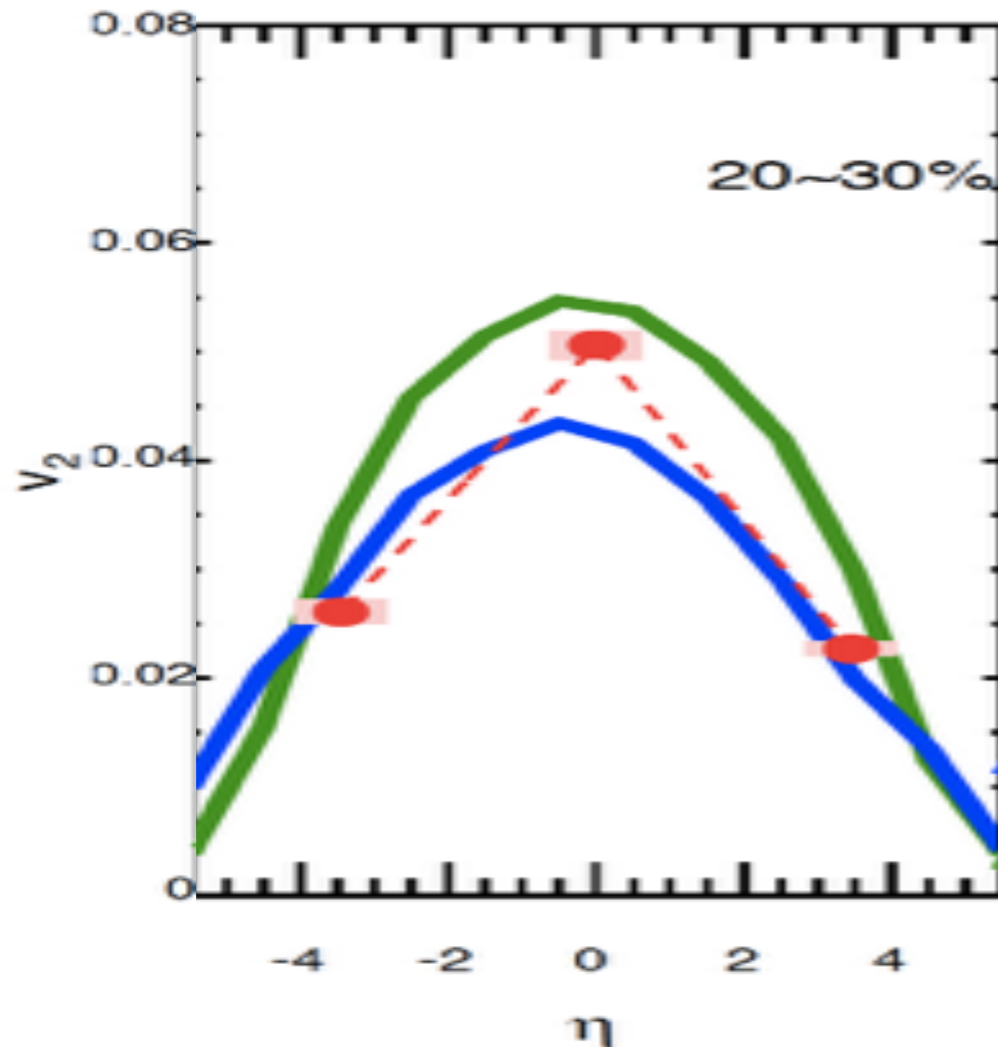


- Hydro(Bozek):Glauber + hydro
- Hydro(Hirano):Glauber + hydro + hadron cascade
- AMPT :Glauber + parton cascade + hadron cascade

✓ Hydrodynamic reproduce v_n

✓ AMPT model well reproduce v_2 and v_3 , but shows opposite sign of v_1

Parton cascade and hydro $v_n(\eta)$



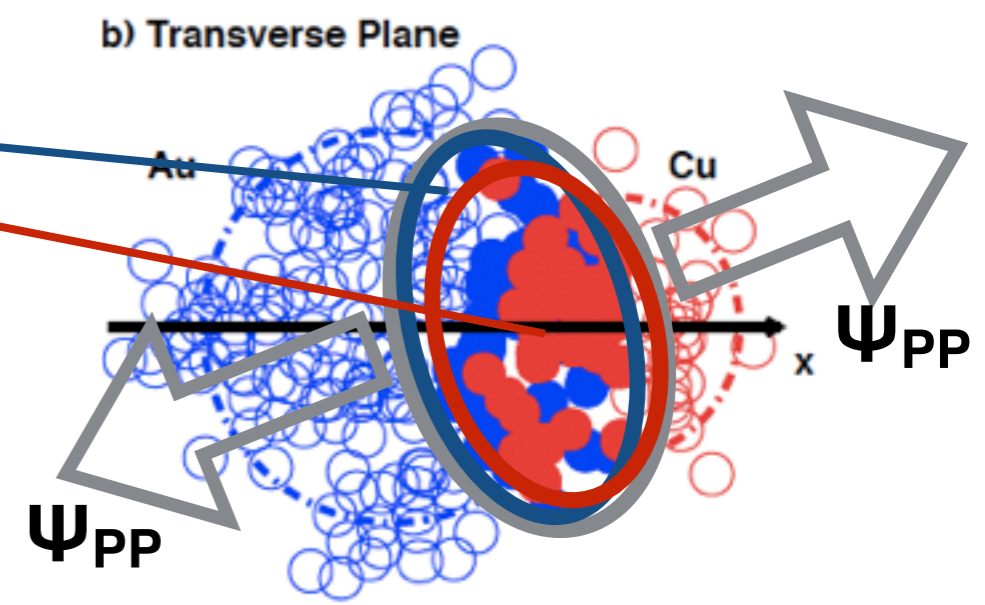
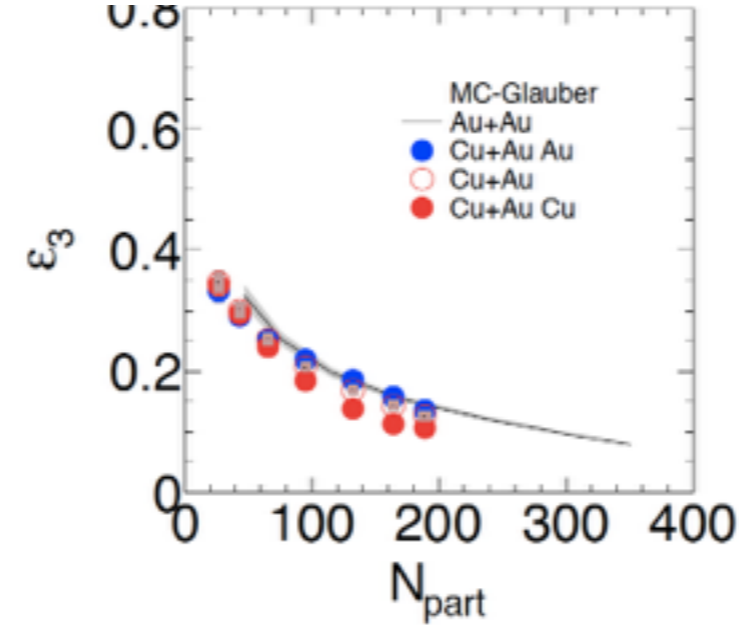
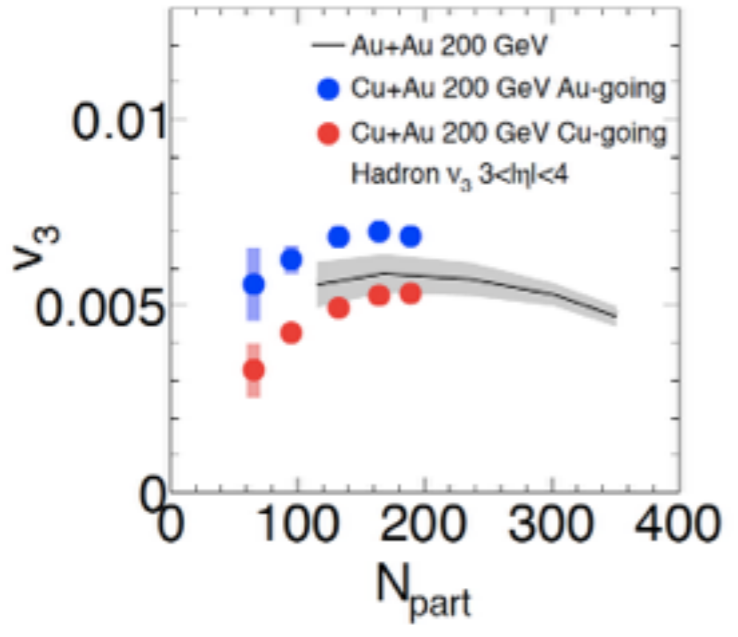
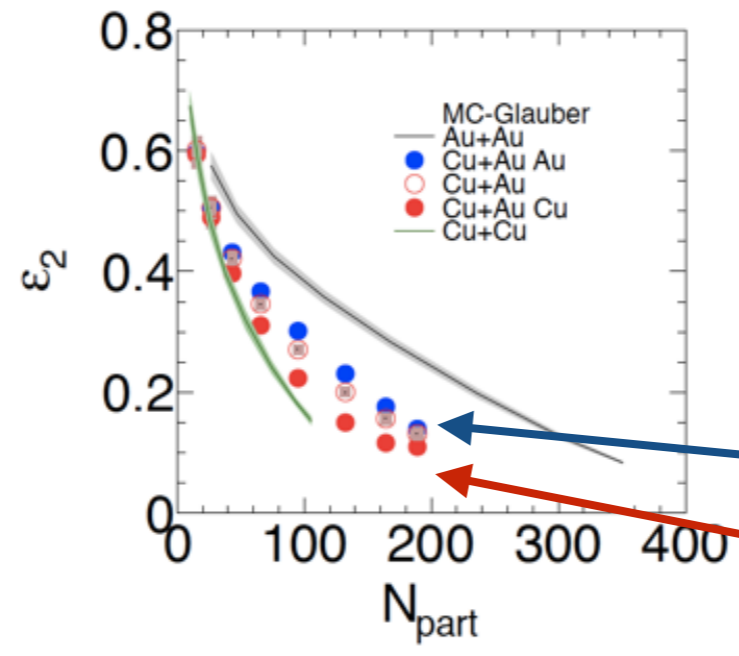
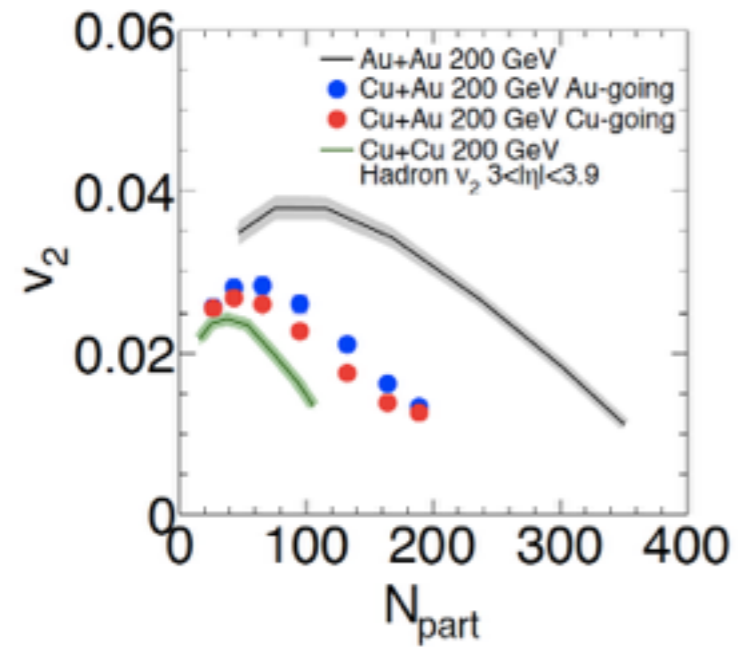
- ✓ AMPT and Hydro predict the magnitude of v_2 at F/B rapidity well
- ✓ AMPT reproduce the magnitude of v_3 at F/B rapidity well
- ✓ Hydro overestimate the magnitude of v_3 at F/B rapidity
 - Hydro: Smooth longitudinal density+hydro
 - AMPT: Fluctuated longitudinal density+parton cascade

Results

Discussions

- v_1, v_2, v_3 at mid- η
- v_2, v_3 at large- η
- **Initial condition study**
- v_1, v_2, v_3 theory comparison

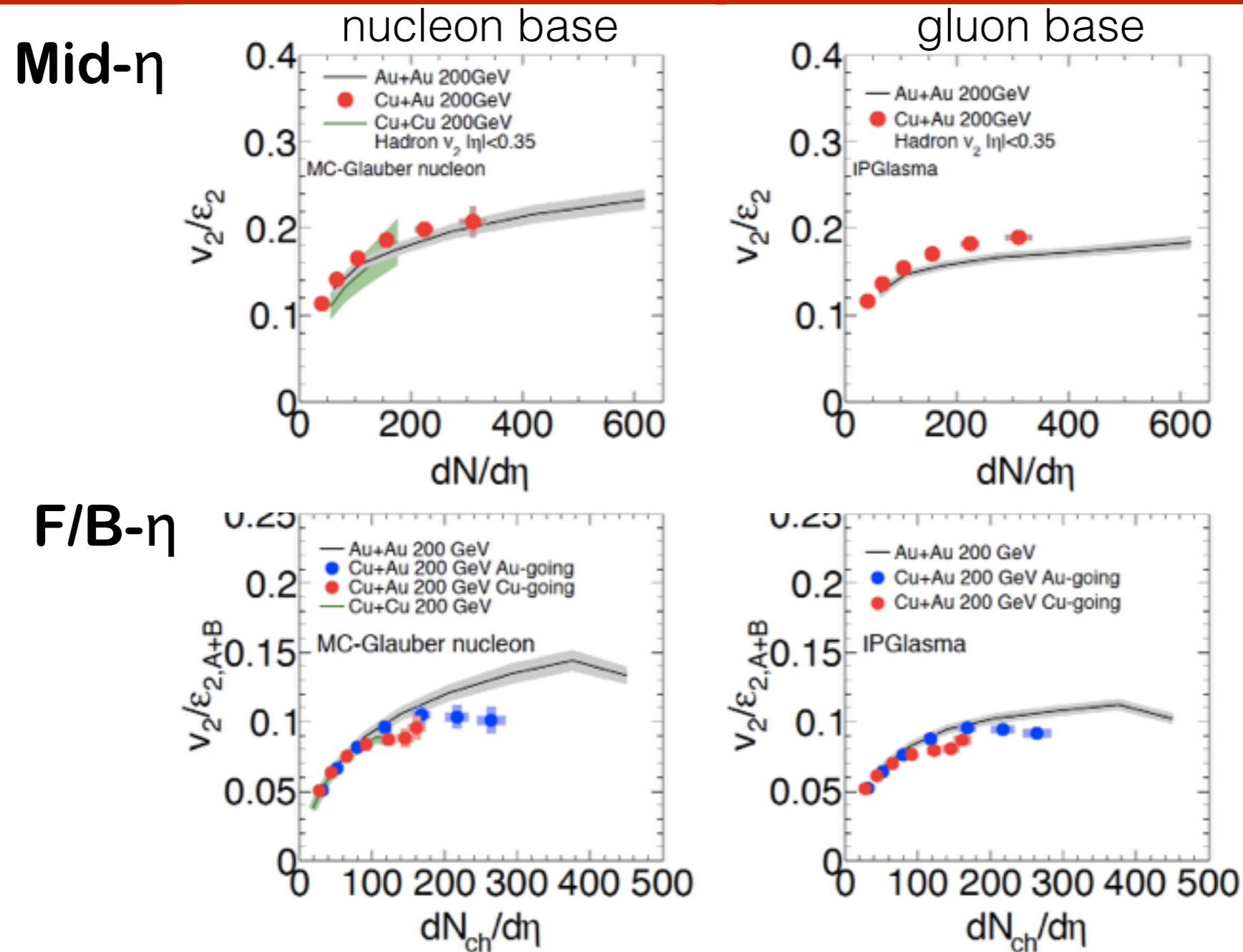
System size dependence of $v_n(N_{part})$ at F/B rapidity



✓ F/B asymmetry of v_2 is consistent that of ϵ_2
 $-\epsilon_{n,Au}$ and $\epsilon_{n,Cu}$ are estimated from Au and Cu participants separately

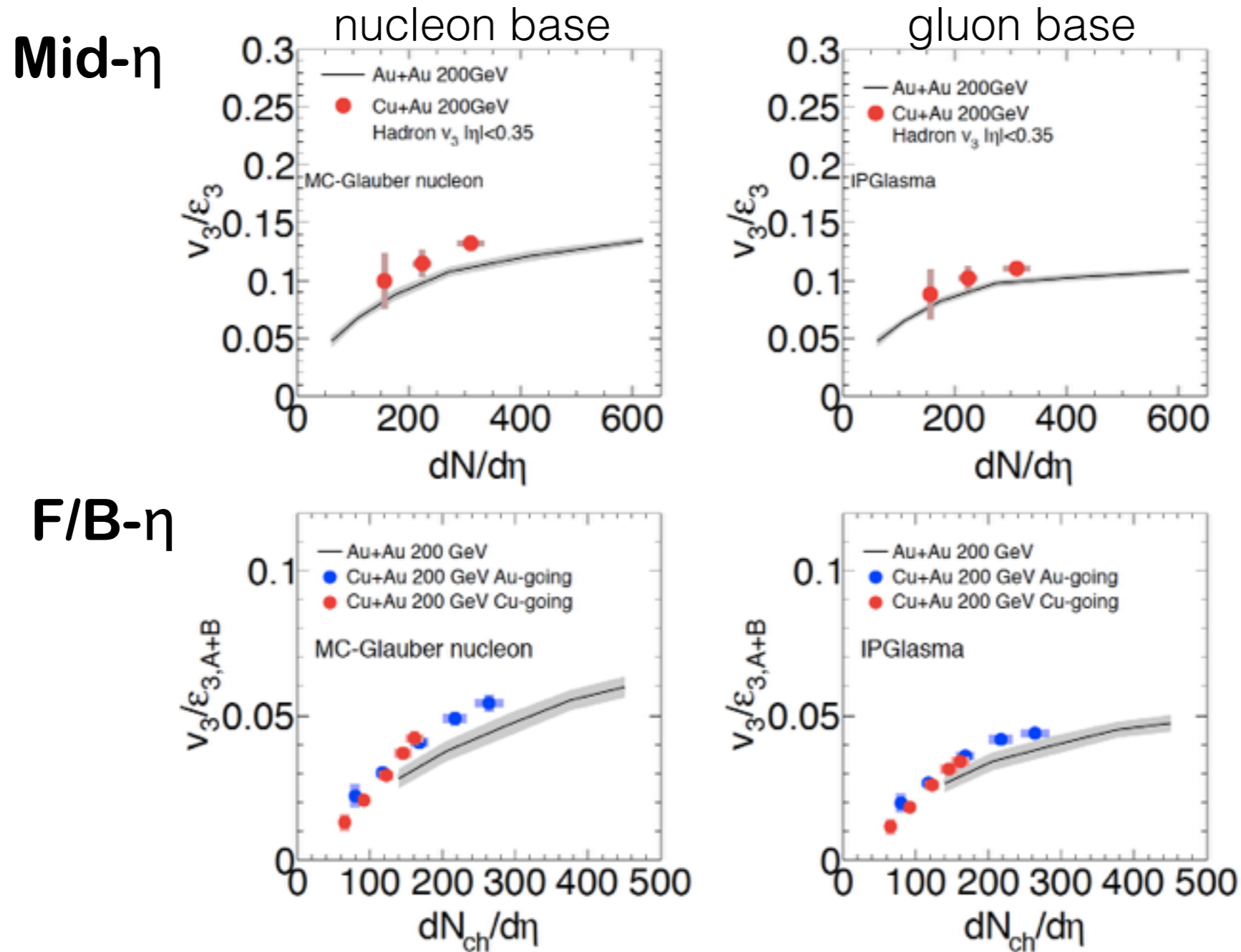
$\epsilon_{n,Au} > \epsilon_{n,Cu} \rightarrow v_{n,Au} > v_{n,Cu} ?$

v_2/ε_2 scaling with Glauber and IPGlasma



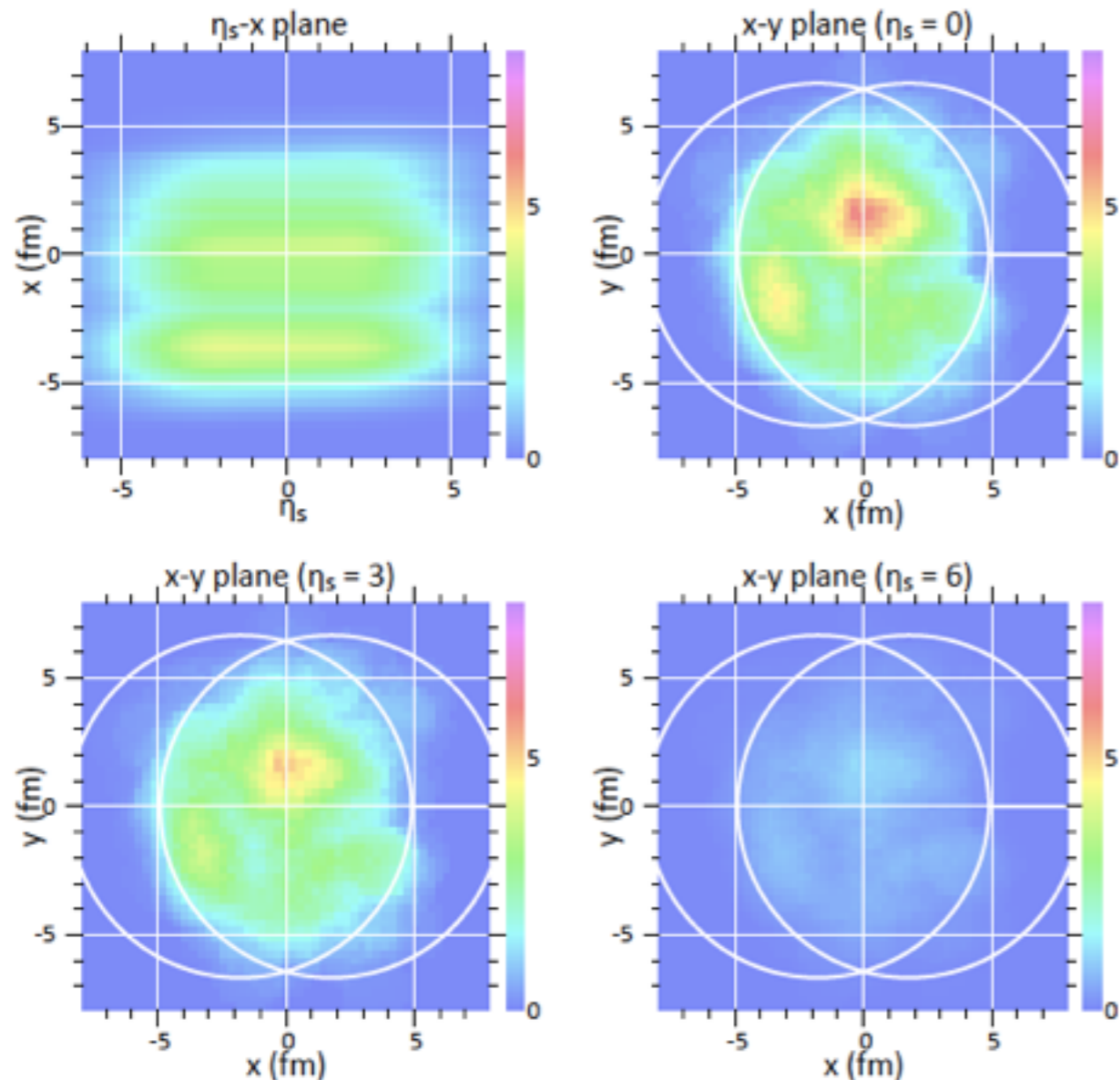
- ✓ At-mid η , the v_2 scaled with nucleon base model are consistent among three collision systems
- ✓ At-F/B η , the v_2/ε_2 with gluon base model in Cu+Au is closer to that in Au+Au

v_3/ϵ_3 scaling with Glauber and IPGlasma

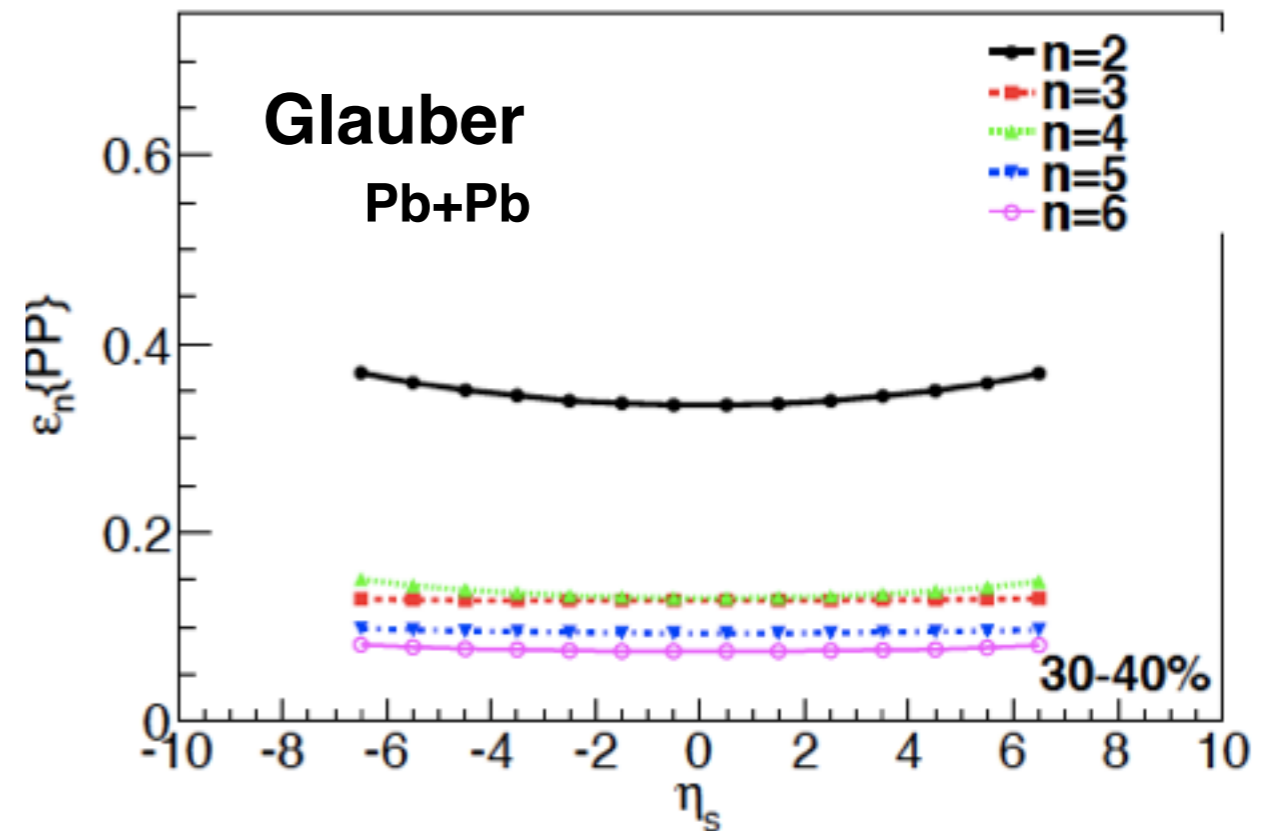


- ✓ At-mid η , the v_3 scaled with gluon base model in Cu+Au is closer to that in Au+Au
- ✓ At-F/B η , the v_3/ϵ_3 with gluon base model in Cu+Au is closer to that in Au+Au

