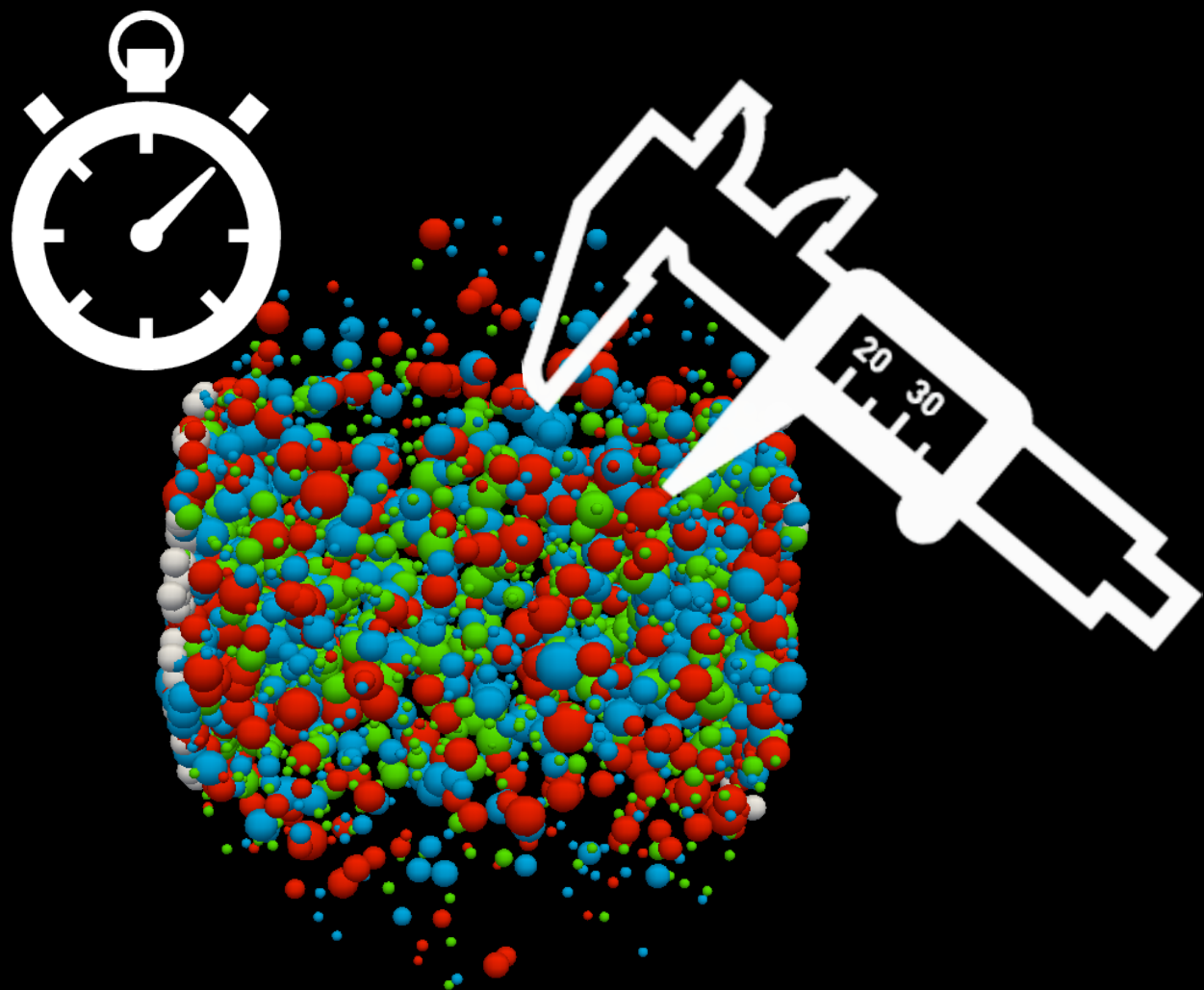


# Measurements of Azimuthal Angle Dependence of HBT radii with respect to event plane in $\sqrt{s_{NN}} = 2.76$ TeV Pb-Pb collisions at LHC-ALICE



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2018.January.24

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High Energy Nuclear Physics  
Group

# Outline

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## ✓ Introduction

- Quark Gluon Plasma
- HBT interferometry

## ✓ Experiment & Analysis

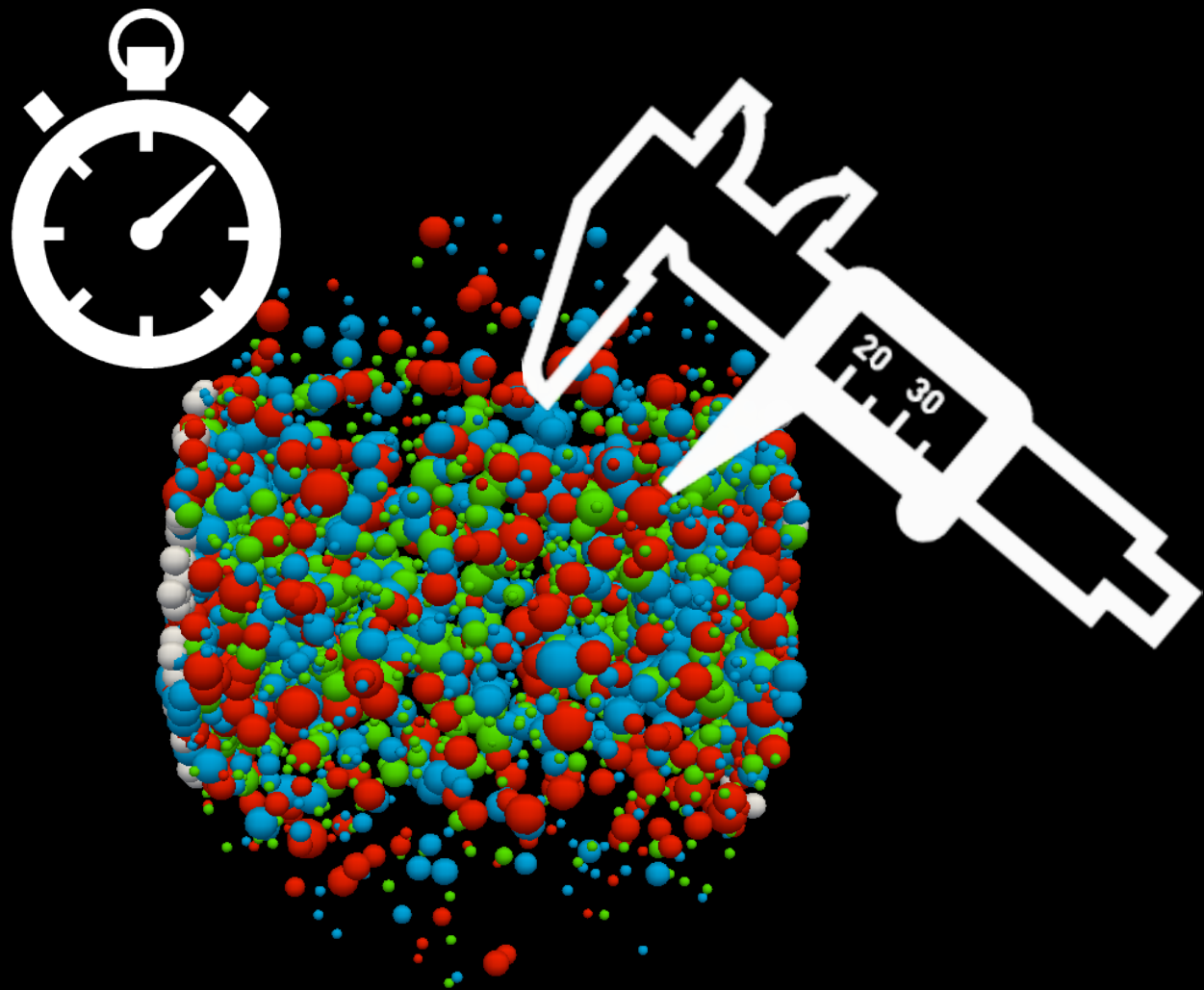
- ALICE
- Analysis methods

## ✓ Result & Discussions

- Azimuthal angle dependence of HBT radii w.r.t.  $\Psi_2$
- Azimuthal anisotropy ( $v_2$  and  $v_3$ ) with ESE cut
- Azimuthal angle dependence of HBT radii w.r.t.  $\Psi_2 + q_2$  cut
- Interpretation with Blast-wave fit
- Azimuthal angle dependence of HBT radii w.r.t.  $\Psi_3$
- Azimuthal angle dependence of HBT radii w.r.t.  $\Psi_3 + q_3$  cut



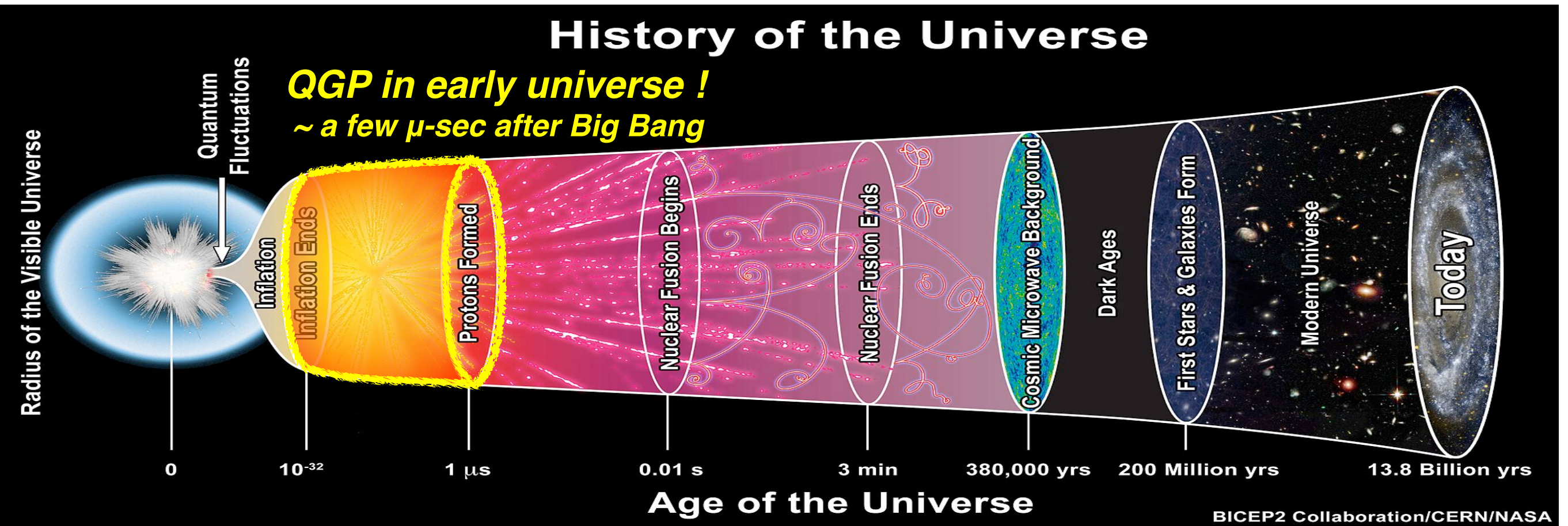
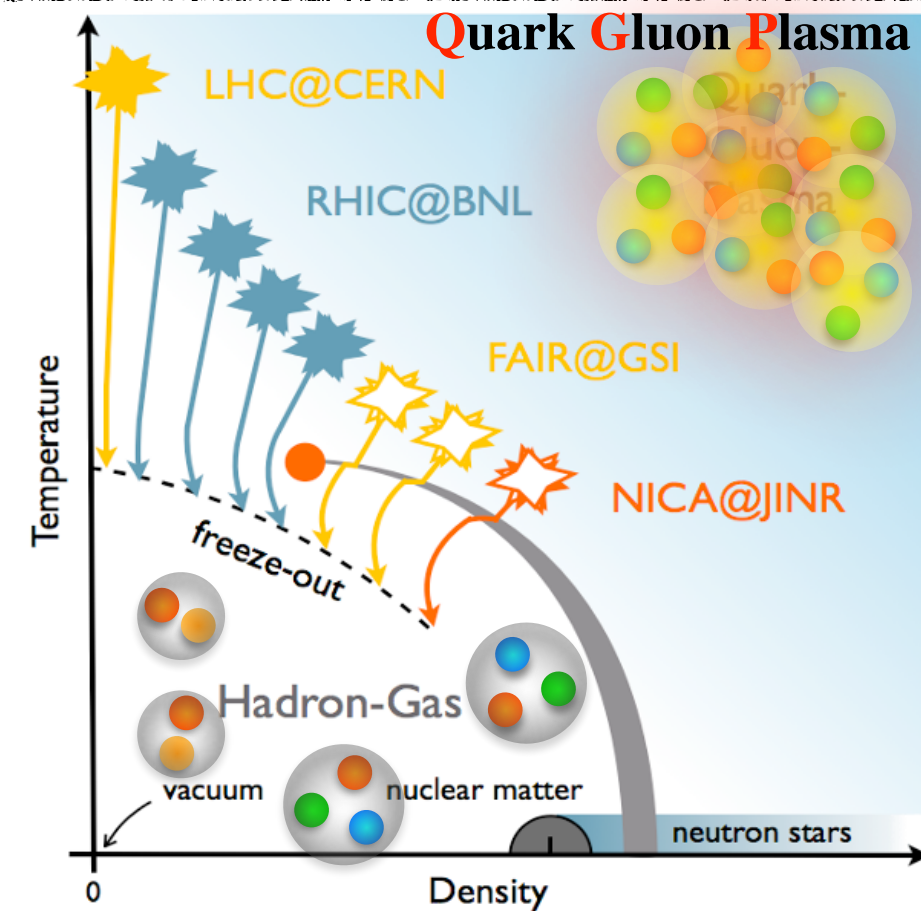
# Introduction



# Quark Gluon Plasma (QGP)

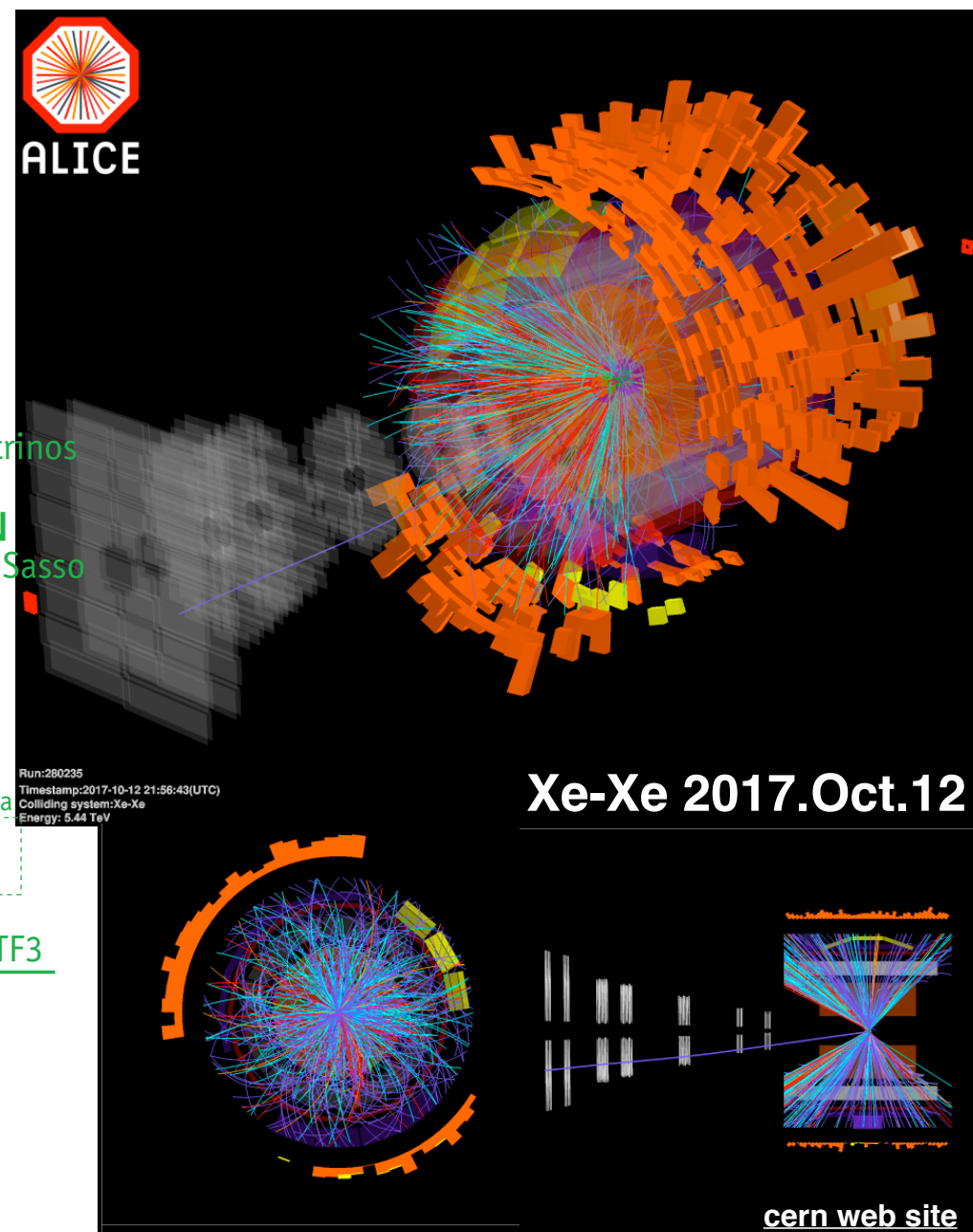
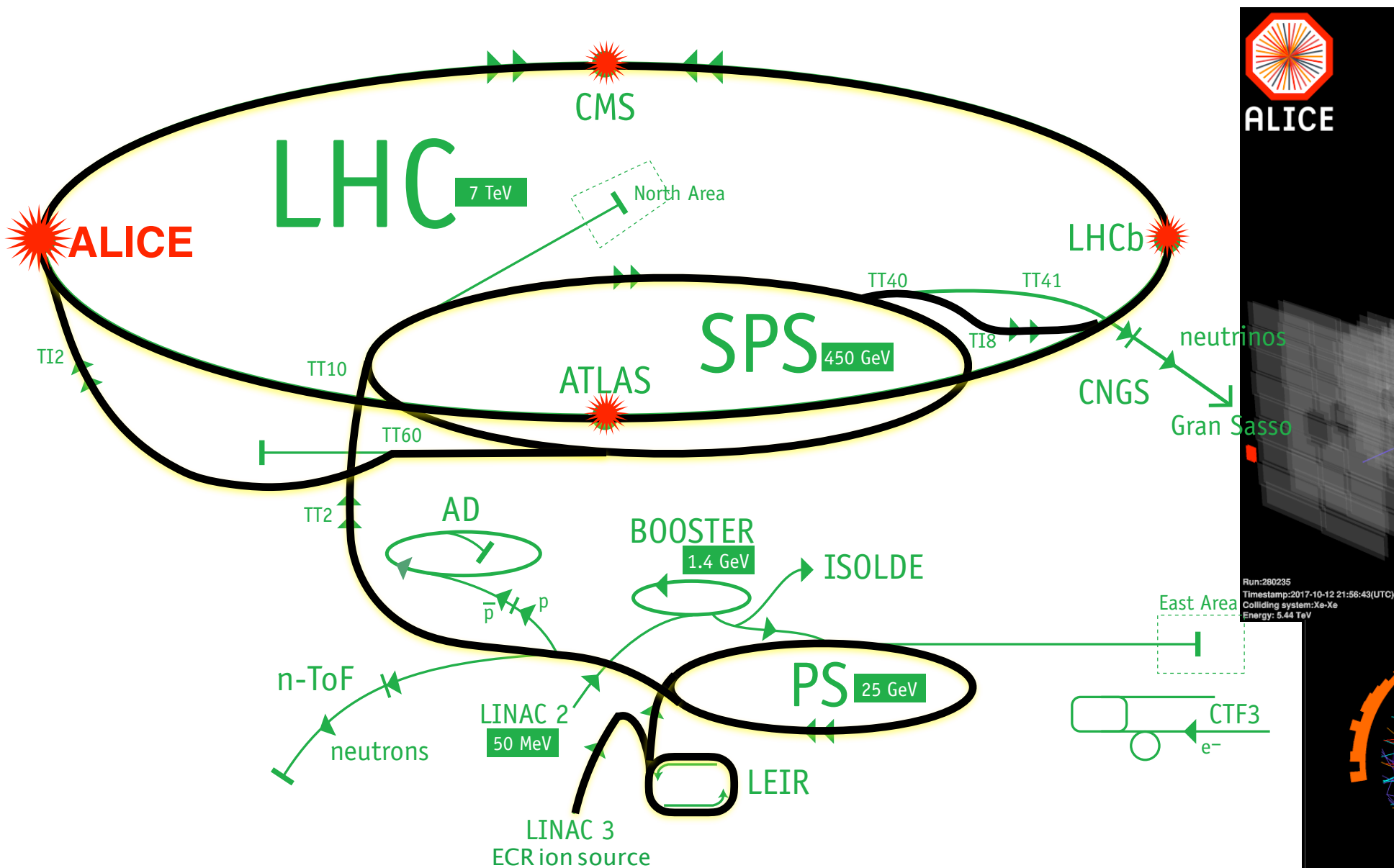
- ✓ Extremely high temperature and density
  - ✓ quarks and gluons are deconfined from hadron
- ✓ Lattice QCD calculation predicts phase transition
  - ✓  $T_c \sim 170 \text{ MeV}$
  - ✓  $\epsilon_c \sim 1 \text{ GeV/fm}^3$
- ✓ QGP exists in early universe and neutron star

**Important to understand History of the universe !**





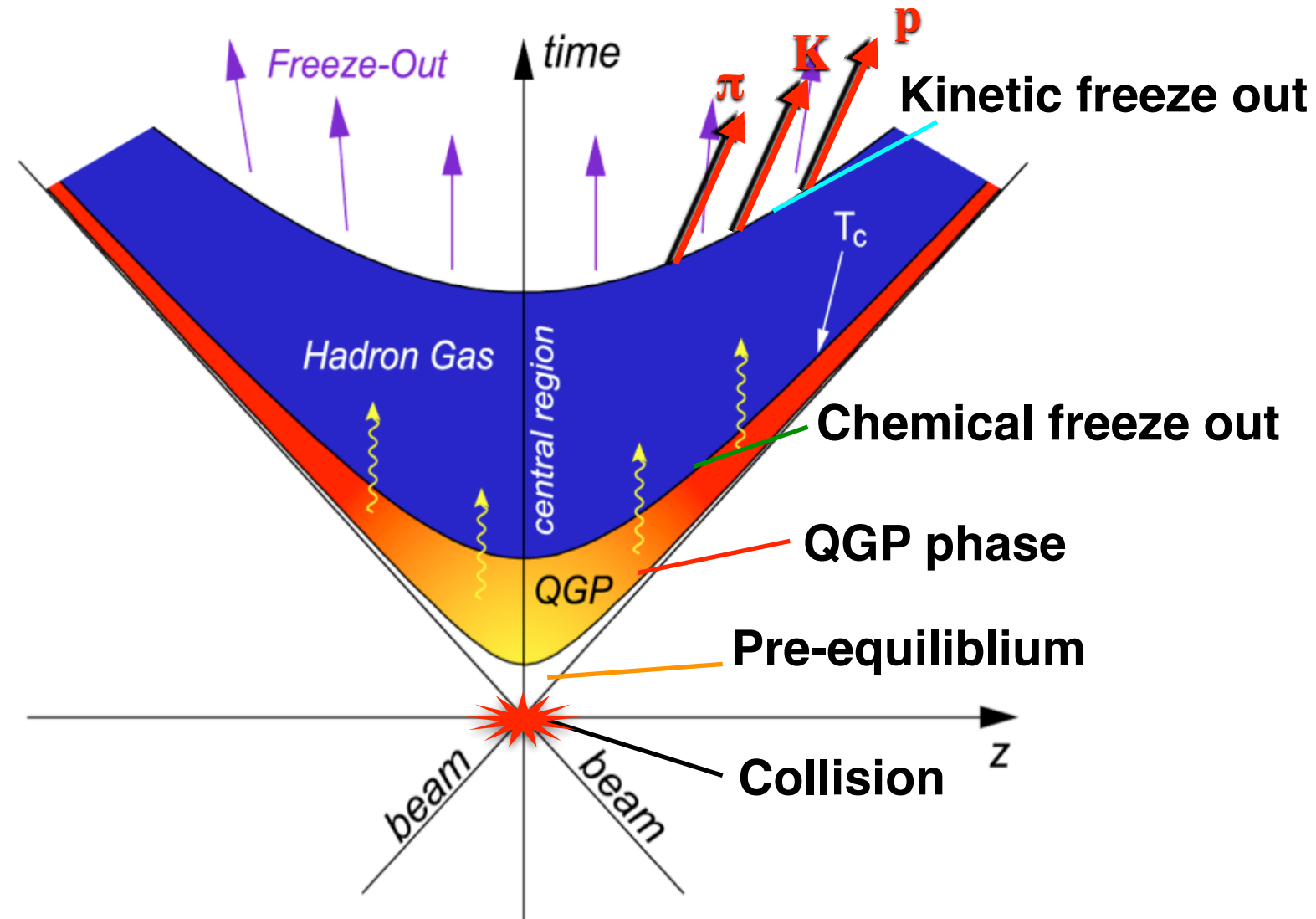
# Heavy ion collision at LHC



Species	Collision energy
Pb-Pb	2.76, 5.02 TeV
p-Pb	5.02, 8.16 TeV
Xe-Xe	5.44 TeV
p-p	0.9, 2.76, 5.02, 7, 13 TeV

- ✓ Highest energy collision (energy dep.)
- ✓ E-loss in QGP with hard probes
- ✓ Detailed study of bulk property

# Space time evolution



- ✓ To quantify the properties of QGP, a precise understanding of spatial and temporal evolution is required
- ✓ Freeze out time, emission duration, system size
  - ➔ HBT is a unique tool to measure the size and lifetime of the source

# HBT interferometry

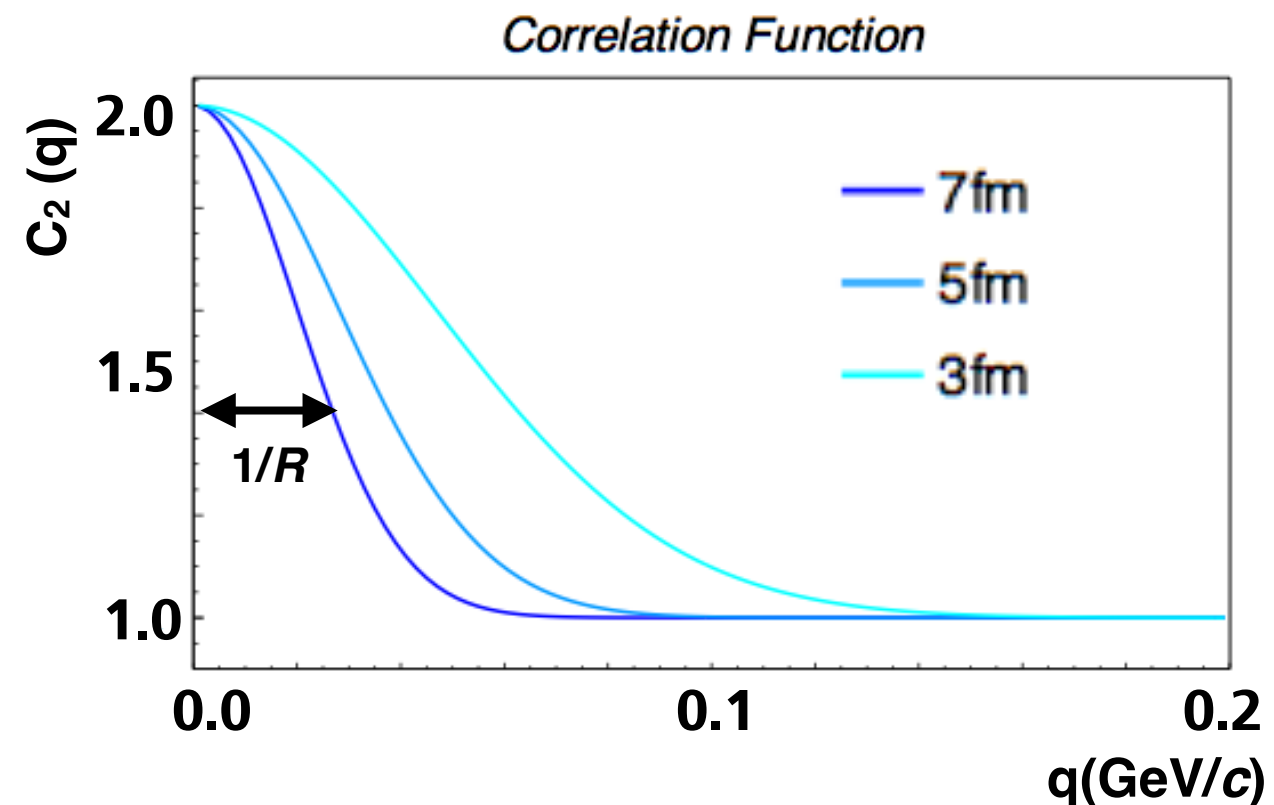
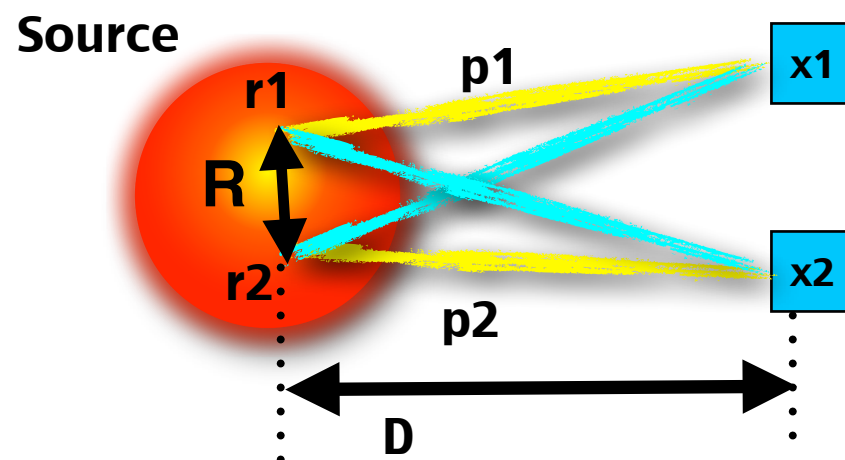
- ✓ **H**anbury **B**rown & **T**wiss (Femtoscscopy, Bose Einstein correlations)
- ✓ Measure the source size with correlation between two identical particles

$$\Psi_{12}(p_1, p_2) = \frac{1}{\sqrt{2}} \left( e^{ip_1(x_1-r_1)} e^{ip_2(x_2-r_2)} \pm e^{ip_1(x_1-r_2)} e^{ip_2(x_2-r_1)} \right) \quad \begin{array}{l} \checkmark \text{ Boson +} \\ \checkmark \text{ Fermion -} \end{array}$$

$$C_2 = \frac{P(p_1, p_2)}{P(p_1) P(p_2)} \approx 1 + |\tilde{\rho}(q)|^2 = 1 + \exp(-R^2 q^2) \quad \checkmark \mathbf{q = p_1 - p_2}$$

- ✓ Source distribution  $\rho$  is assumed to be gaussian

$$\rho(r) \equiv \exp\left(-\frac{r^2}{2R^2}\right)$$



# 3D HBT analysis

■ For **more detailed spatial information**, correlation function is expanded to 3-dimension

## Bartsch-Pratt parametrization

$$C_2 = 1 + \lambda G$$

$$G = \exp(-R_x^2 q_x^2 - R_y^2 q_y^2 - R_z^2 q_z^2 - \Delta\tau q_0^2)$$

$$\approx \exp(-R_{side}^2 q_{side}^2 - \underline{\underline{(R_{out}^{\prime 2} + \beta_T \Delta\tau^2)} q_{out}^2} - R_{long}^2 q_{long}^2)$$

$$G = \exp(-R_{side}^2 q_{side}^2 - \underline{\underline{R_{out}^2}} q_{out}^2 - R_{long}^2 q_{long}^2 - 2R_{os}^2 q_{out} q_{side} - 2R_{sl}^2 q_{side} q_{long} - 2R_{ol}^2 q_{out} q_{long})$$

**LCMS** ( **L**ongitudinal **C**o-**M**oving **S**ystem )

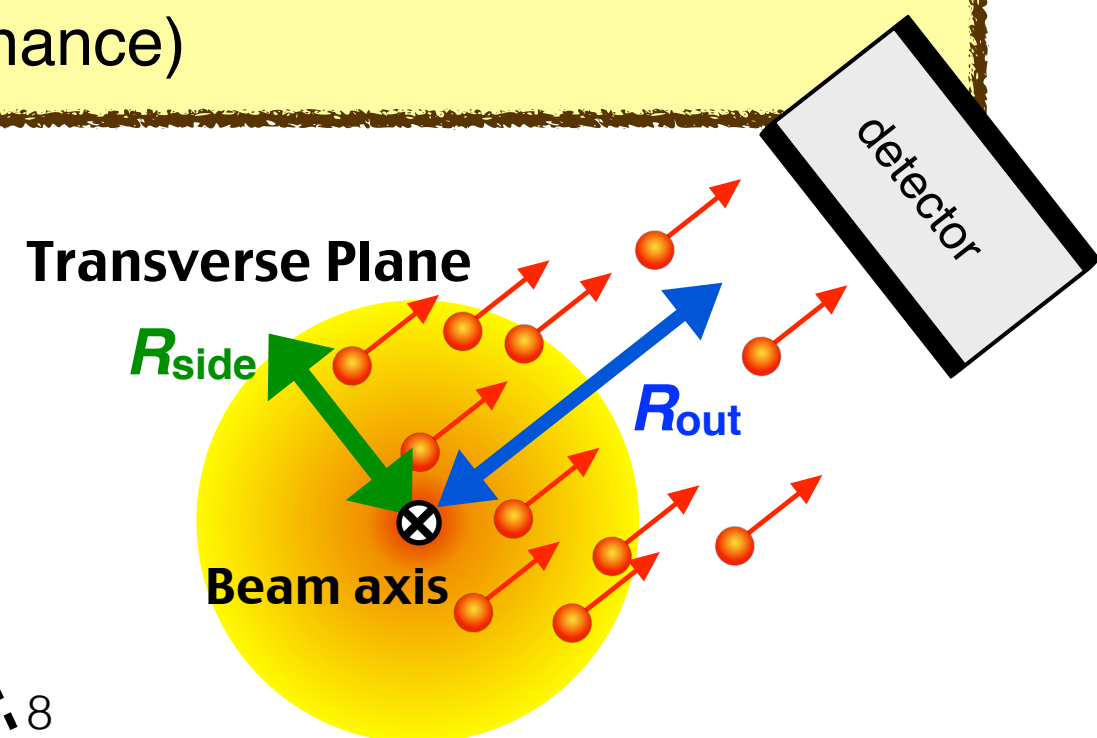
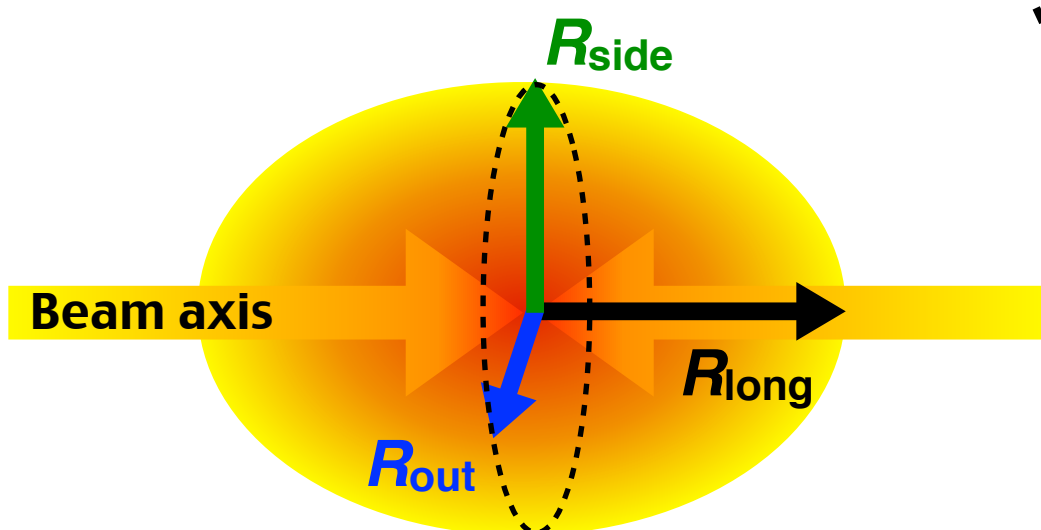
$$\checkmark \quad p_{z1} + p_{z2} = 0$$

$R_{long}$  : source size along the longitudinal direction (beam direction)

$R_{out}$  : source along the pair transverse momentum + **emission duration**

$R_{side}$  : source size along the perpendicular to  $R_{out}$

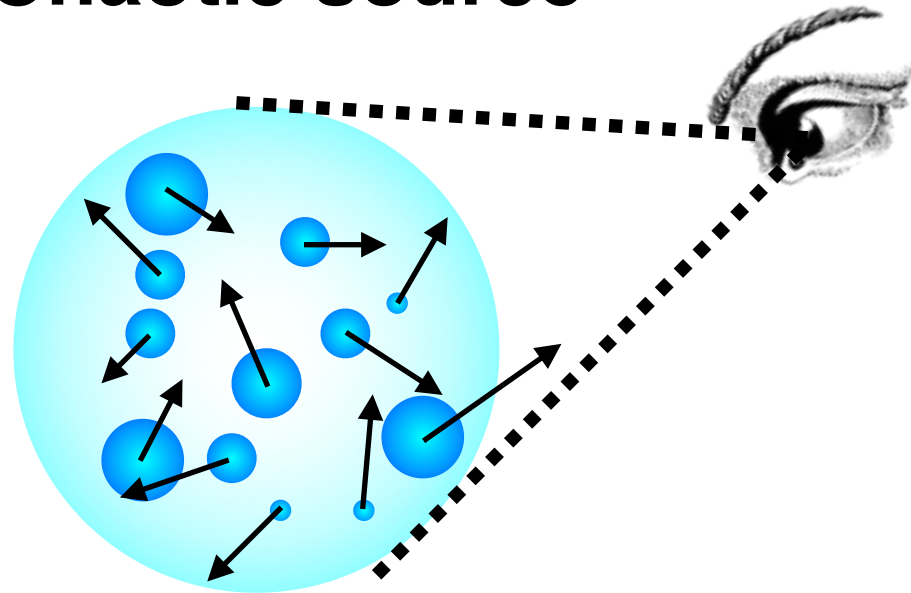
$\lambda$  : chaoticity = (in coherence) – (resonance)





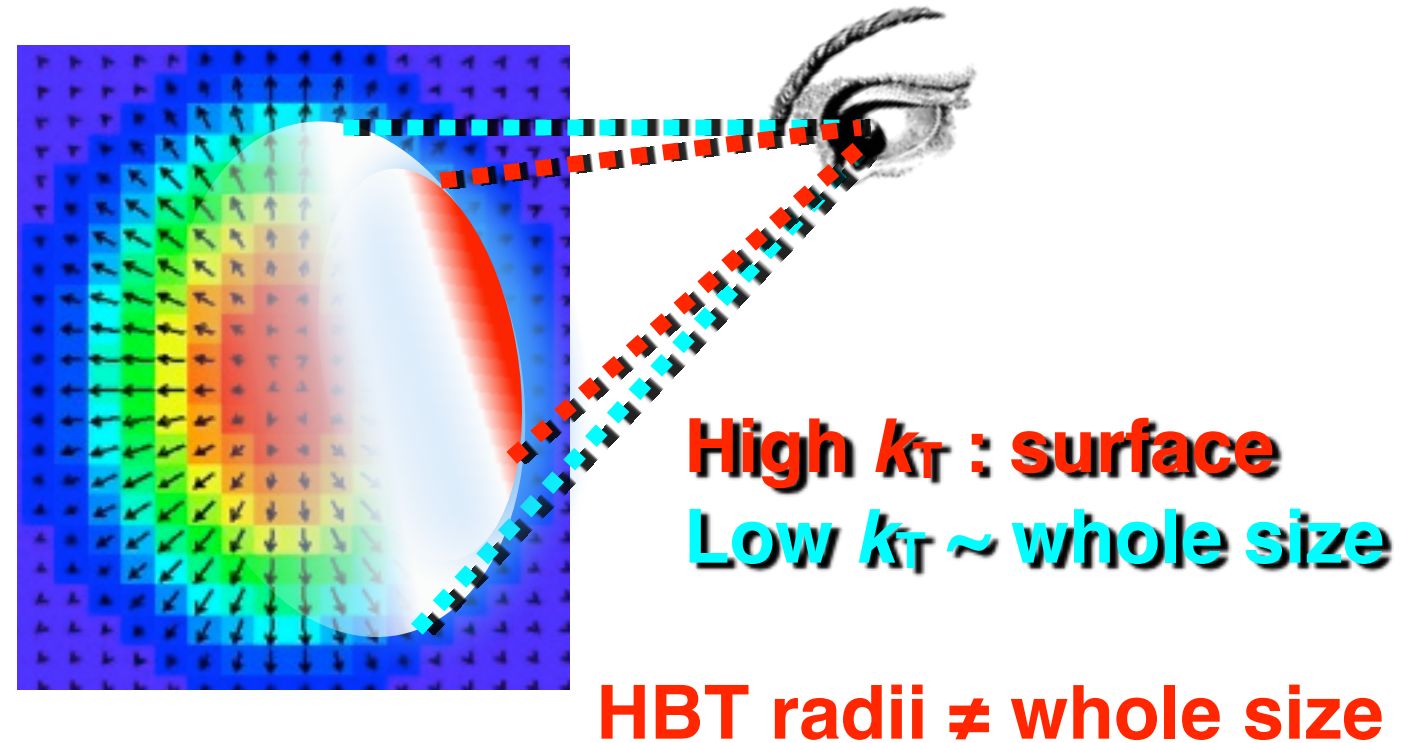
# HBT radii = geometrical source size ??

## Chaotic source



HBT radii = whole size

## Dynamical source



- ◆ For static source, HBT radii = Geometrical source size
- ◆ For dynamical source, HBT radii = “Length of homogeneity region”
- ✓ HBT radii depends on Pair transverse momentum :  $k_T$

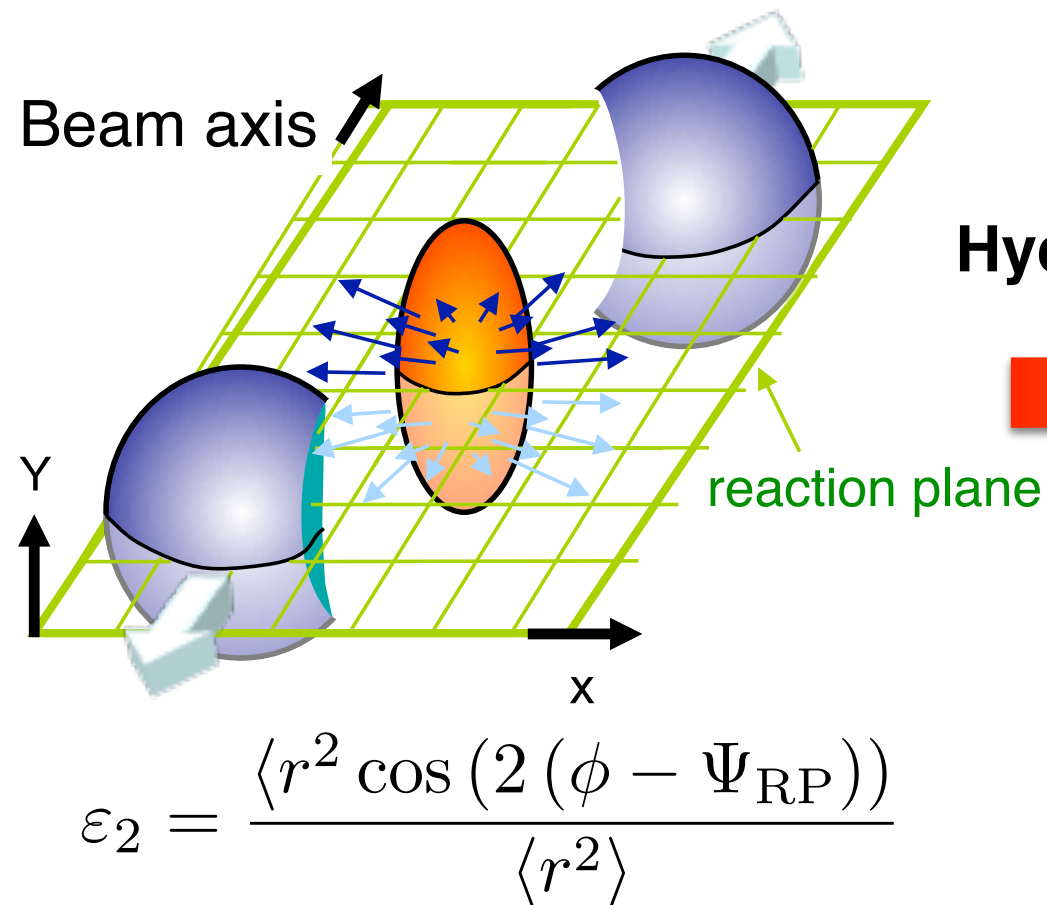
$$k_T = \frac{\vec{p}_{T1} + \vec{p}_{T2}}{2}$$

$k_T$  dependence of HBT radii is important to understand system evolution

# Azimuthal anisotropy

## ◆ Initial state

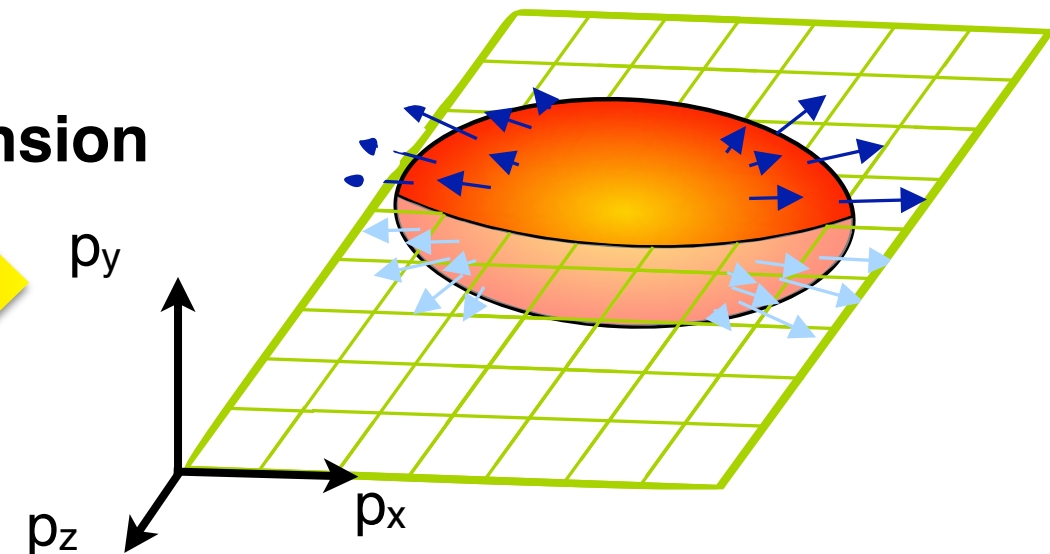
### ▸ Geometrical coordinate



## ◆ Freeze-out

### ▸ Momentum coordinate

Hydrodynamic expansion



$$v_2 = \langle \cos(2(\phi - \Psi_{RP})) \rangle$$

◆ Initial geometry  $\varepsilon_2$  makes anisotropic pressure gradient

◆ Hydrodynamic expansion convert  $\varepsilon_2$  to  $v_2$

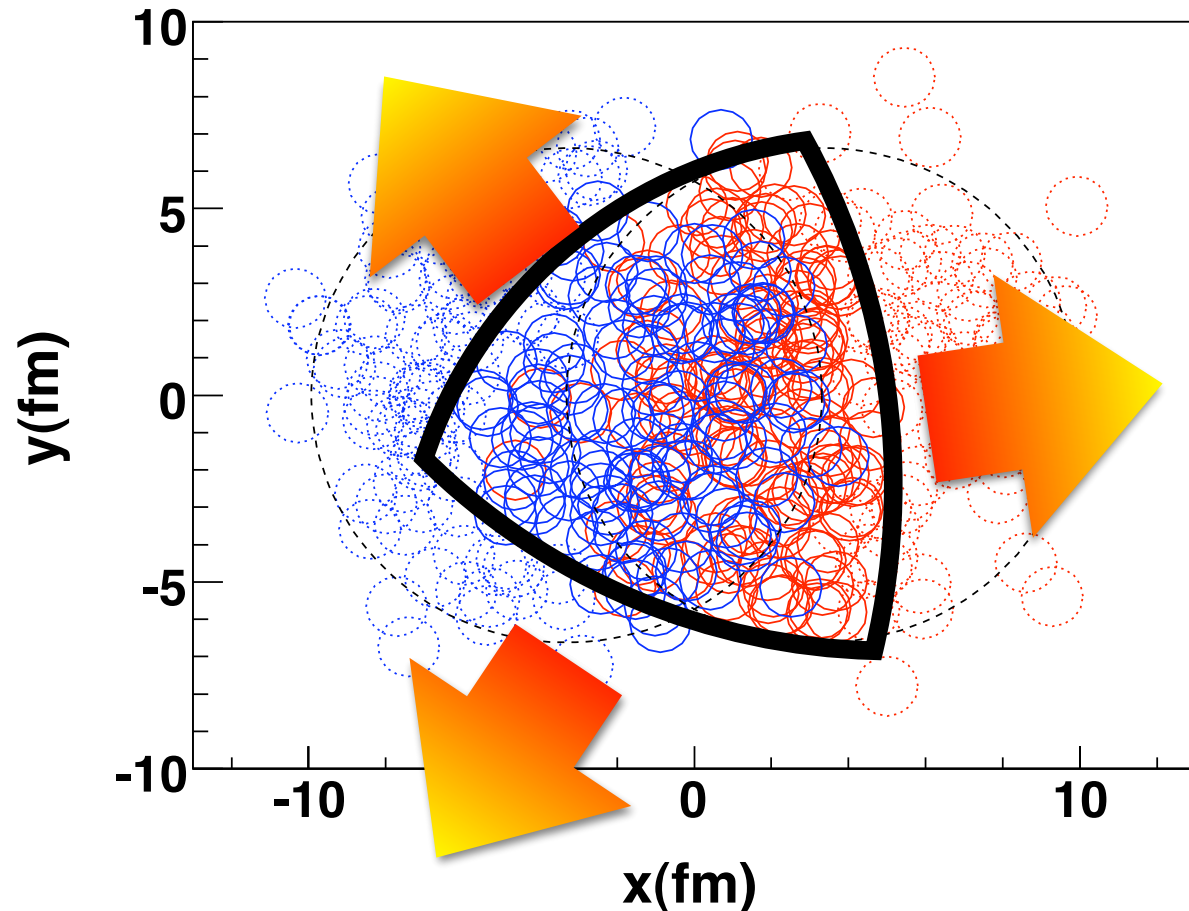
✓ **Sensitive to viscosity and initial geometry**



# 3<sup>rd</sup>-order azimuthal anisotropy

## ◆ Initial geometry

### ► MC Glauber simulation (arXiv:1408.2549)



$$\frac{dN}{d\phi} \propto 1 + 2v_2 \cos 2(\phi - \Psi_2) + 2v_3 \cos 3(\phi - \Psi_3)$$

◆ Initial participant shape  $\neq$  smooth elliptic shape

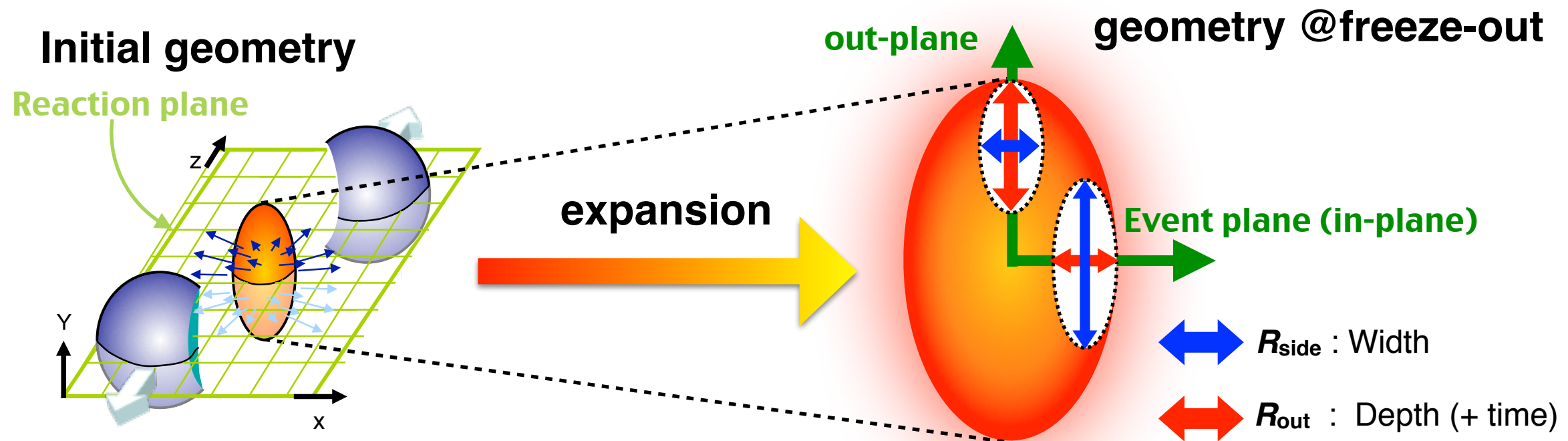
◆ Finite number of nucleons makes 3<sup>rd</sup>-order anisotropy