η_s dependence of ε_n



arXiv:12004.5814v2

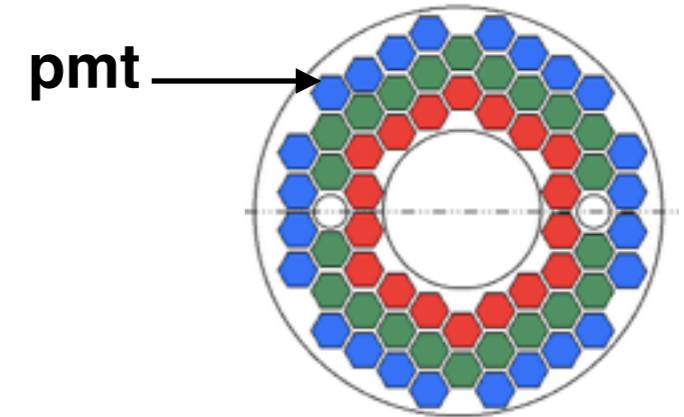


- ✓ Longitudinal structure is less understood
 - Transverse direction can be described by Glauber, CGC...
- ✓ Initial spatial geometry $\varepsilon_n(\eta)$ are η symmetric
 - Smooth longitudinal density profile, streak-like structure

v_n measurement at Bbc ($3 < |\eta| < 4$)

✓ v_n is measured using 64 Bbc pmts

- Bbc can't reconstruct tracks
- pmt based v_n include back ground



✓ Full Giant simulation with PHENIX configuration

- pmt based $v_n \rightarrow$ track based v_n

$$v_n^{track} = R_n * v_n^{pmt} \quad R_n = \frac{v_{n,input}^{Sim}}{v_{n,output}^{Sim}}$$

$v_{n,input}^{Sim}$

Input v_n from particle simulation

$v_{n,output}^{Sim}$

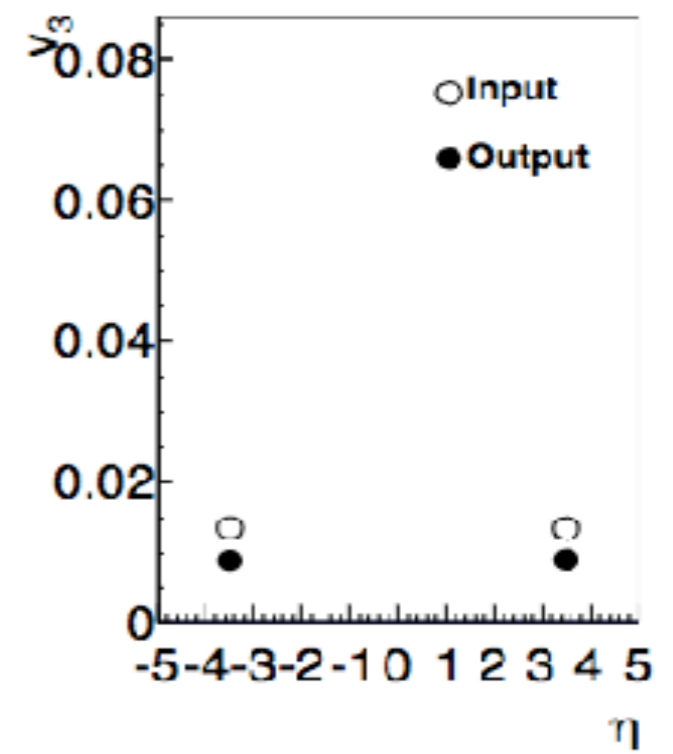
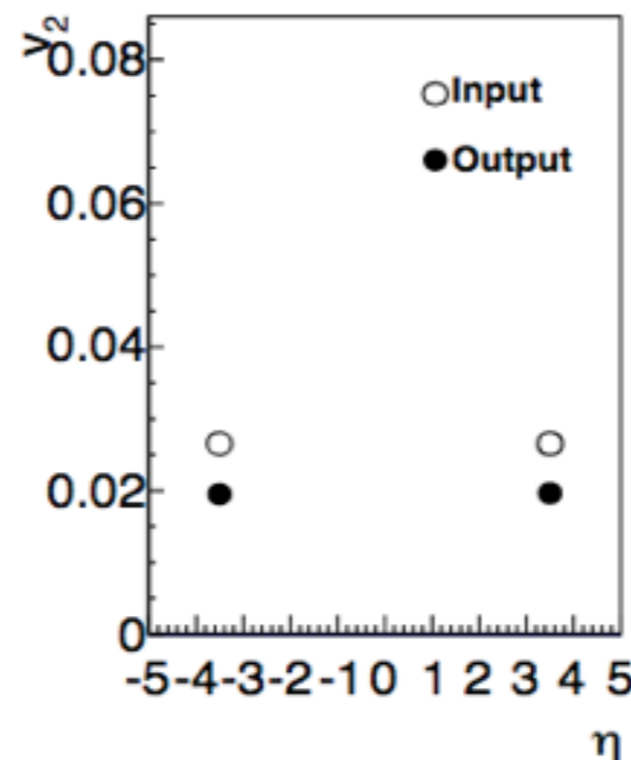
Output v_n from Giant simulation

✓ Correction factor R_n

- R_2 : 0.73
- R_3 : 0.65

✓ Systematic study

- $dN/d\eta$
- pT spectra
- $v_n(pT)$
- $v_n(\eta)$



Initial spatial anisotropy

Glauber Monte Carlo simulation

-Wood Saxon density profile

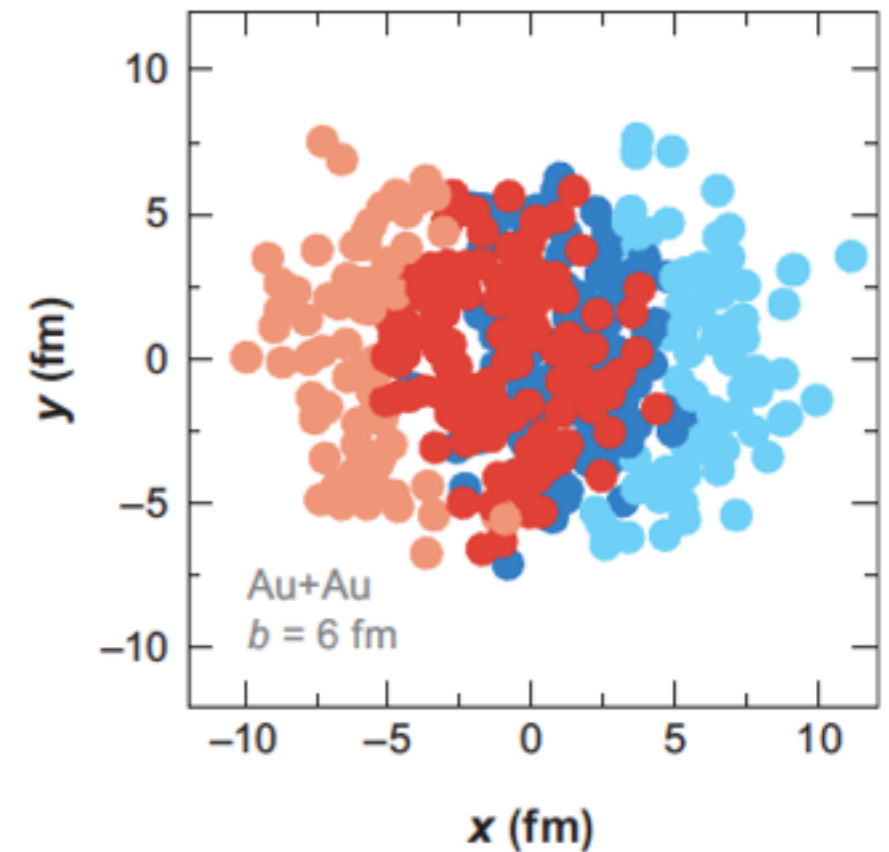
- collision is occurred, if $d < \sqrt{(\sigma_{nn}/\pi)}$

d : distance between nucleons

σ_{nn} : total cross section(pp collision)

$$\epsilon_n = \frac{\langle r^2 \cos[n(\phi - \Psi_{n,PP})] \rangle}{\langle r^2 \rangle}$$

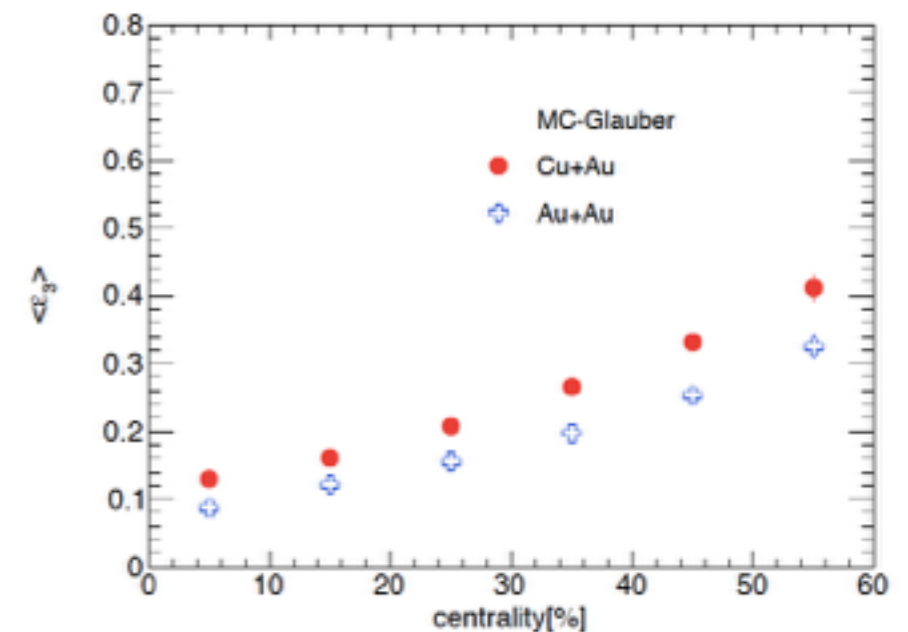
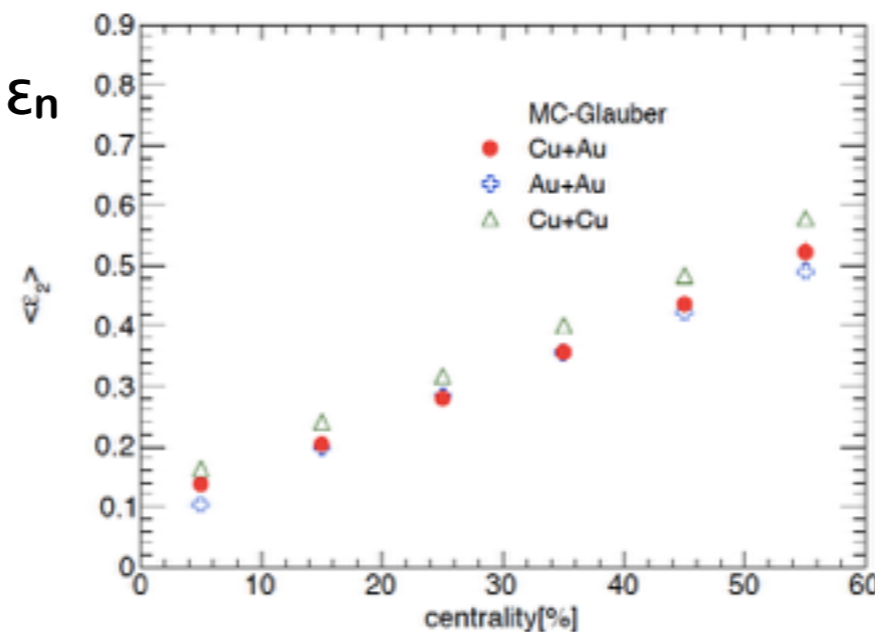
$$\Psi_{n,PP} = \frac{1}{n} \left[\tan^{-1} \frac{\langle r^2 \sin(n\phi) \rangle}{\langle r^2 \cos(n\phi) \rangle} + \pi \right]$$



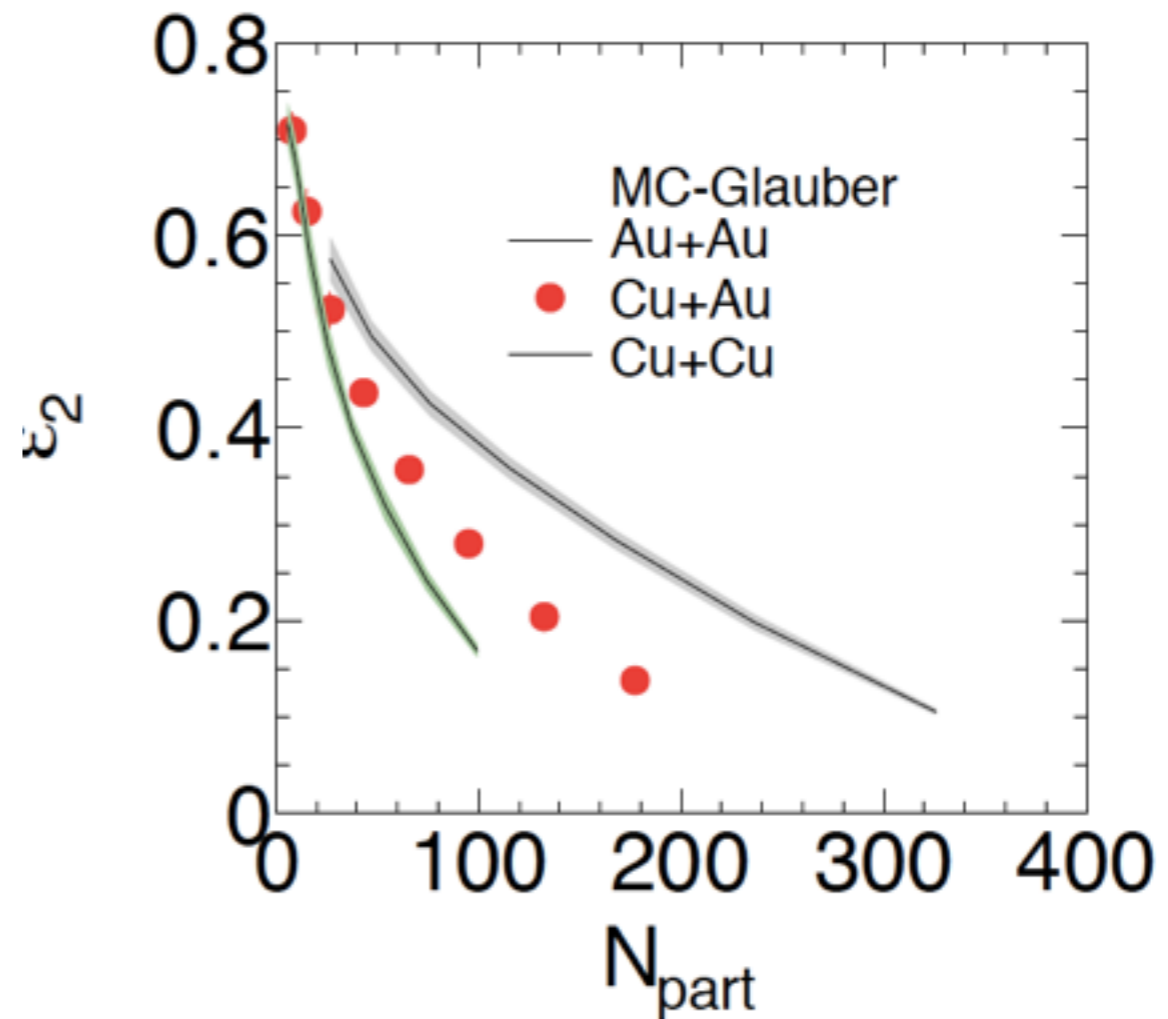
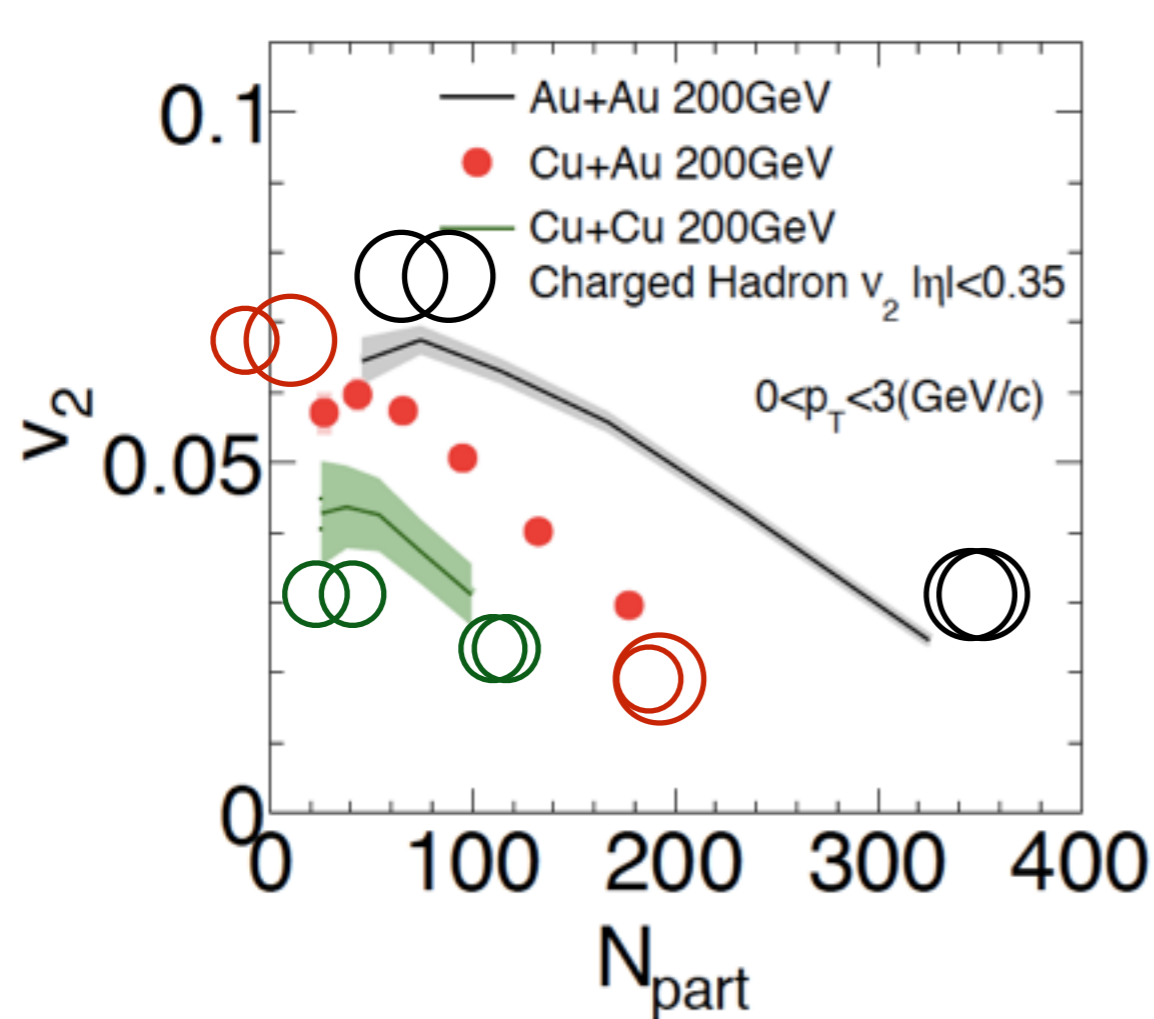
Centrality dependence of ϵ_n

ϵ_2 : CuCu > CuAu ~ AuAu

ϵ_3 : CuAu > AuAu

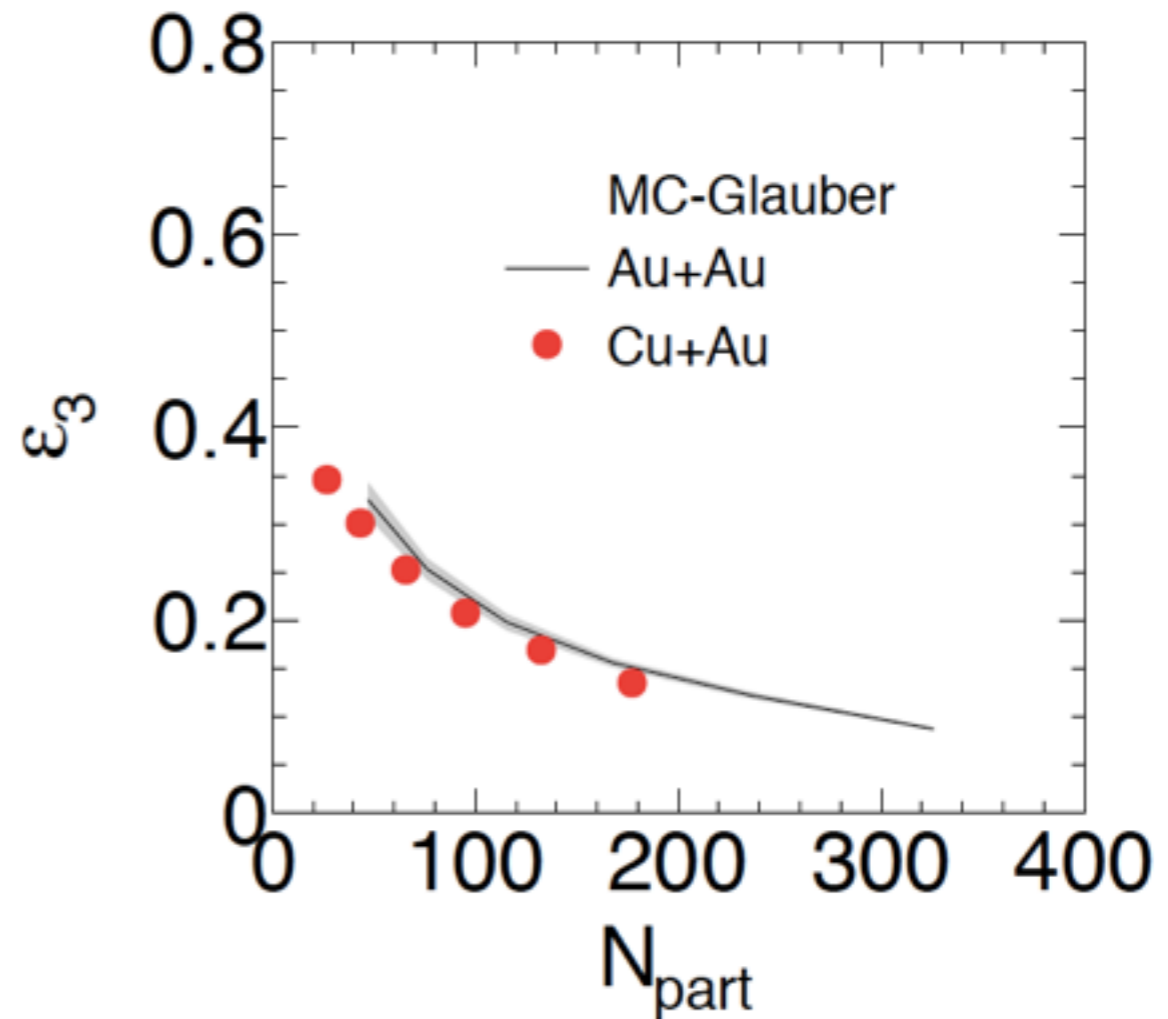
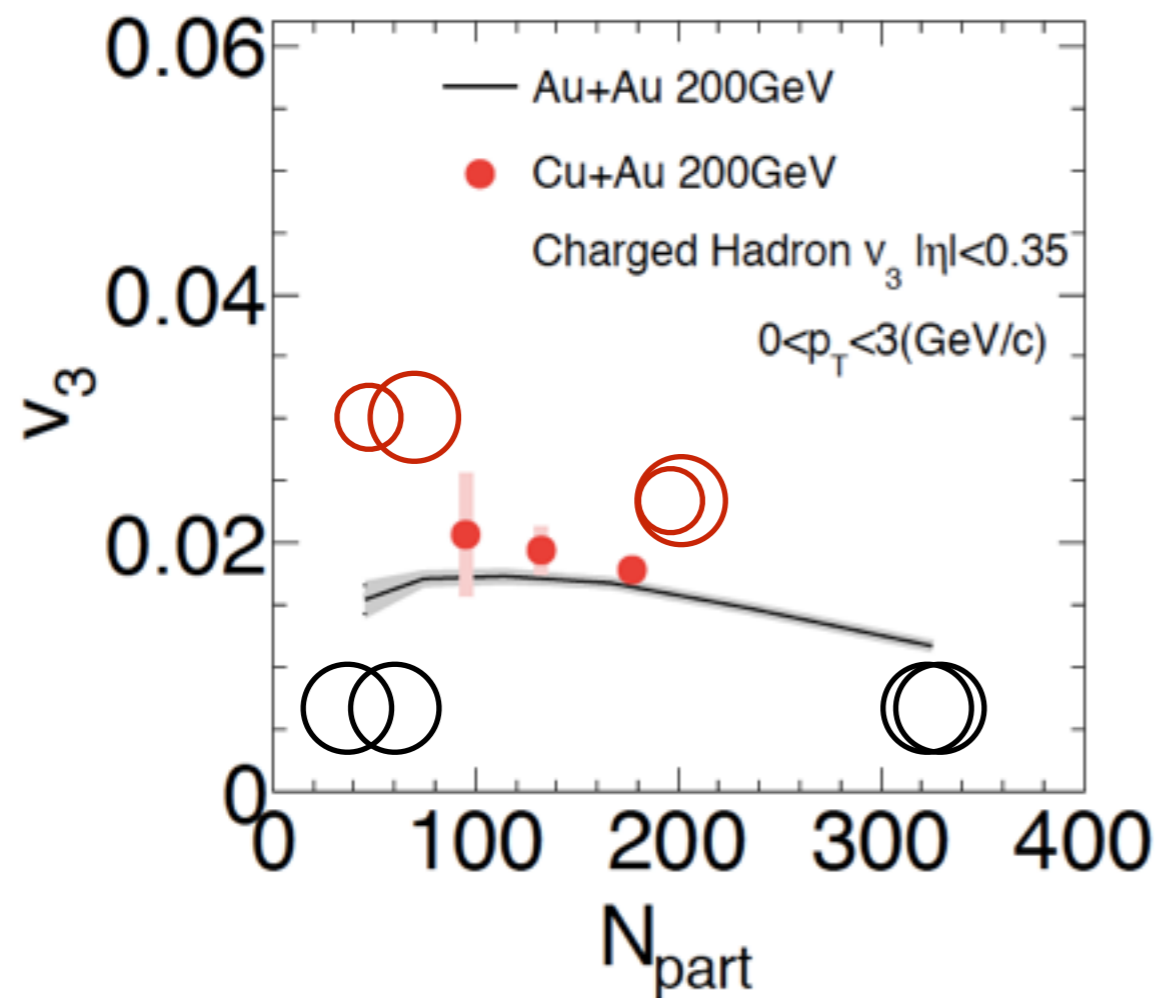


System size dependence of $v_2(N_{\text{part}})$ and $\varepsilon_2(N_{\text{part}})$



- ✓ $v_2(N_{\text{part}})$ and $\varepsilon_2(N_{\text{part}})$ are similar system size dependence
- N_{part} : Number of participants from MC-Glauber
- $v_2(\text{AuAu}) > v_2(\text{CuAu}) > v_2(\text{CuCu}) \sim \varepsilon_2(\text{AuAu}) > \varepsilon_2(\text{CuAu}) > \varepsilon_2(\text{CuCu})$

System size dependence of $v_3(N_{\text{part}})$ and $\varepsilon_3(N_{\text{part}})$



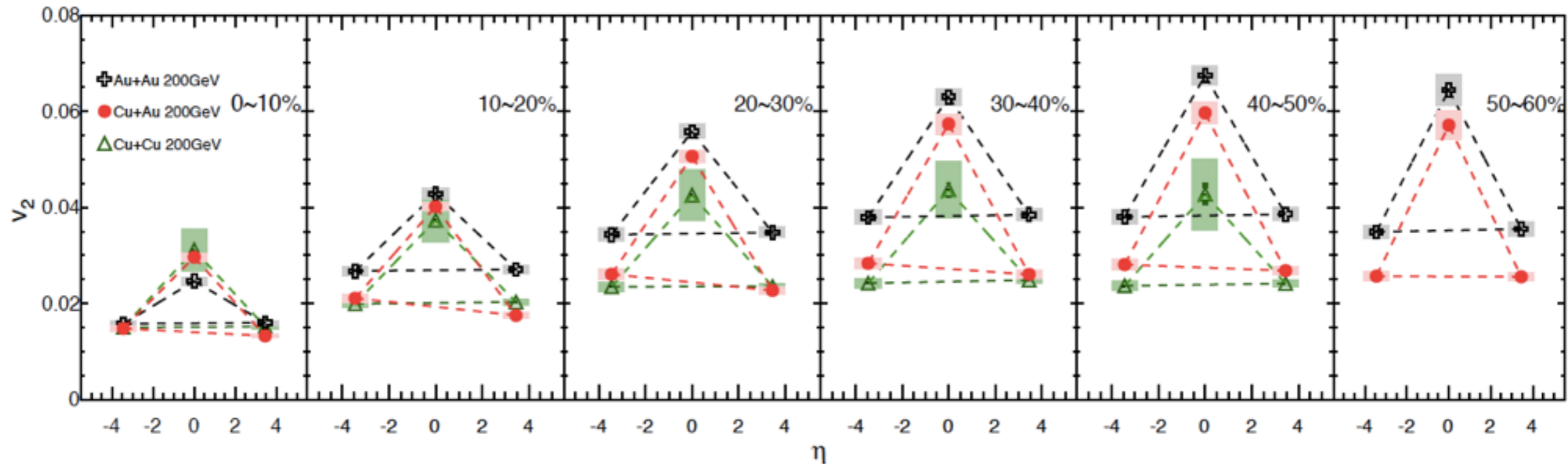
✓ Unlike $v_2(N_{\text{part}})$, no significant system size dependence of $v_3(N_{\text{part}})$ and $\varepsilon_3(N_{\text{part}})$

- The ordering of the magnitude of v_3 is reversed with that of ε_3

- v_3 in Cu+Au are almost same or slightly larger than those in Au+Au

-> intrinsic triangularity of asymmetric overlap zone?