◆ Initial triangular shape is converted to  $v_3$

◆ Initial geometry and viscosity are more sensitive to  $v_3$  than  $v_2$

# Azimuthal angle dependence of HBT radii w.r.t. $\Psi_2$

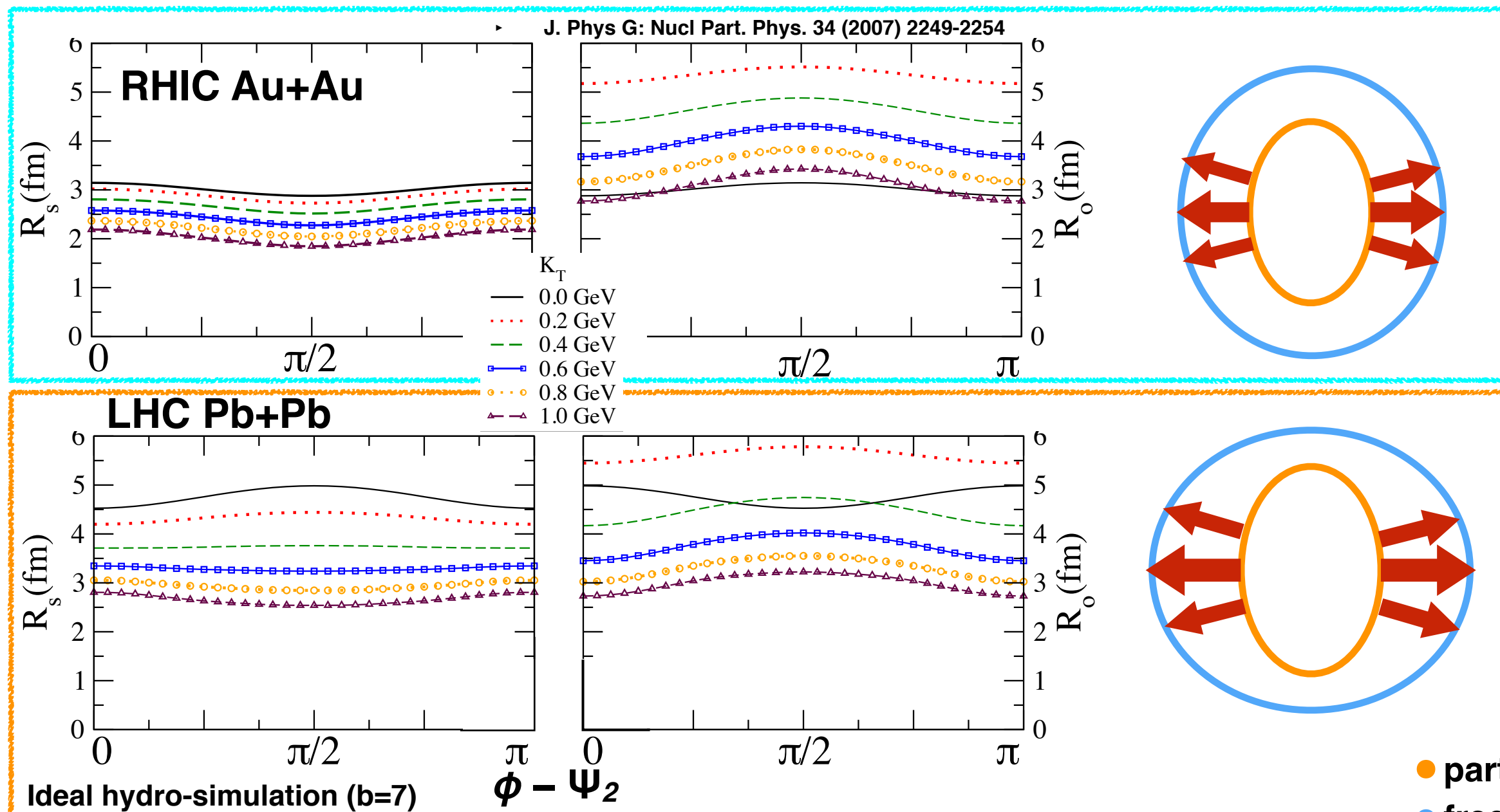
- ✓ Azimuthal angle dependence of 3D HBT radii gives us the **source shape** at freeze-out
- ✓ Event plane  $\Psi_2 \sim$  reaction plane (determined with azimuthal anisotropy)
- ✓ Relation between initial and final source shape will constrain the freeze-out parameter
  - **flow velocity profile, system life time and viscosity**



- Spherical source
  - $R_{\text{side}} (\text{in-plane}) = R_{\text{side}} (\text{out-plane})$
- Out-plane elongated elliptic source
  - $R_{\text{side}} (\text{in-plane}) > R_{\text{side}} (\text{out-plane})$  &  $R_{\text{out}} (\text{in-plane}) < R_{\text{out}} (\text{out-plane})$
- In-plane elongated elliptic source
  - $R_{\text{side}} (\text{in-plane}) < R_{\text{side}} (\text{out-plane})$  &  $R_{\text{out}} (\text{in-plane}) > R_{\text{out}} (\text{out-plane})$

# Final source eccentricity @ LHC energy

- Hydro model predicts  $R_{\text{side}}$  and  $R_{\text{out}}$  oscillate in phase at lower  $k_T$ 
  - ✓ At RHIC energy, out-plane elongated elliptic shape still remains at freeze-out
  - ✓ Initial elliptic shape will be vanished or even reversed in LHC



✓ This effect can be observed in LHC ??

- participant
- freeze-out source
- flow

# Final source **triangular shape** and HBT w.r.t. $\Psi_3$

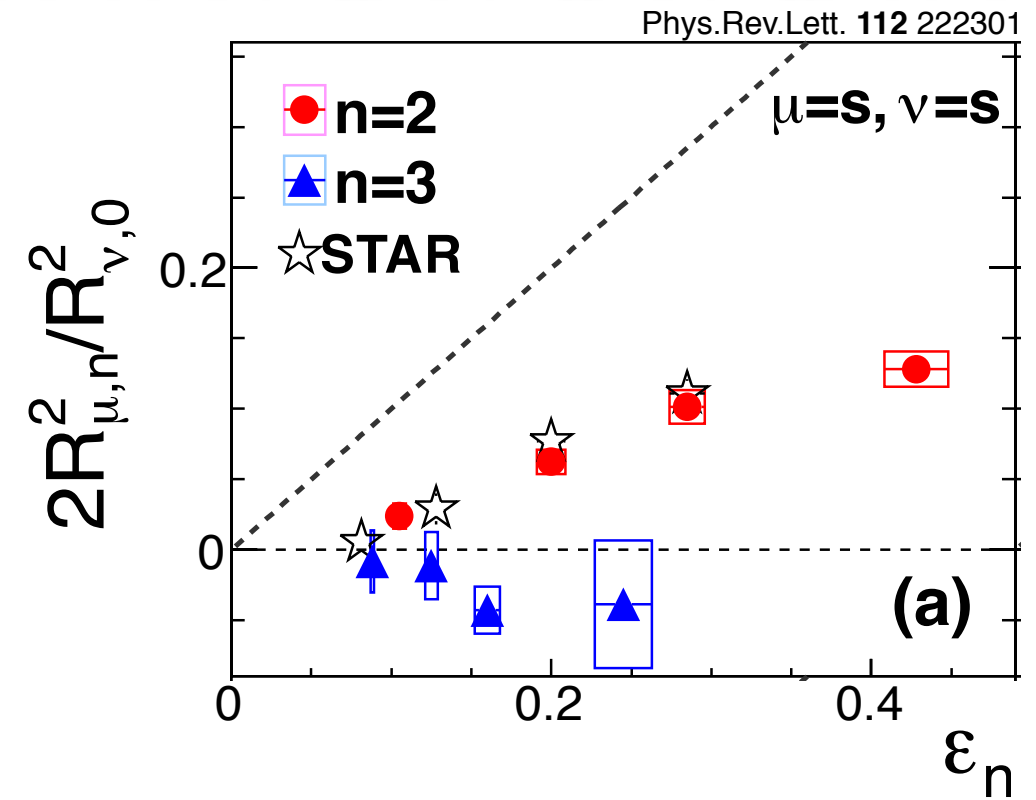
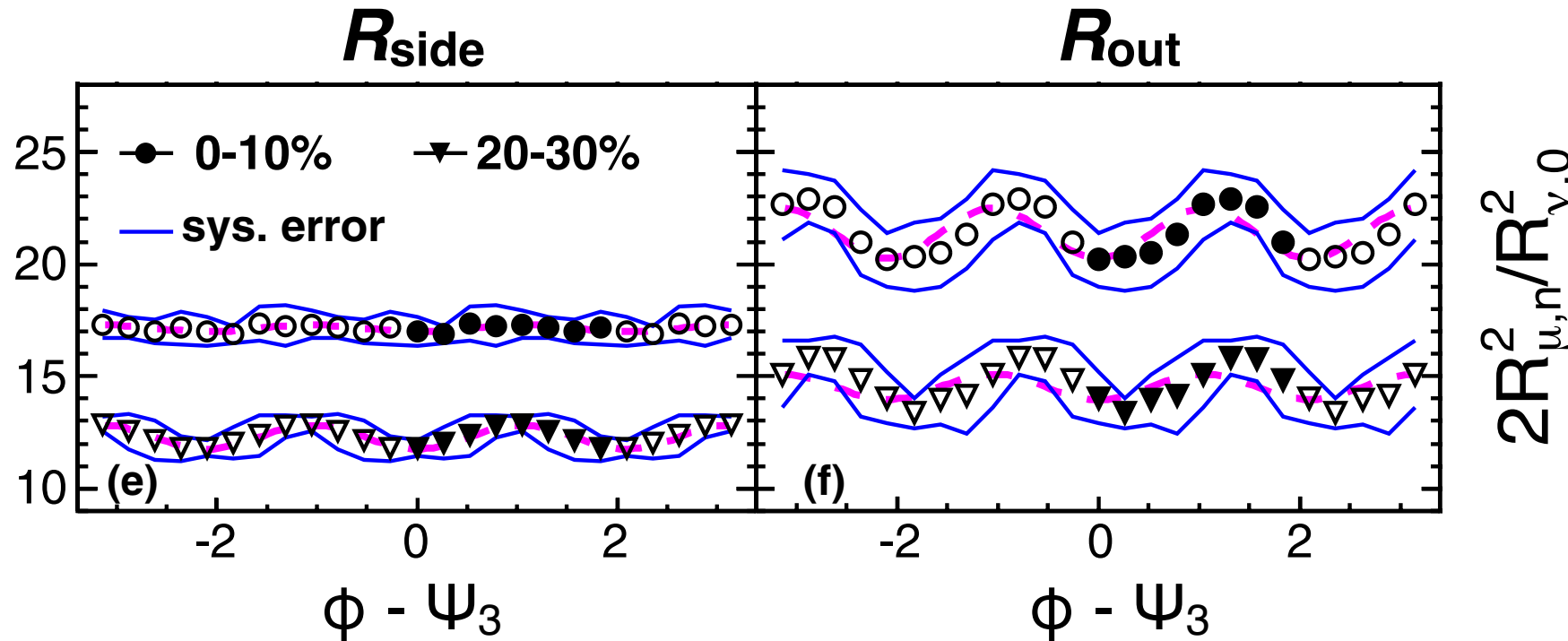
◆ Model suggests HBT w.r.t.  $\Psi_3$  shows finite oscillation in expanding source

✓ S.Voloshin, J. Phys. G38, 124097

◆ First measurement of HBT w.r.t.  $\Psi_3$  was measured @ PHENIX Au+Au 200GeV

✓ Negative or zero oscillation was observed in  $R_{\text{side}}$

Au+Au 200GeV @ PHENIX



☑ In order to constrain the freeze-out parameters, to determine the oscillation sign and centrality dependence is indispensable !!

✓ Precise measurement @LHC is expected



# Event shape engineering (ESE)

## □ Event by event flow amplitude selection

J. Schukraft et al., Phys. Lett. B719, 394-398 (2013)

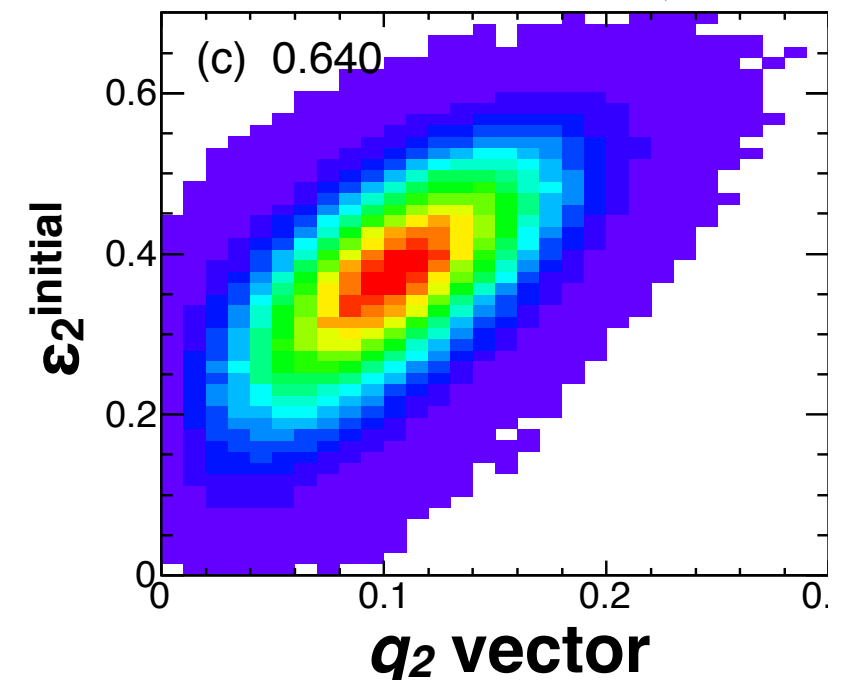
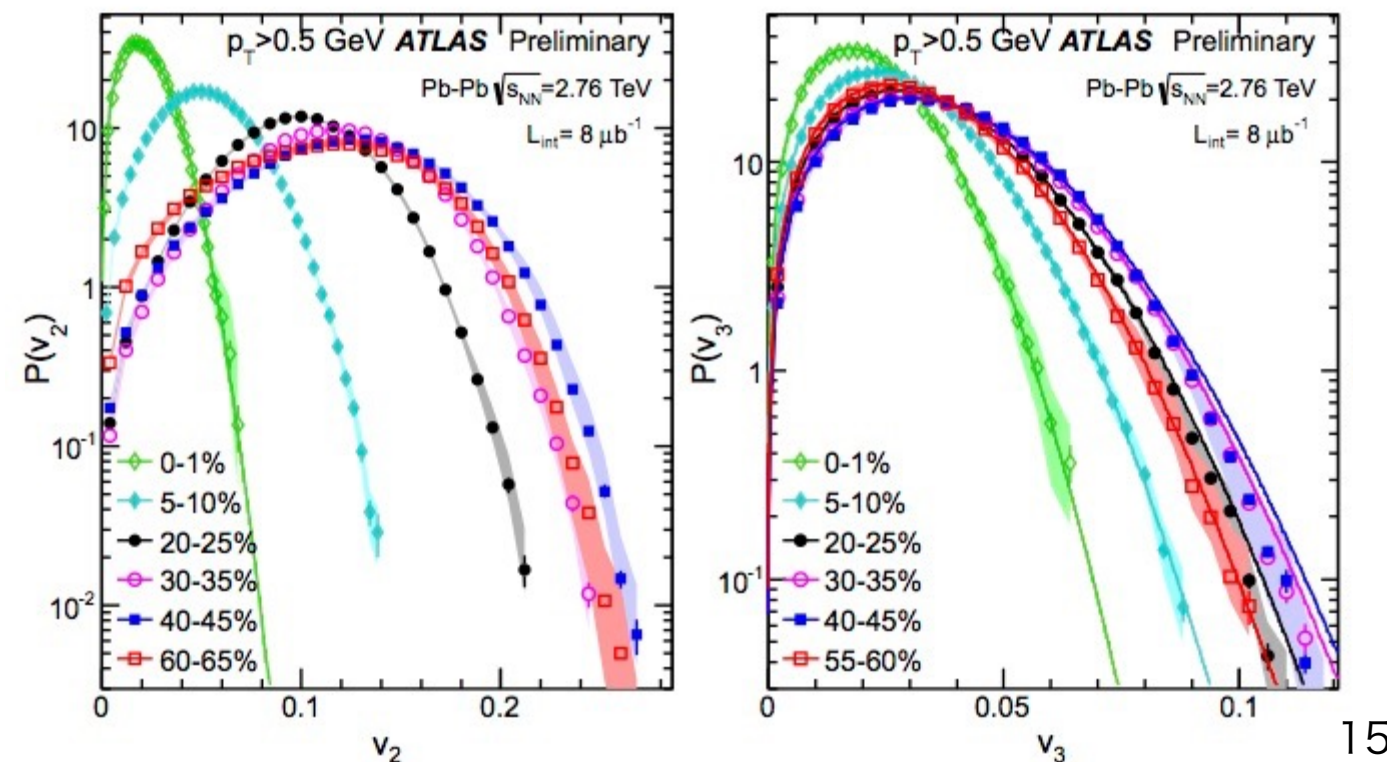
- $v_2$  and  $v_3$  largely fluctuate within a fixed centrality
- **Event by event  $v_2(v_3)$  fluctuation is selected with flow vector  $q_2(q_3)$**
- ✓ **Possibly control the initial eccentricity**

★ q-vector is defined by  $q_n = \sqrt{Q_{n,x}^2 + Q_{n,y}^2}$   $\left( \begin{array}{l} Q_{n,x} = \sum w_i \cos(n\phi) / \sum w_i \\ Q_{n,y} = \sum w_i \sin(n\phi) / \sum w_i \end{array} \right)$

- **Centrality is not best probe for initial geometry!! (system size also changes)**
- By applying ESE technique to other observables, **separation of volume effect and geometrical effect** can be allowed

## □ Explicit correlation between $q_2$ and $\epsilon_2^{\text{initial}}$

- **AMPT simulation** ▸ J.Jia et al., arXiv:1430.6077



# Motivation

□ Study the space time evolution of QGP with Azimuthally sensitive HBT and Event Shape Engineering in 2.76TeV Pb-Pb collisions

## ♦ Elliptic shape

- Measurements of azimuthally sensitive HBT w.r.t.  $\Psi_2$  in LHC energy
- Relation between Initial and final source eccentricity with **ESE**
- Extract freeze out parameters with **Blast-wave fit**

## ♦ Triangular shape

- Measurements of azimuthally sensitive HBT w.r.t.  $\Psi_3$
- Relation between  $v_3$  ( initial triangular shape ) and HBT oscillation with **ESE ( $q_3$ ) selection**

# My activity

## Master

- DCAL construction
- EMCAL SRU work @cern
- DCAL commissioning
- Shift taking @ PHENIX
- Development of read out module with FPGA and Flash ADC
- KEK summer challenge M1->D4
- Development of radon detector ->D4
- Azimuthal angle dependence of HBT radii w.r.t.  $\Psi_2$  and  $\Psi_3$

## Doctor

▸ Talk

JPS fall 2016

▸ Poster

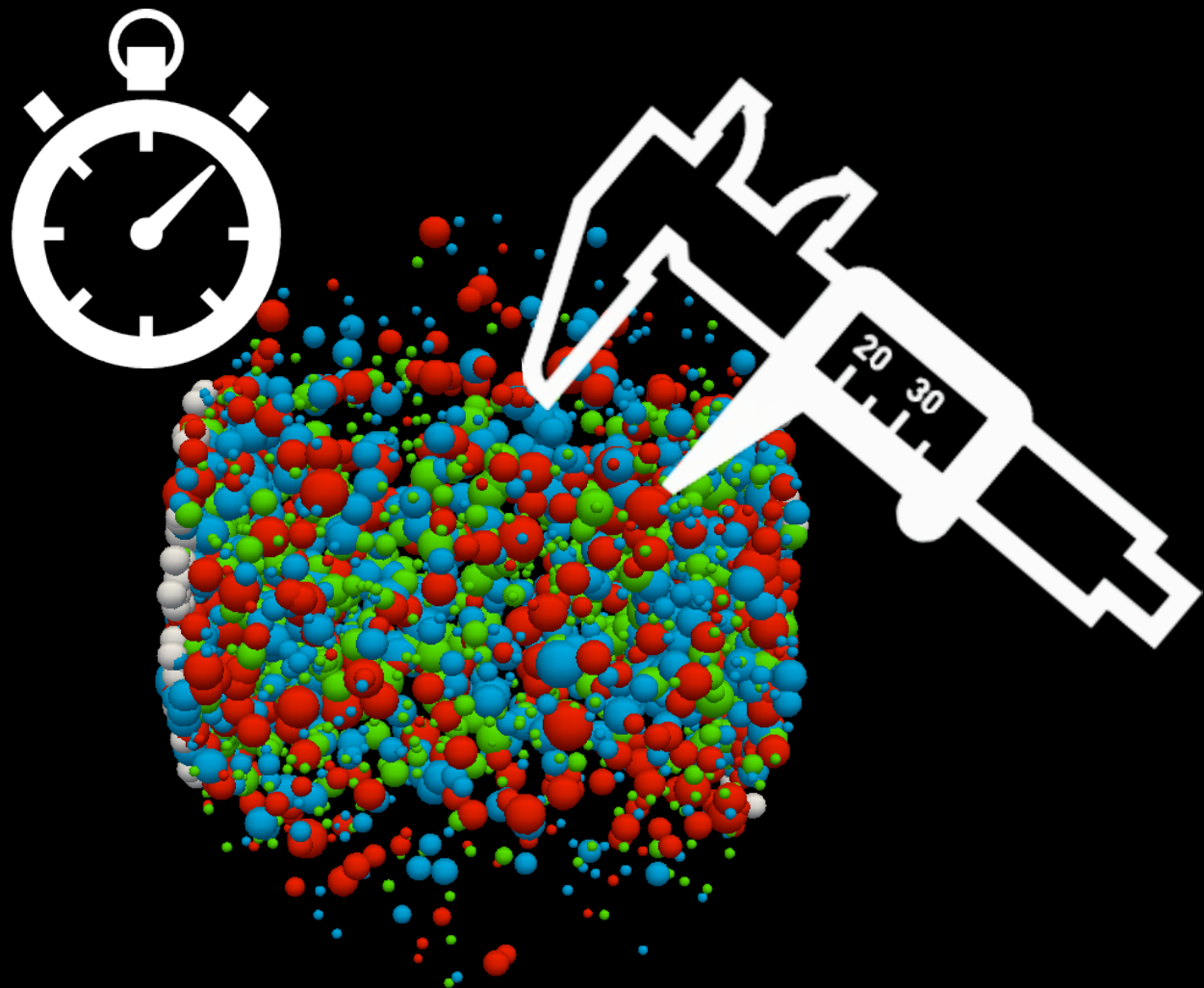
QM2016

▸ Talk

WPCF2017

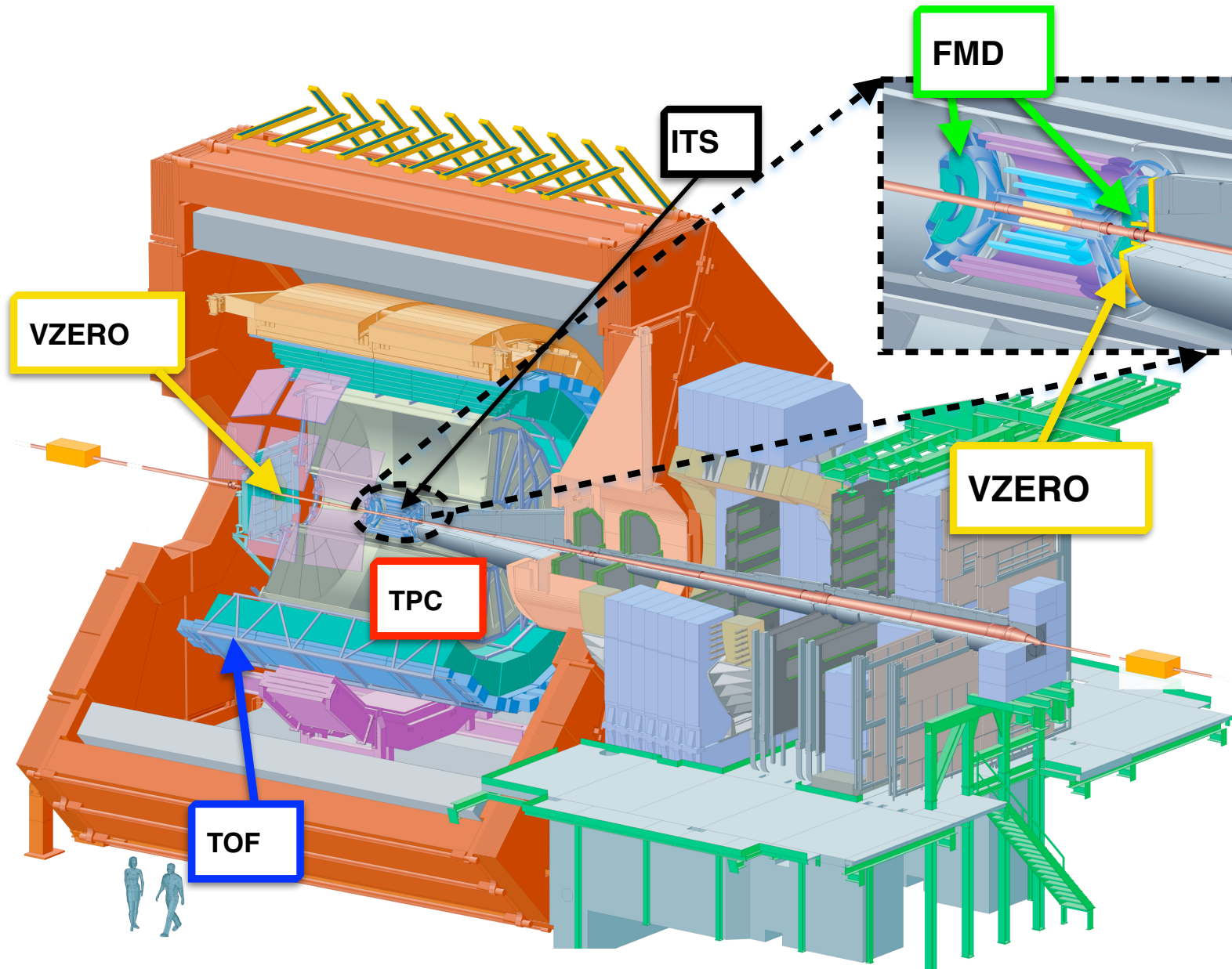
- Shift taking @ ALICE
- HBT w.r.t. Jet axis
- HBT relative to  $\Psi_2$  and  $\Psi_3$  with ESE

# Experiment & Analysis





# ALICE Detector



## In this analysis

### VZERO

- ✓ Trigger & centrality
- ✓  $V0_A : 2.8 < \eta < 5.1$
- ✓  $V0_C : -3.7 < \eta < -1.7$

### TPC & ITS

- ✓ Tracking & PID
- ✓ Vertex
- ✓  $|\eta_{\text{track}}| < 0.8$

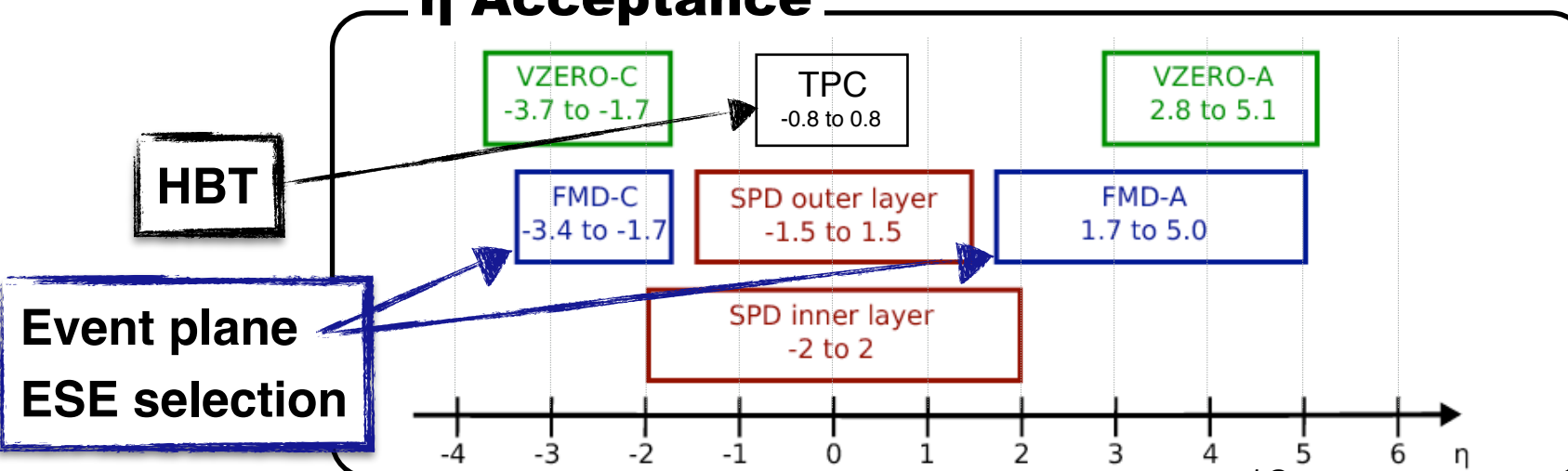
### TOF

- ✓ PID
- ✓  $|\eta_{\text{track}}| < 0.8$

### FMD

- ✓ Event plane
- ✓  $FMD_A : 1.7 < \eta < 5.0$
- ✓  $FMD_C : -3.4 < \eta < -1.7$

## $\eta$ Acceptance

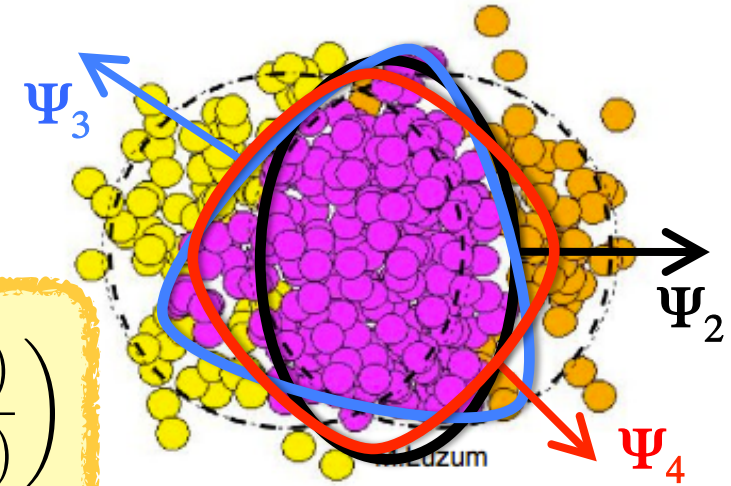


# Event Plane determination

## ■ The FMD Detector

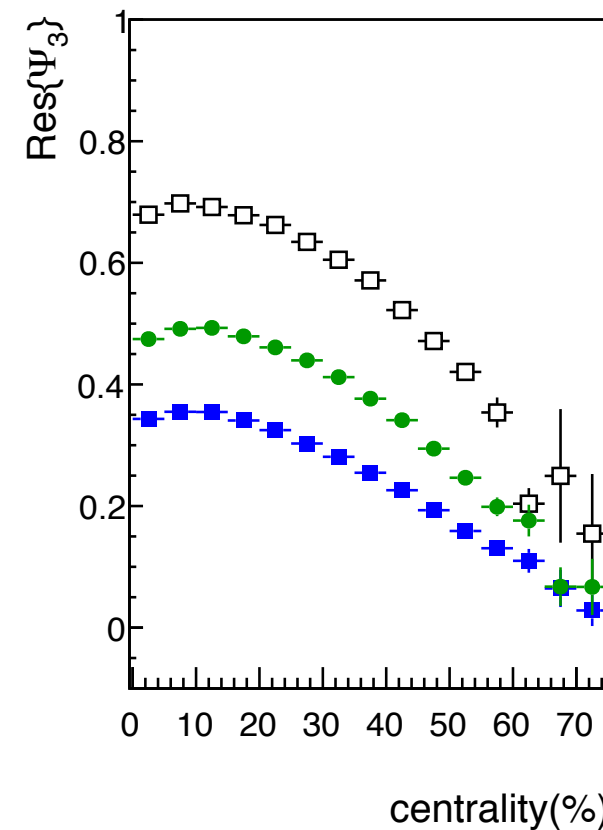
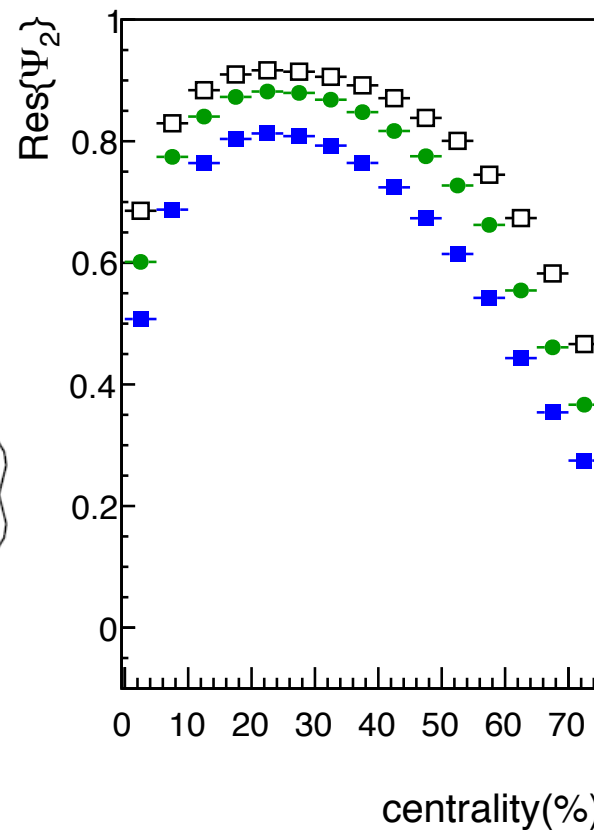
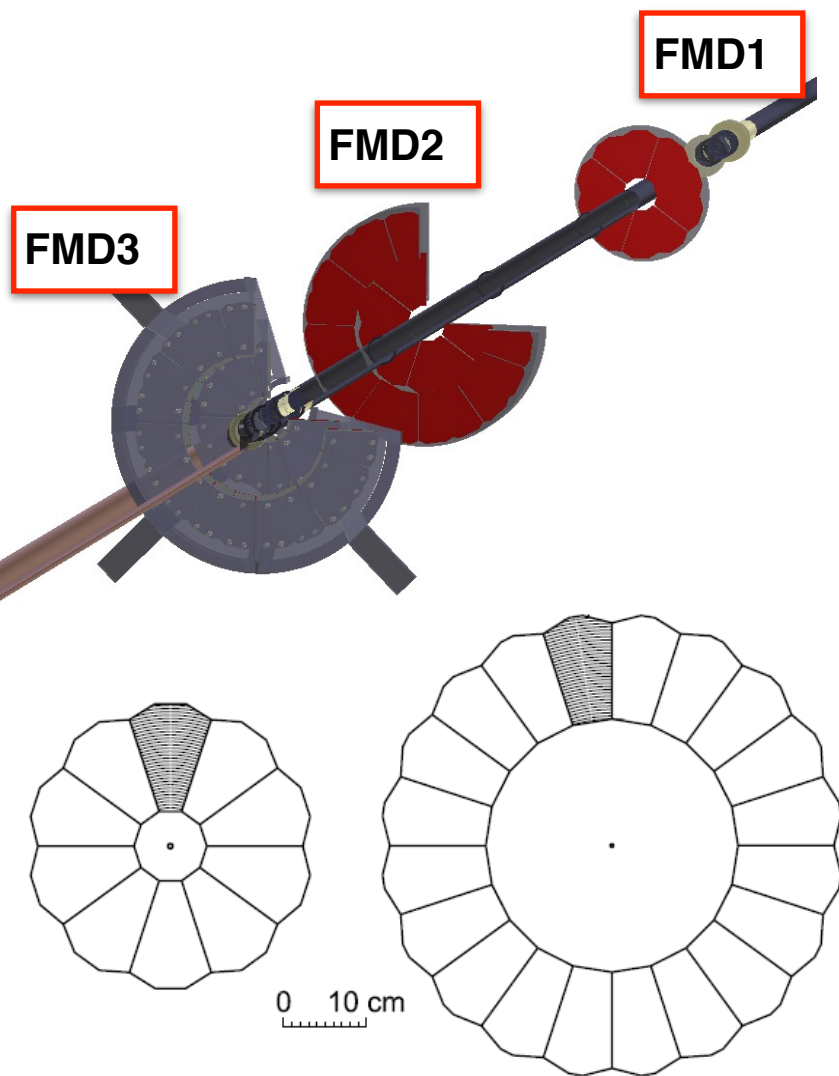
- Silicon strip detector
- 2 type rings : inner and outer
  - inner : 20 sectors
  - outer : 40 sectors

$$\Psi_n = \frac{1}{n} \tan^{-1} \left( \frac{\sum w_i \sin(n\phi_i)}{\sum w_i \cos(n\phi_i)} \right)$$



## • E.P. resolution with 3 sub method

$$\text{Res} \{ \Psi_n \} = \sqrt{\frac{\langle \cos(n(\Psi_n^A - \Psi_n^B)) \rangle \langle \cos(n(\Psi_n^A - \Psi_n^C)) \rangle}{\langle \cos(n(\Psi_n^B - \Psi_n^C)) \rangle}}$$



E.P. Resolution

—□— TPC(TPC, FMDA, FMDC)

$|\eta| < 1.0$

—●— FMD<sub>AC</sub>(FMD<sub>C</sub>, FMD<sub>A</sub>, TPC)

$-3.4 < \eta < -1.7, 1.7 < \eta < 5.0$

—■— V0<sub>AC</sub>(V0<sub>C</sub>, V0<sub>A</sub>, TPC)

$-3.7 < \eta < -1.7, 2.8 < \eta < 5.1$

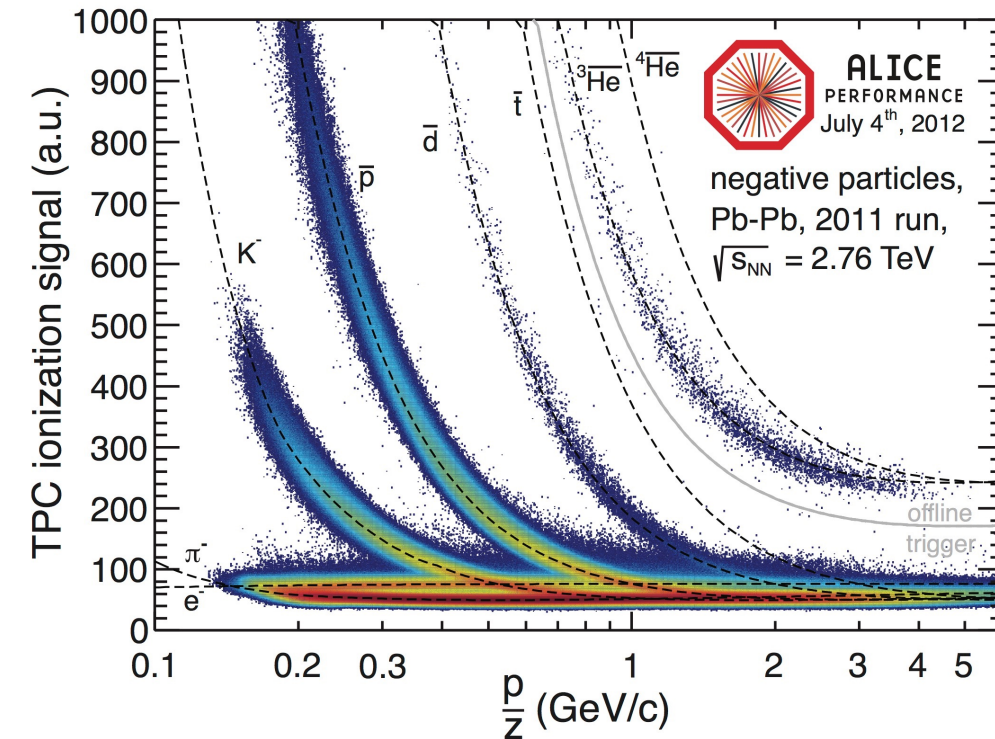
This excellent resolution allows us precise measurement of higher order E.P. 20



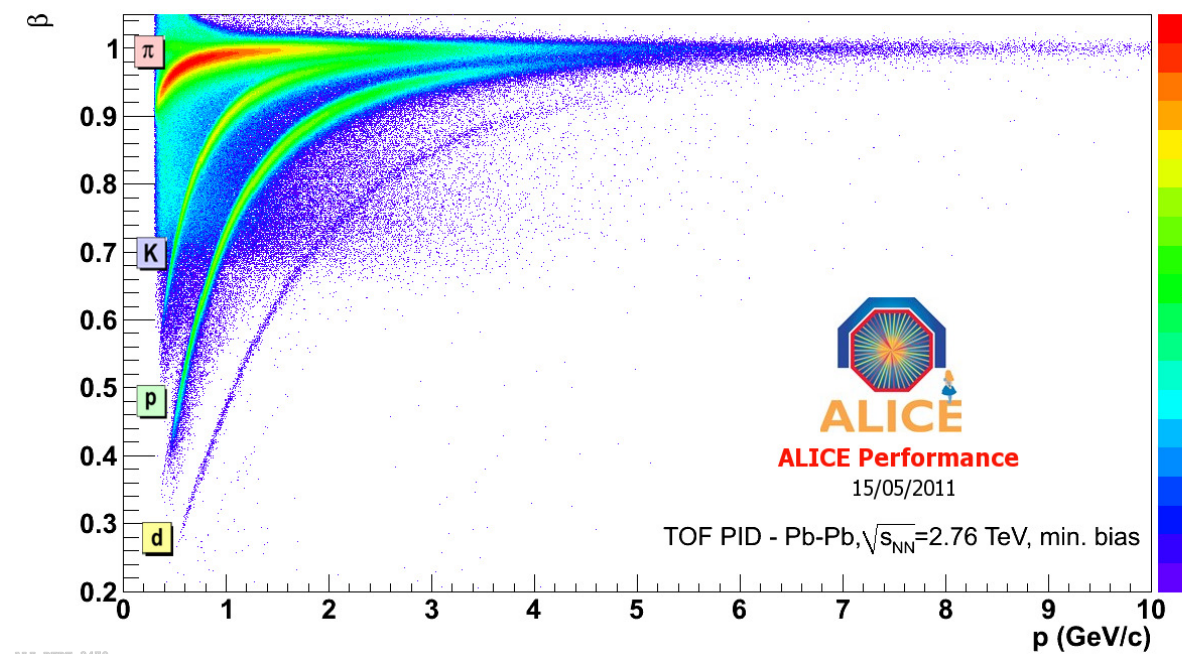
# PID

## Charged hadron identification

- charged pions are identified with TPC+TOF
- TPC
  - Energy loss (dE/dx)
  - dE/dx resolution  $\sim 6.8\%$  in  $dN_{dy} = 8000$
- TOF
  - Time of flight, mass
  - Performance evaluated  $\sigma_{TOF} = 60$  (ps)



$$m^2 = p^2 \left( \left( \frac{t}{L} \right)^2 - 1 \right)$$



# Two track resolution

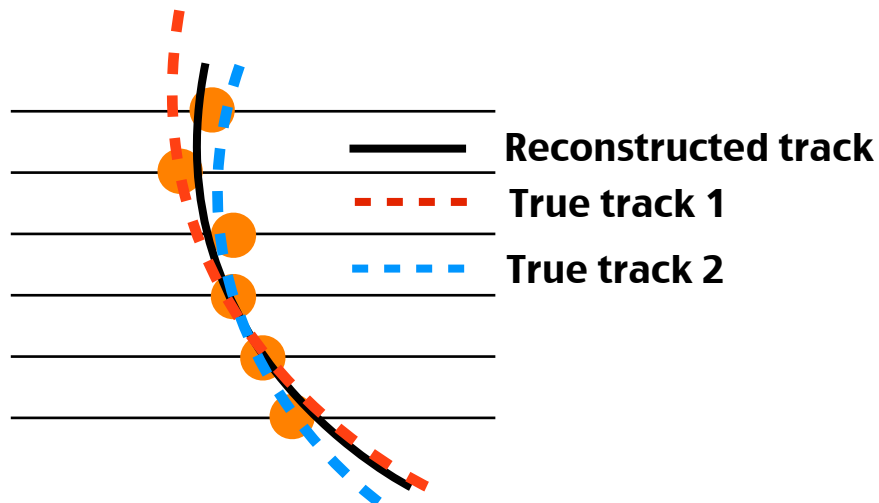
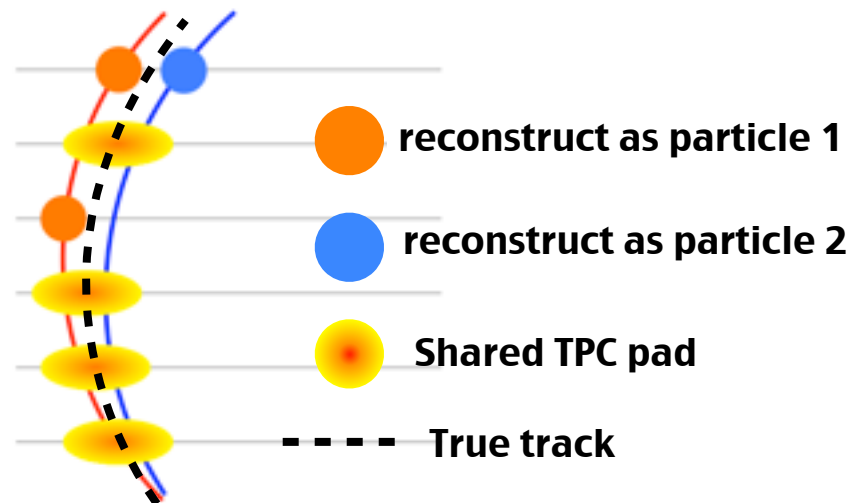
## ■ Due to the high multiplicity event

### • Track splitting

- A track is falsely reconstructed as two tracks that are spatially close

### • Track merging

- Two tracks that are spatially close are falsely reconstructed as one
- These effect modify measured correlation function



## ✓ Applied pair cut

- Fraction of shared TPC cluster  $< 5\%$
- Angular distance in  $\Delta\phi^*$ ,  $\Delta\eta$

# HBT for experimental approach

## How to calculate correlation function $C_2$ in experiment

$$C_2 = \frac{P(p_1, p_2)}{P(p_1)P(p_2)} = \frac{Q_{Real}}{Q_{Mix}}$$

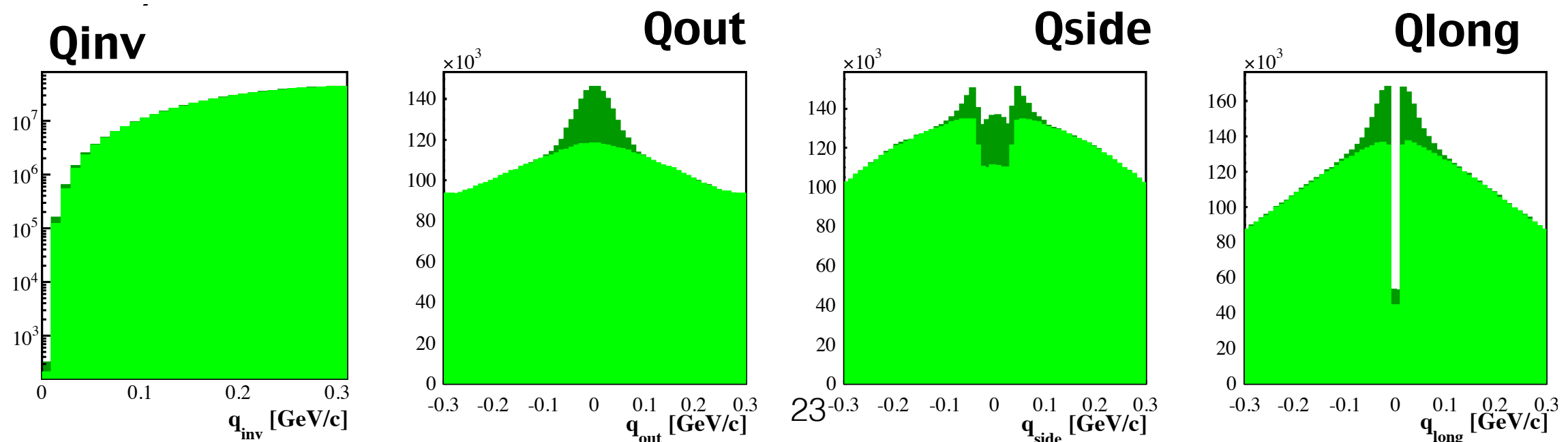
●  $Q_{Real}$  : pair in same event (HBT effect)  
●  $Q_{Mix}$  : pair in different event (no HBT effect)

- Event Mixing

- Real eventとMix eventを同じ特徴を持ったeventから選ぶ

ことにより、**アクセプタンスの効果、検出効率の効果**をキャンセルできる

→測定したい物理的相関のみを観測することができる



# Final state interaction and resonance

- Like-sign pairs that is spatially close are repulsive with Coulomb

- **Correlation function is suppressed for low  $q$  pairs**
- Coulomb weight is calculated with Coulomb wave function

$$\left[ -\frac{\hbar^2 \nabla^2}{2\mu} + \frac{Z_1 Z_2 e^2}{r} \right] = E \Psi_c(r)$$