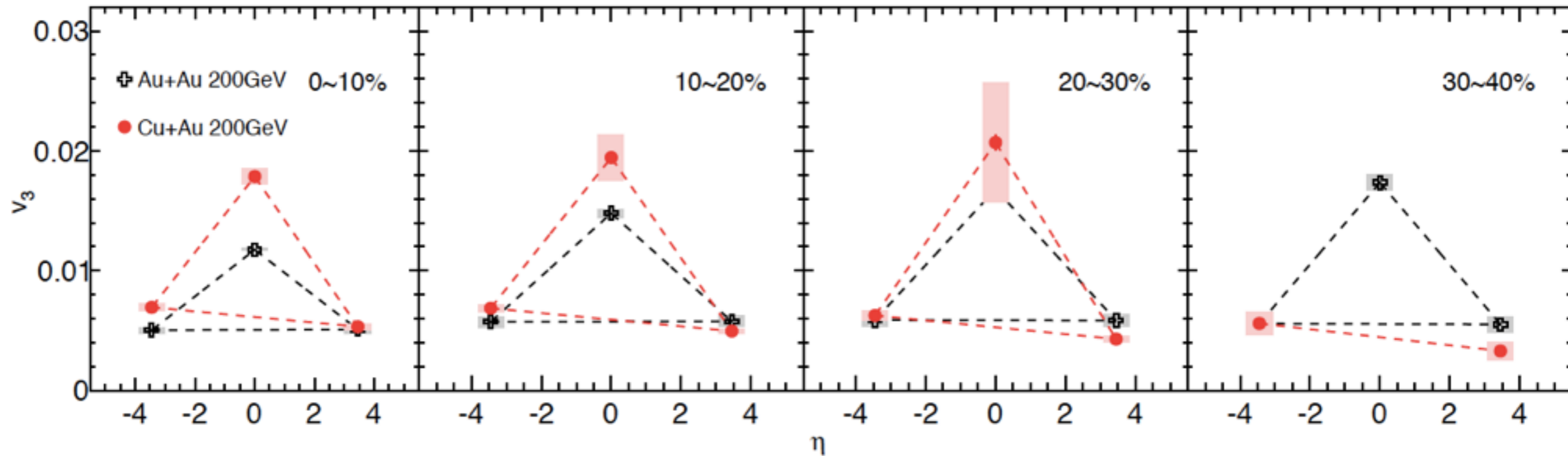
System size dependence of v_2 at F/B



✓ In Cu+Au collisions, F/B asymmetry of v_2 is observed.

- central & peripheral collisions: $v_2(\text{Au-going}) \sim v_2(\text{Cu-going})$
- mid-central collisions : $v_2(\text{Au-going}) > v_2(\text{Cu-going})$
- >caused by different initial geometries in Au and Cu ?

System size dependence of v_3 at F/B



✓ Weak centrality dependence of v_3 is seen for all collision systems

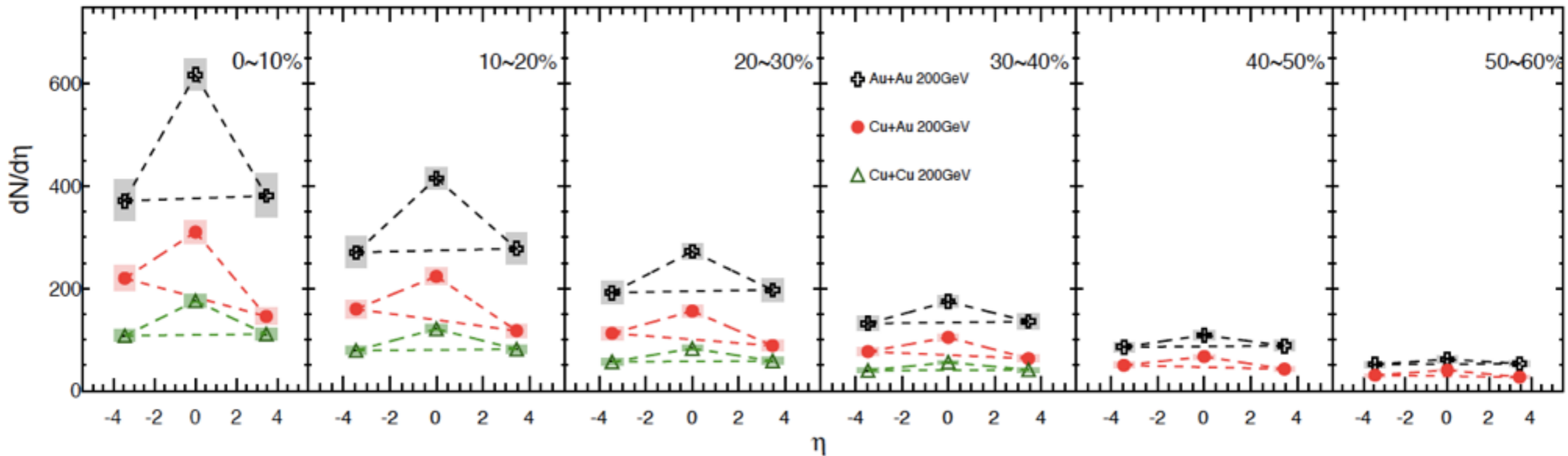
- AuAu: same centrality dependence as seen mid η

- CuAu: v_3 decrease as centrality decrease

✓ In CuAu collisions, $v_3(\text{Au-going}) > v_3(\text{Cu-going})$ for all centrality bins

-> Like v_2 , the different initial geometry cause the different v_3 ?

F/B asymmetry of $dN/d\eta$

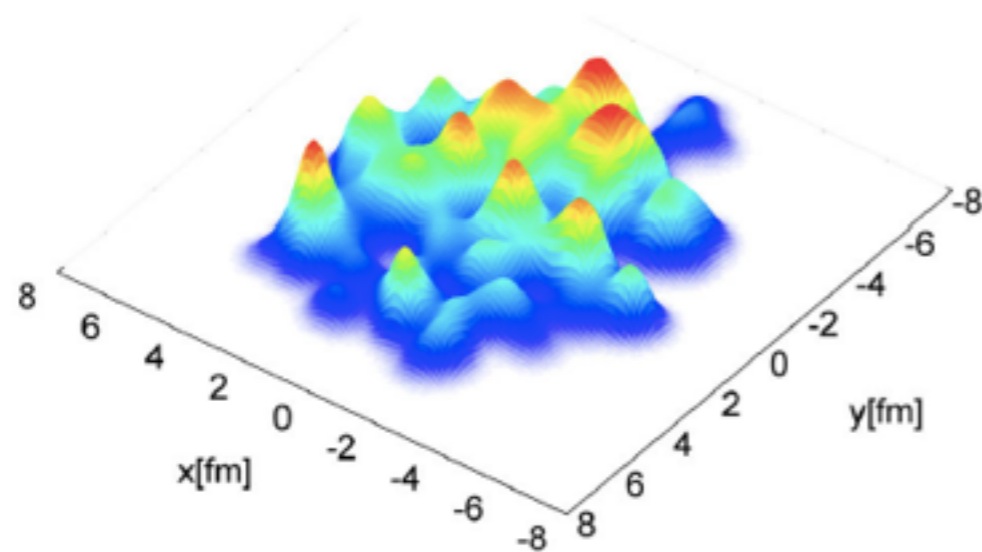


✓ Like the v_n , the $dN/d\eta$ in Au-going side is higher

✓ In 50-60%, the $dN/d\eta$ in Au-going side and Cu-going side are almost same due to similar N_{part} .

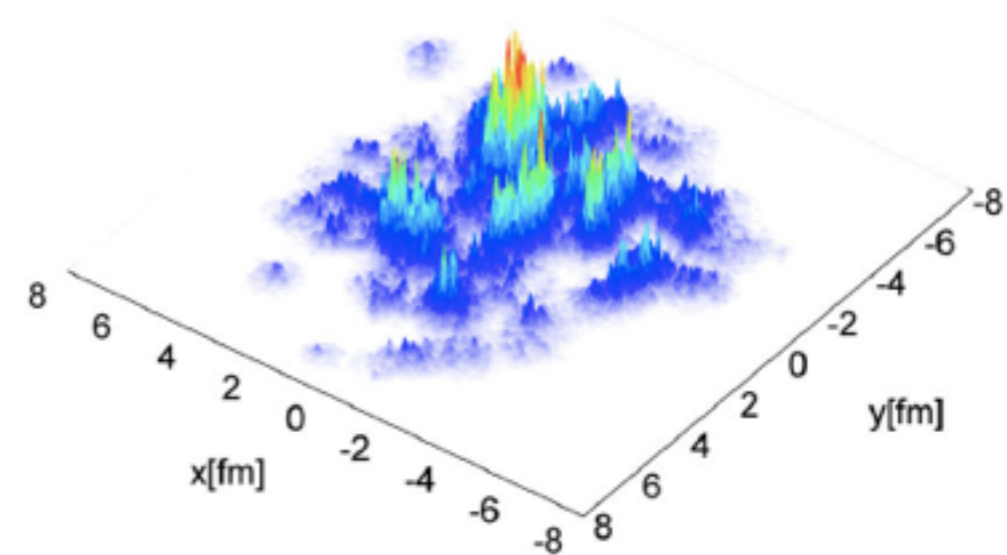
Initial geometry model

Glauber nucleon



Smooth structure

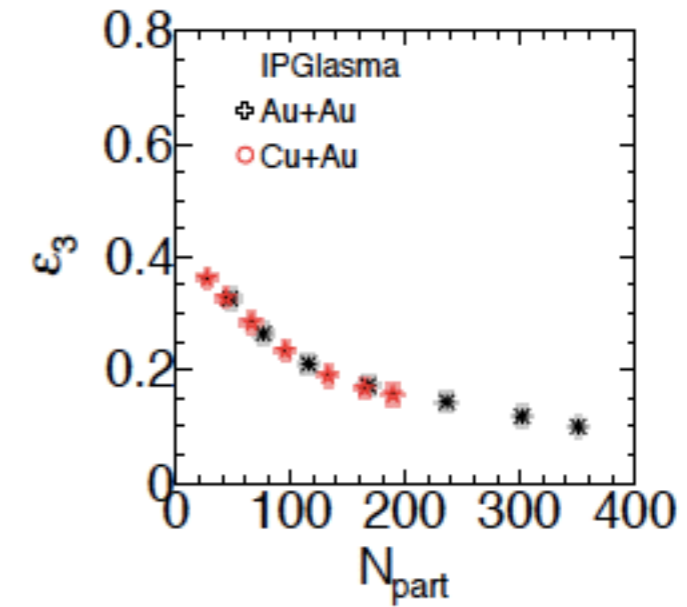
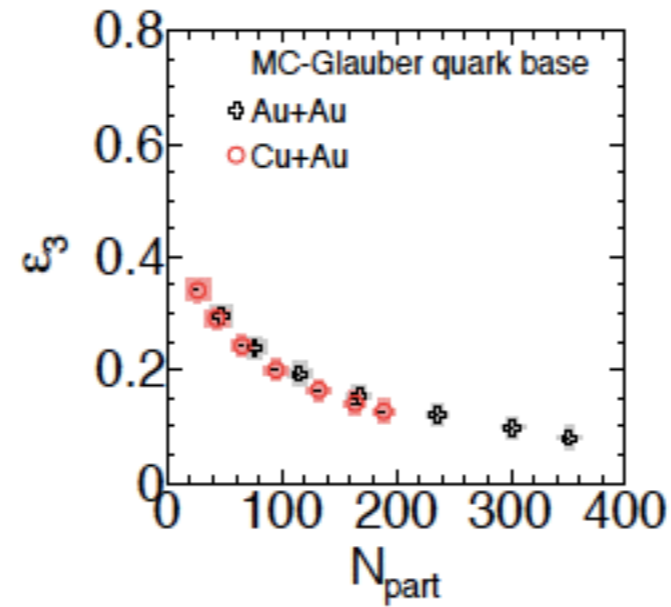
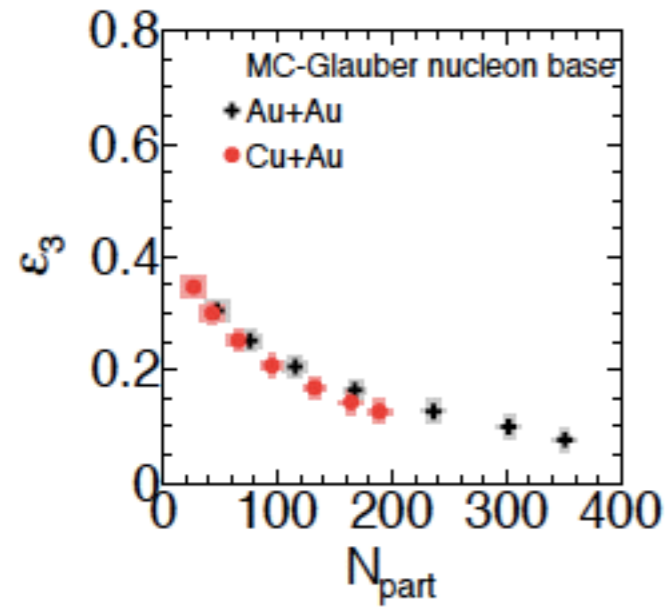
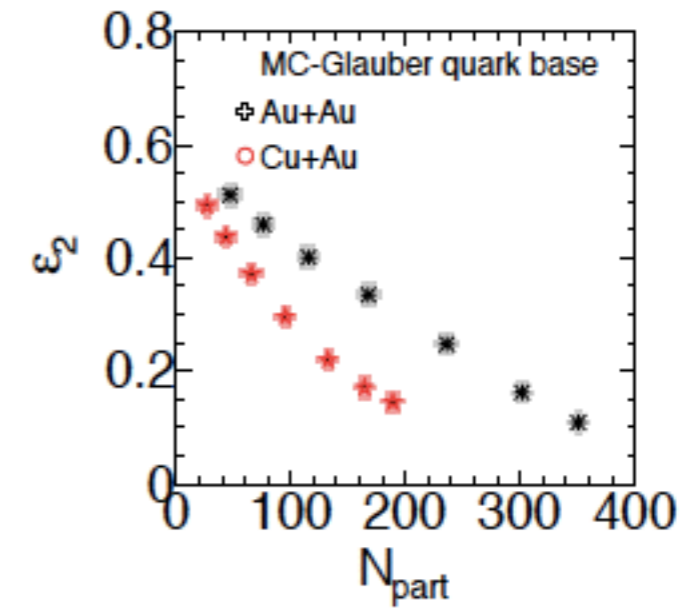
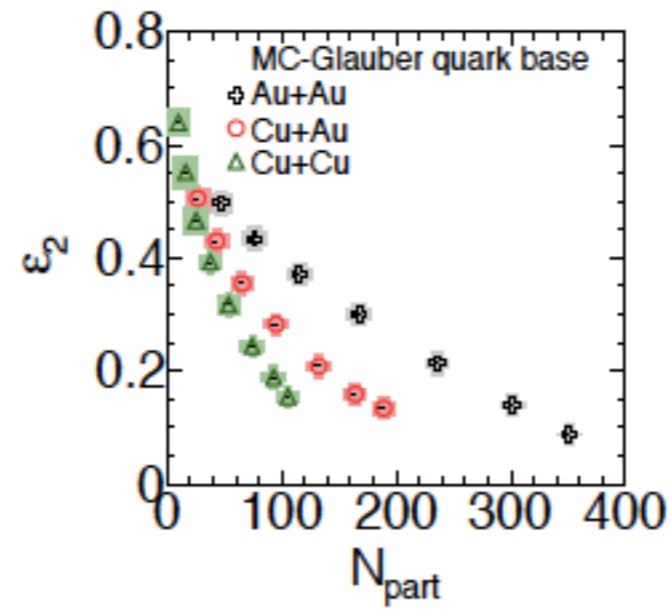
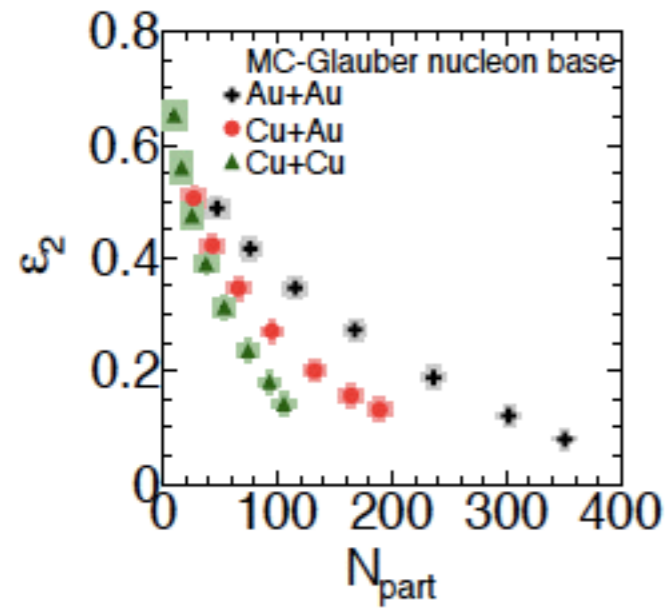
IPGlasma



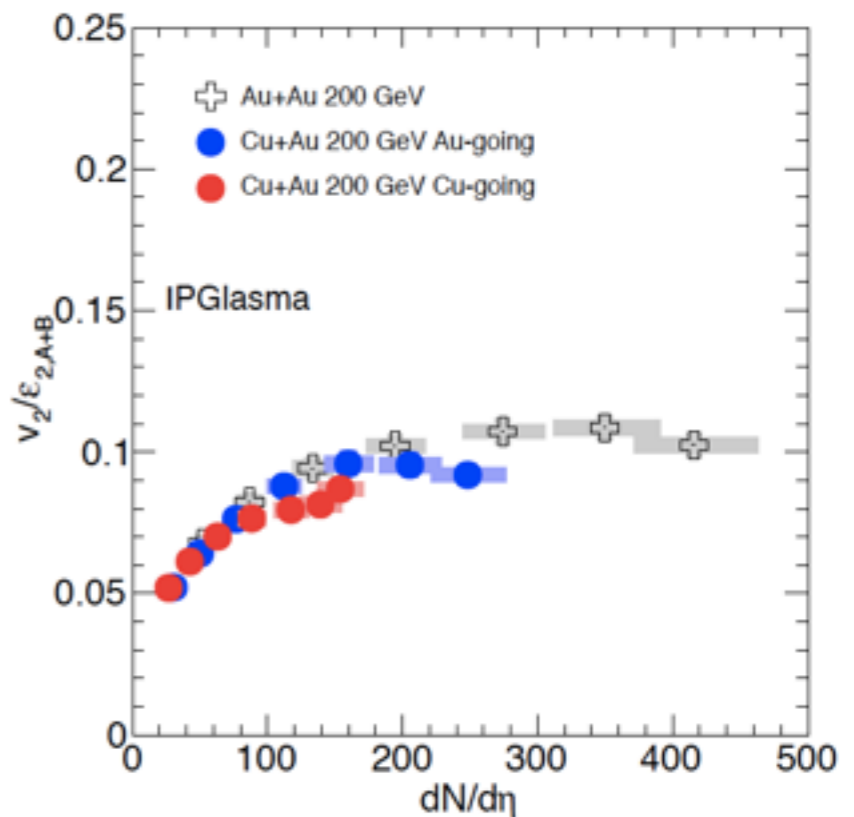
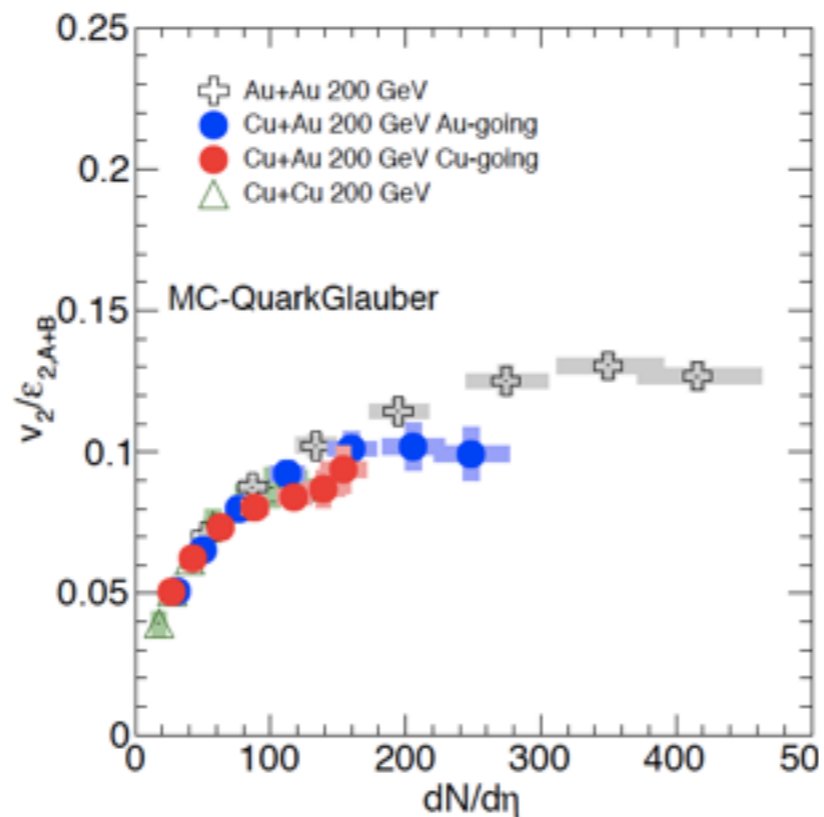
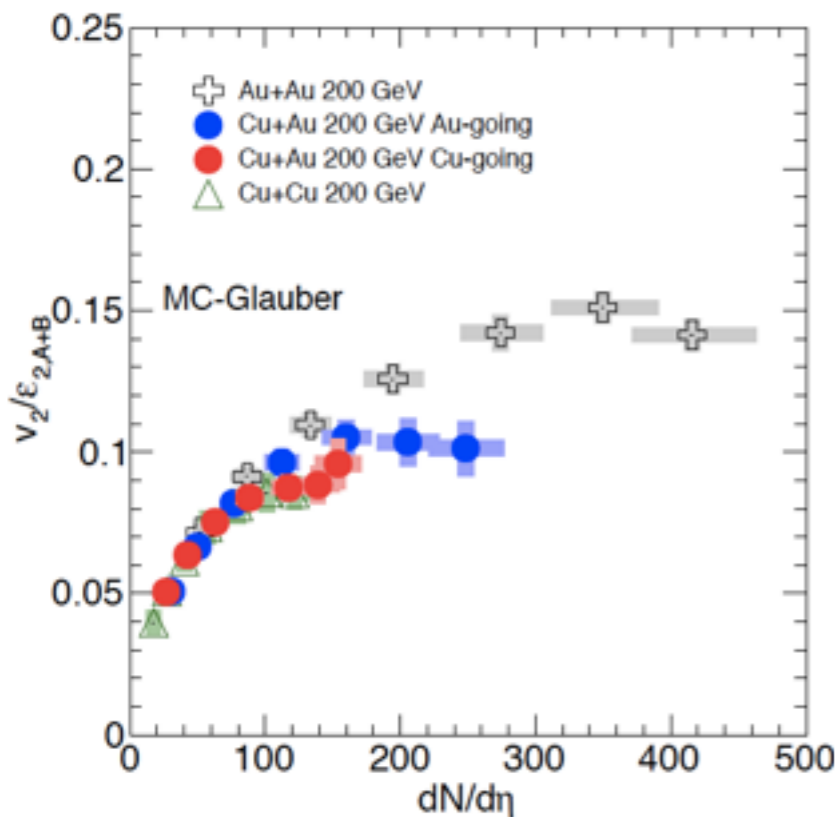
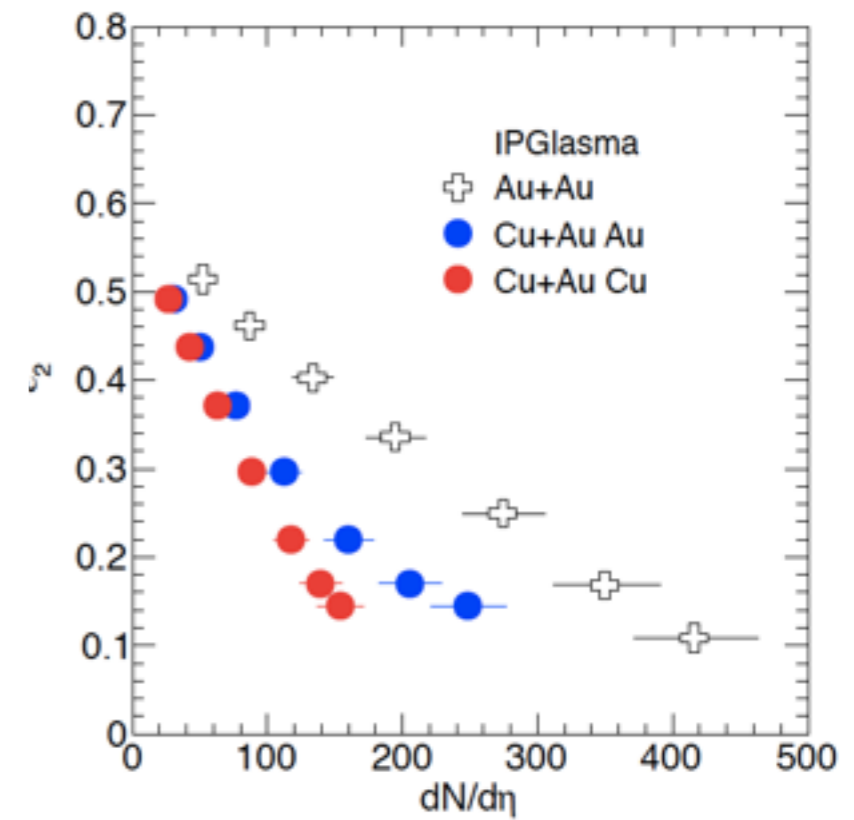
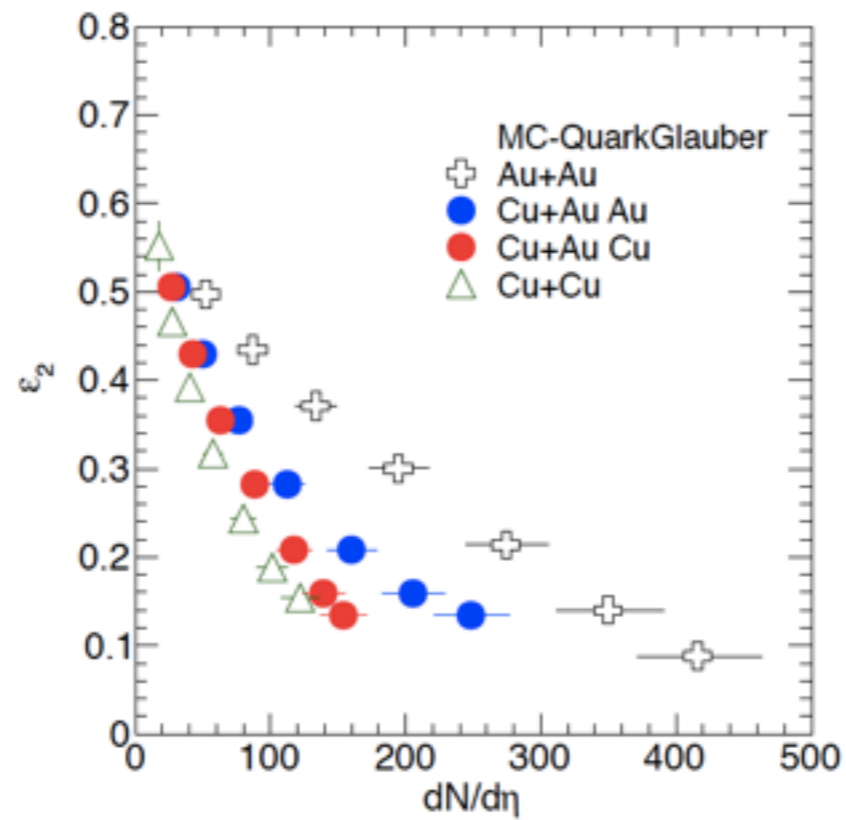
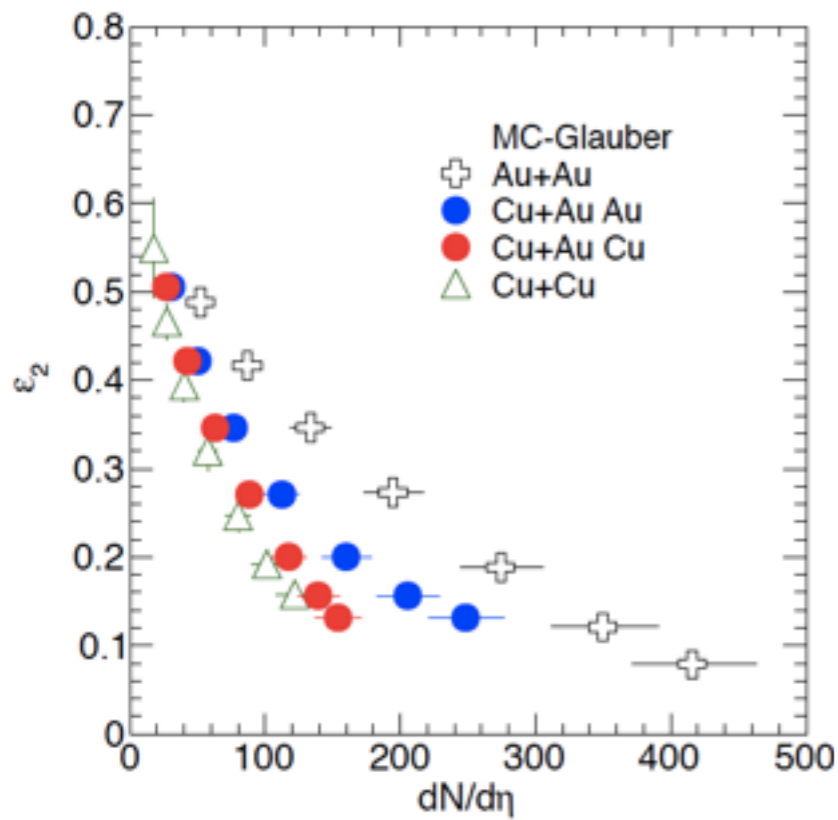
Fine structure

- ✓ Glauber Monte Carlo model:nucleon base
 - ✓ Glauber Monte Carlo model:Constituent quark base
PRC 93 024901
 - ✓ IPGlasma Model : gluon base(CGCG), PRC 89, 064908
- >fineness: gluon base>quark base > nucleon base

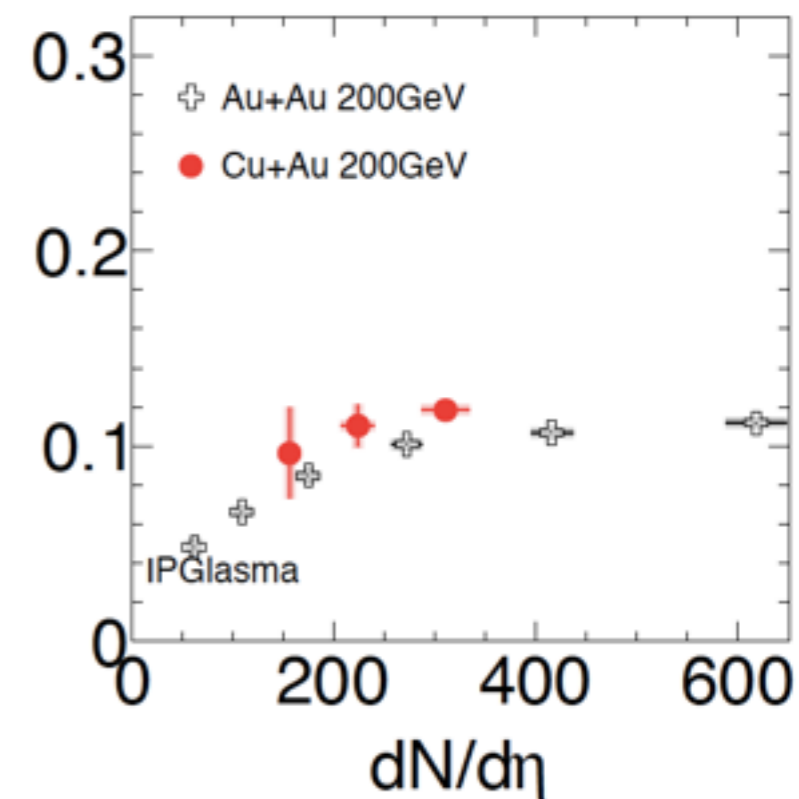
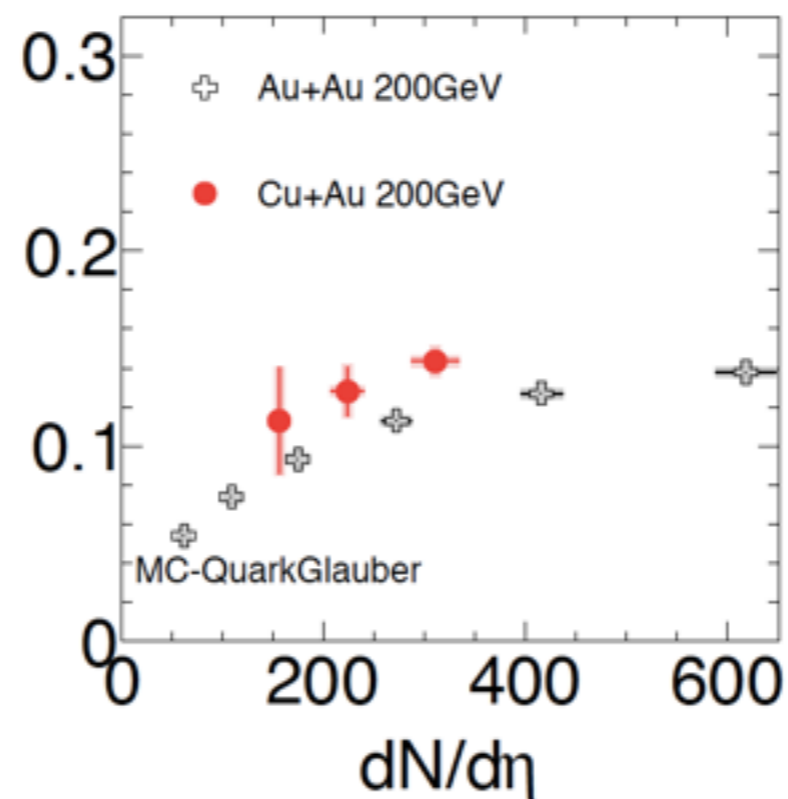
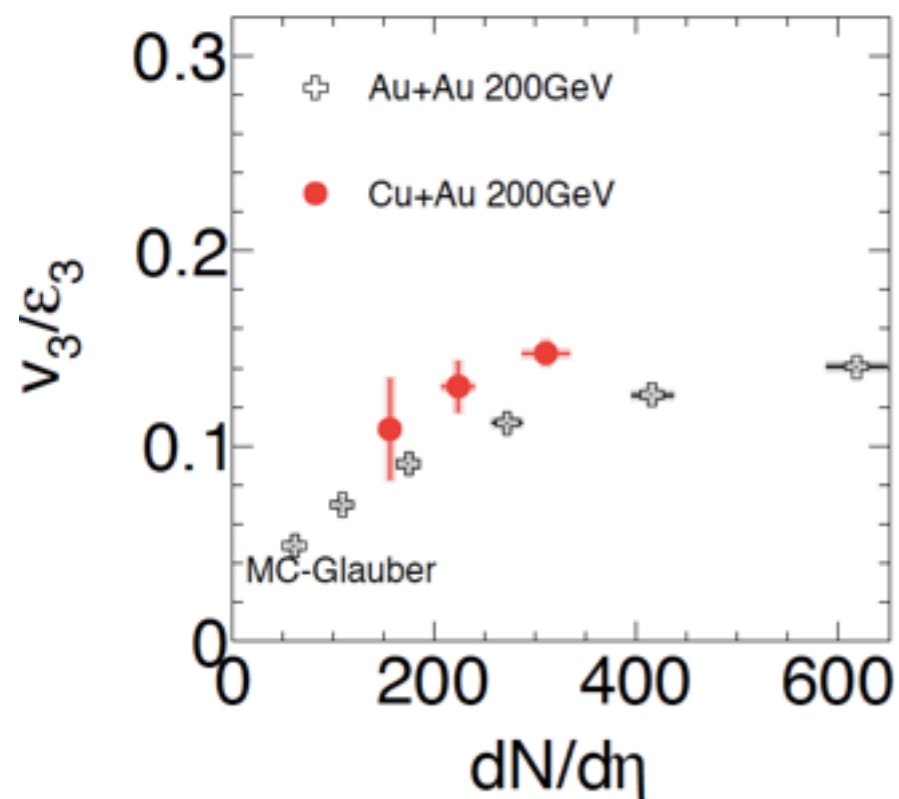
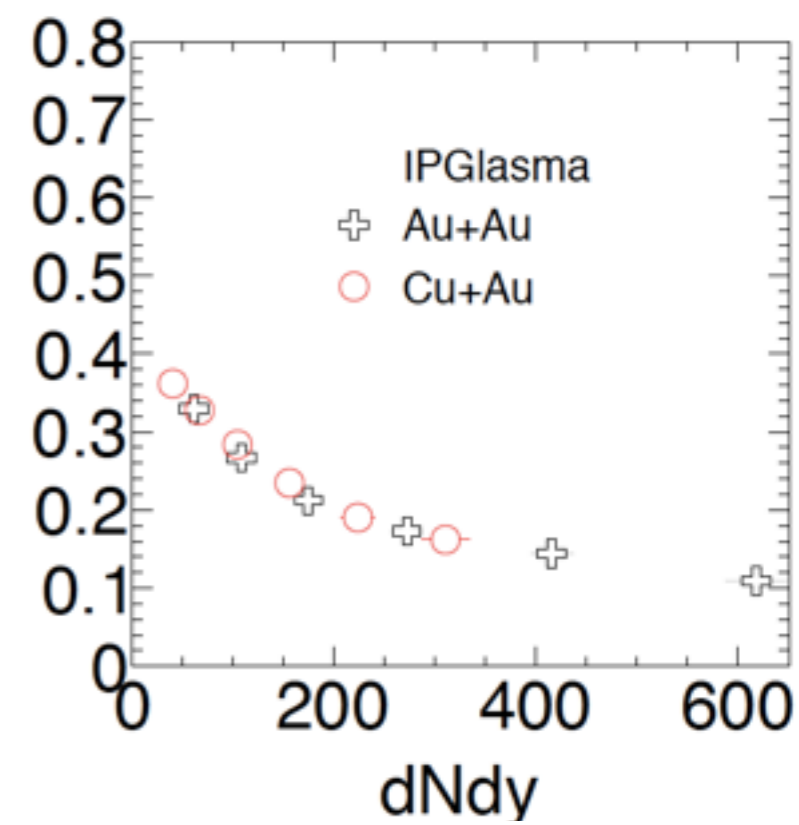
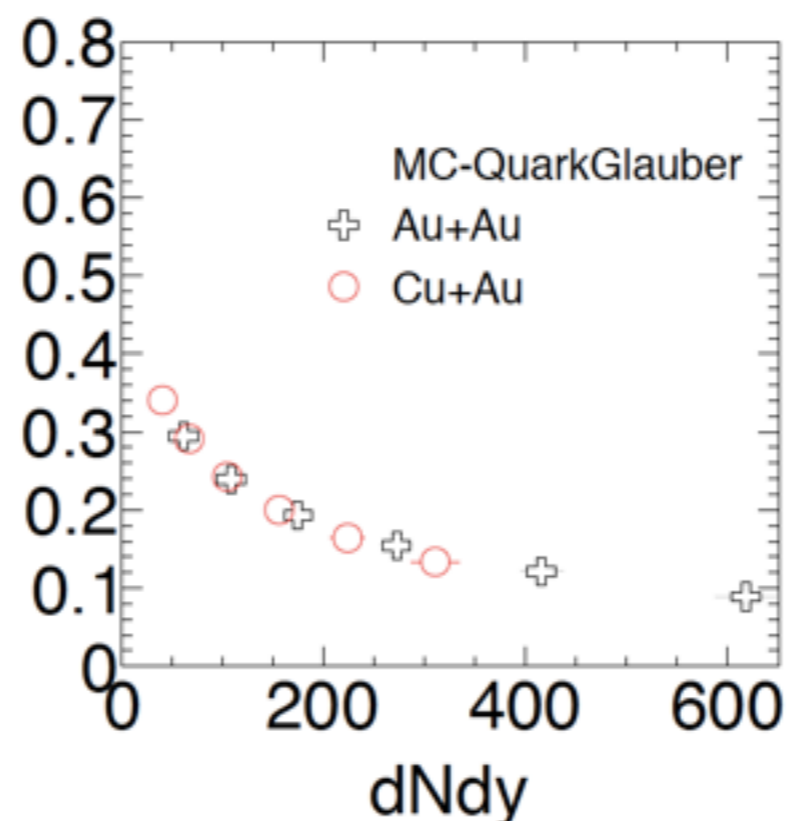
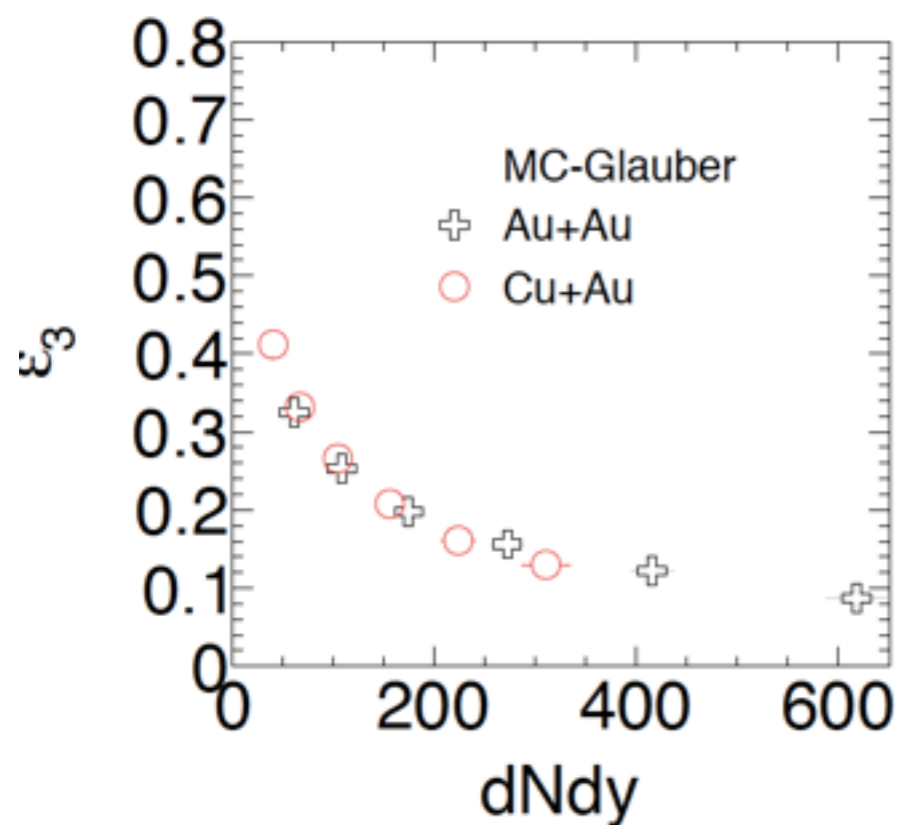
Model dependence of 2nd and 3rd Eccentricity



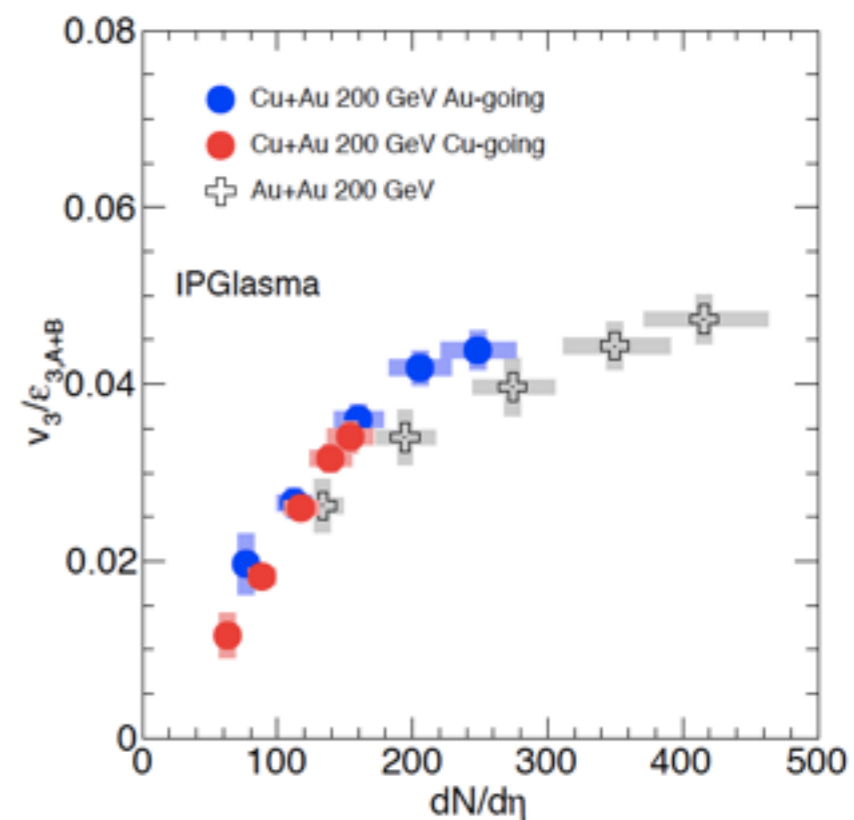
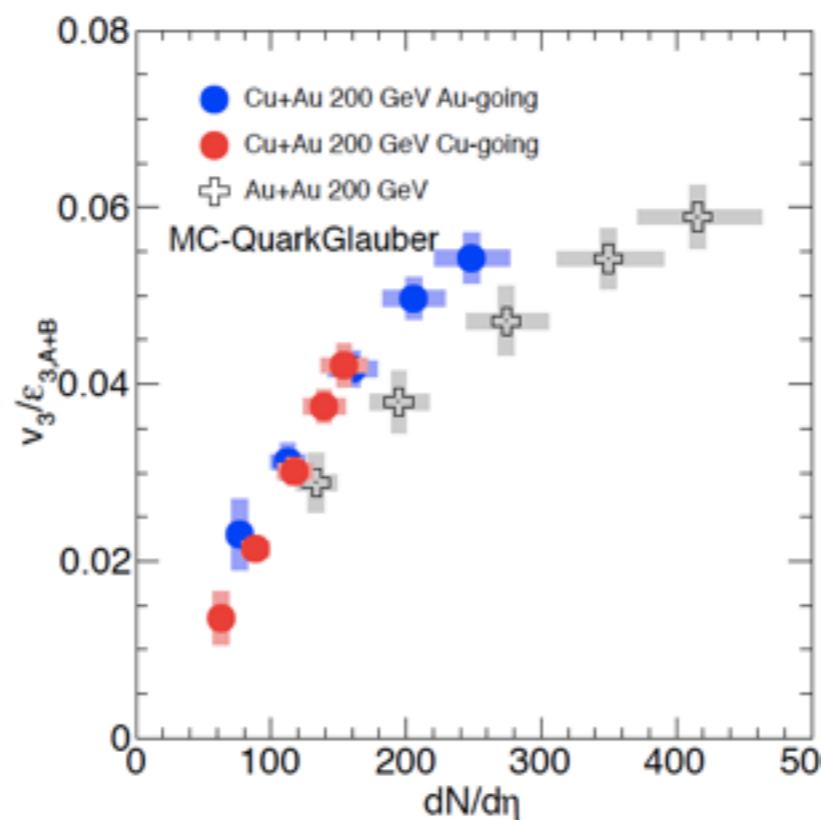
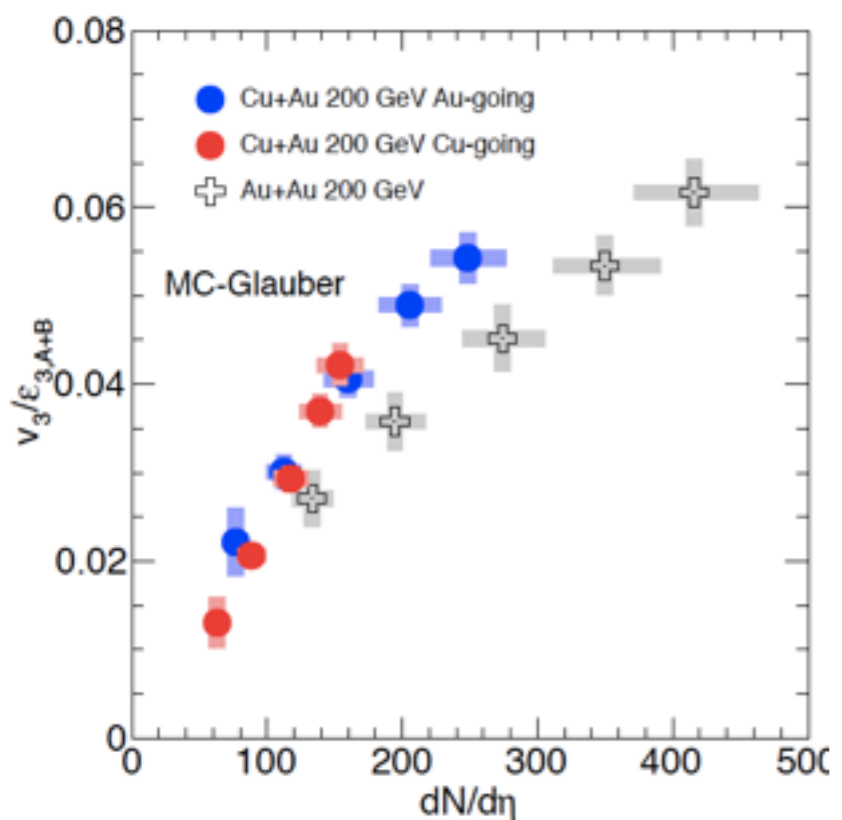
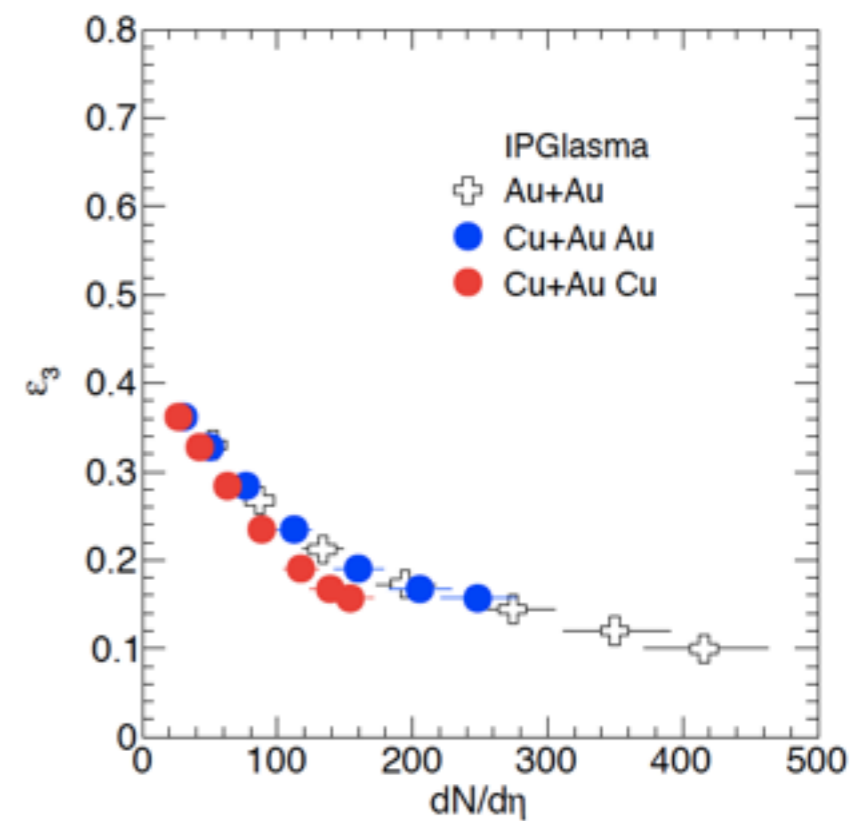
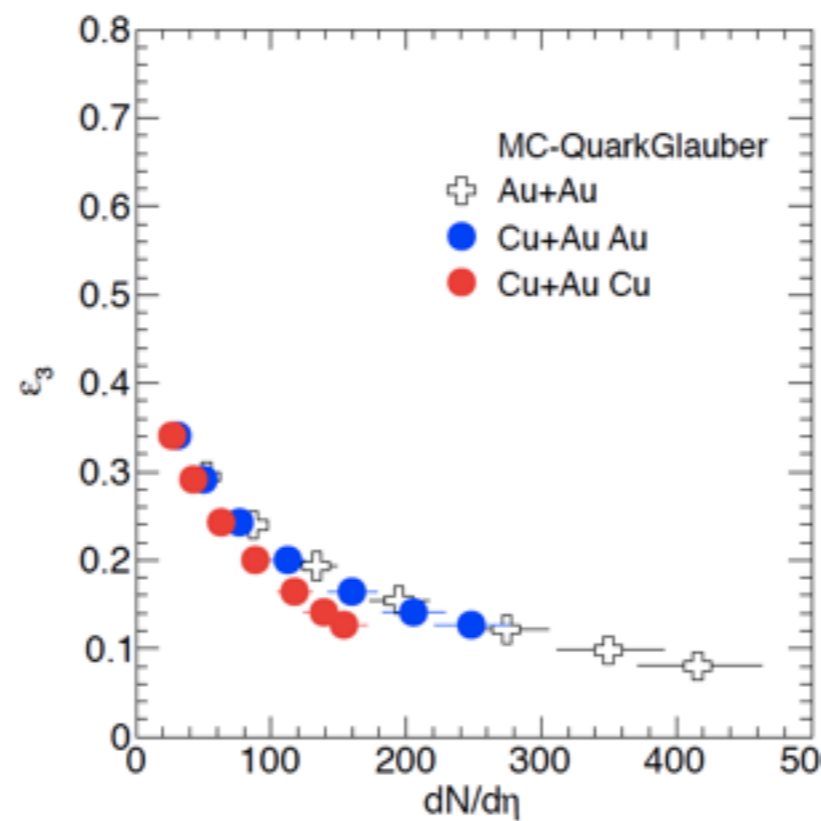
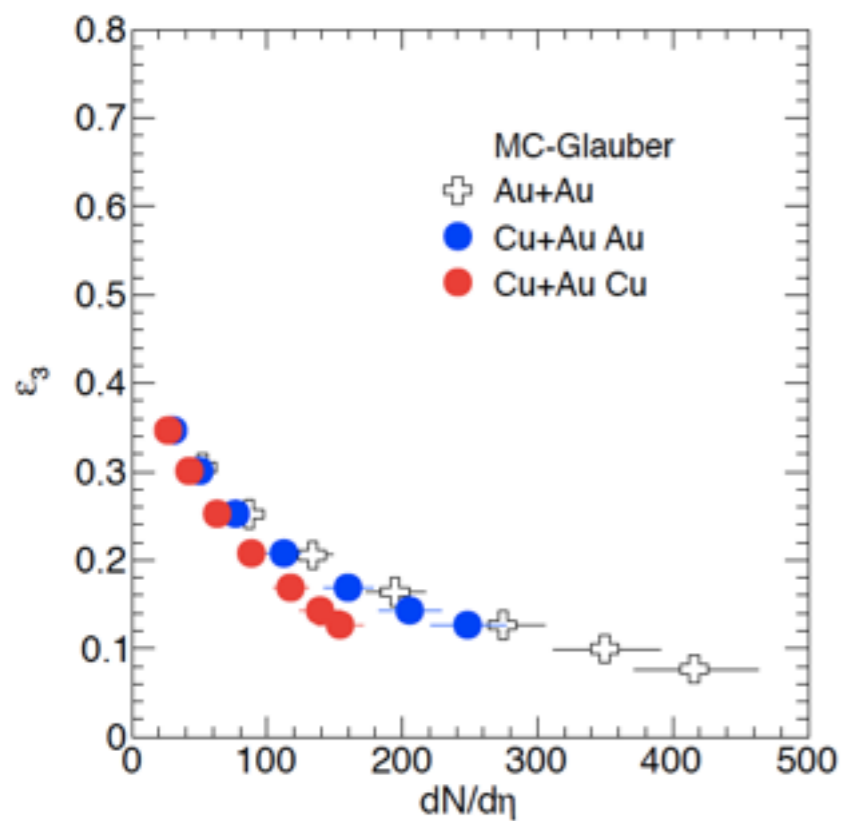
v_2/e_2 at f/b rapidity vs $dN/d\eta$