## ■ Resonance decay

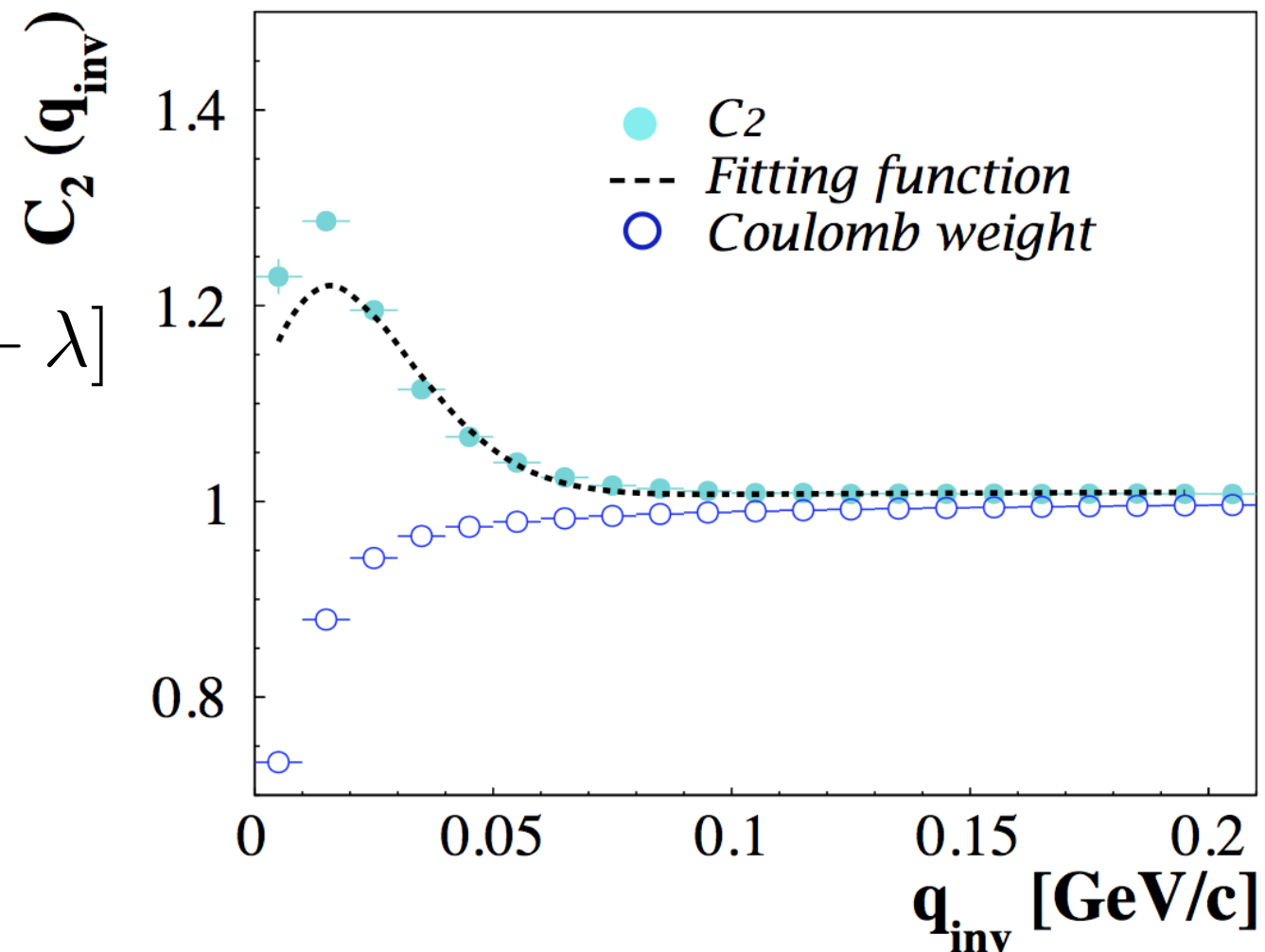
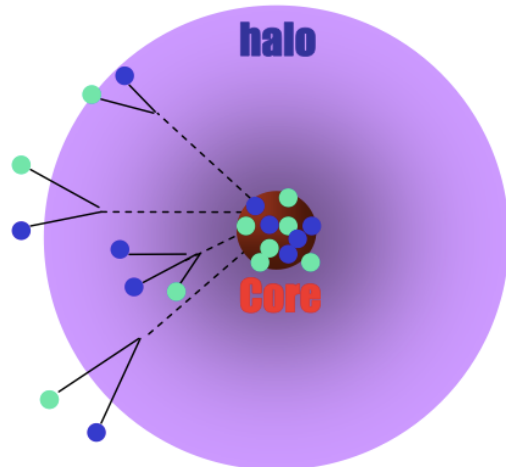
- $\lambda$  in  $C_2$  is sensitive to purity
- Core-halo model

$$C_2 = C_2^{core} + C_2^{halo}$$

$$= N [\lambda (1 + G) F_{coul}] + [1 + \lambda]$$

✓  $G$  : HBT interferometry

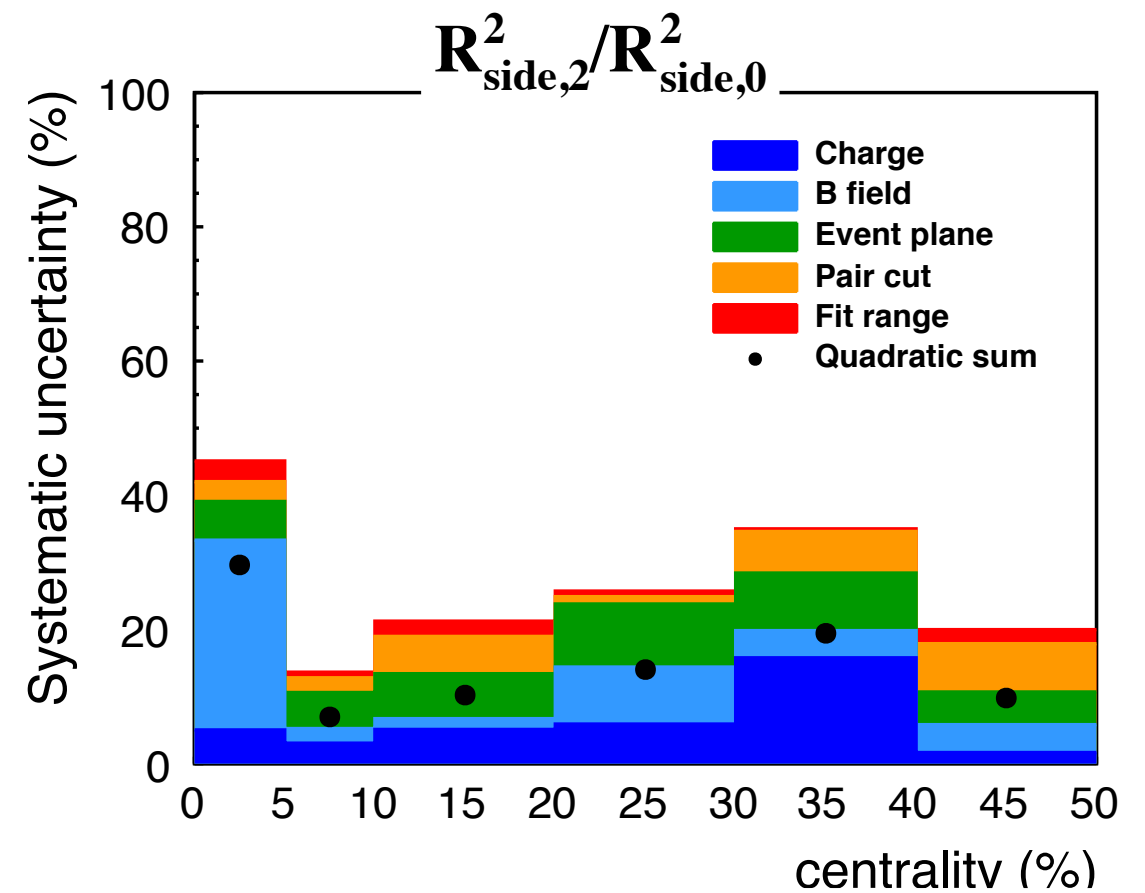
✓  $F_{coul}$  : Coulomb interaction



# Systematic uncertainties

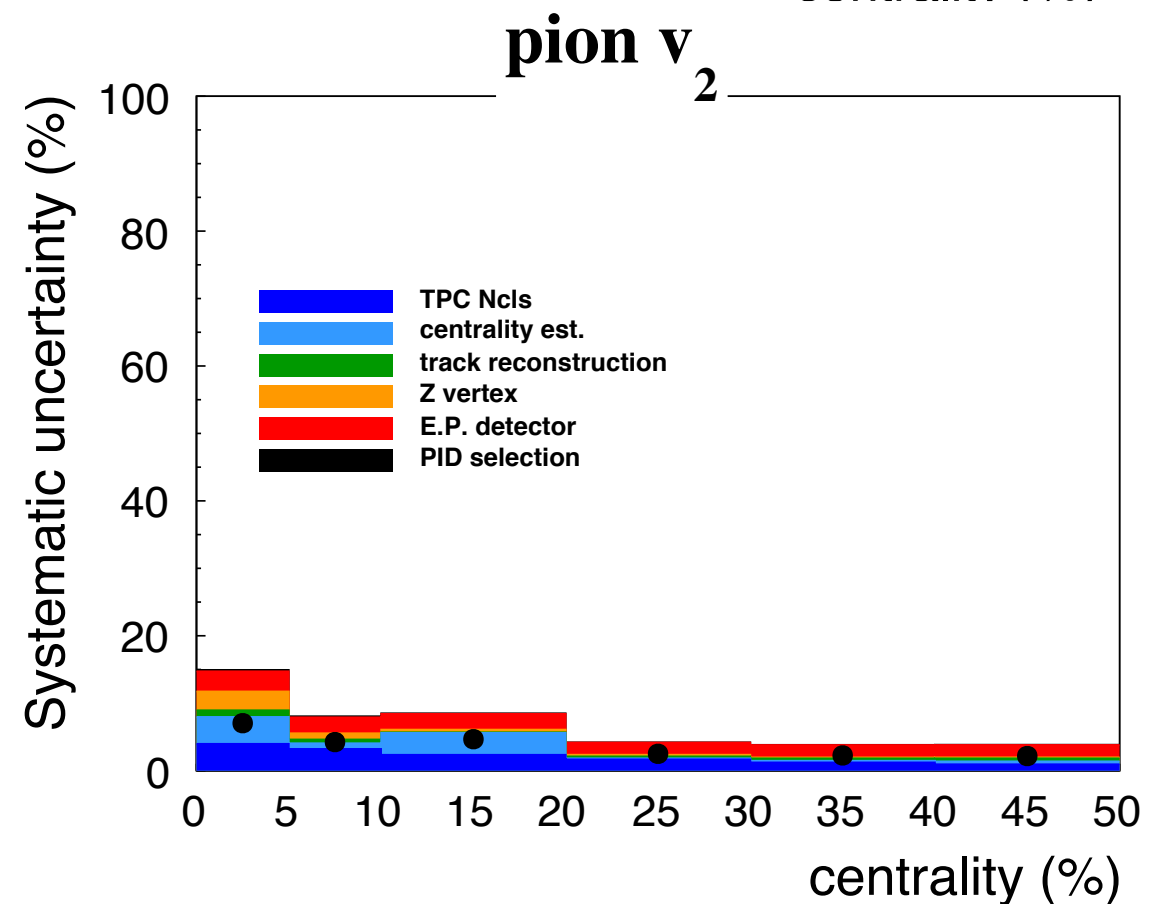
## □ HBT analysis

- ✓ charge ( $\pi^+\pi^+$  pair and  $\pi^-\pi^-$  pair)
- ✓ B field (positive and negative)
- ✓ Event plane (VZERO detector)
- ✓ Pair cut (tight cut  $3.5\sigma$ )
- ✓ Fit range (140, 130 MeV/c)

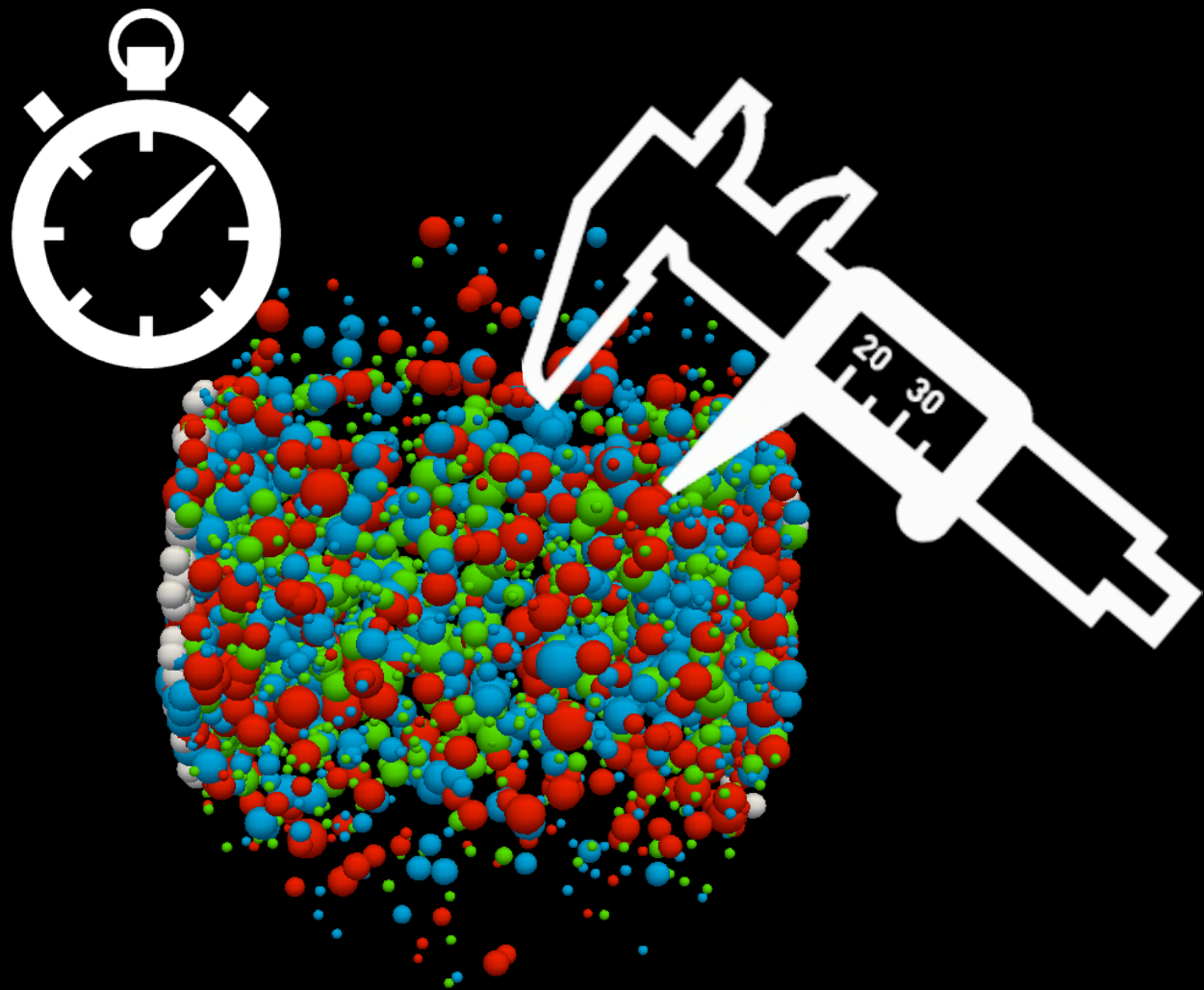


## □ Flow analysis

- ✓ TPC # of clusters (50, 90)
- ✓ Centrality estimator (ITS 2<sup>nd</sup> layer)
- ✓ Z-vertex (5, 10cm)
- ✓ Event Plane
  - ✓ FMDA, FMDC, V0A, V0C, V0AC,
  - TPC( $-1 < \eta < -0.5$ ) and TPC( $0.5 < \eta < 1.0$ )
- ✓ PID probability (75, 90%)



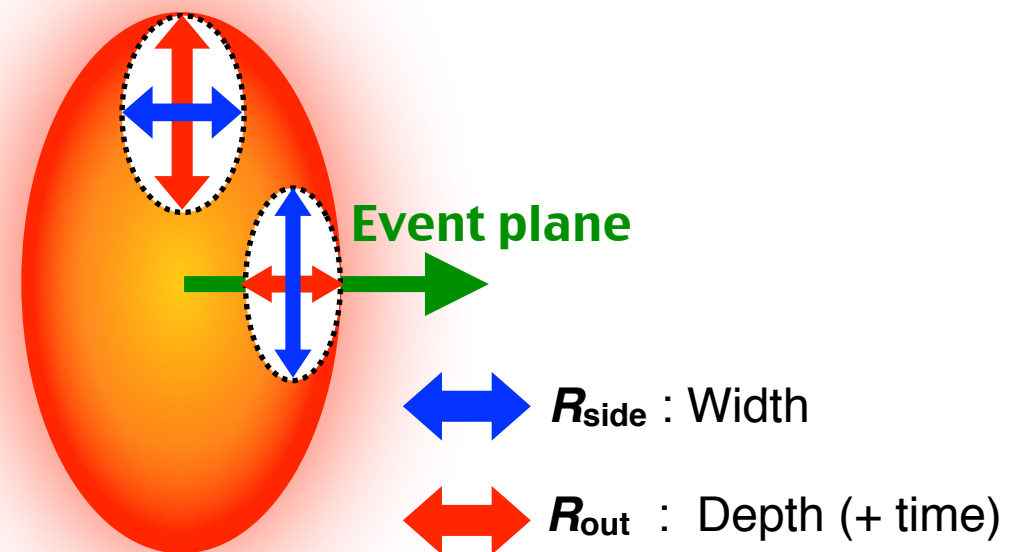
# Result & Discussion



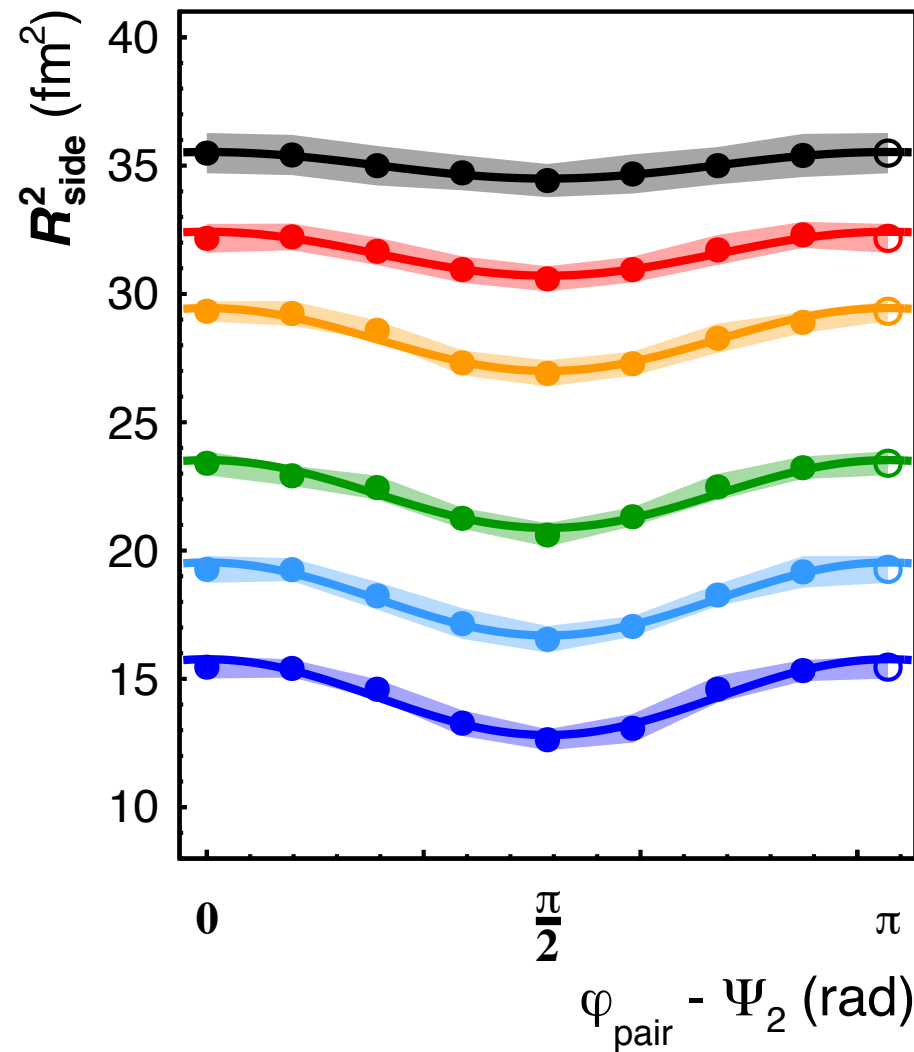
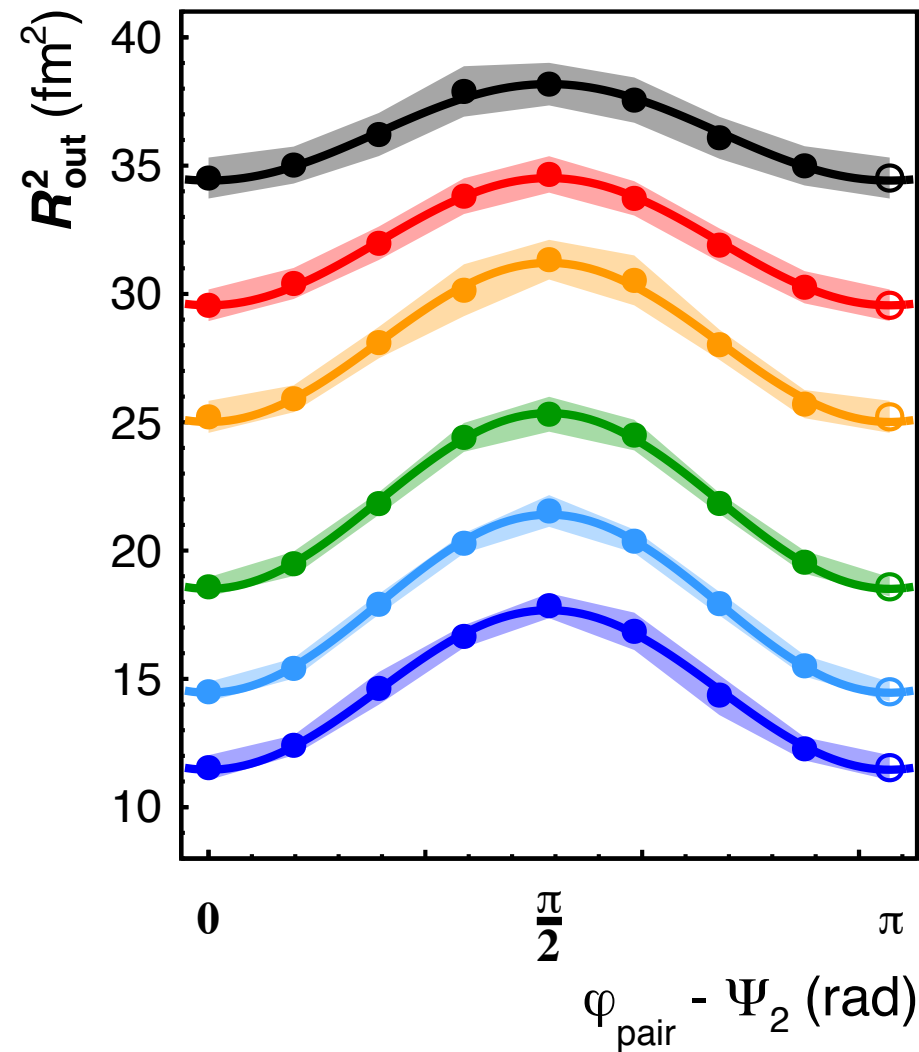


# Second harmonics

geometry @freeze-out



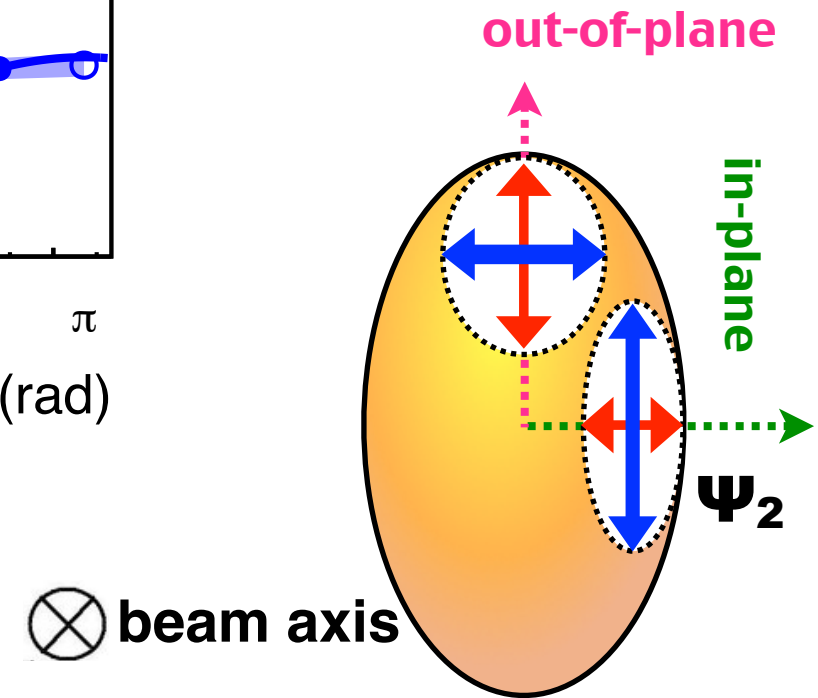
# Azimuthal angle dependence of HBT w.r.t. $\Psi_2$



Pb-Pb  $\sqrt{s_{NN}}=2.76$  TeV  
 $\pi^+\pi^+$  and  $\pi^-\pi^-$  combined  
 $k_T : 0.2-1.5$  GeV/c  
 centrality

- 0-5%
- 5-10%
- 10-20%
- 20-30%
- 30-40%
- 40-50%

- Fit function :  $R^2_{\mu,0} + 2 R^2_{\mu,2} \cos(2(\phi_{\text{pair}} - \Psi_2))$ 
  - $R^2_{\mu,0}$  : Average HBT radii
  - $R^2_{\mu,2}$  : Oscillation amplitude

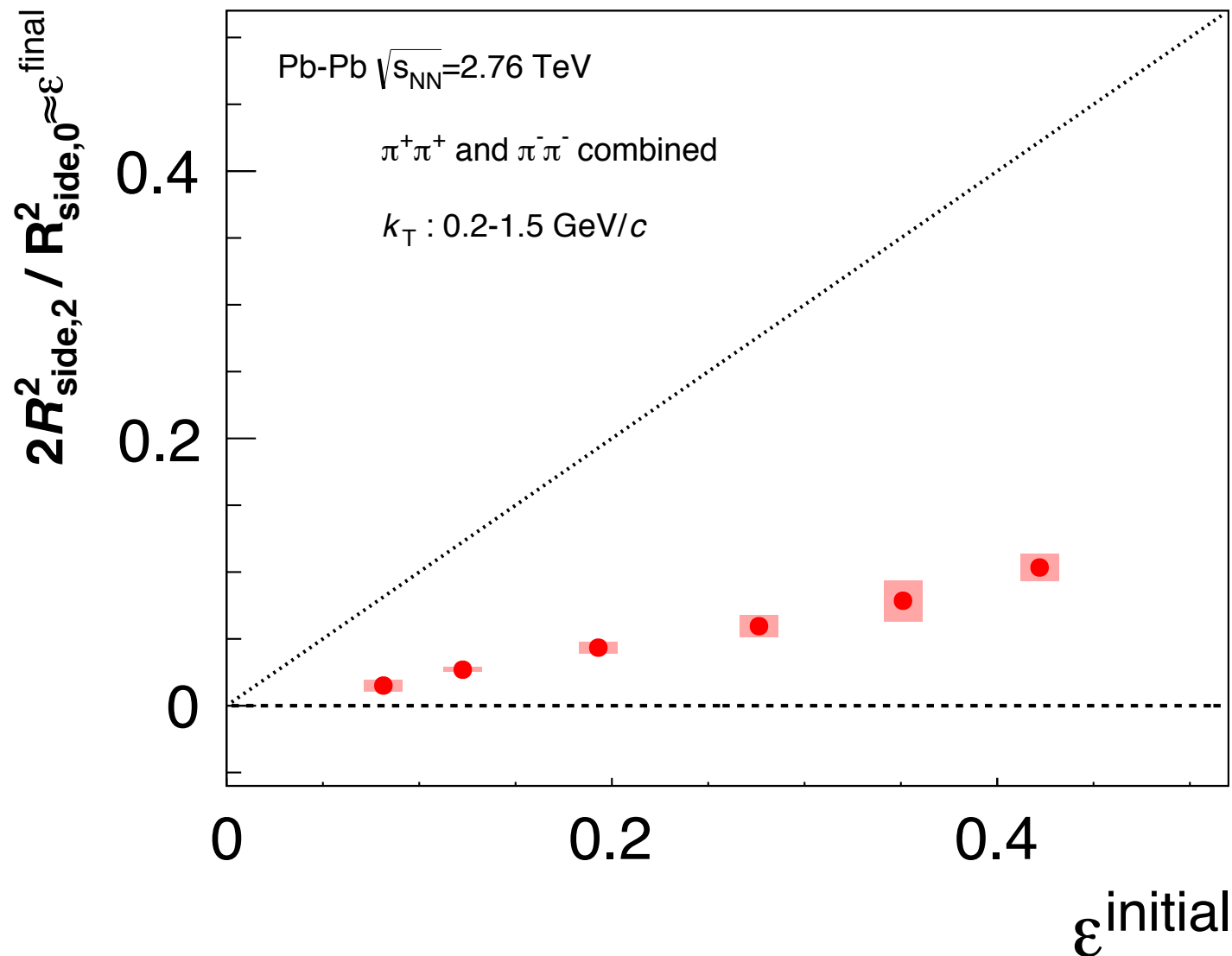


$\longleftrightarrow$   $R_{\text{side}}$  : width  
 $\longleftrightarrow$   $R_{\text{out}}$  : depth + time

- Explicit oscillation can be seen in  $R_{\text{out}}$ ,  $R_{\text{side}}$
- Oscillation of  $R_{\text{out}}$  and  $R_{\text{side}}$  is out-phase
- $R_{\text{out}}$  has larger oscillation than  $R_{\text{side}}$ . sensitivity to duration time !