v_3/e_3 at mid rapidity vs dN/dy

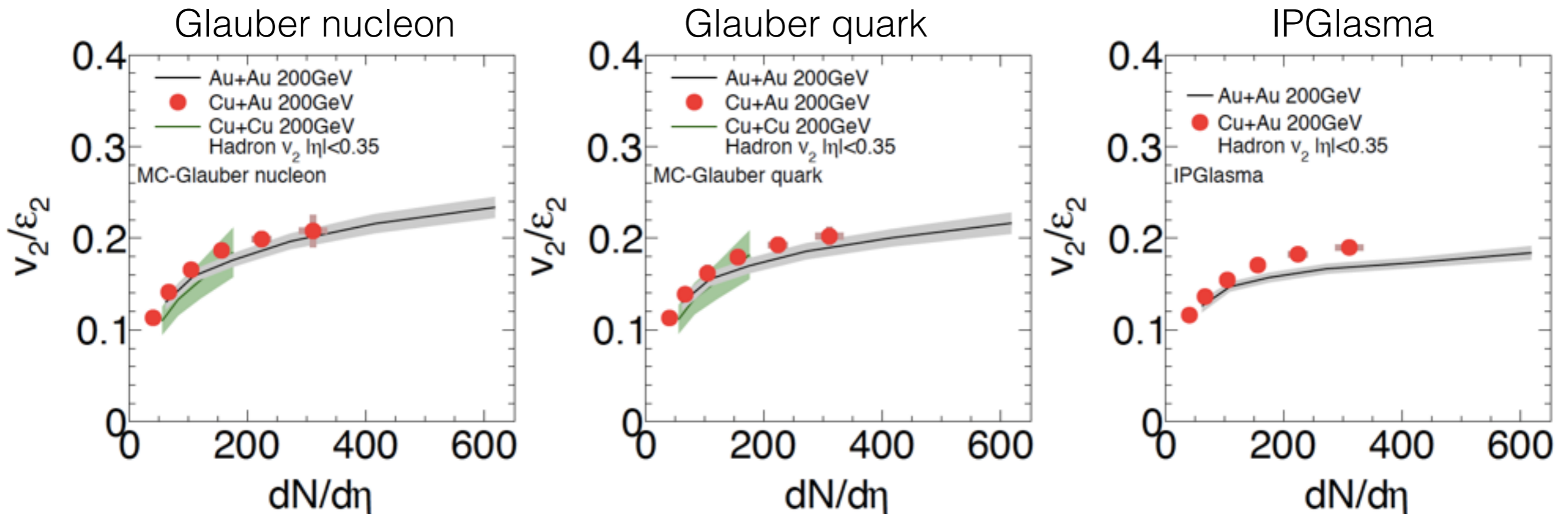


v_3/e_3 at f/b rapidity vs $dN/d\eta$



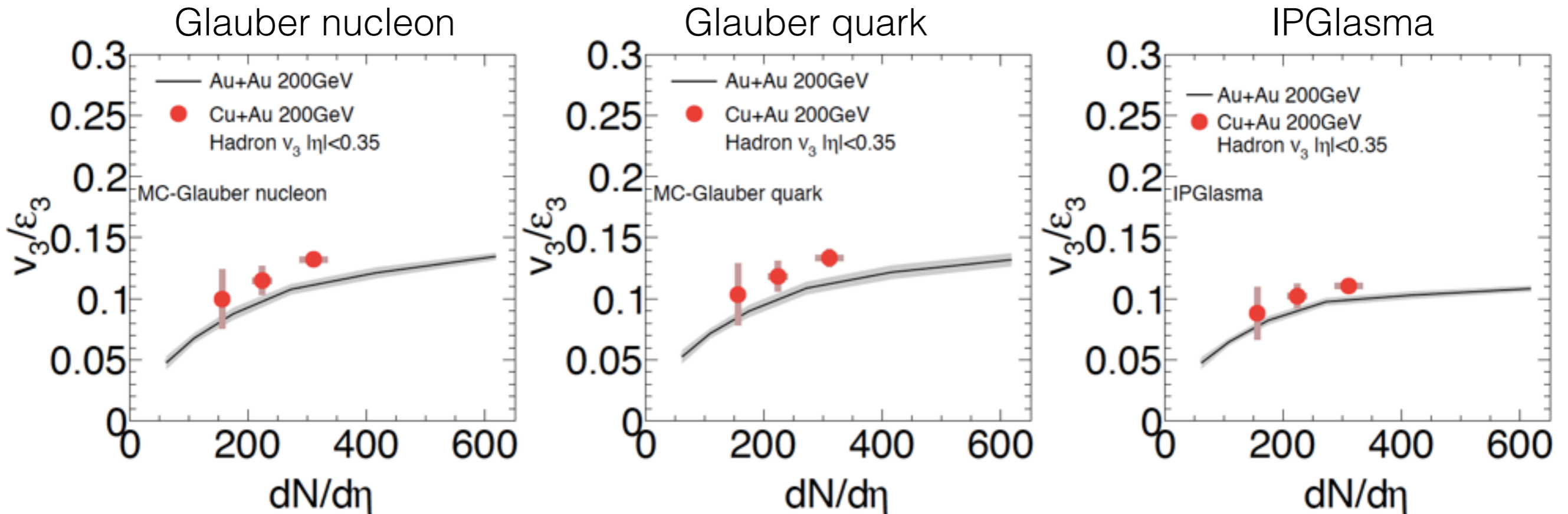
vn vs Npart

v_2/ε_2 scaling at mid-rapidity



- ✓ v_2 scaled with Glauber model (nucleon, quark) are consistent among three collision systems
- ✓ The deviation is seen in central for IPGlasma model

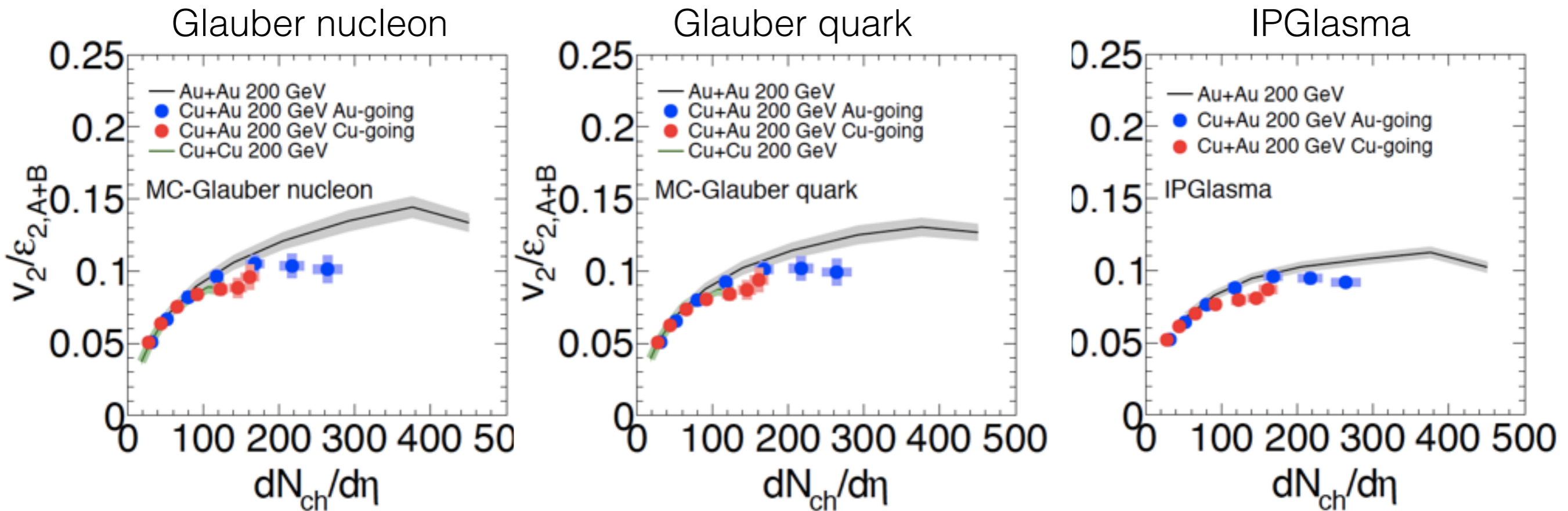
v_3/ε_3 scaling at mid-rapidity



✓ In Glauber model (nucleon, quark), the deviation is seen at central bin

✓ In IPGlasma model, AuAu v_3/ε_3 and CuAu v_3/ε_3 are close to each other

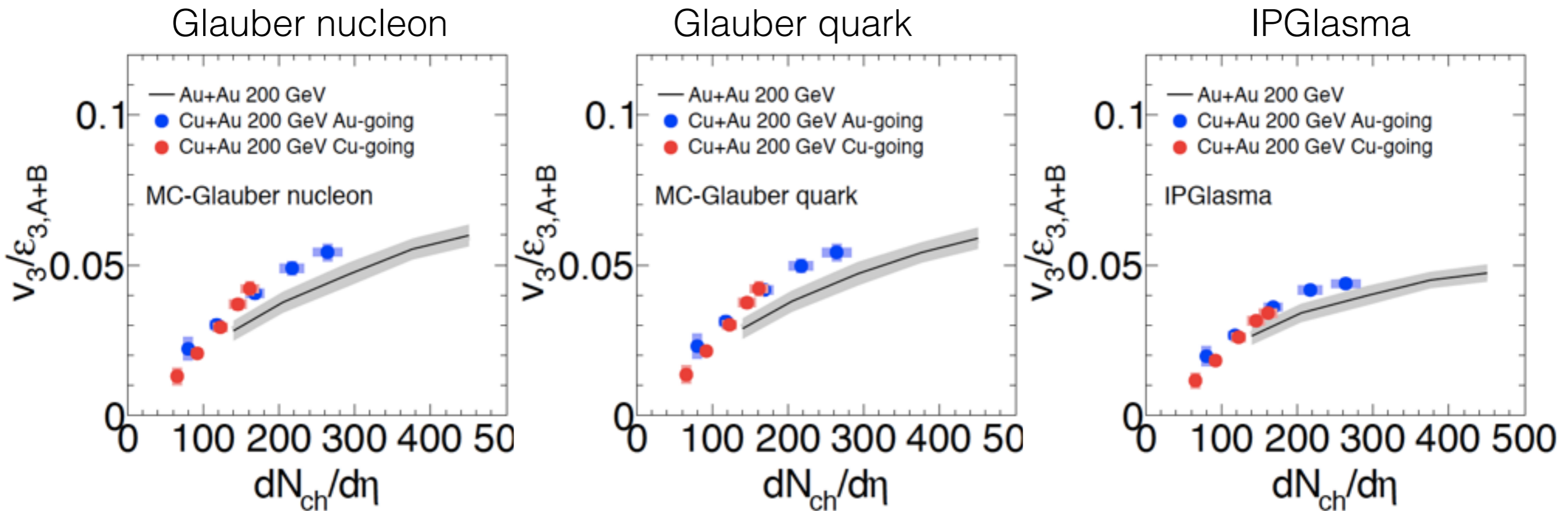
v_2/ε_2 scaling at f/b-rapidity



✓ In Glauber model (nucleon, quark), the deviations between CuAu and AuAu are seen at central bin

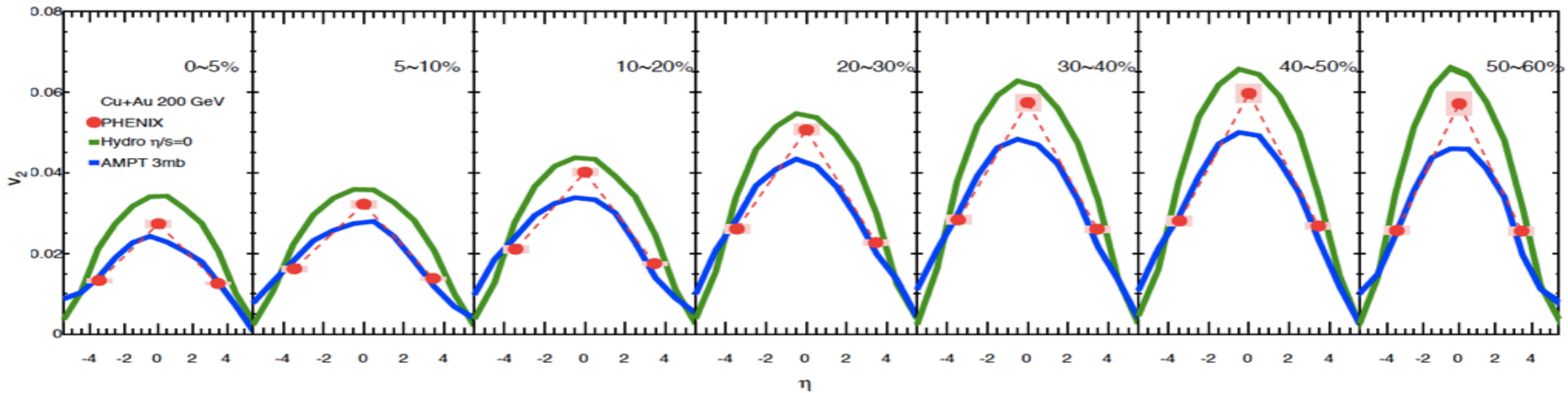
✓ In IPGlasma model, AuAu v_2/ε_2 and CuAu v_2/ε_2 are close to each other

v_3/ε_3 scaling at f/b-rapidity

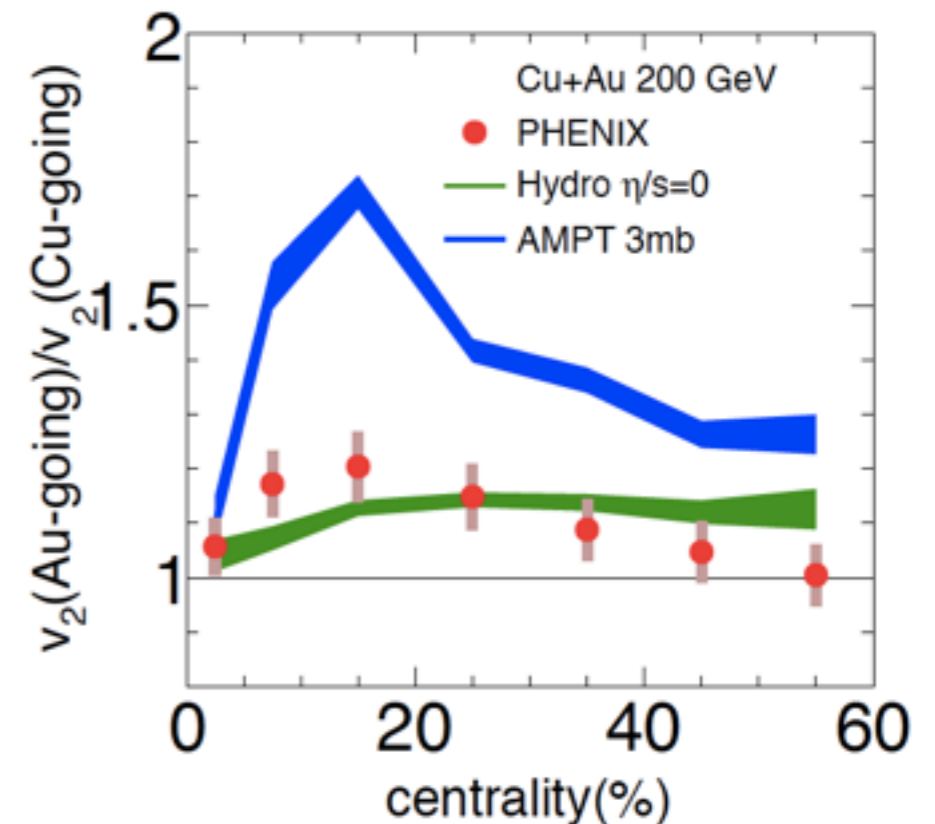


- ✓ In Glauber model (nucleon, quark), the deviation is seen from central to mid-central
- ✓ In IPGlasma model, AuAu v_3/ε_3 and CuAu v_3/ε_3 are close to each other

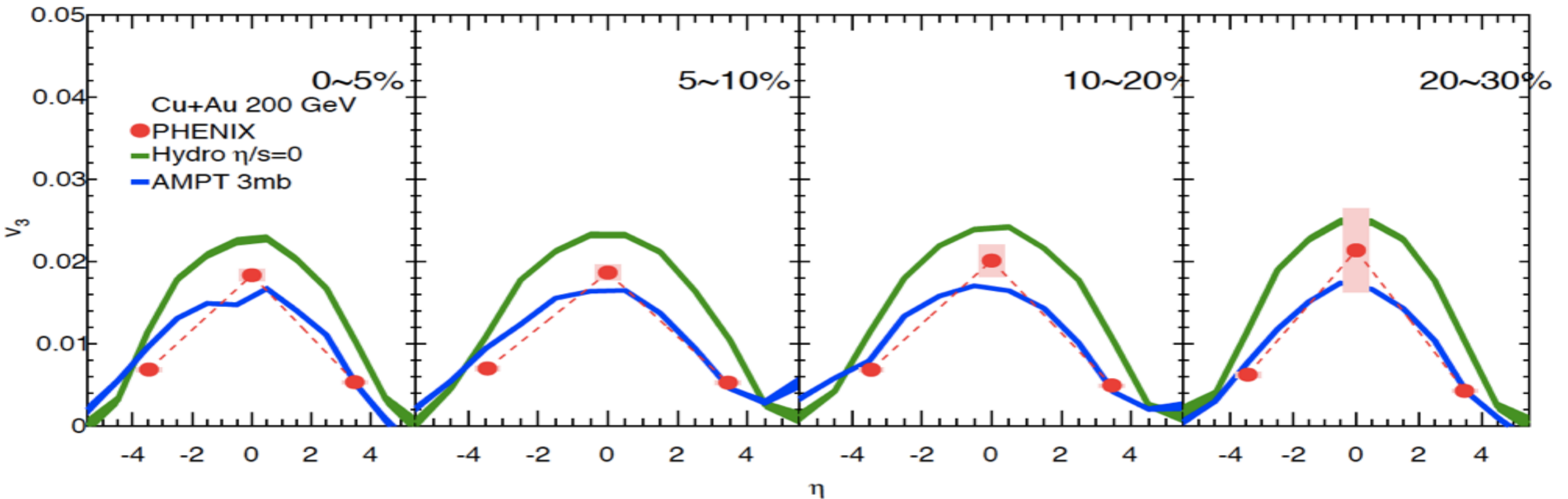
Parton cascade and hydro $v_2(\eta)$



- ✓ AMPT and Hydro predict magnitude of v_2 at F/B rapidity well
- Hydro: Smooth longitudinal density + hydro
- AMPT: Fluctuated longitudinal density + parton cascade
- ✓ Hydro reproduces the ratio of F/B v_2
 - In peripheral collisions, the F/B ratio becomes constant
- ✓ AMPT model over-estimate the ratio

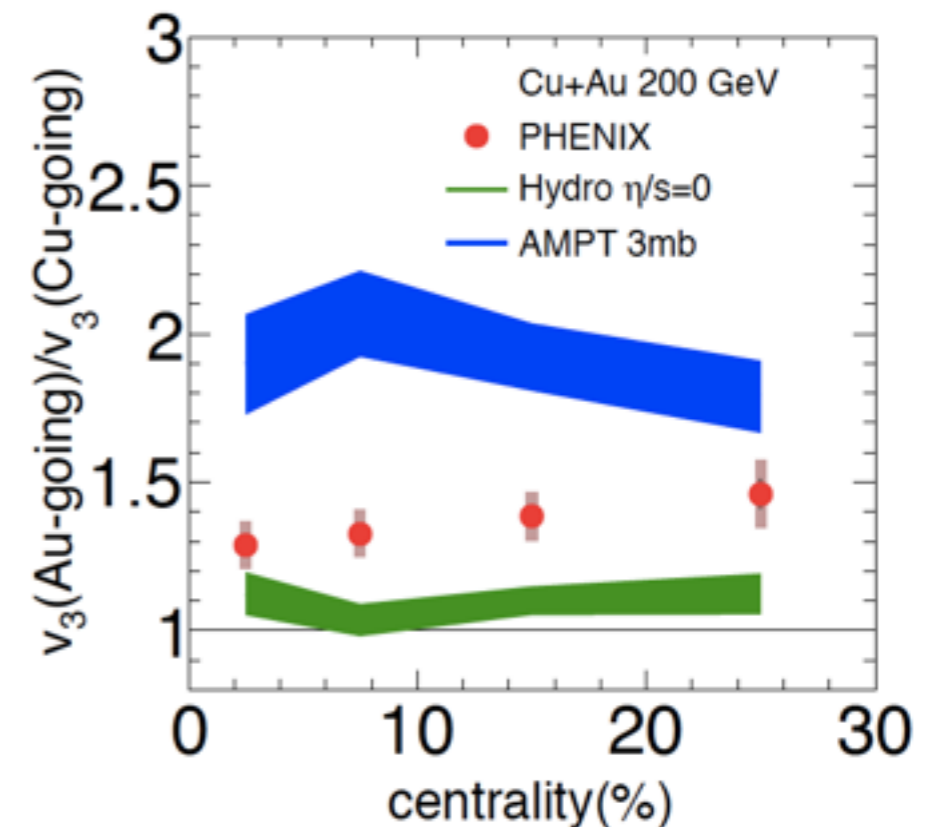


Parton cascade and hydro $v_3(\eta)$

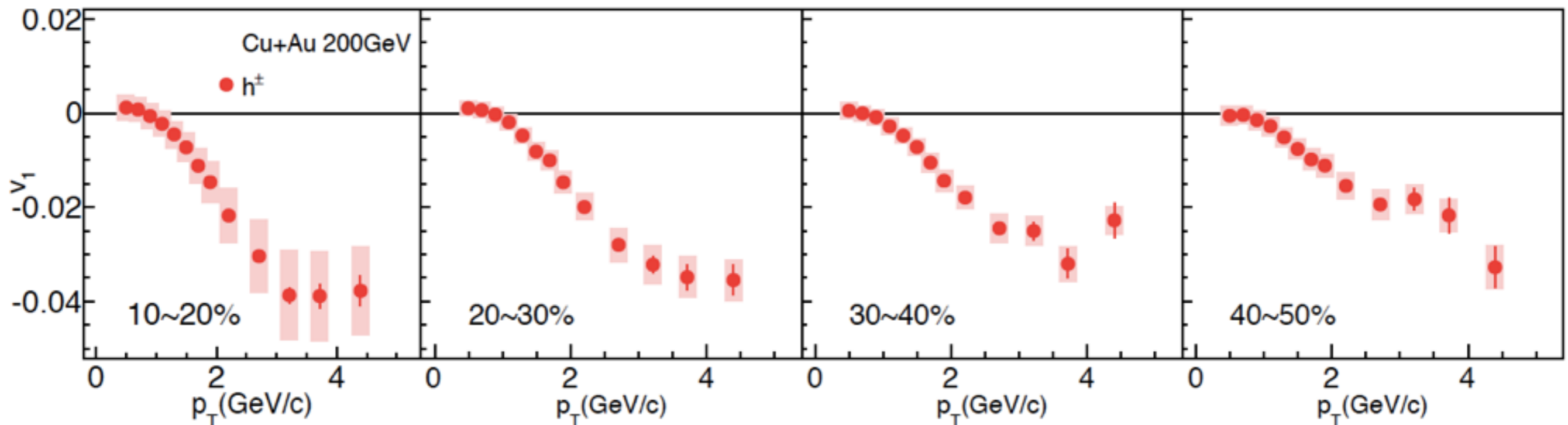
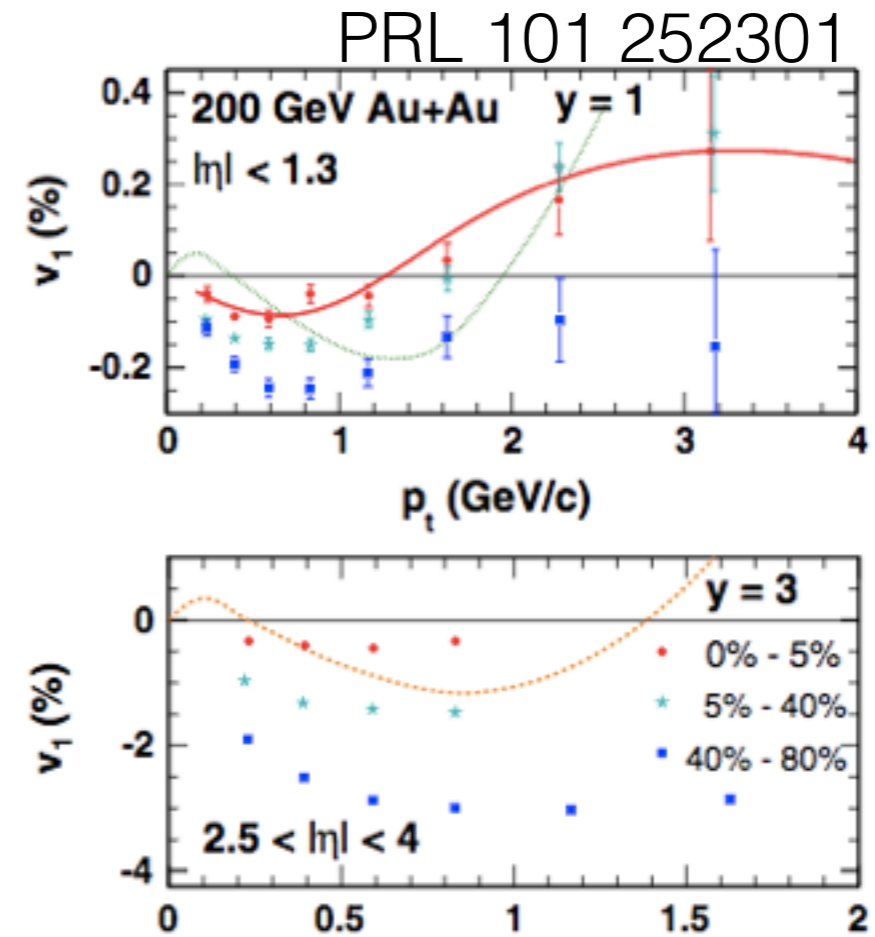
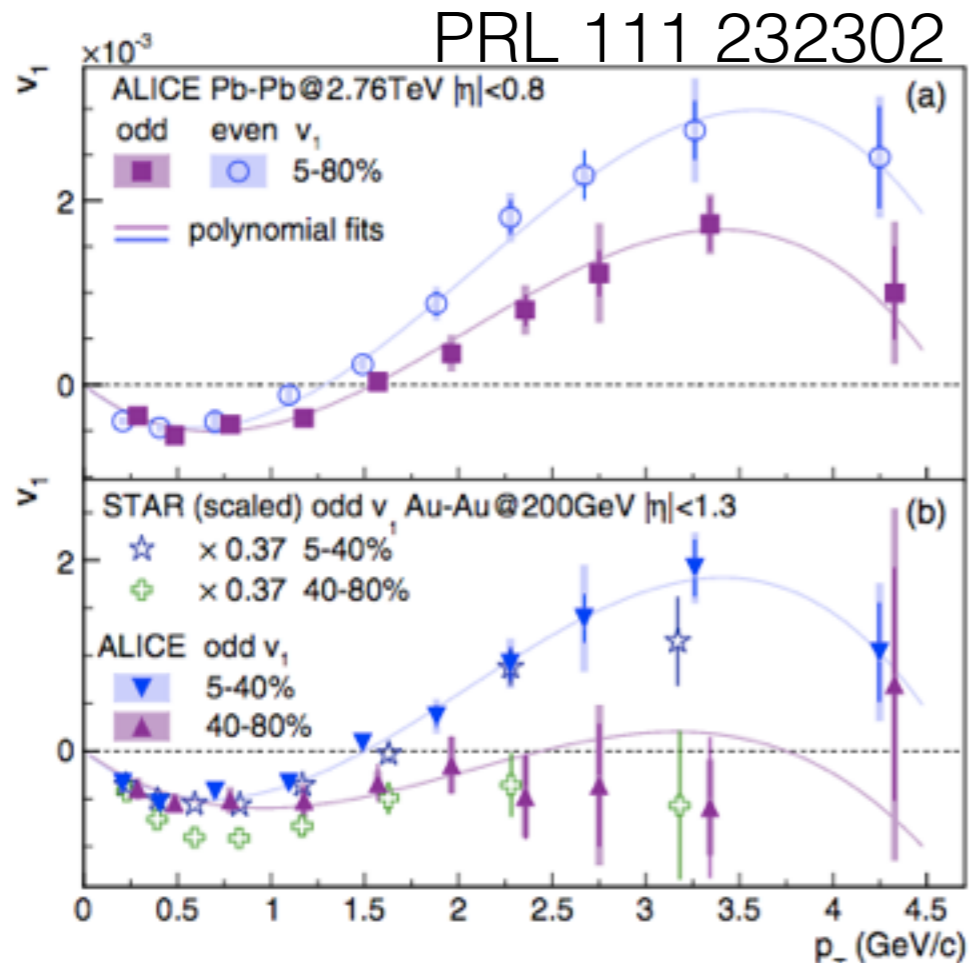


✓ AMPT show the F/B asymmetry of v_3
 - v_3 (Au-going) $>$ v_3 (Cu-going)
 -> Fluctuated longitudinal density show larger F/B asymmetry of v_n

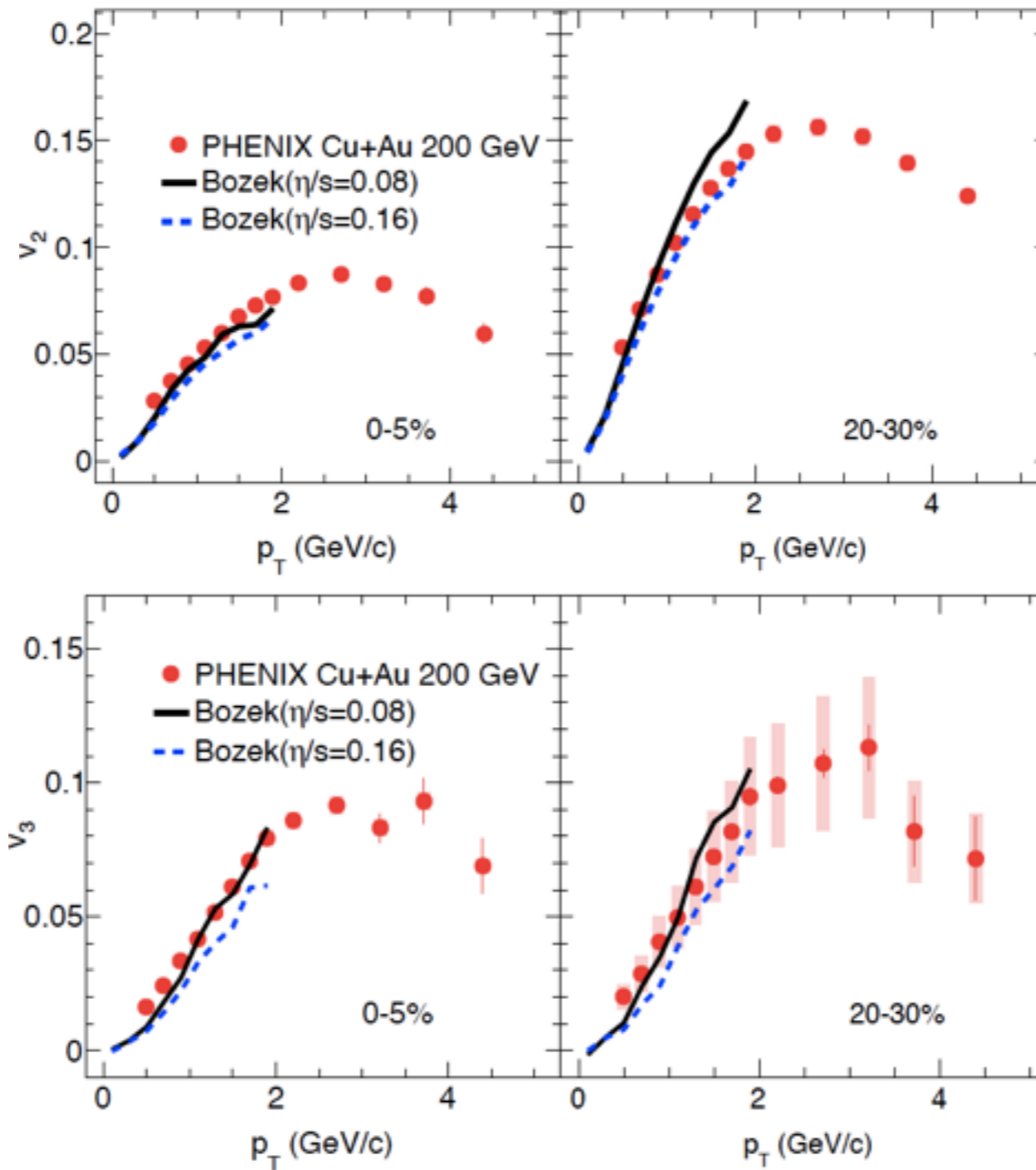
✓ Hydrodynamics show weak F/B asymmetry of v_3
 - v_3 (Au-going) \sim v_3 (Cu-going)
 -> Smooth longitudinal density show weaker F/B asymmetry of v_n



Directed flow in comparison to STAR and ALICE

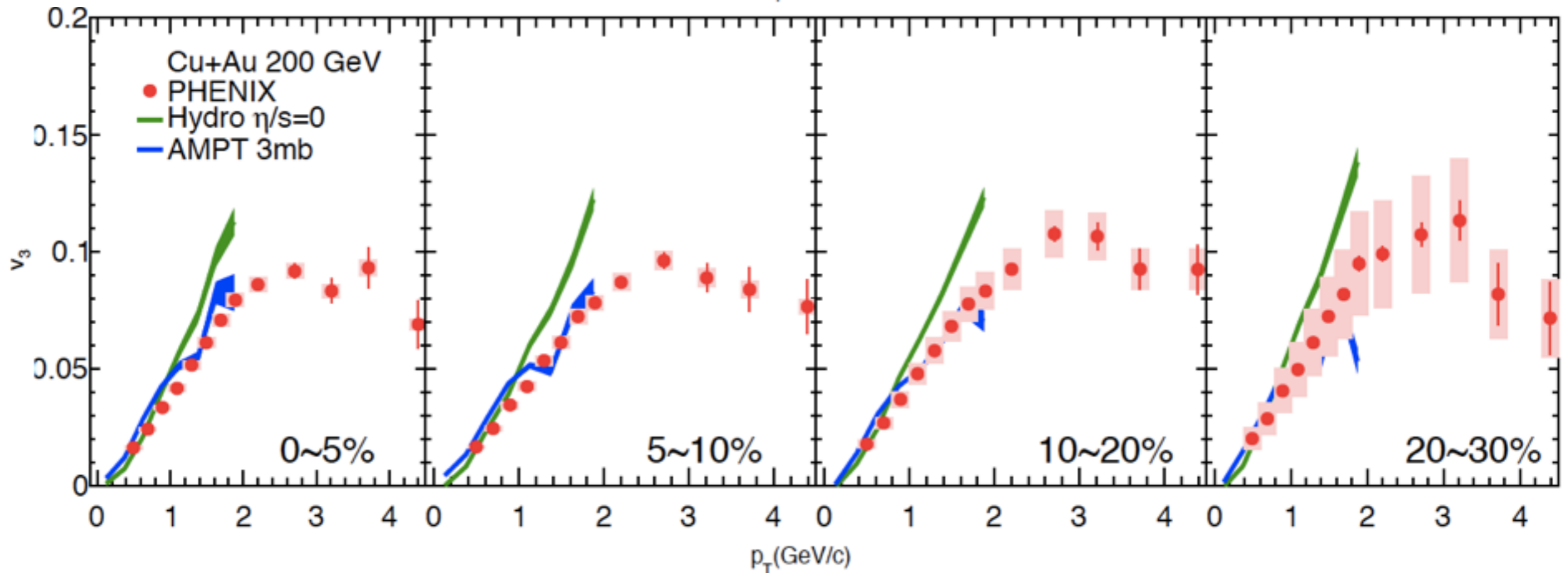
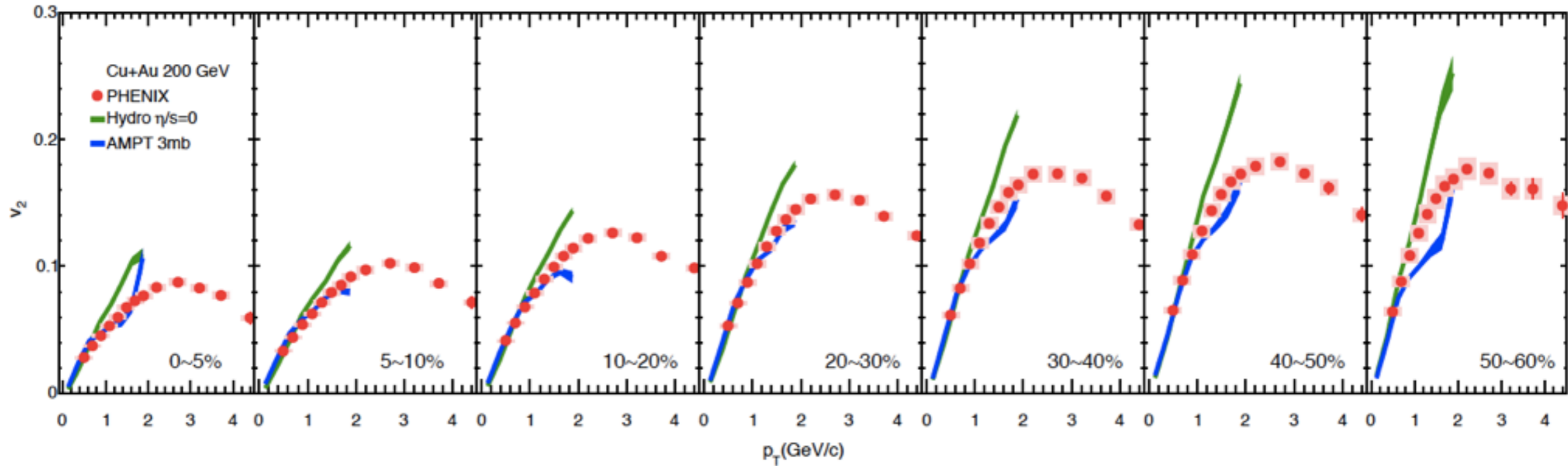


MC-Glauber E-by-E hydro v_2, v_3 at mid- η



For both centrality, both value of η/s agree with data

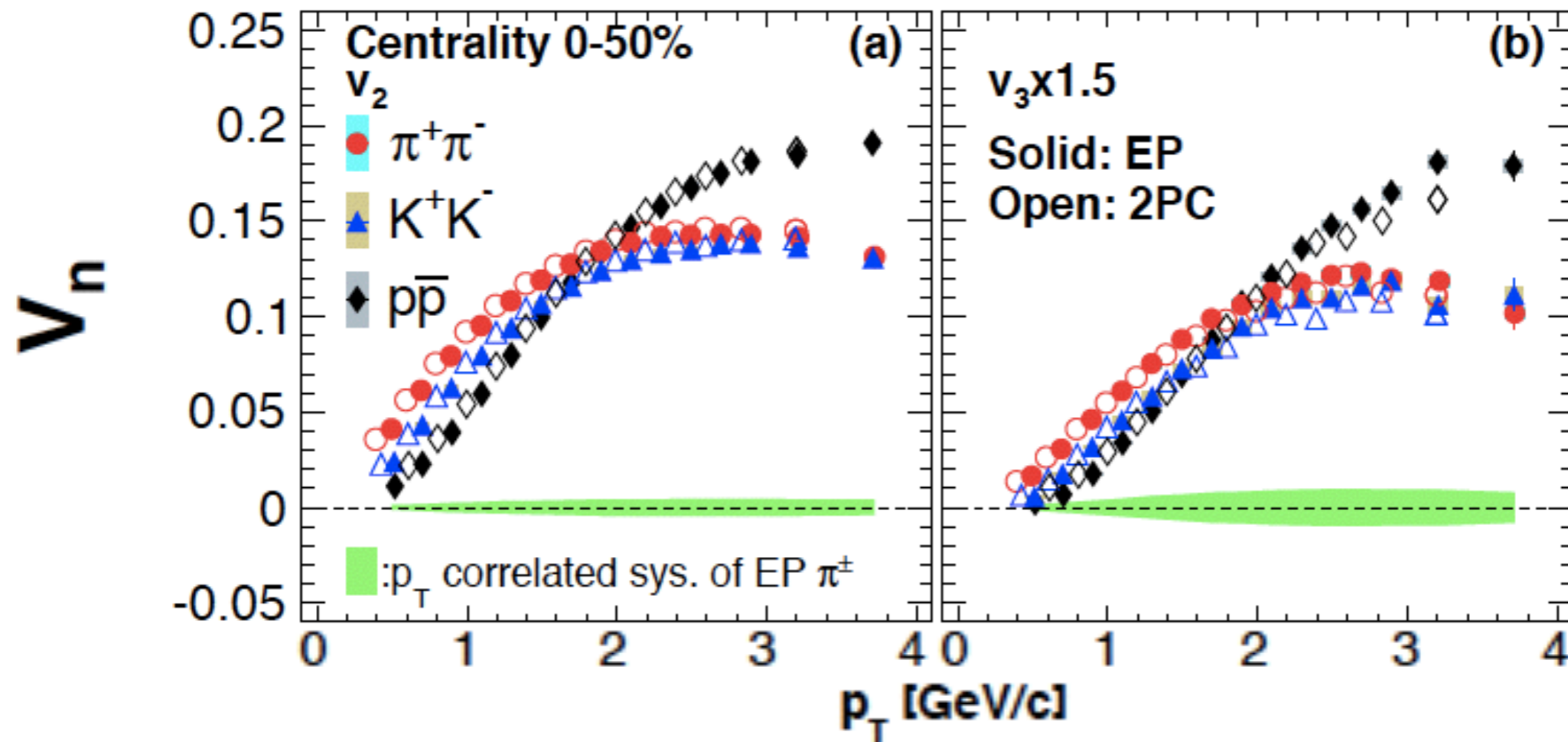
v_n : AMPT and Hydrodynamics





pi, K, p flow

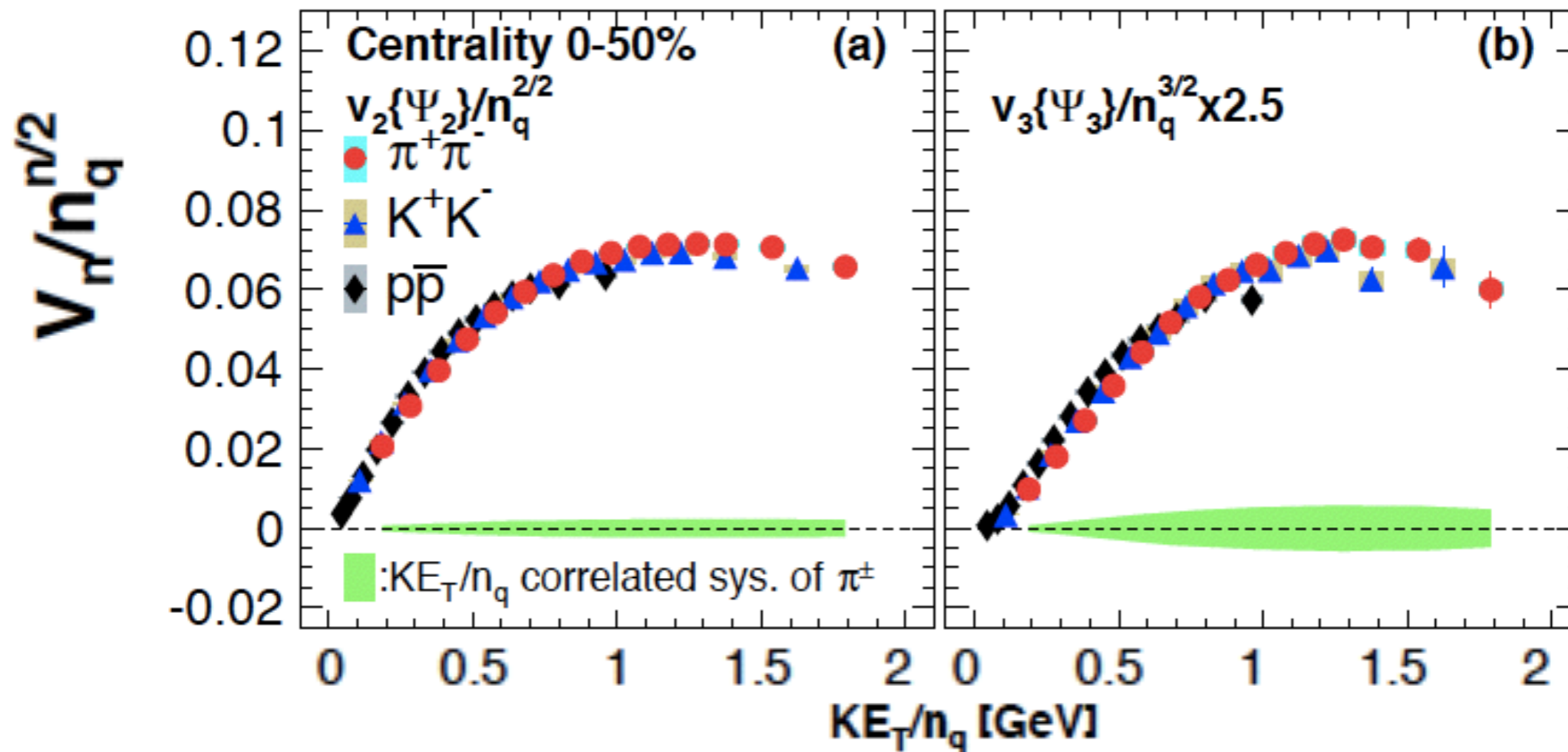
arXiv:1412.1038



v_2, v_3 have similar particle dependence
 v_3 scaled with $n_q^{3/2}$

Scaling property : quark number scaling

arXiv:1412.1038



v_2, v_3 have similar particle dependence
 v_3 scaled with $n_q^{3/2}$

Track identification at CNT ($|\eta| < 0.35$)

TOF.E and TOF.W are used

- TOF.E : Scintillation counter 130ps
- TOF.W : MRPC 95ps

Time of flight method

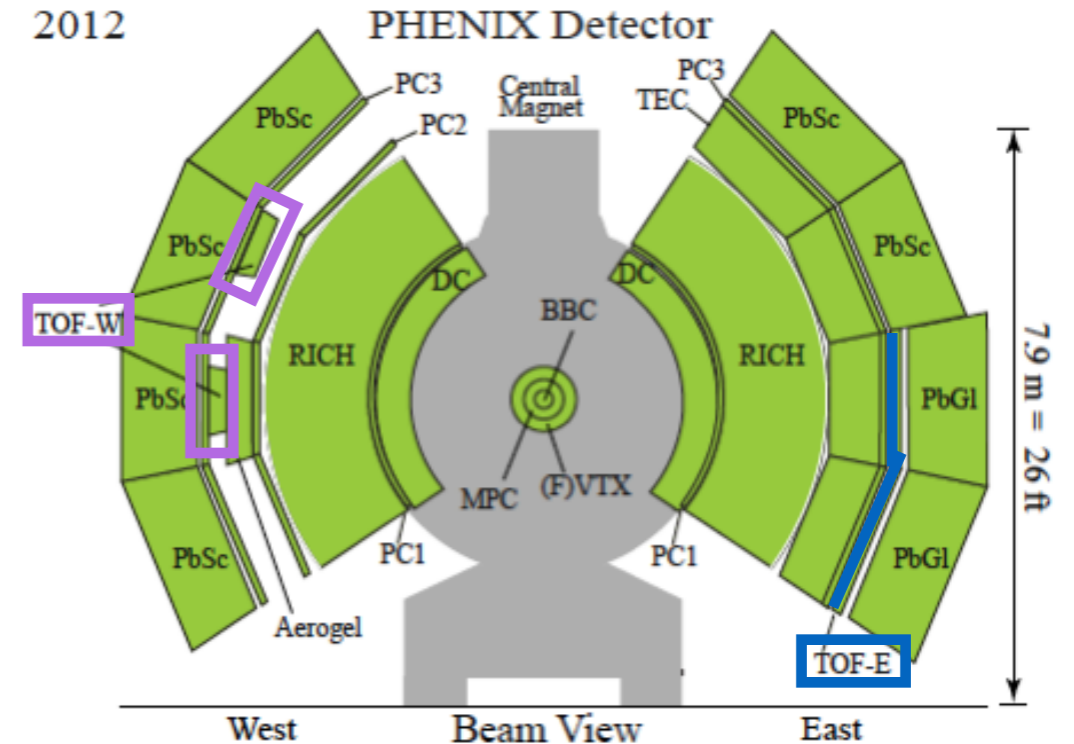
$$m^2 = p^2 \left(\left(\frac{ct}{L} \right)^2 - 1 \right)$$