✓  $R_{\text{out}}$  is sensitive to  $\beta_T$  ( $R^2_{\text{out}} = R^{2*}_{\text{out}} + \beta_T \Delta\tau^2$ )

# Initial $\epsilon_2$ v.s. final $\epsilon_2$

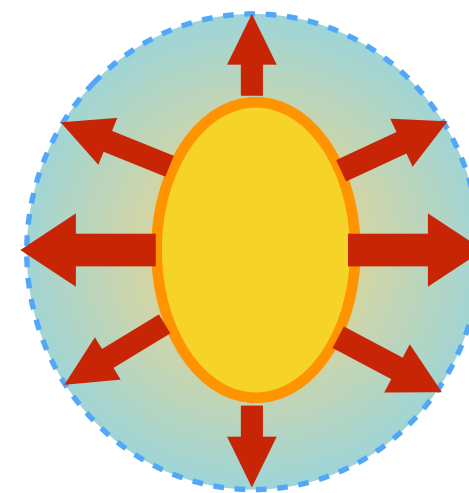


## Final source Eccentricity

$$\epsilon_{final} = 2 \frac{R_{side,2}}{R_{side,0}} = -2 \frac{R_{out,2}}{R_{side,0}} = 2 \frac{R_{os,2}}{R_{side,0}}$$

-  $\epsilon_{final}$  is extracted via HBT oscillation ( $k_T \rightarrow 0$ )

F. Retiere and M.A.Lisa, PRC70.044907

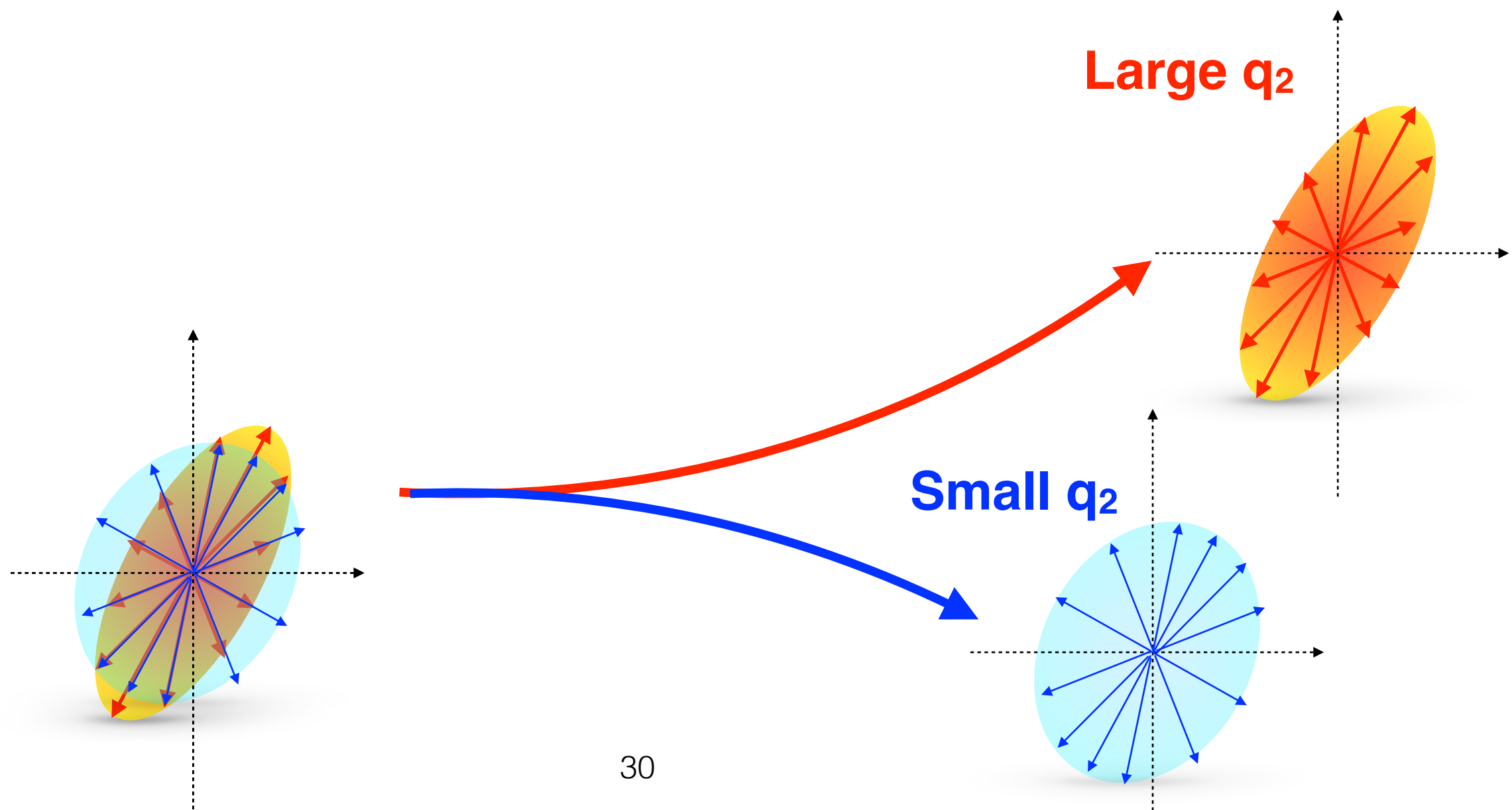


- participant
- freeze-out source
- flow

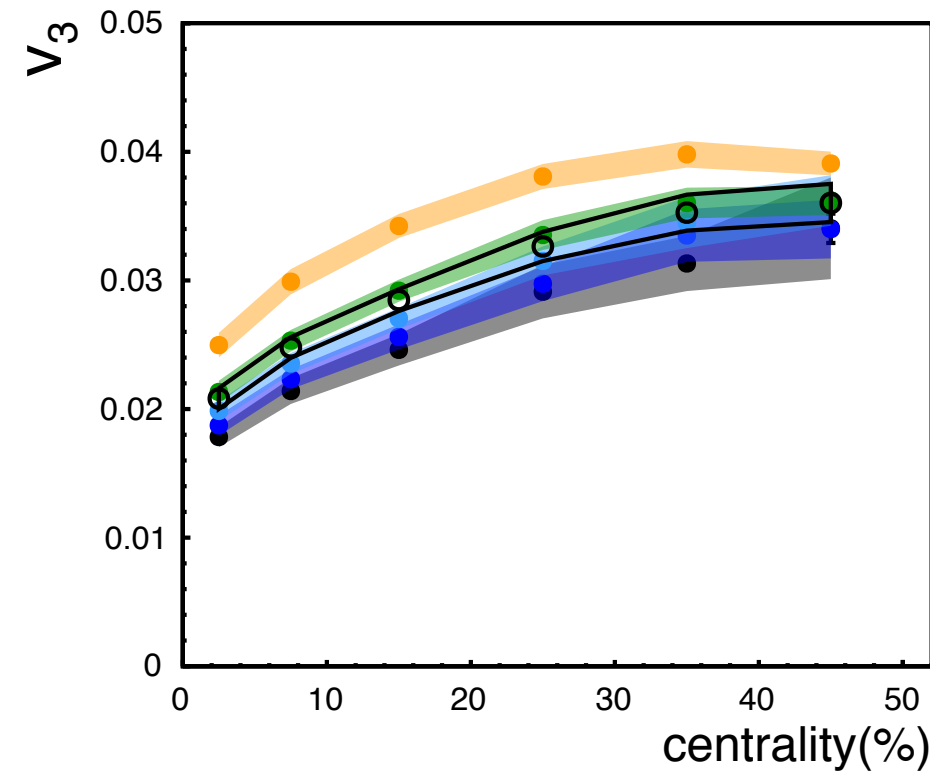
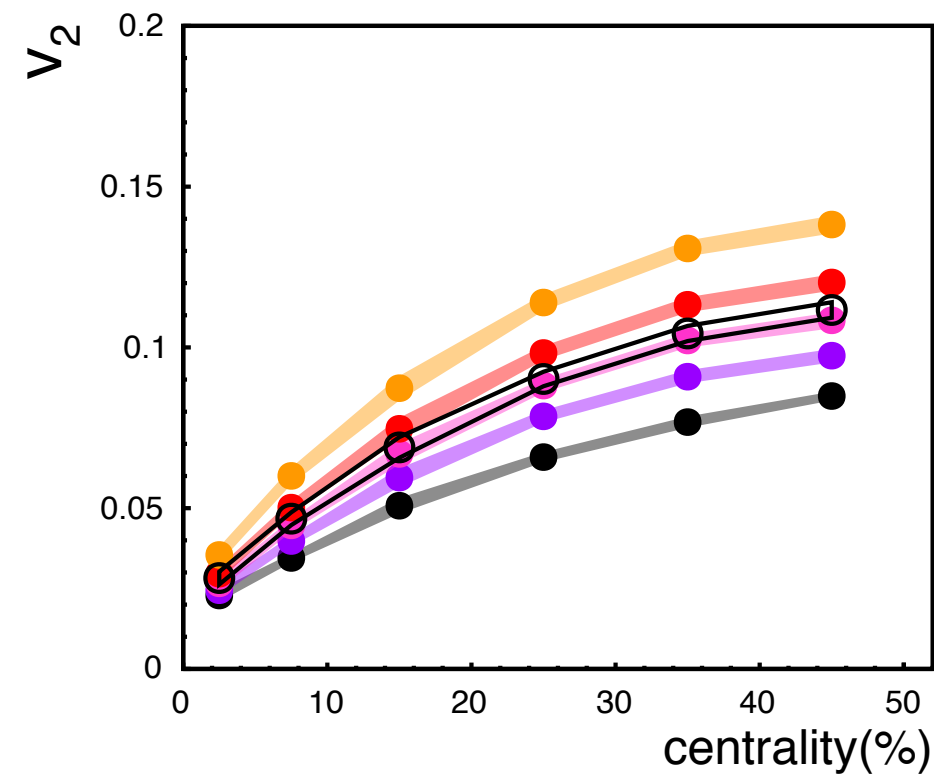
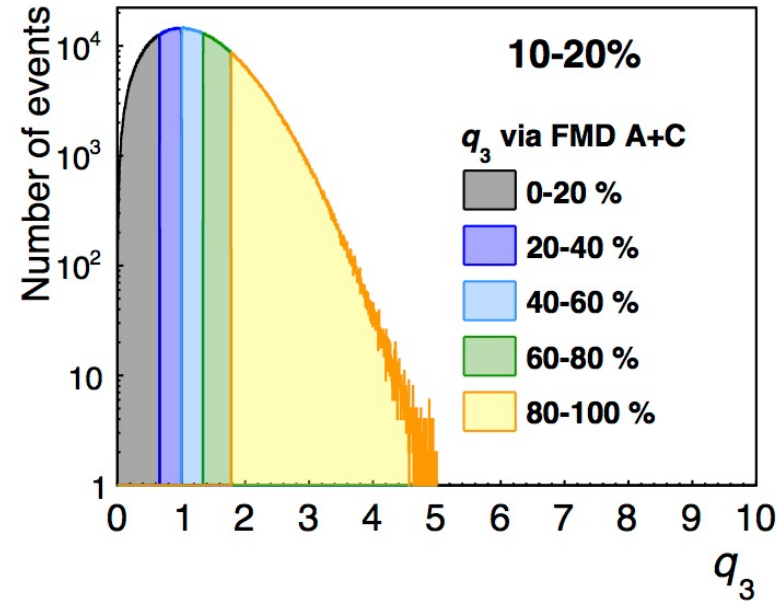
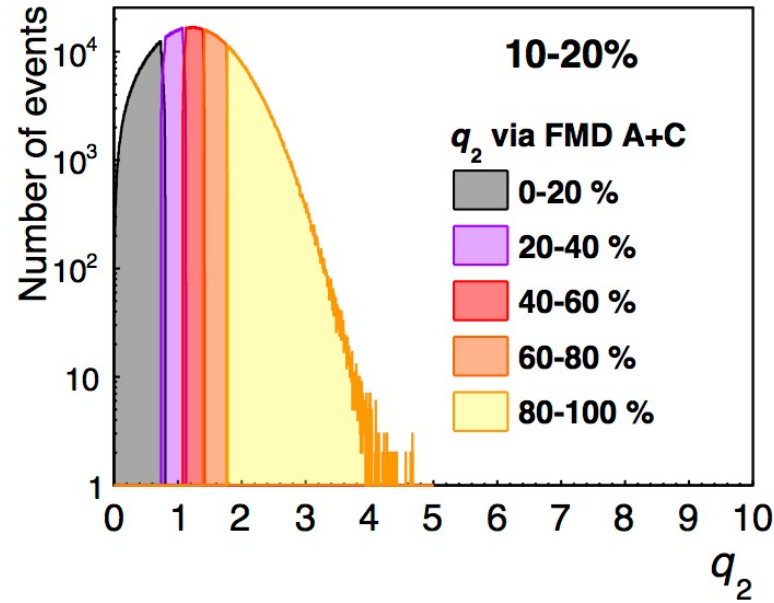
- ▶ Initial elliptic shape has strongly diluted with radial flow and elliptic flow
- ▶ Final source eccentricity linearly increases with increasing  $\epsilon_{initial}^2$ 
  - ➔ Dilution effect linearly increases to  $\epsilon_{initial}^2$  ?
- ▶ Even in most central collision ,  $2R_{side,2}^2 / R_{side,0}^2 > 0$ 
  - ➔ Initial out-plane elongated elliptic shape still remains at freeze-out time

# Event Shape Engineering

## $v_n$ cut (initial $\varepsilon_n$ selection)



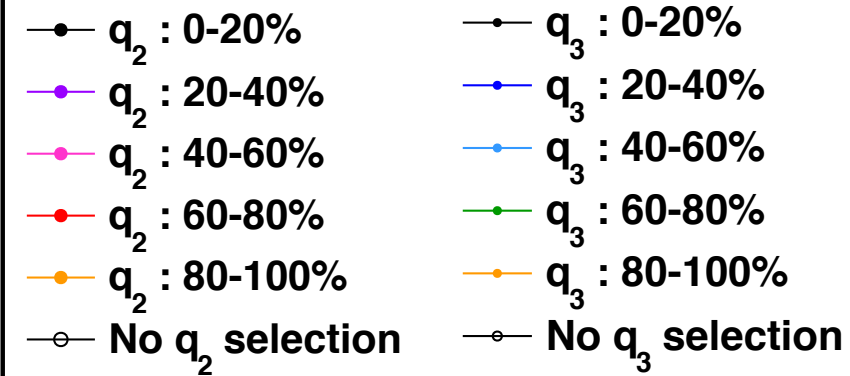
# $v_n$ for each 20% Event shape $q_2, q_3$ selection



Pb-Pb  $\sqrt{s_{NN}}=2.76$  TeV

$\Psi_n$  determined via FMD A+C

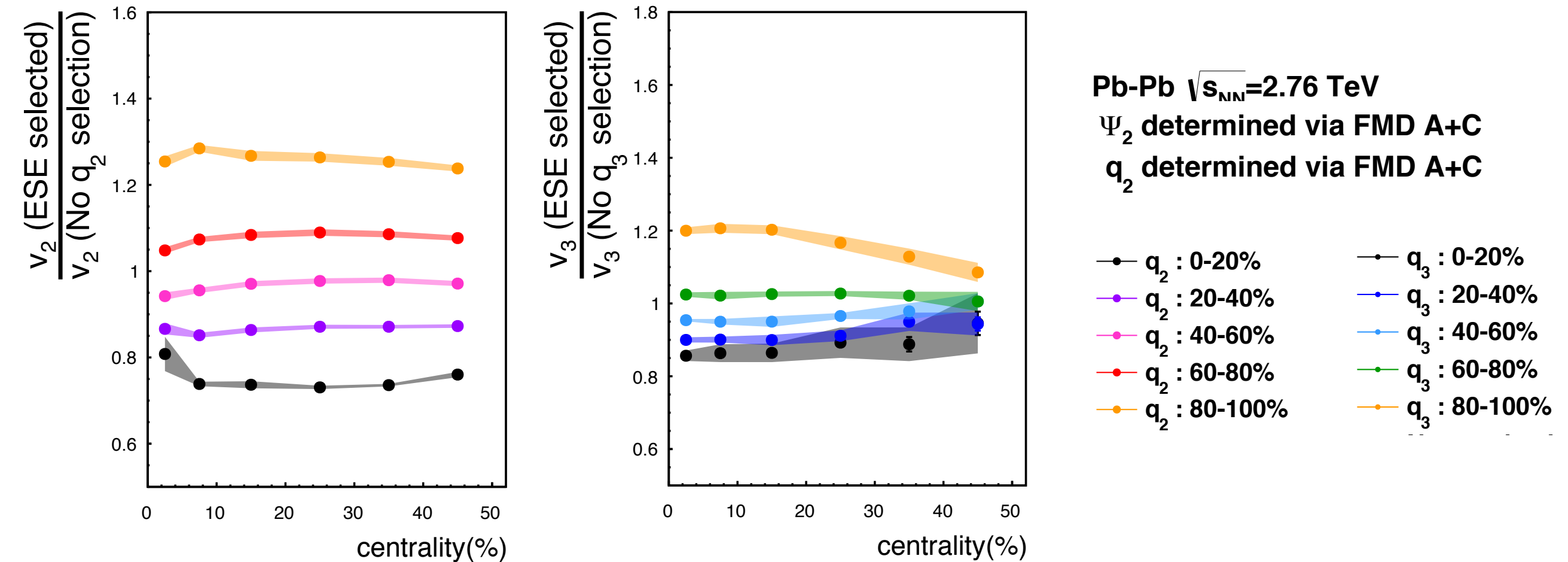
$q_n$  determined via FMD A+C



□ 0-20% (80-100%)  $q_n$  selection denotes top (bottom) 20% cut

□ Event by event  $v_2$  and  $v_3$  fluctuations can be selected with ESE cut

# Ratio of $v_2$ and $v_3$ (ESE selected / No ESE cut)

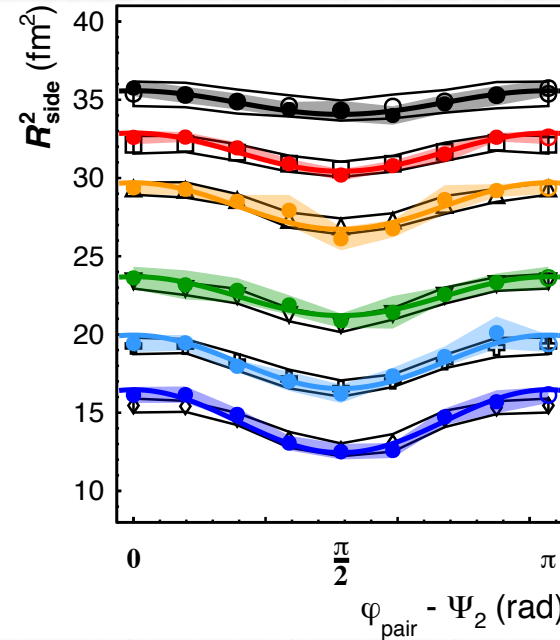
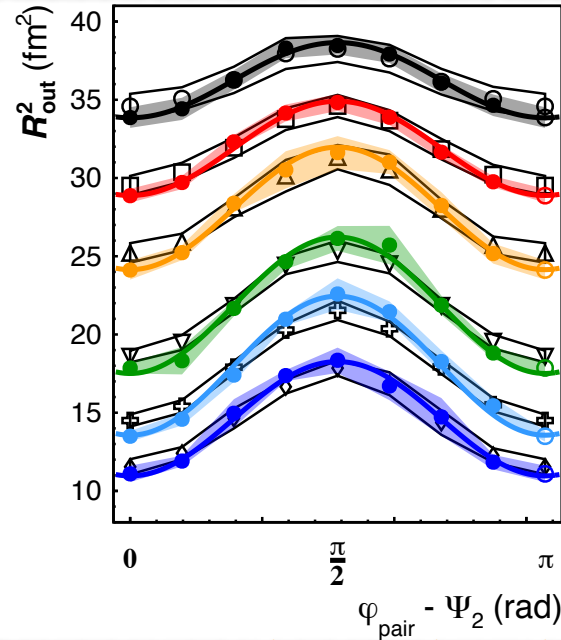
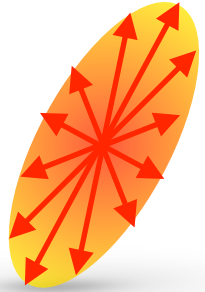


- Both  $q_2$  and  $q_3$ , enhancement (suppression) with ESE cut can be found
- Ratio of  $v_2$  slightly depends on centrality
- Enhancement(suppression) effect becomes smaller from central to peripheral collisions in ratio of  $v_3$
- “Selectivity “ of  $q_2$  cut is larger than that of  $q_3$ 
  - Centrality dependence and difference of selectivity can be interpreted with Event plane resolution



# $q_2$ selection + azimuthal angle dependence of HBT w.r.t. $\Psi_2$

Top 20%  $q_2$



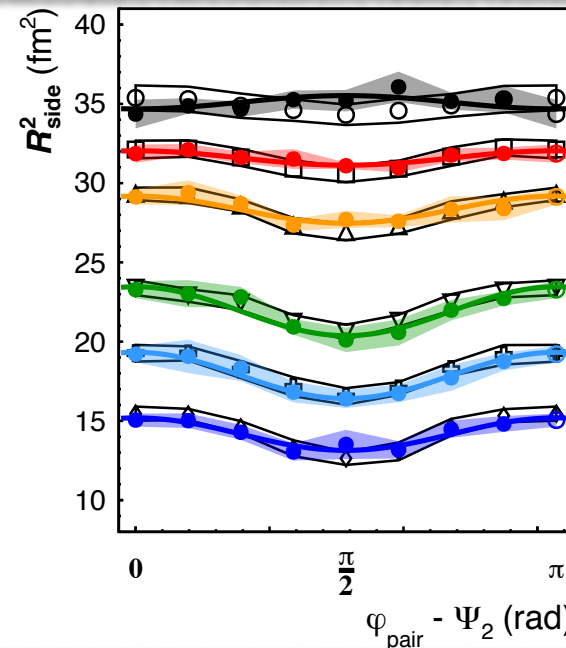
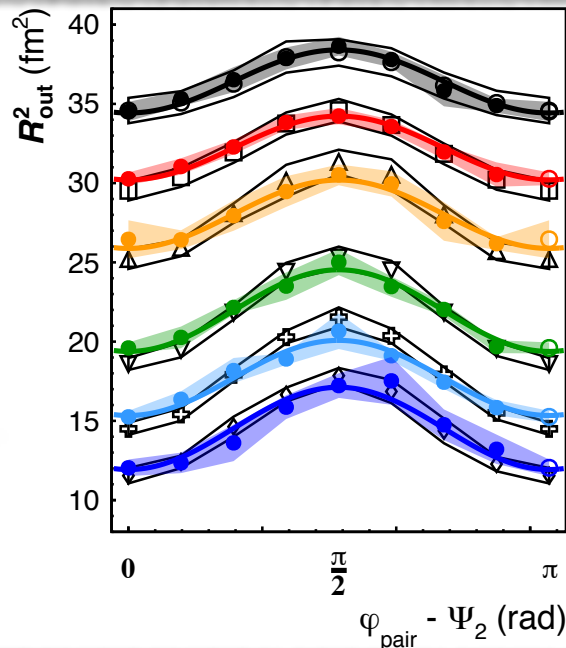
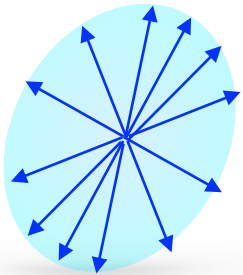
$q_2$  cut centrality

- 0-5%
- 5-10%
- 10-20%
- 20-30%
- 30-40%
- 40-50%

No  $q_2$  selection centrality

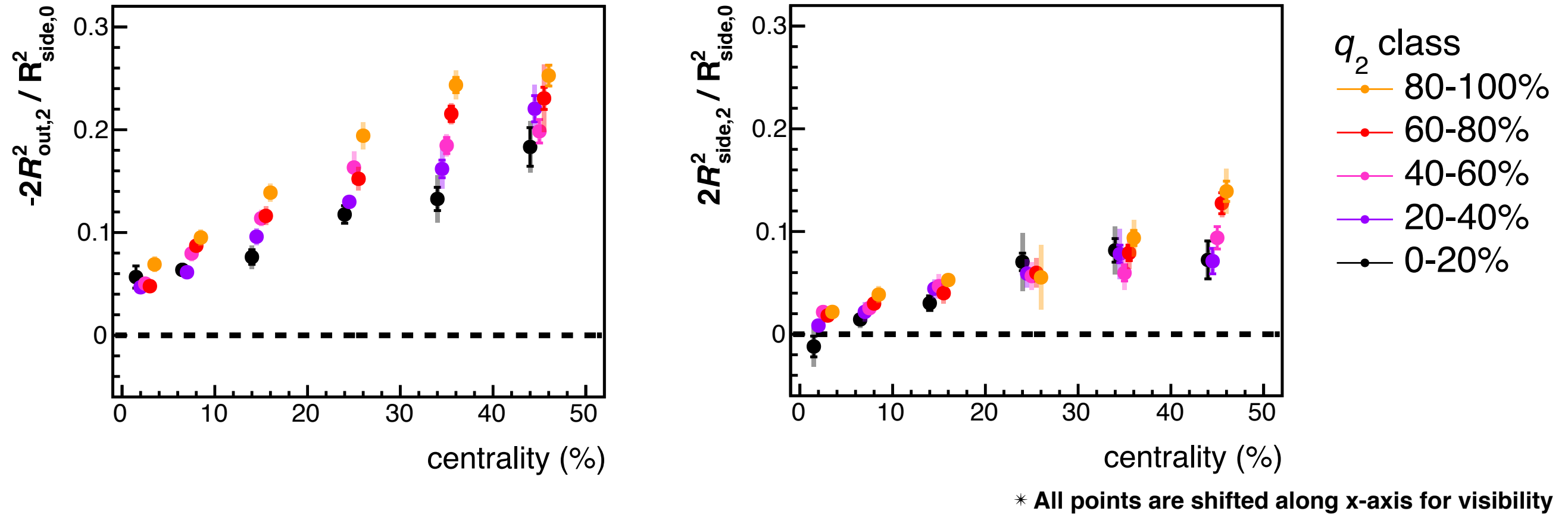
- 0-5%
- 5-10%
- △— 10-20%
- ▽— 20-30%
- ⊕— 30-40%
- ◇— 40-50%