m:particle mass, p:momentum, L:flight pass
c:light velocity, t:time of flight

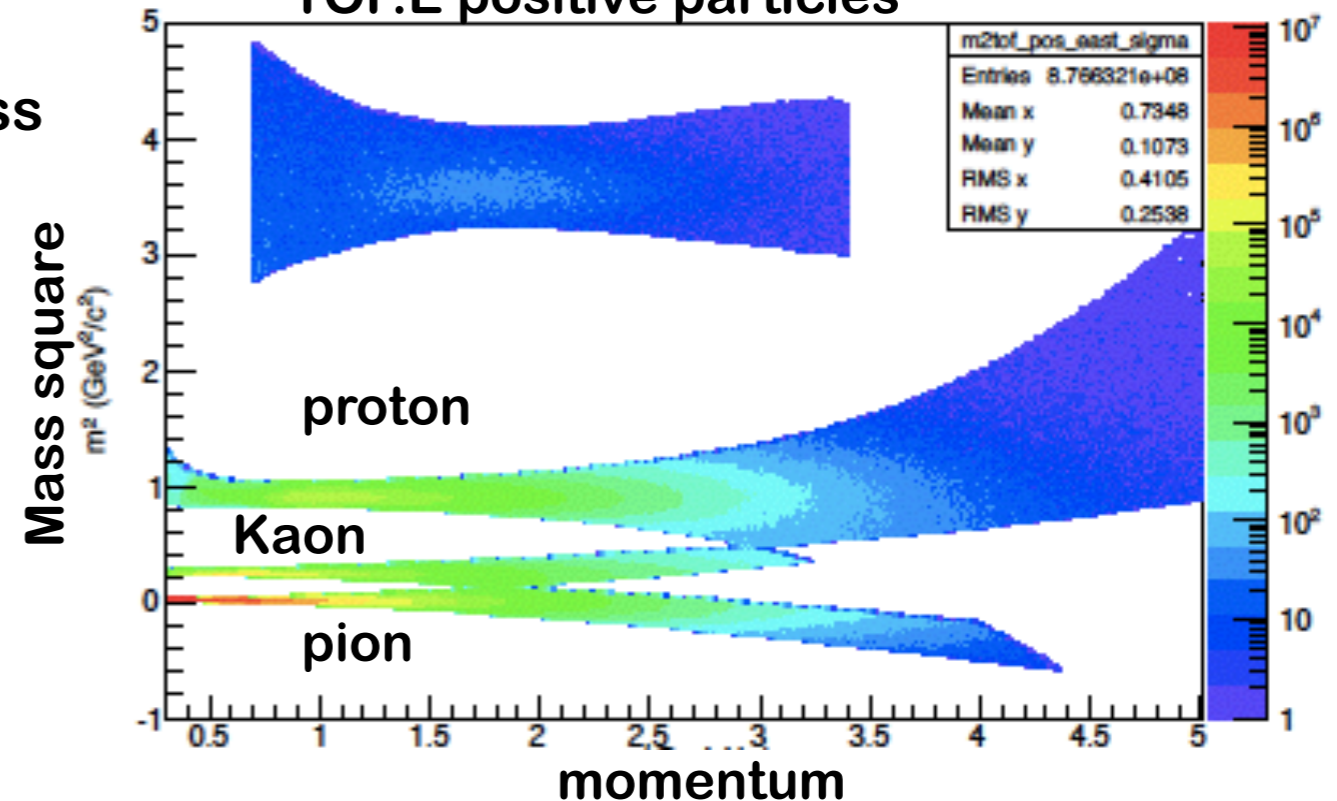
Charged pi,K,p

-pi/K up to 3GeV

-K/p up to 4GeV



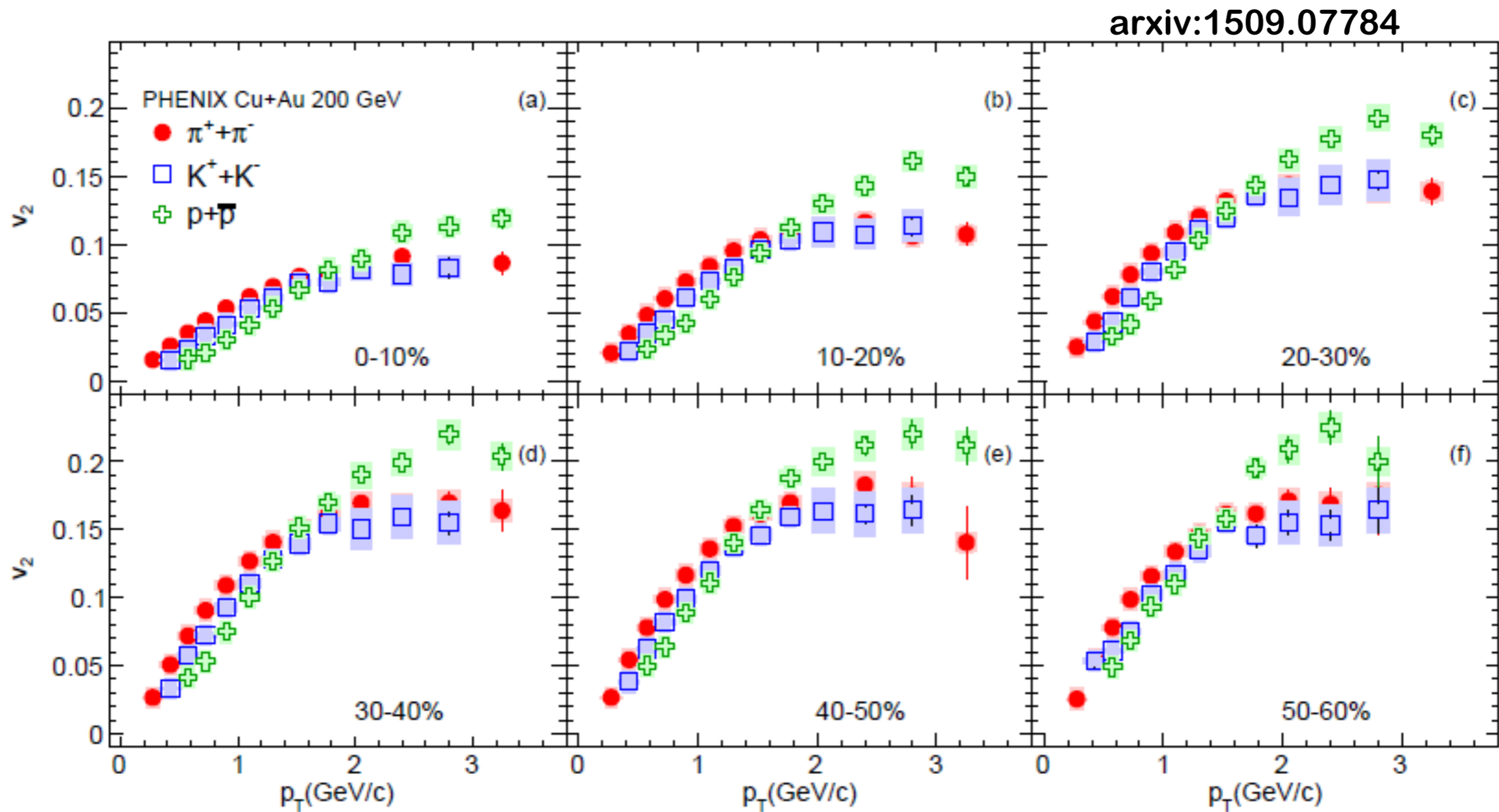
TOF.E positive particles



Results & Discussions

- System size dependence
- **PID** v_n
- Rapidity dependence
- Theory comparison

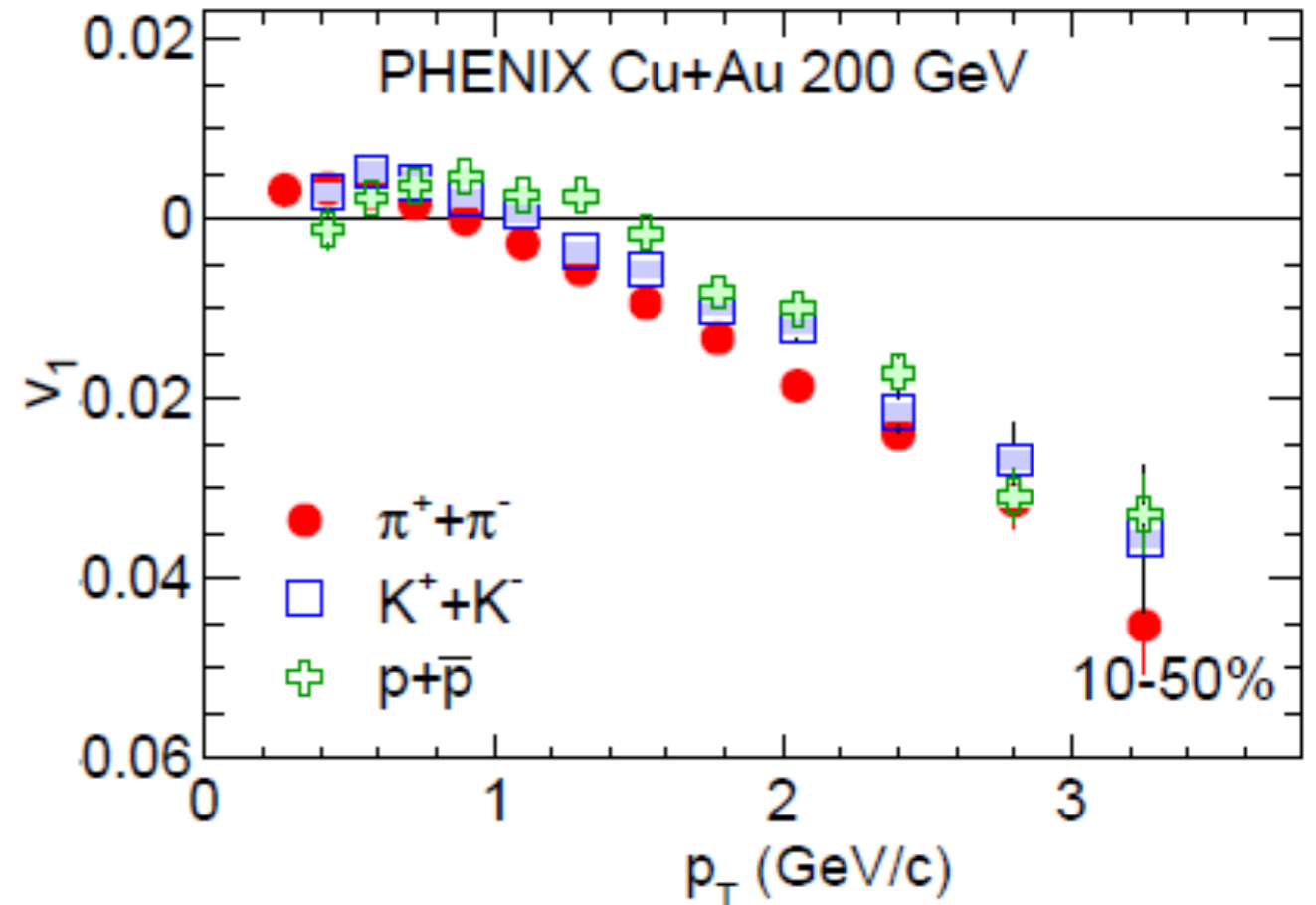
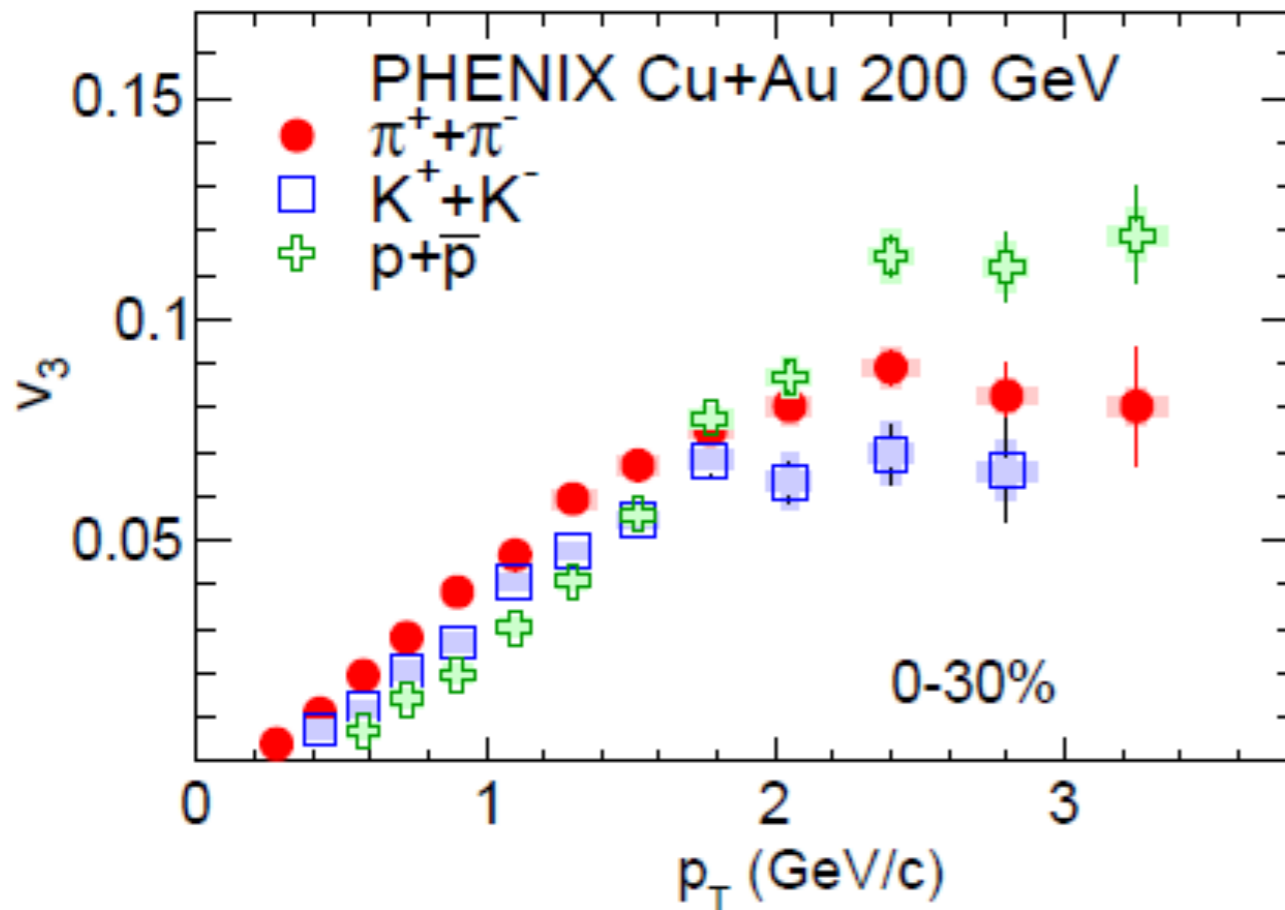
Identified particle v_2 in Cu+Au



Mass ordering at low p_T for v_2 for all centralities
Baryon and meson splitting at mid- p_T is seen

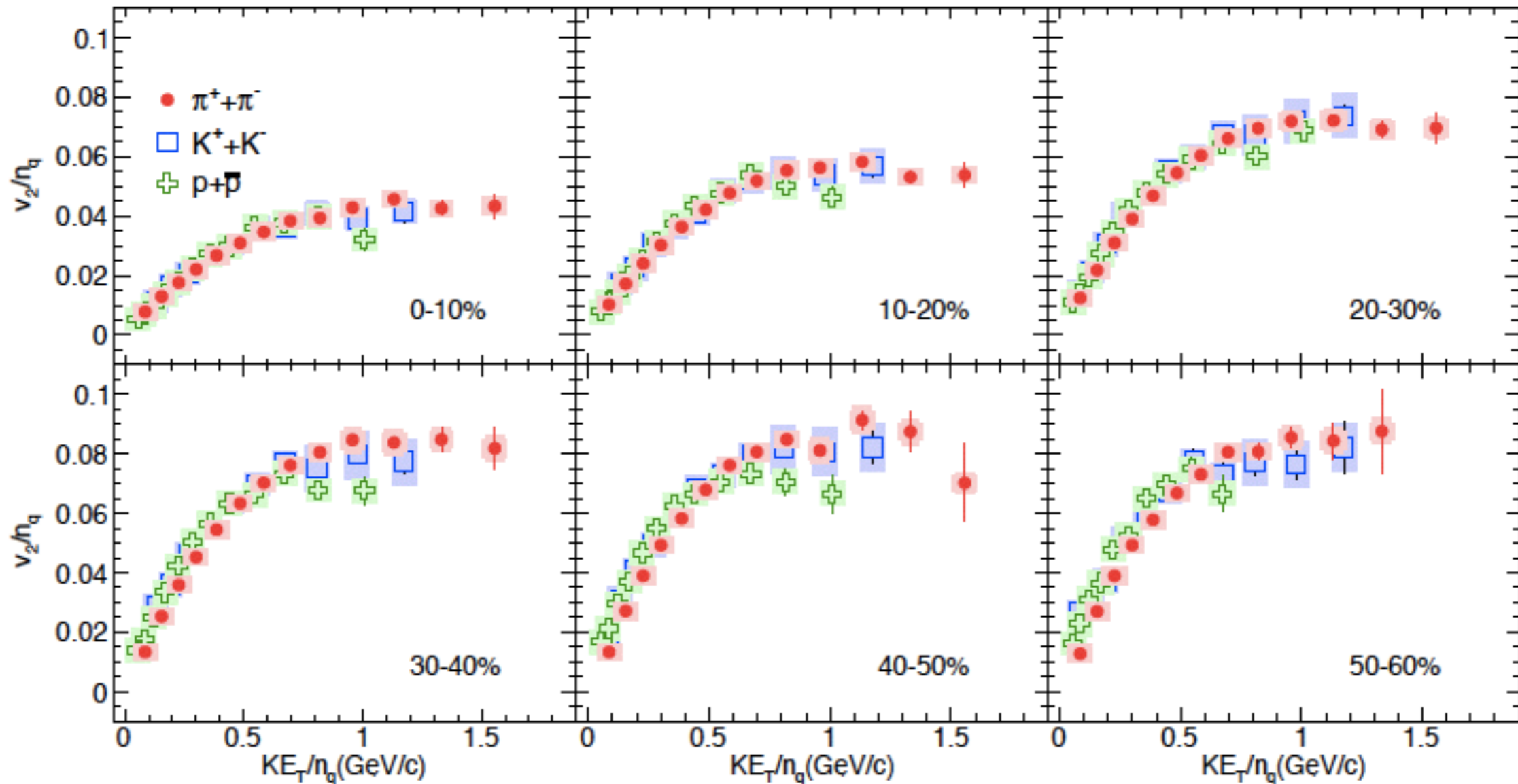
Identified particle v_1, v_3 in Cu+Au

arxiv:1509.07784



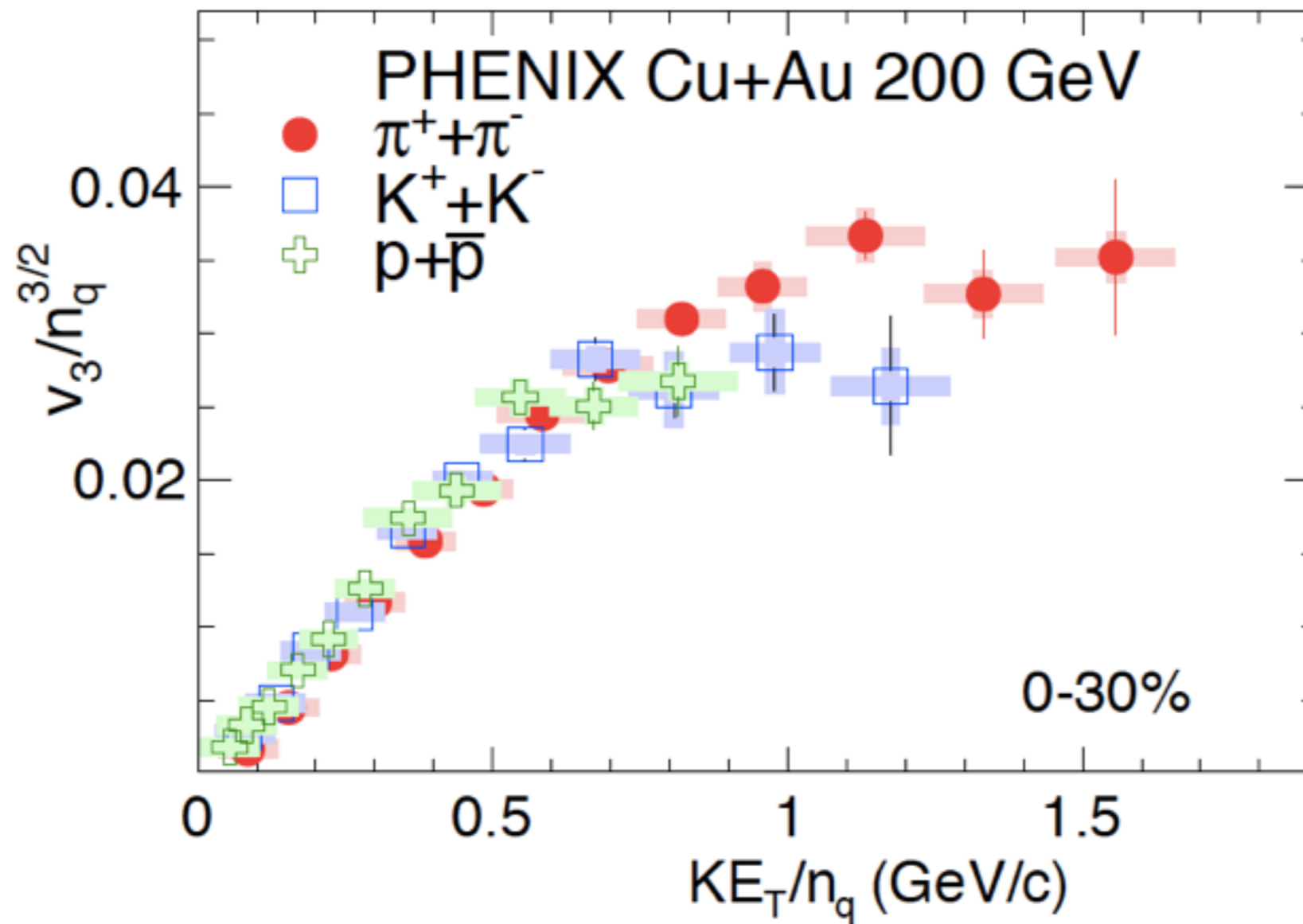
- Same particle dependence of v_3 is seen as seen in v_2
 Mass ordering is also seen for v_1
- At $1 < p_T < 2.5$ GeV, Mass ordering is seen
 - At low and high p_T region, baryon $v_1 \sim$ meson v_1
 - Not same trend as seen in v_2, v_3