Bottom 20%  $q_2$



- 20%  $q_2$  selection enhanced(suppressed) oscillation of  $R_{out}$  and  $R_{side}$ 
  - Correlation between  $v_2$  and  $\varepsilon_2$  final can be found
- For smallest  $q_2$  selection(0-20%)
  - $R_{side}$  could have positive sign oscillation

# Relative amplitude of HBT radii (**2<sup>nd</sup>** harmonics)



- ◆  $-2R_{out,2}^2 / R_{side,0}^2$  increase from small  $q_2$  to large  $q_2$  in all centrality
- ◆  $2R_{side,2}^2 / R_{side,0}^2$  ( $\sim \epsilon_2^{\text{final}}$ ) increases with increasing  $q_2$  in 0-20% and 40-50% collisions
- ◆ In most centrality 0-5% and smallest  $q_2$ ,  $2R_{side,2}^2 / R_{side,0}^2$  ( $\sim \epsilon_2^{\text{final}}$ ) shows negative (or zero)
  - ➔ Elliptic shape at freeze out might be vanished or even reversed



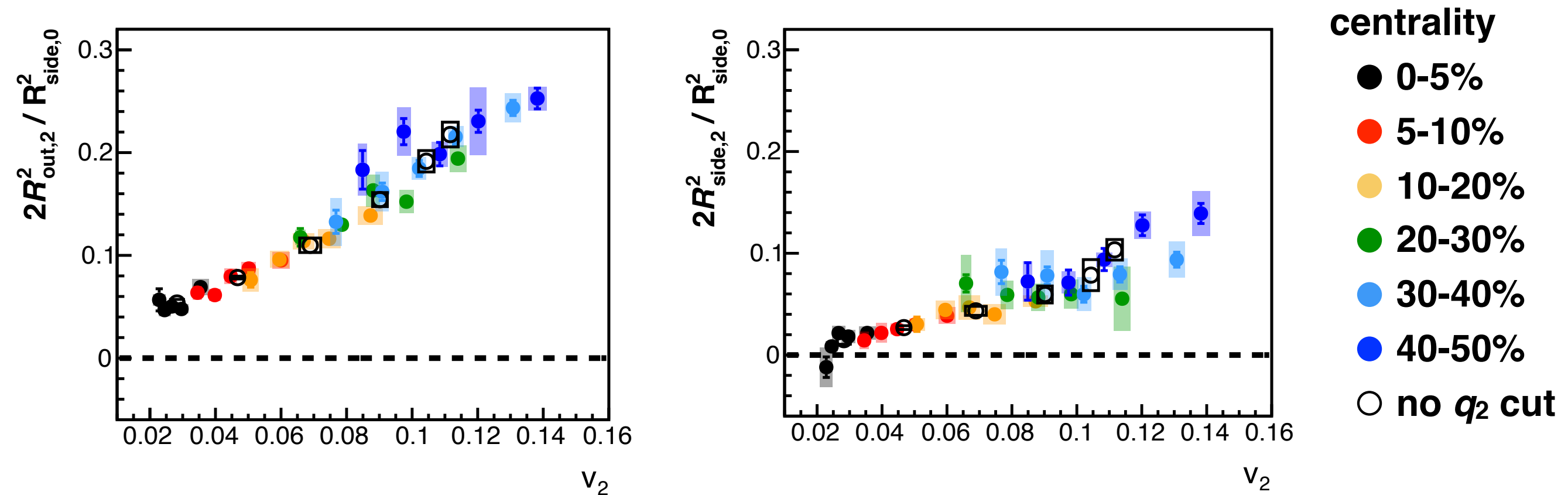
# $v_2$ scaling to Relative amplitude of HBT radii

✓ Difference of event by event initial geometry fluctuation can not be reflected to “centrality”

✓ More sensitive probe is necessary !

◆ Empirical correlation between  $v_2$ ,  $\varepsilon_2^{\text{initial}}$  and energy density

◆  $v_2 \propto \varepsilon_2^{\text{initial}} \cdot f(dN/d\eta)$



✓ Both relative amplitudes of  $R_{\text{out}}$  and  $R_{\text{side}}$  are scaled with  $v_2$

✓ In a same  $dN/d\eta$ (centrality), correlation between  $v_2$  and relative amplitudes of HBT radii  $\sim$  correlation between  $\varepsilon_2^{\text{initial}}$  and  $\varepsilon_2^{\text{final}}$

✓ In centrality 20-40%,  $2R_{\text{side},2}^2 / R_{\text{side},0}^2$  ( $\sim \varepsilon_2^{\text{final}}$ ) does not depends on  $\varepsilon_2^{\text{initial}}$

# Blast-wave fit for spectra, $v_2$ and HBT radii

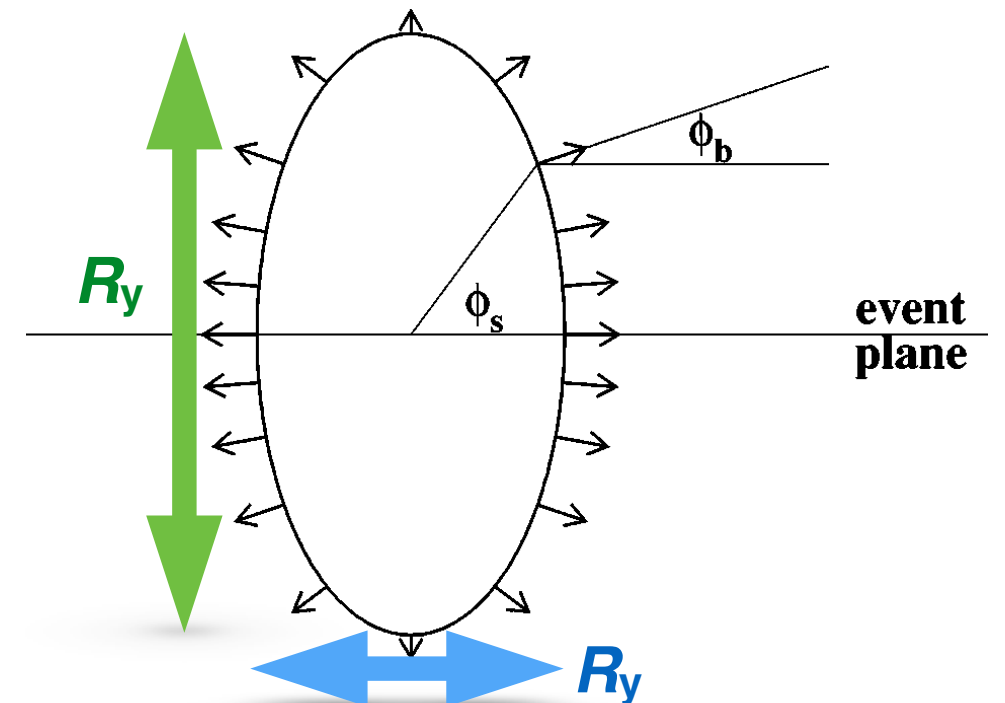
- What makes the difference of relative amplitude of HBT radii with  $q_2$  selection ?
  - ◆ Blast-wave model allows us to extract spatio-temporal parameters, analytically
- Blast-wave model is based on the hydrodynamical model
- Extended to Azimuthally sensitive HBT interferometry (Phys. Rev. C 70 044907)

## ★ Blast-wave parameters

- Freeze out temperature :  $T_f$
- Flow velocity :  $\rho(r, \phi_s) = r ( \rho_0 + \rho_2 \cos(2\phi_b) )$
- Transverse extents  $R_x, R_y$
- System lifetime :  $\tau_0$
- Emission duration :  $\Delta\tau$

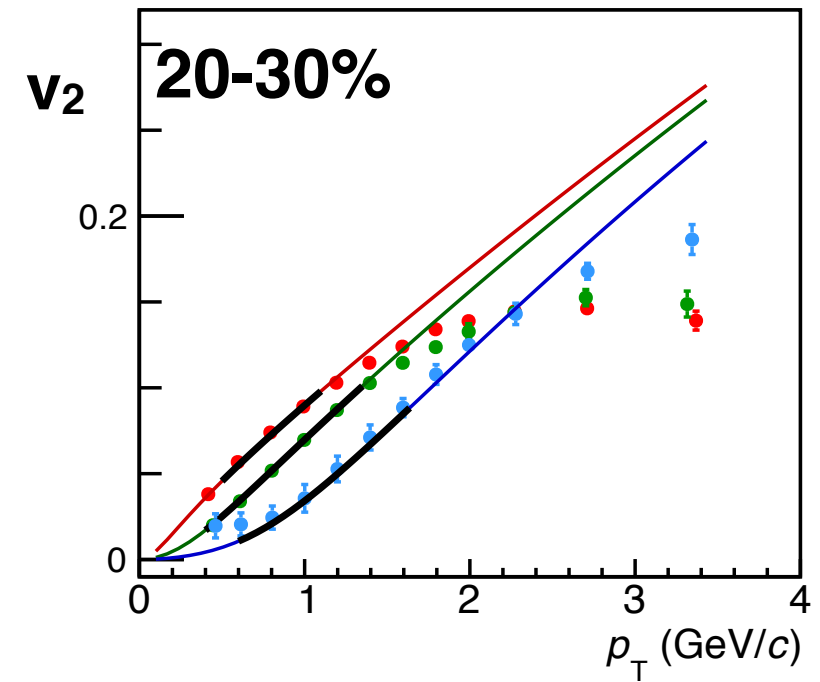
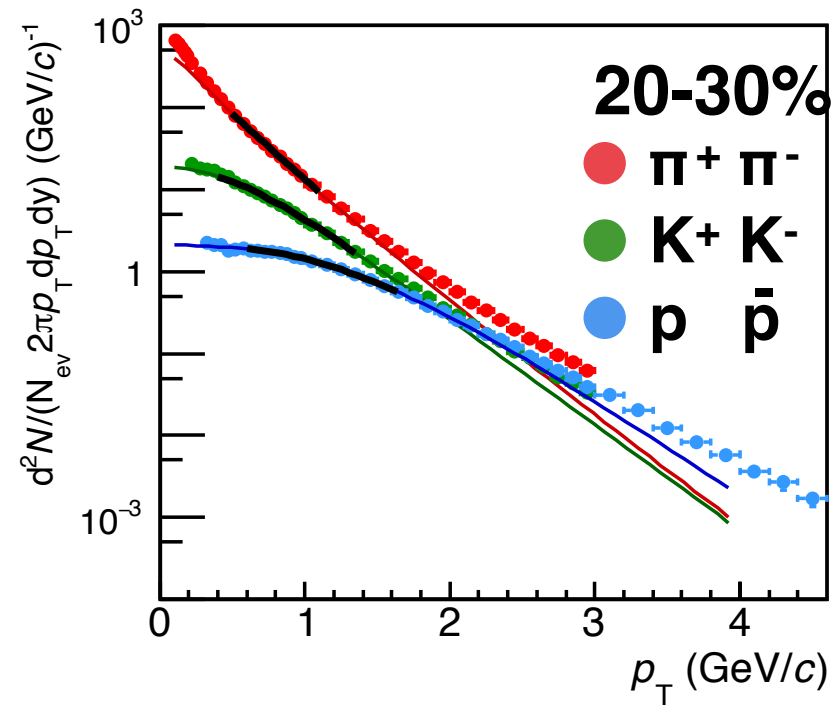
$$\Omega(r, \phi_s) = \frac{1}{1 + e^{(\tilde{r}-1)/a_s}}$$

$$\tilde{r}(r, \phi_s) \equiv \sqrt{\frac{(r \cos(\phi_s))^2}{R_x^2} + \frac{(r \sin(\phi_s))^2}{R_y^2}}$$

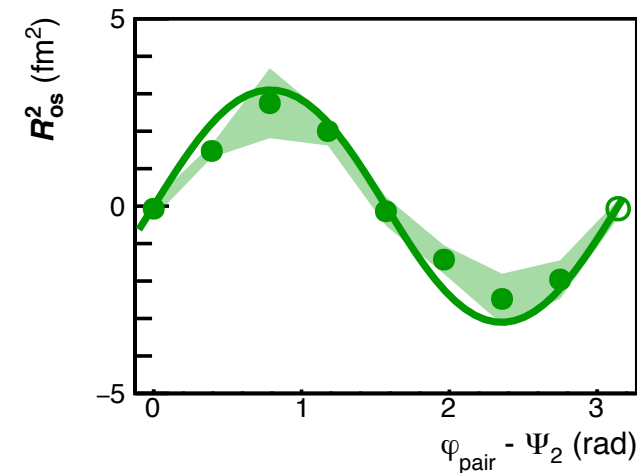
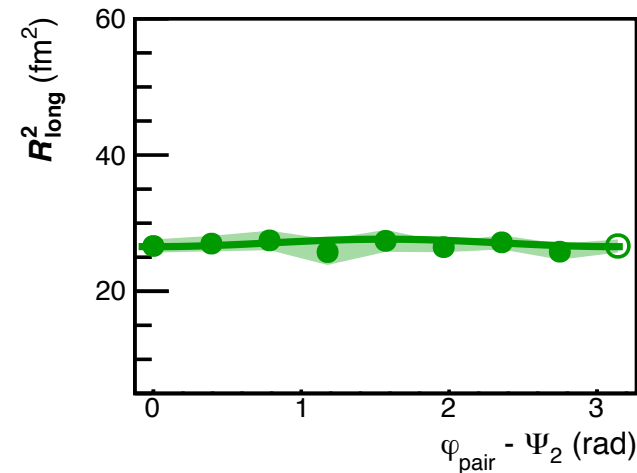
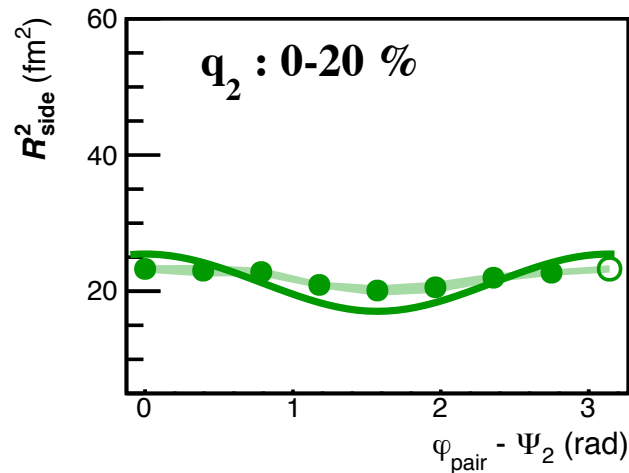
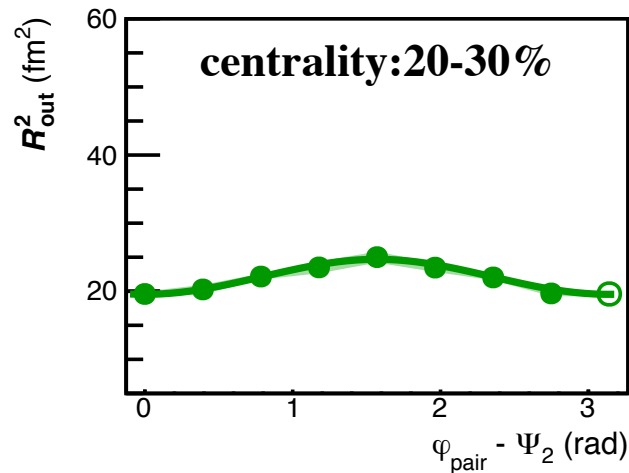


# Blast wave fit for Spectra, $v_2$ and HBT radii

- ▶  $T_f$ ,  $\rho_0$  is determined with  $\pi$ , K, p spectra (independent of  $v_2$  and HBT)
  - ✓ assuming that  $T_f$  and  $\rho_0$  don't change within systematic uncertainties
- ▶  $\rho_2$ ,  $R_x$ ,  $R_y/R_x$ ,  $\tau_0$ ,  $\Delta\tau$  are determined with simultaneous fitting of  $v_2$  and HBT fit

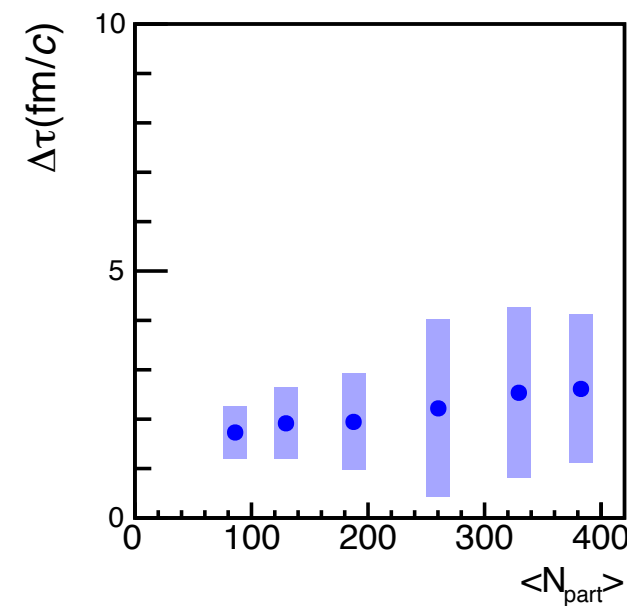
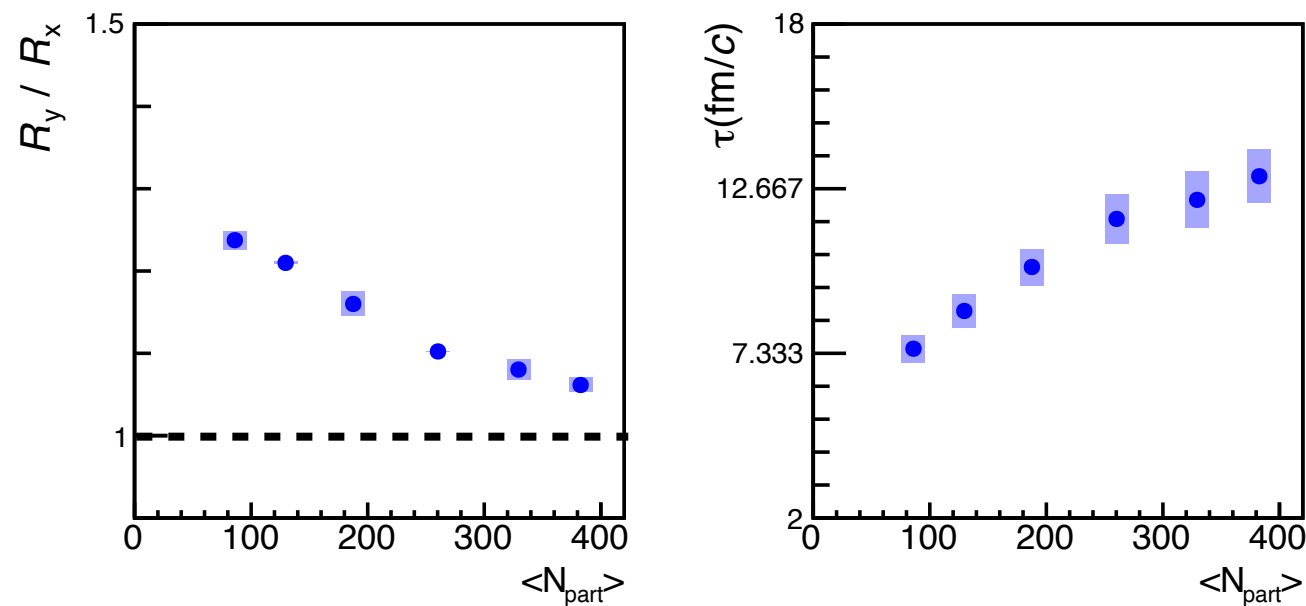
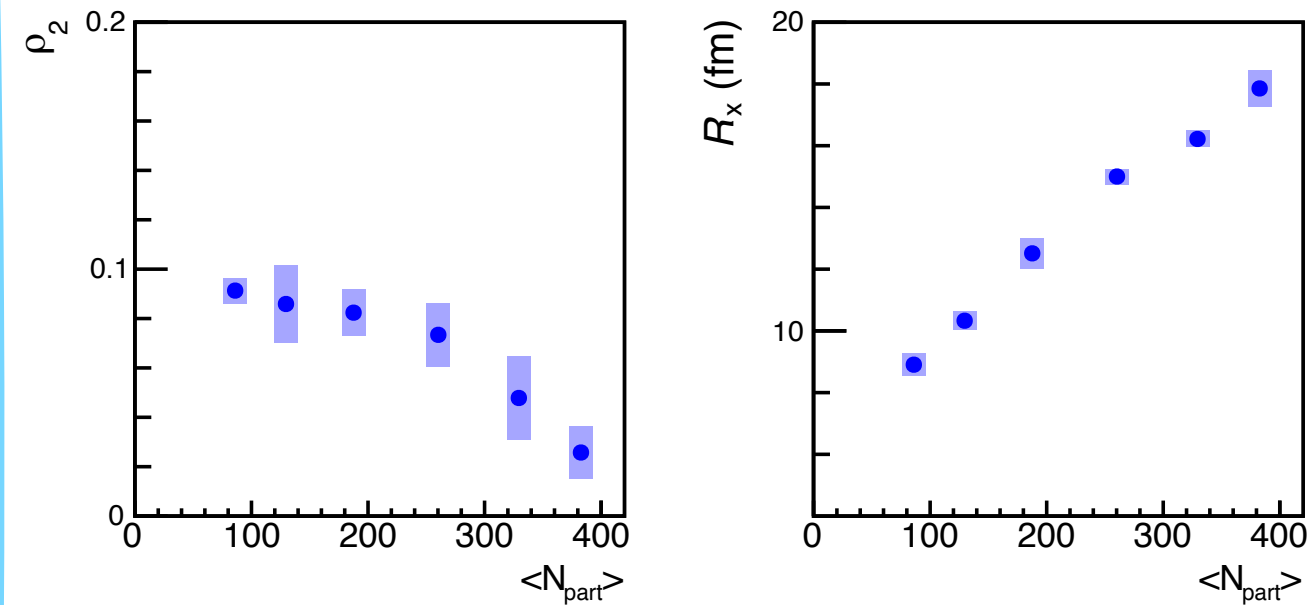
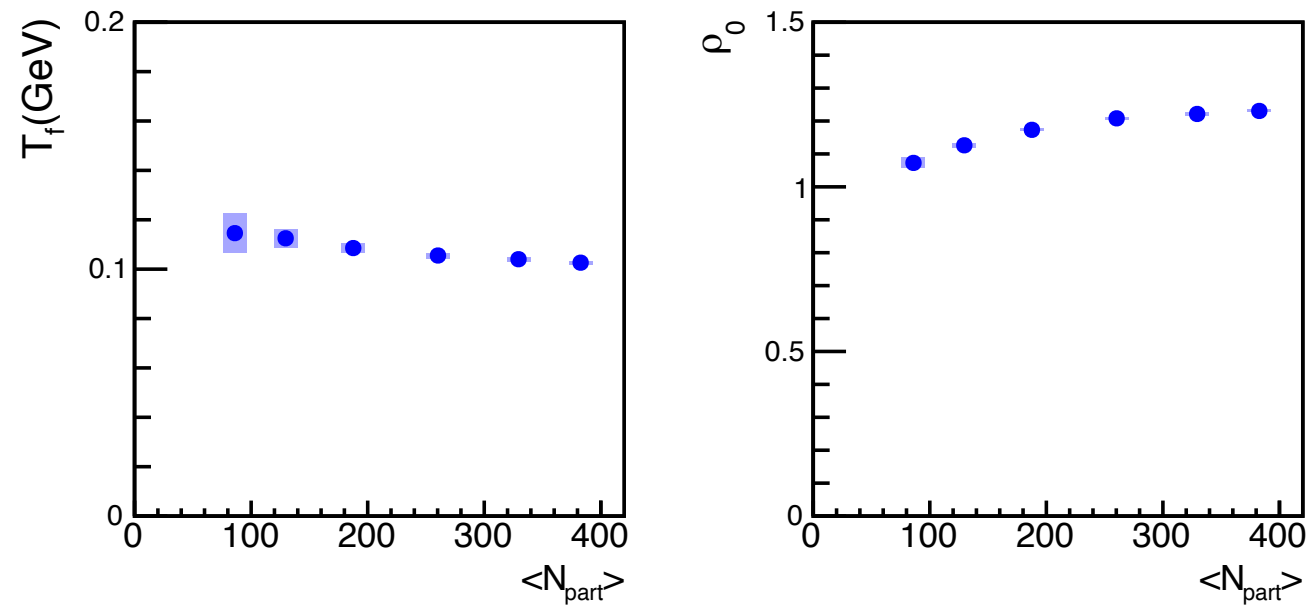


❖ spectra (Phys.Rev.C 88, 044910 [2013])