Quark Number Scaling of v_2



Quark Number Scaling works v_2 in CuAu

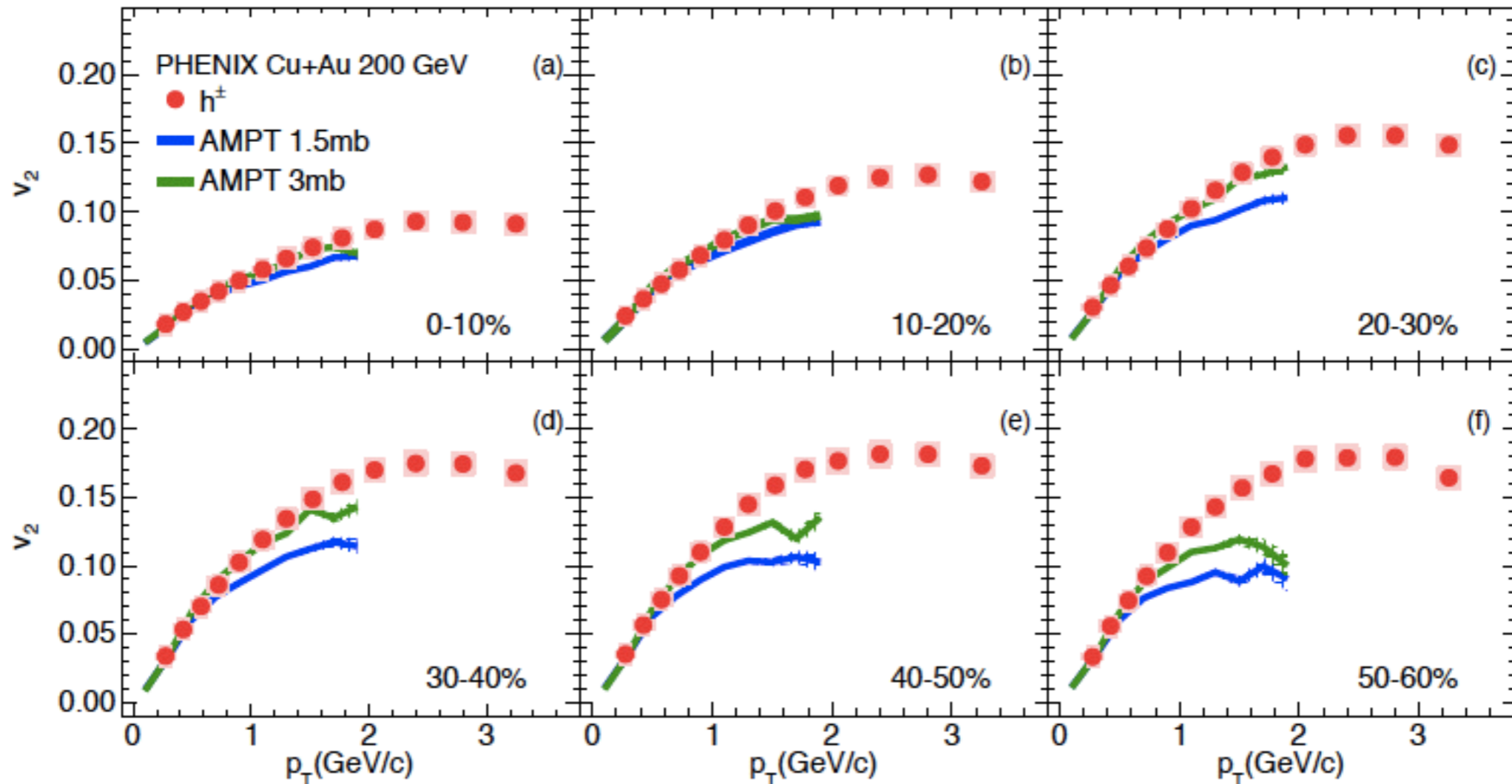
Quark Number Scaling for v3



Quark Number Scaling work v3 in CuAu

Comparison to AMPT v2

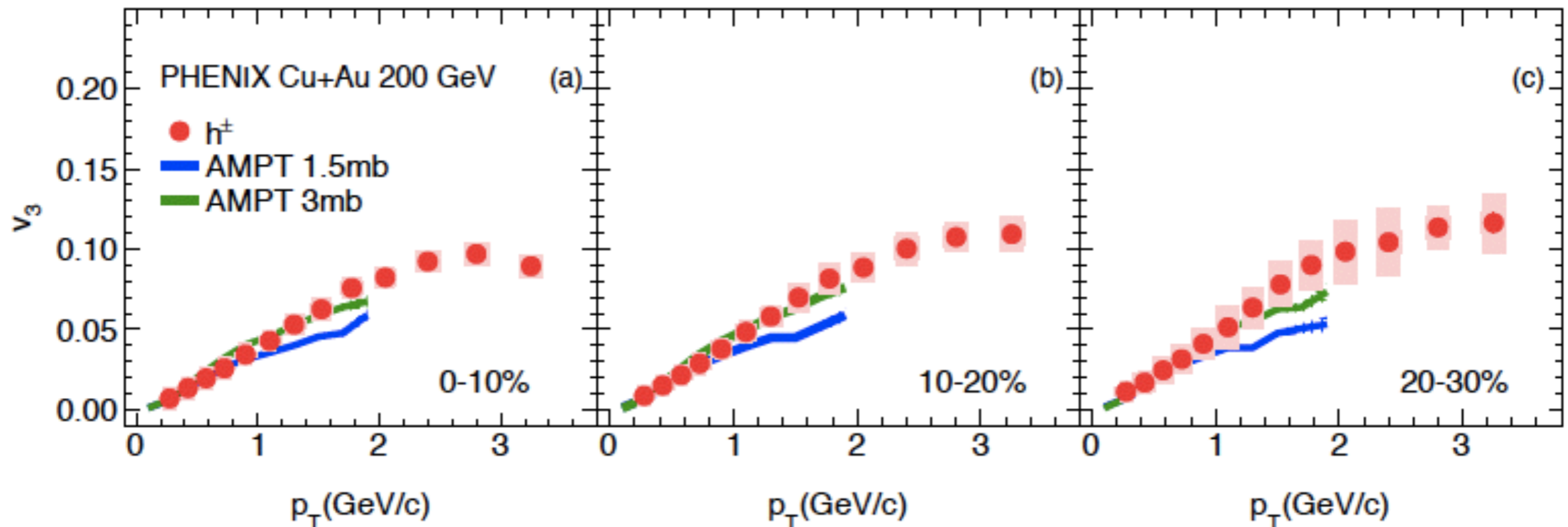
arxiv:1509.07784



AMPT with 3mb reproduce v_2
-In 0-30%, up to 2GeV
-In 30-60%, up to 1GeV

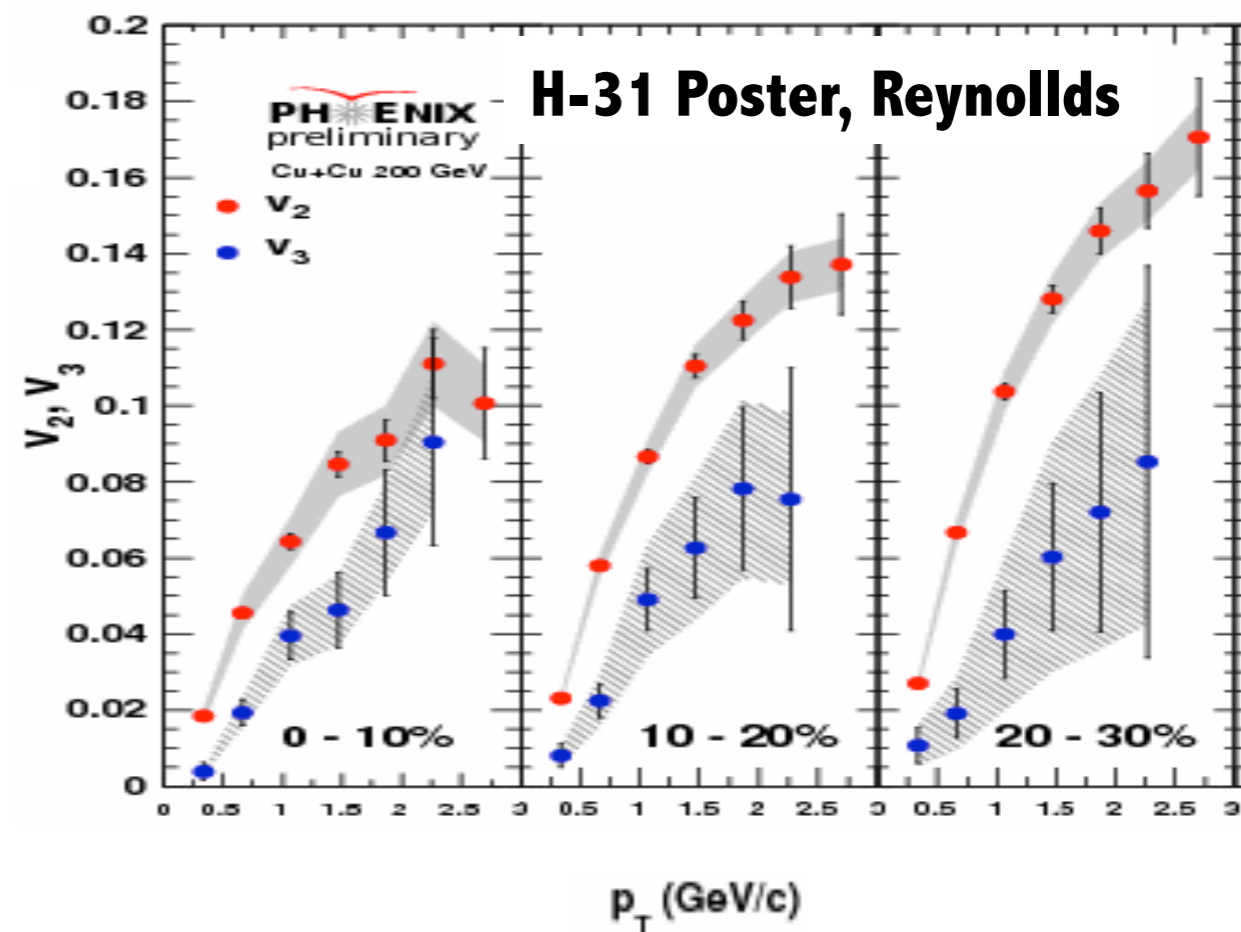
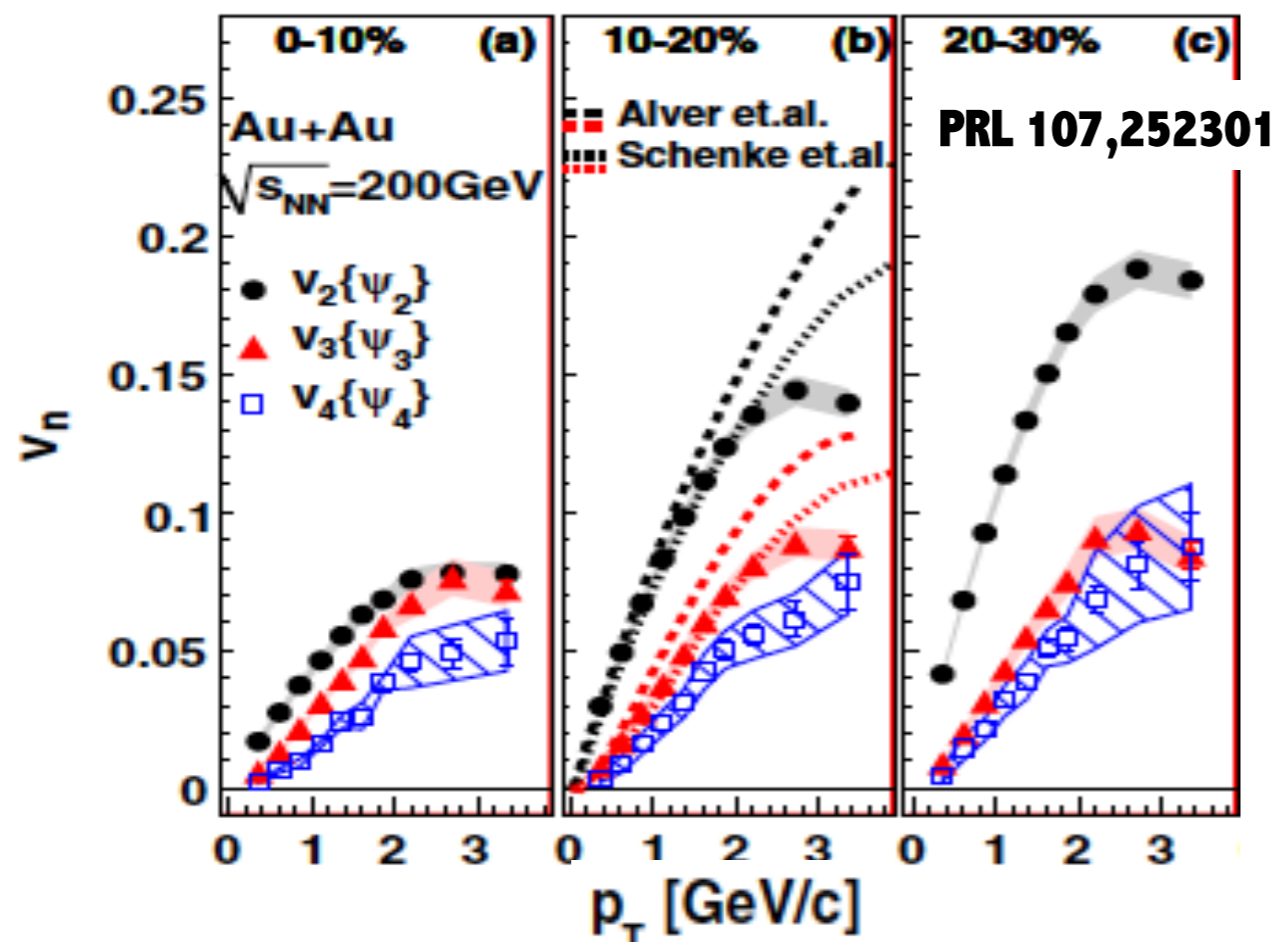
Comparison to AMPT v3

arxiv:1509.07784



**AMPT with 3mb reproduce v_3
-In 0-30%, up to 2GeV**

Flow in symmetric collisions system



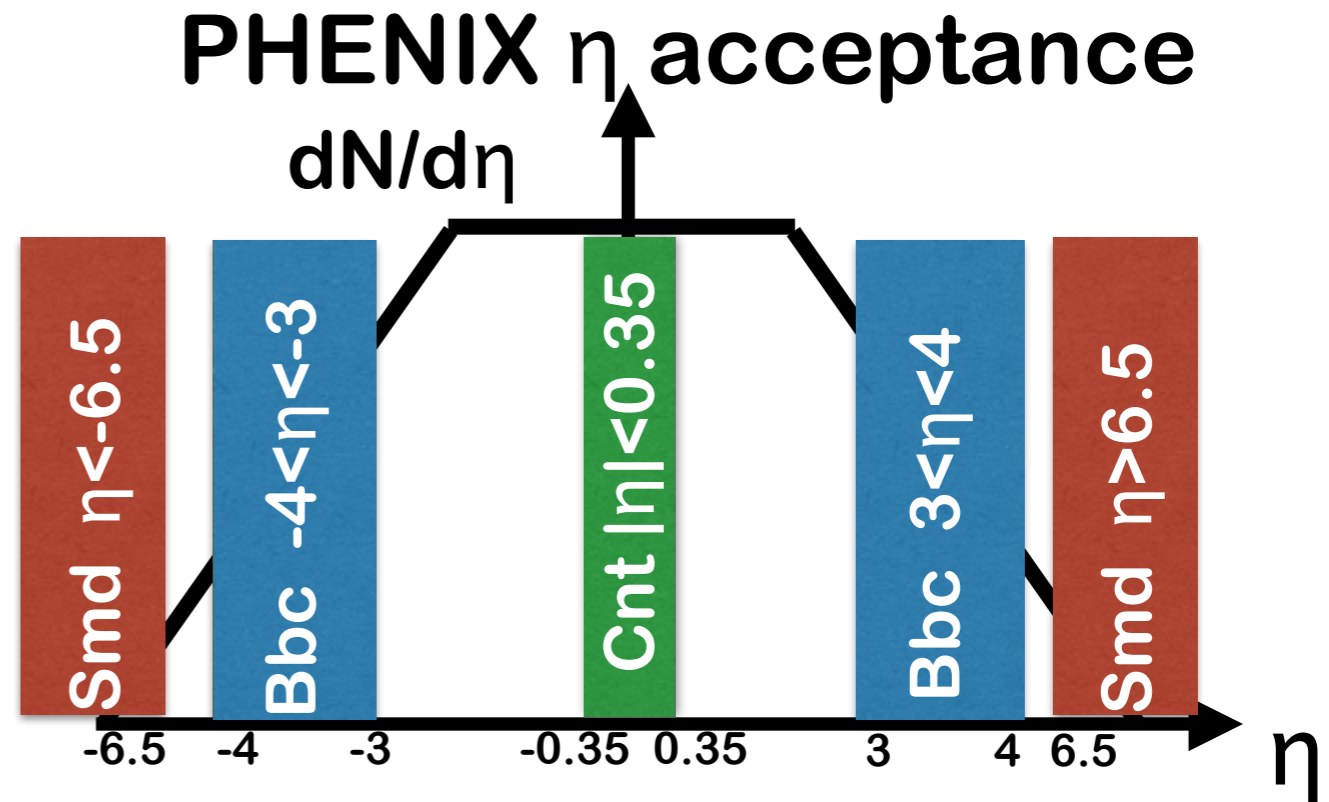
3sub method

Event Plane detectors

- 2nd, 3rd Event plane
- Bbc, Cnt
- 1st Event plane
- Bbc, Smd

Event Plane resolution

-Estimated from EP correlations(3sub method)



$$Res\{\Psi_{n,A}^{obs}\} = \sqrt{\frac{\langle \cos(n[\Psi_{n,A}^{obs} - \Psi_{n,B}^{obs}]) \rangle \langle \cos(n[\Psi_{n,A}^{obs} - \Psi_{n,C}^{obs}]) \rangle}{\langle \cos(n[\Psi_{n,B}^{obs} - \Psi_{n,C}^{obs}]) \rangle}}$$

$$\begin{aligned} \langle \cos(n[\Psi_{n,A}^{obs} - \Psi_{n,B}^{obs}]) \rangle &= \langle \cos(n[\Psi_{n,A}^{obs} - \Psi_n^{true} + \Psi_n^{true} - \Psi_{n,B}^{obs}]) \rangle \\ &= \langle \cos(n[\Psi_{n,A}^{obs} - \Psi_n^{true}]) \rangle \langle \cos(n[\Psi_n^{true} - \Psi_{n,B}^{obs}]) \rangle \\ &= Res\{\Psi_{n,A}\} Res\{\Psi_{n,B}\} \end{aligned}$$

Average v_n at Mid-rapidity

How to integrate $v_n(p_T)$

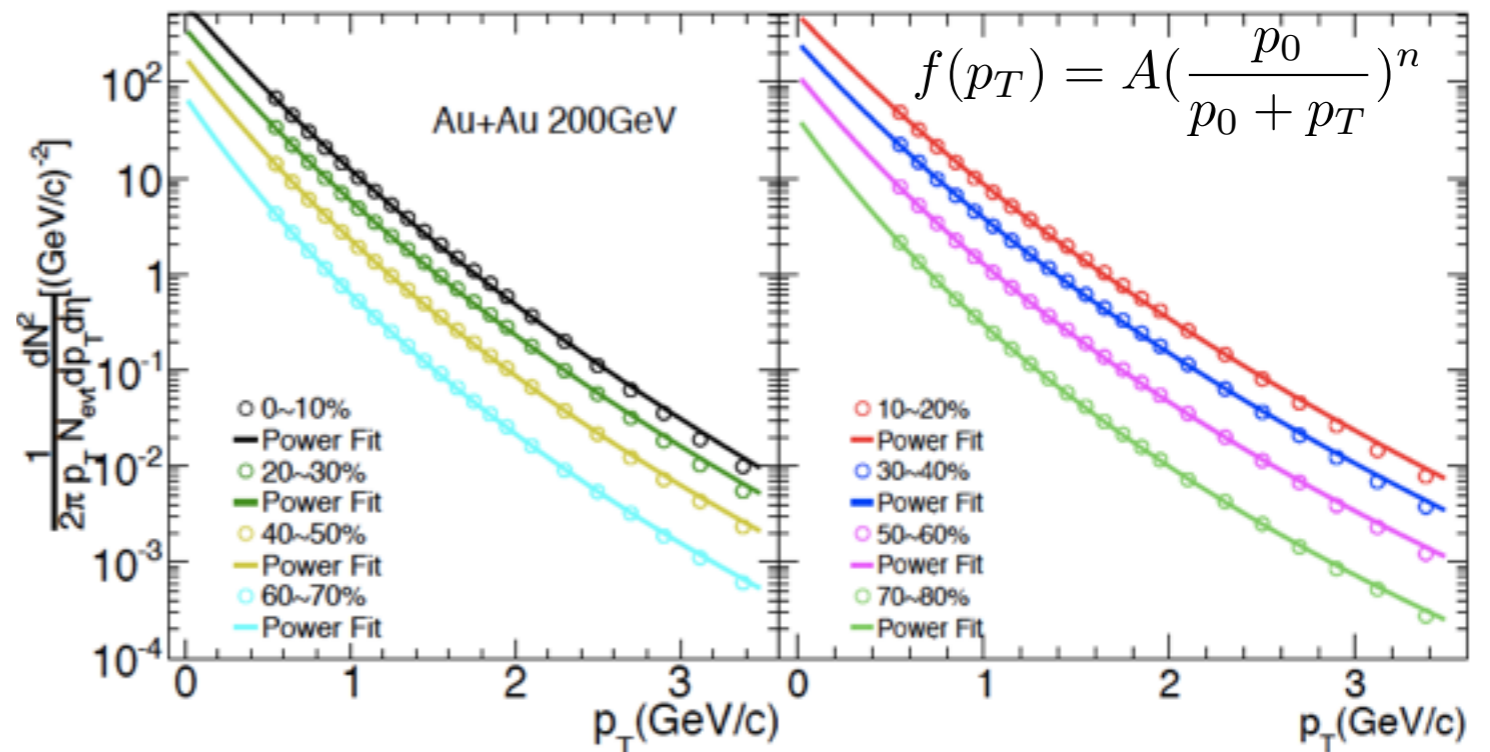
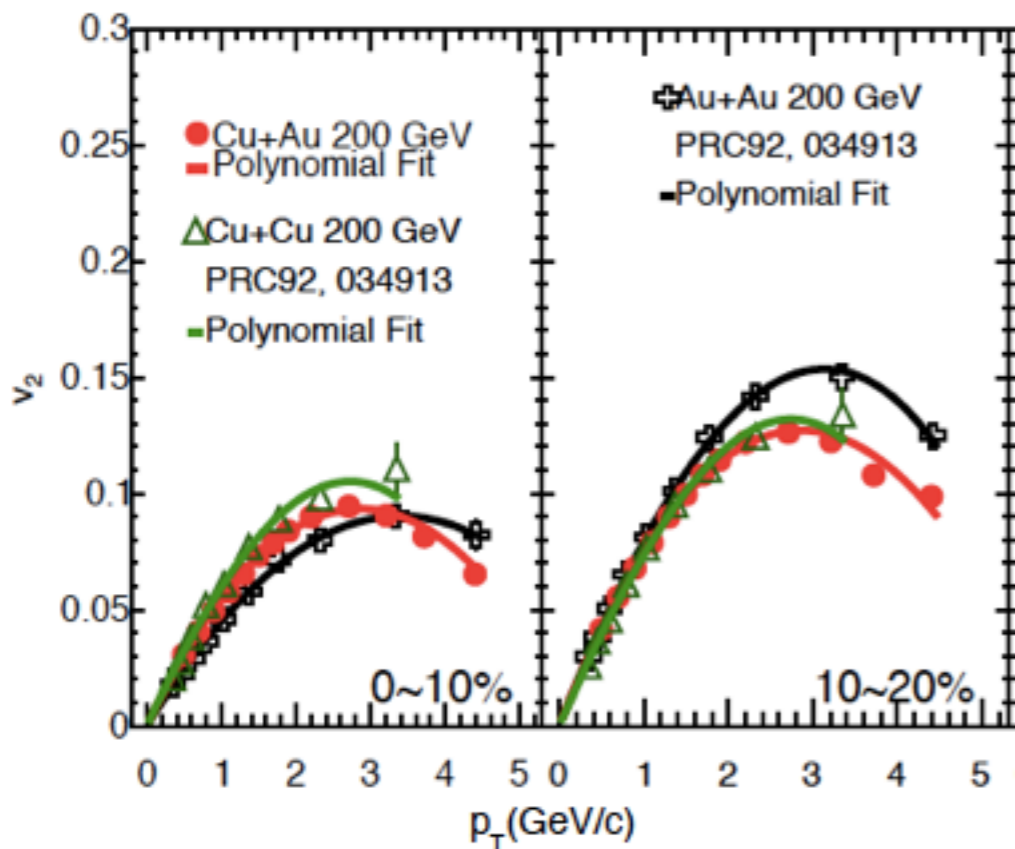
Weighted average using p_T spectra as weights

- p_T spectra: PHENIX AuAu (ppg023)

- v_n : PHENIX AuAu, CuAu, CuCu (ppg124, 132, 183)

$$\langle v_n \rangle = \frac{\sum_i \frac{dN}{dp_{T,i}} v_n(p_{T,i})}{\sum_i \frac{dN}{dp_{T,i}}}$$

- $v_n(p_{T,i})$ and $dN/dp_{T,i}$ values are obtained from fitting functions



Determination of pT spectra in Cu+Cu and Cu+Au

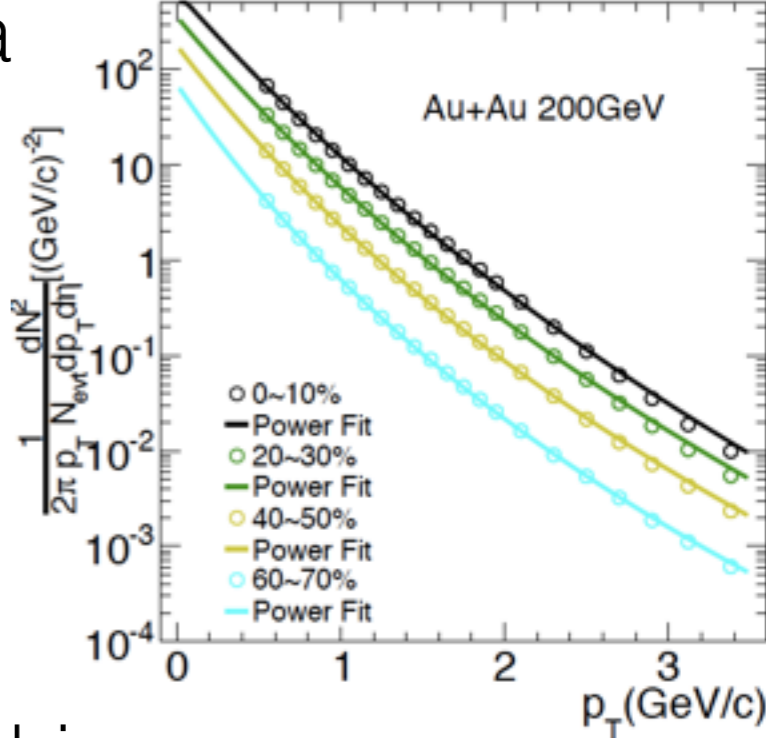
Cu+Cu and Cu+Au spectra are assumed using Au+Au spectra

-There no published Cu+Cu and Cu+Au spectra

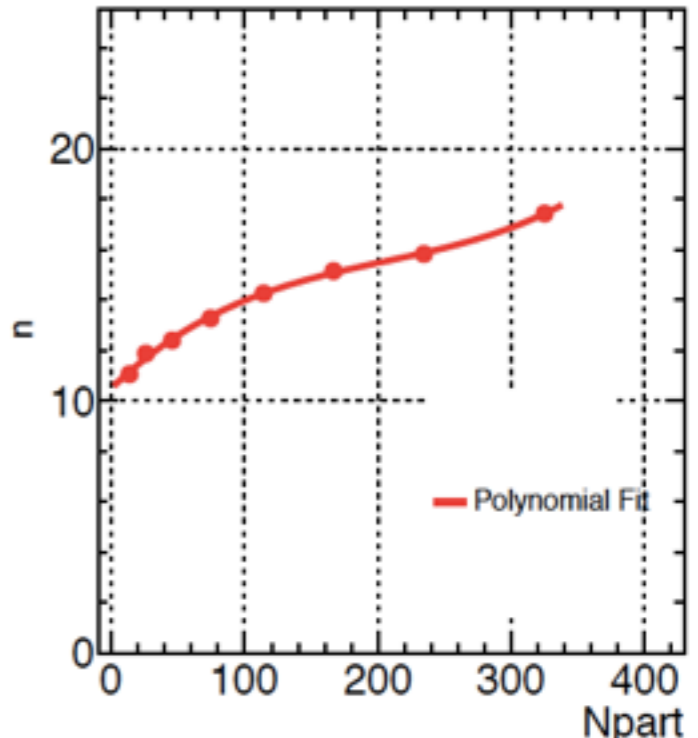
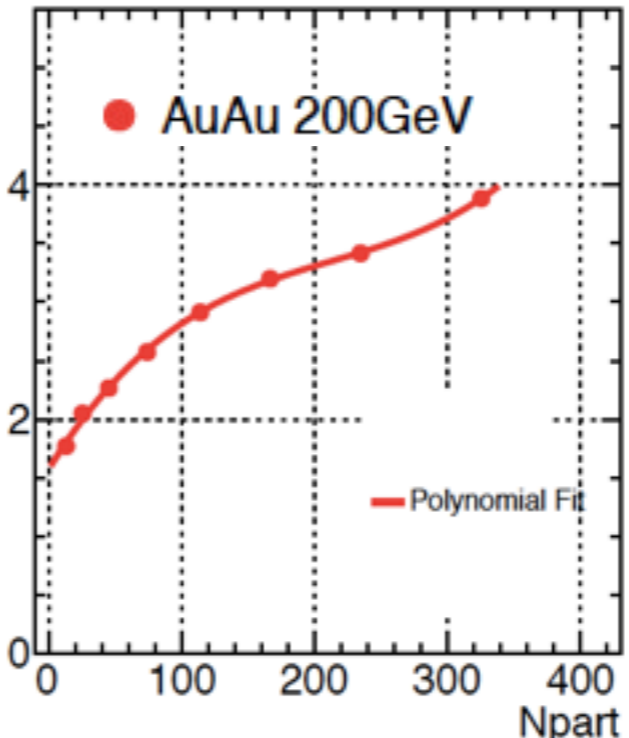
- $dN_{ch}/d\eta$ and $\langle p_T \rangle$ depends on N_{part}

Procedure

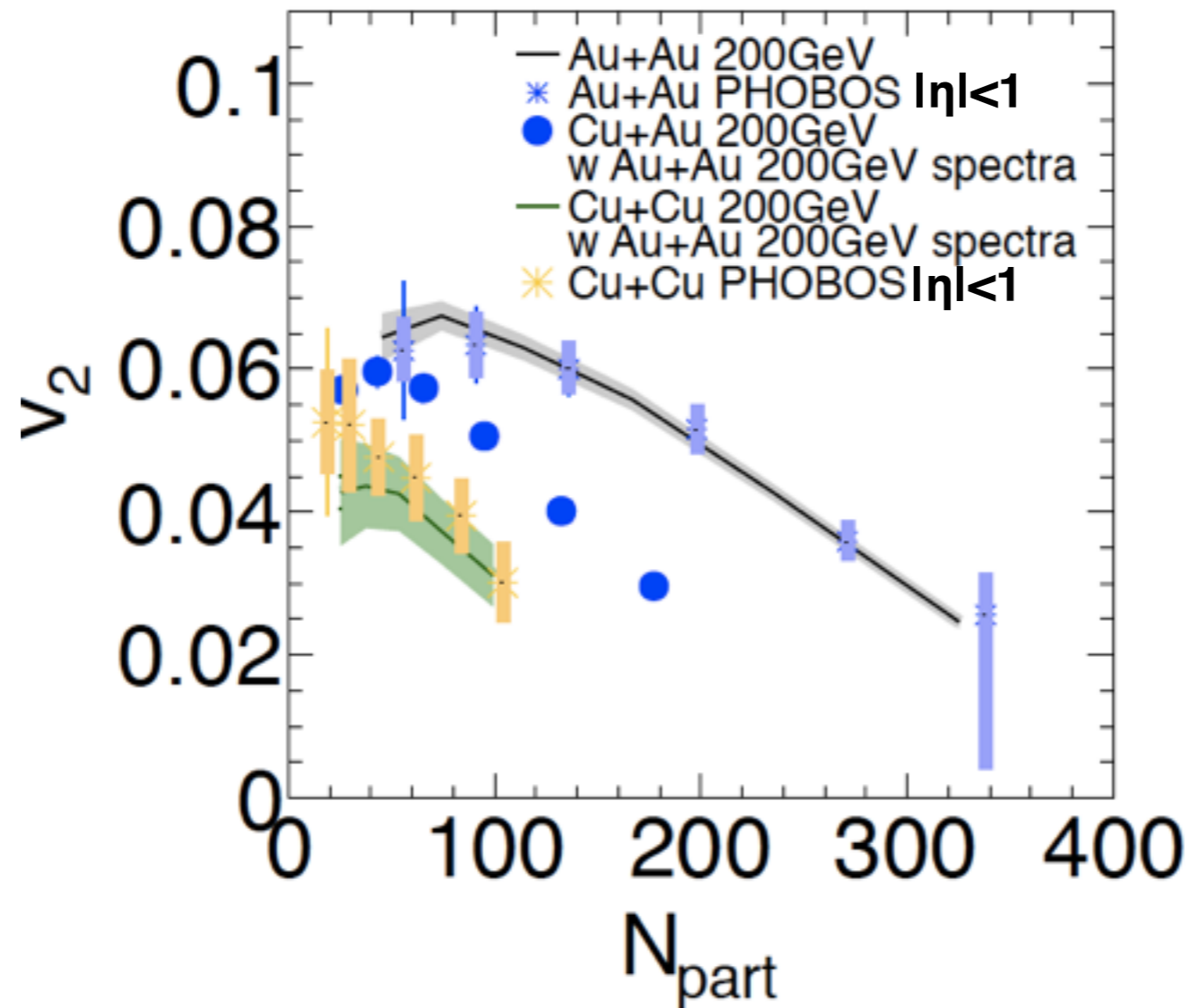
1. Fit Au+Au spectra with $f(p_T) = A \left(\frac{p_0}{p_0 + p_T} \right)^n$
 p_0 and n are free parameter
2. Obtain p_0 and n as a function of N_{part}
3. Make pT spectra for Cu+Cu and Cu+Au
 using $p_0(N_{part})$ and $n(N_{part})$ for corresponding N_{part} bins



$$f(p_T, N_{part}) = \left(\frac{p_0(N_{part})}{p_0(N_{part}) + p_T} \right)^{n(N_{part})}$$



Comparison to PHOBOS



My results are consistent with PHOBOS within the error
- η range is different, PHOBOS's results are obtained wider range
pT integration is successfully done