# Extracted Blast Wave parameters

✓ Fully consistent with published result



Pb-Pb  $\sqrt{s_{\text{NN}}} = 2.76$  TeV

$\pi^+\pi^+$  and  $\pi^-\pi^-$

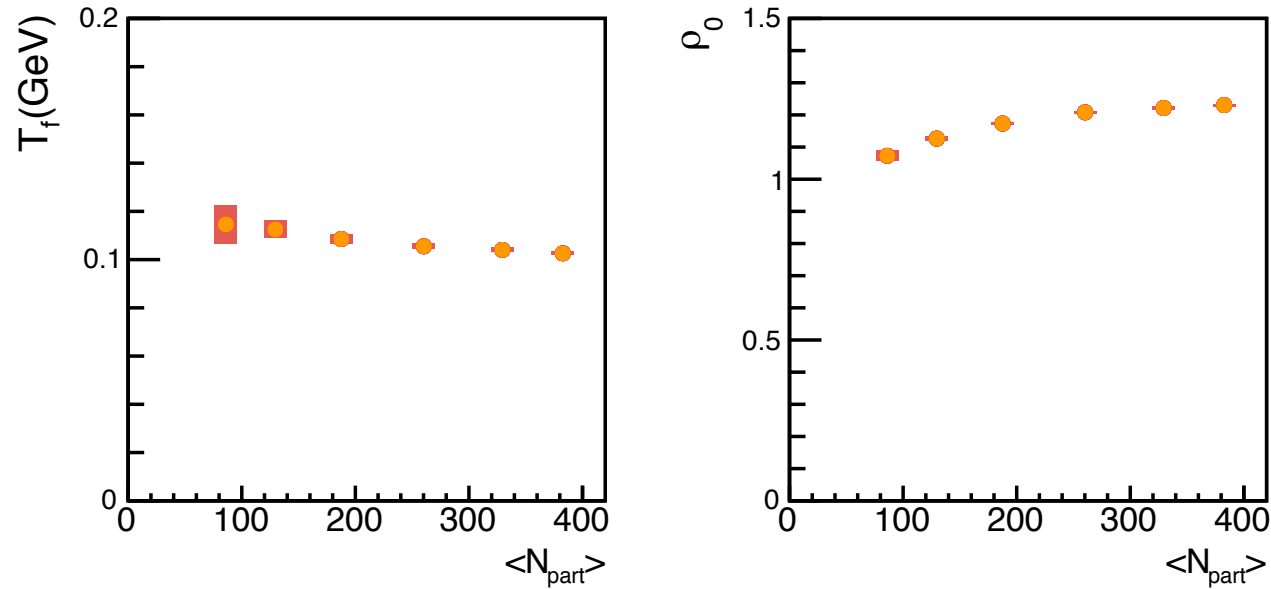
$k_T : 0.2-1.5$  GeV/c

- ◆ Source size( $R_x$ ) and freeze out time ( $\tau_0$ ) increases as a function of  $\langle N_{\text{part}} \rangle$
- ◆ Emission duration slightly increase with increasing  $\langle N_{\text{part}} \rangle$
- ◆  $R_y/R_x$ ,  $T_f$  and  $\rho_2$  decrease from peripheral to central

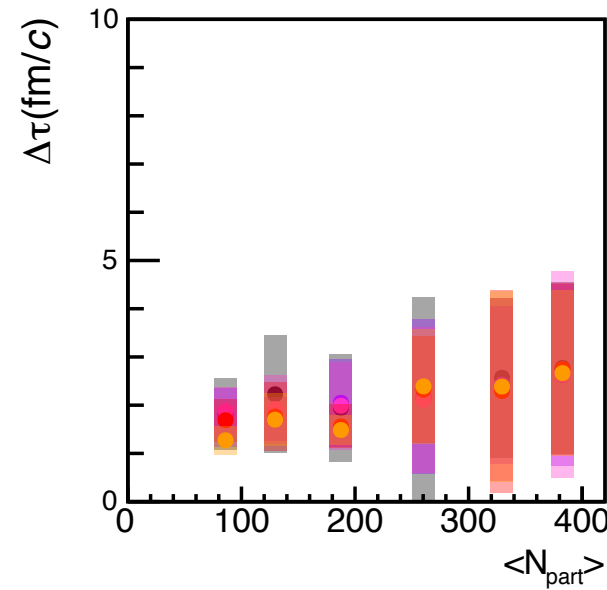
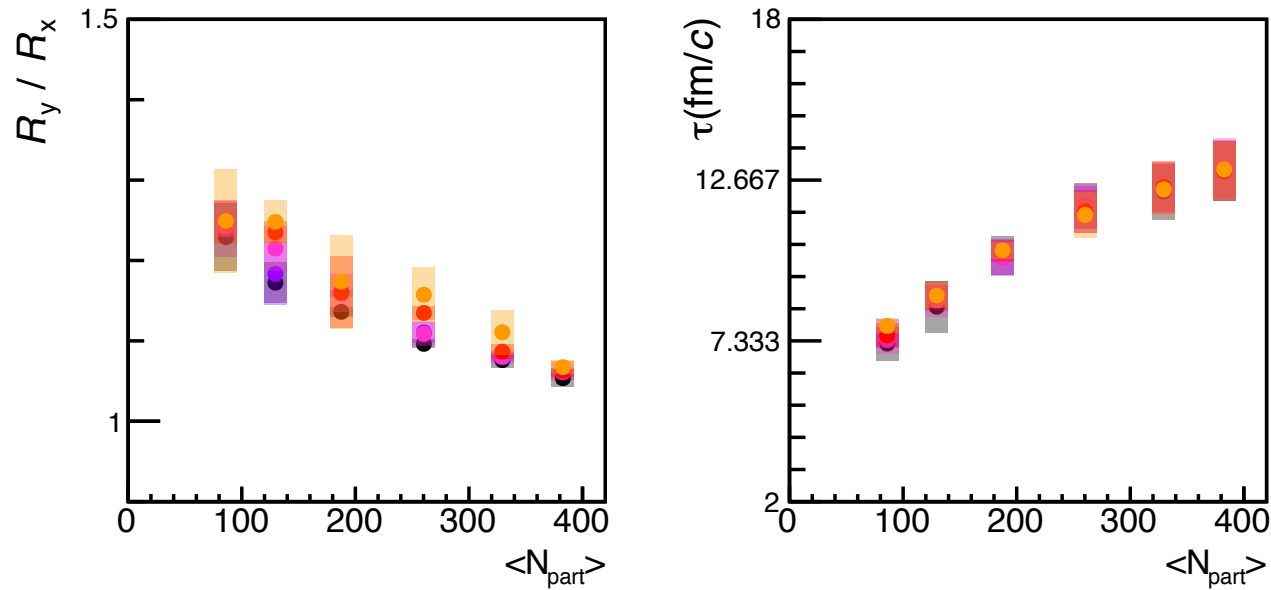
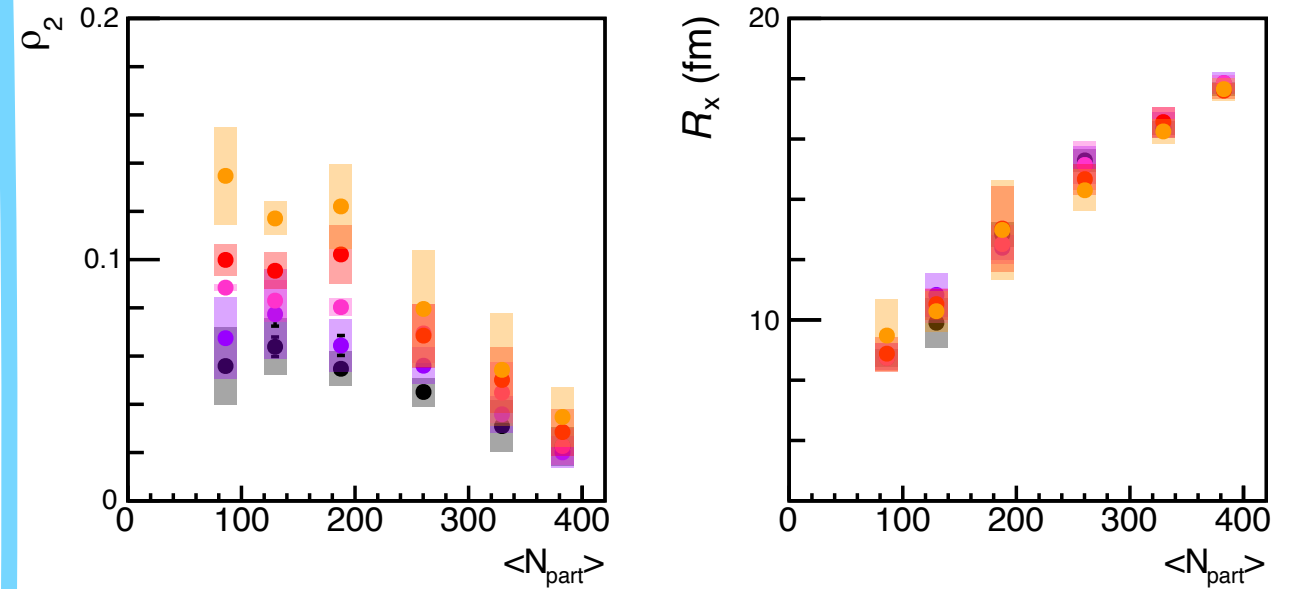
✓ Out-plane elongated elliptic shape can be found even in most central events

# Extracted Blast Wave parameters with ESE $q_2$ cut

## ◆ Spectra fit



## ◆ $v_2$ and HBT fit

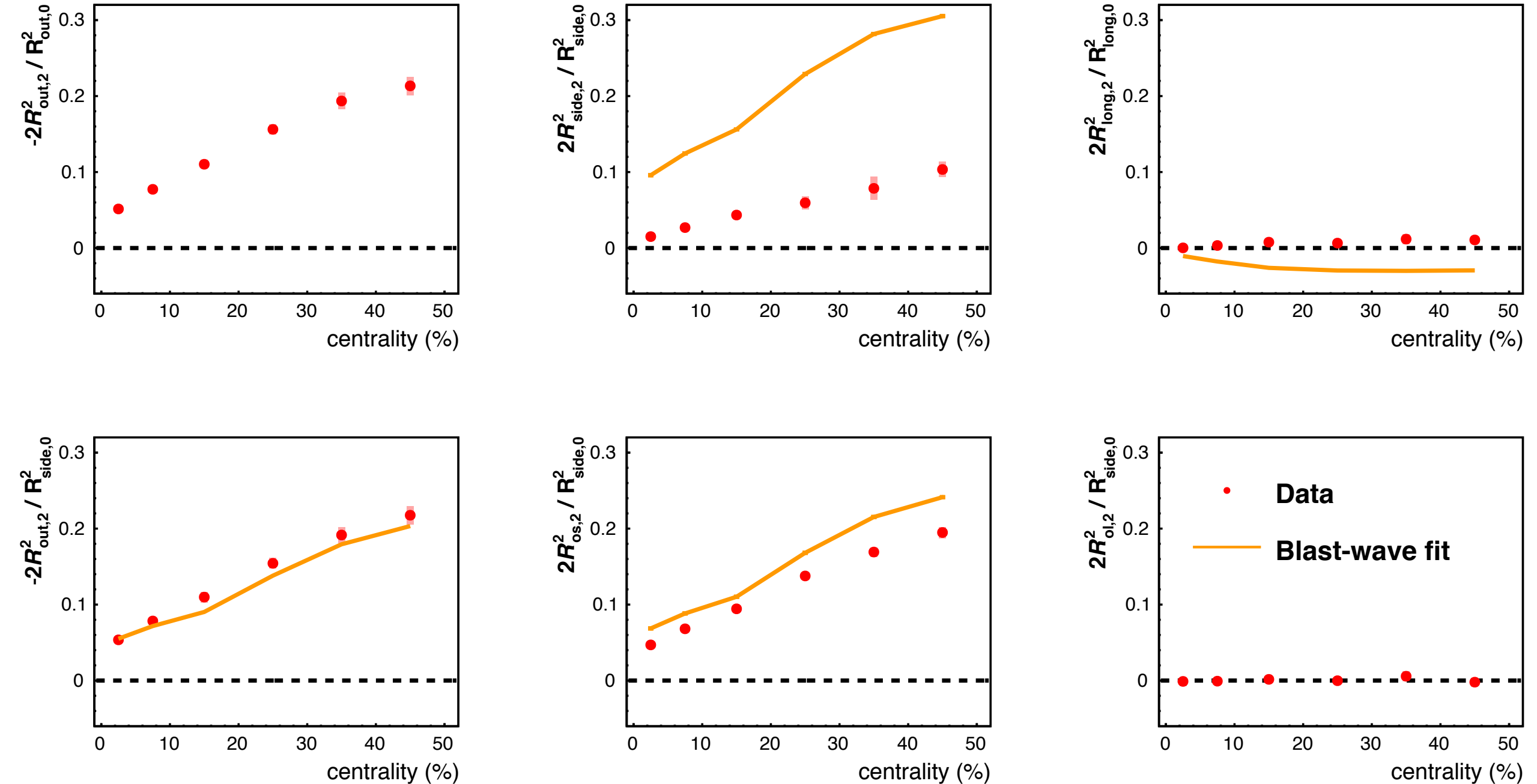


Pb-Pb  $\sqrt{s_{\text{NN}}} = 2.76$  TeV  
 $\pi^+\pi^+$  and  $\pi^-\pi^-$   
 $k_T : 0.2-1.5$  GeV/c  
 $q_2$   
 • 0-20%  
 • 20-40%  
 • 40-60%  
 • 60-80%  
 • 80-100%

- ◆  $\rho_2$  significantly changes with  $q_2$  selection
- ◆  $R_y/R_x$ ,  $\tau$  slightly changes with  $q_2$  cut, but consistent within systematic uncertainties
- ◆ No significant difference can be found in  $R_x$ ,  $\Delta\tau$



# Comparison with Blast-wave model (relative amplitude)



- ◆  $-2R_{\text{out},2}^2 / R_{\text{side},0}^2$  is consistent within a systematic uncertainty
- ◆  $2R_{\text{side},2}^2 / R_{\text{side},0}^2$  of Blast-wave is much larger than that of Data
- ◆  $2R_{\text{os},2}^2 / R_{\text{side},0}^2$  of Blast-wave is slightly larger than that of Data
- ★ More realistic model is necessary

# Summary-1

- ✦ **Azimuthal angle dependence of HBT relative to 2<sup>nd</sup> order event plane**
  - Explicit oscillation can be found in  $R_{\text{out}}$ ,  $R_{\text{side}}$
  - Initial elliptic shape is strongly diluted by collective flow, but out-plane elongated elliptic shape still remains at freeze-out
  
- ✦ **ESE applies to measurements of azimuthal anisotropy ( $v_2$  and  $v_3$ )**
  - Both  $v_2$  and  $v_3$  are enhanced (suppressed) with large (small)  $q_2$  and  $q_3$  cut
  - “Selectivity” of  $q_2$  to  $v_2$  is larger than that of  $q_3$  to  $v_3$
  
- ✦ **ESE applies to HBT measurements w.r.t. 2<sup>nd</sup> order event plane**
  - First measurement of  $q_2$  selection + HBT
  - Relative amplitudes of  $R_{\text{out}}$ ,  $R_{\text{side}}$  and  $R_{\text{os}}$  vary with  $q_2$  selection
  - In most central collisions 0-5% and smallest  $q_2$ , relative amplitude of  $R_{\text{side}}$  is negative or zero
  - Modification with  $q_2$  was scaled with  $v_2$ , but  $q_2$  dependence of  $R_{\text{side}}$  could change in centrality 20-40%

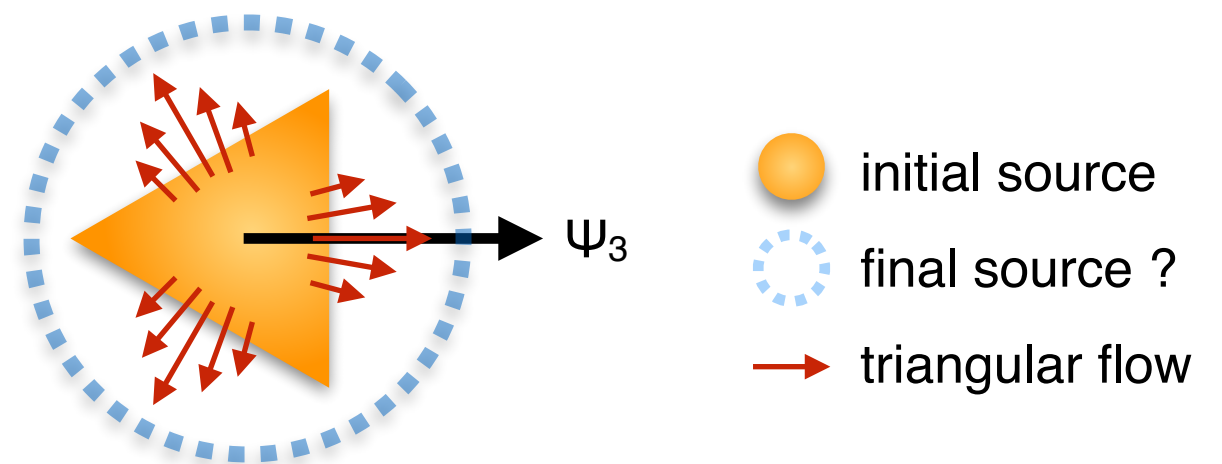
# Summary-2

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## ♦ Interpretation with Blast-wave model

- $\rho_2$  explicitly changes with  $q_2$  selection
- $R_y/R_x$ , system life time slightly changes with  $q_2$  selection, but consistent within systematic uncertainties
- Oscillation of  $R_{\text{side}}$  can not be reproduced with Blast-wave model

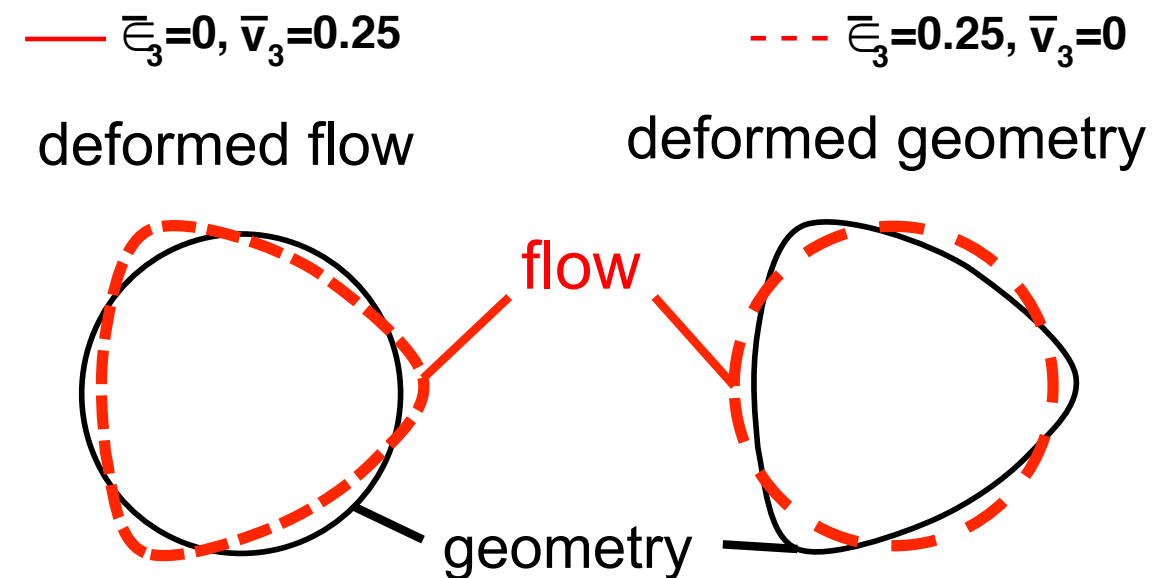
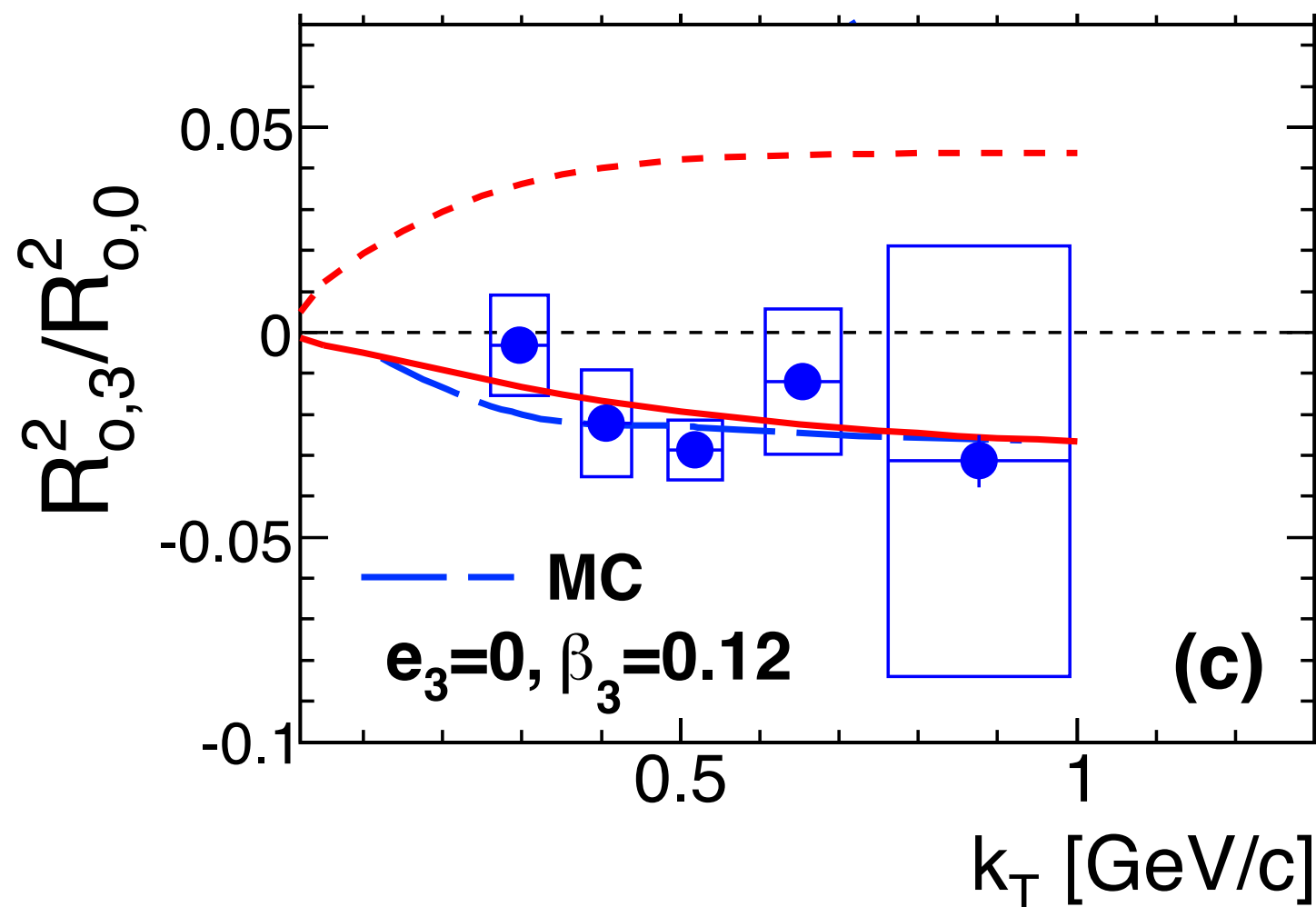
# Triangular shape @ freeze-out



# Oscillation of HBT w.r.t. $\Psi_3$ is flow dominant

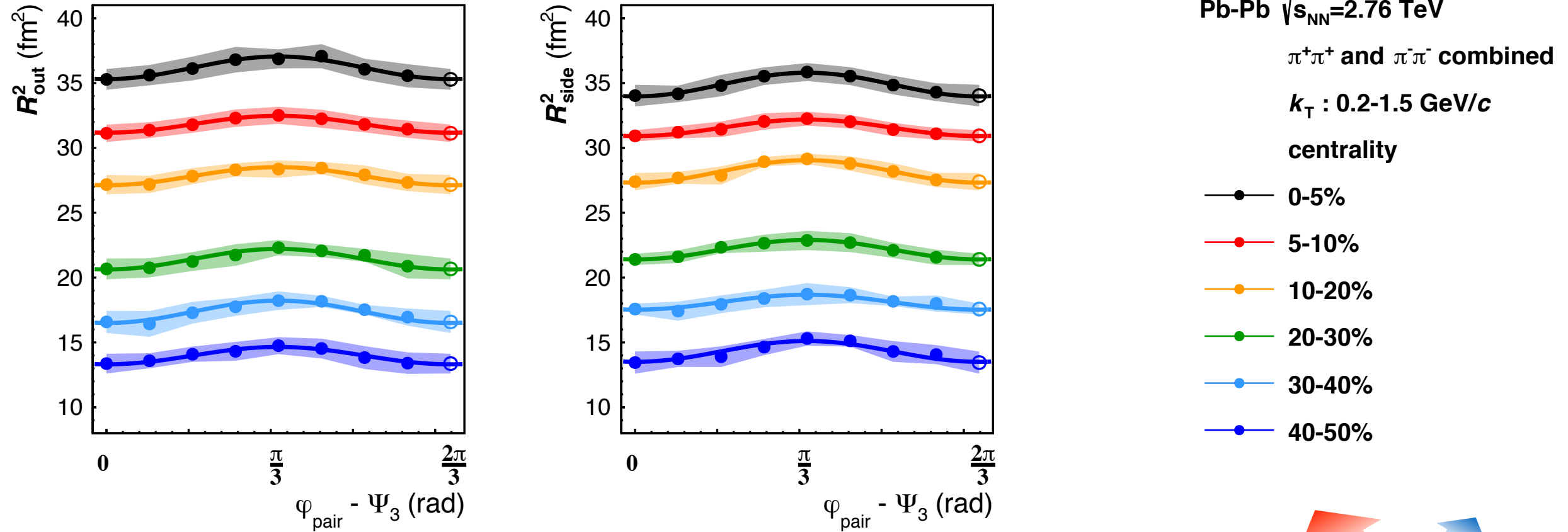
- $k_T$  dependence of 3<sup>rd</sup>-order oscillation at PHENIX is described by flow dominant case of Gaussian toy model

→  $q_3$  + Azimuthal angle dependence of HBT radii is direct measurement of relation between  $v_3$  and oscillation of HBT radii

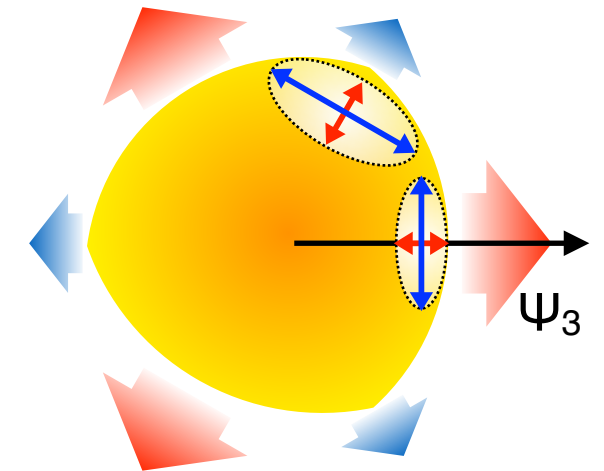




# Azimuthal angle dependence of HBT radii w.r.t. $\Psi_3$

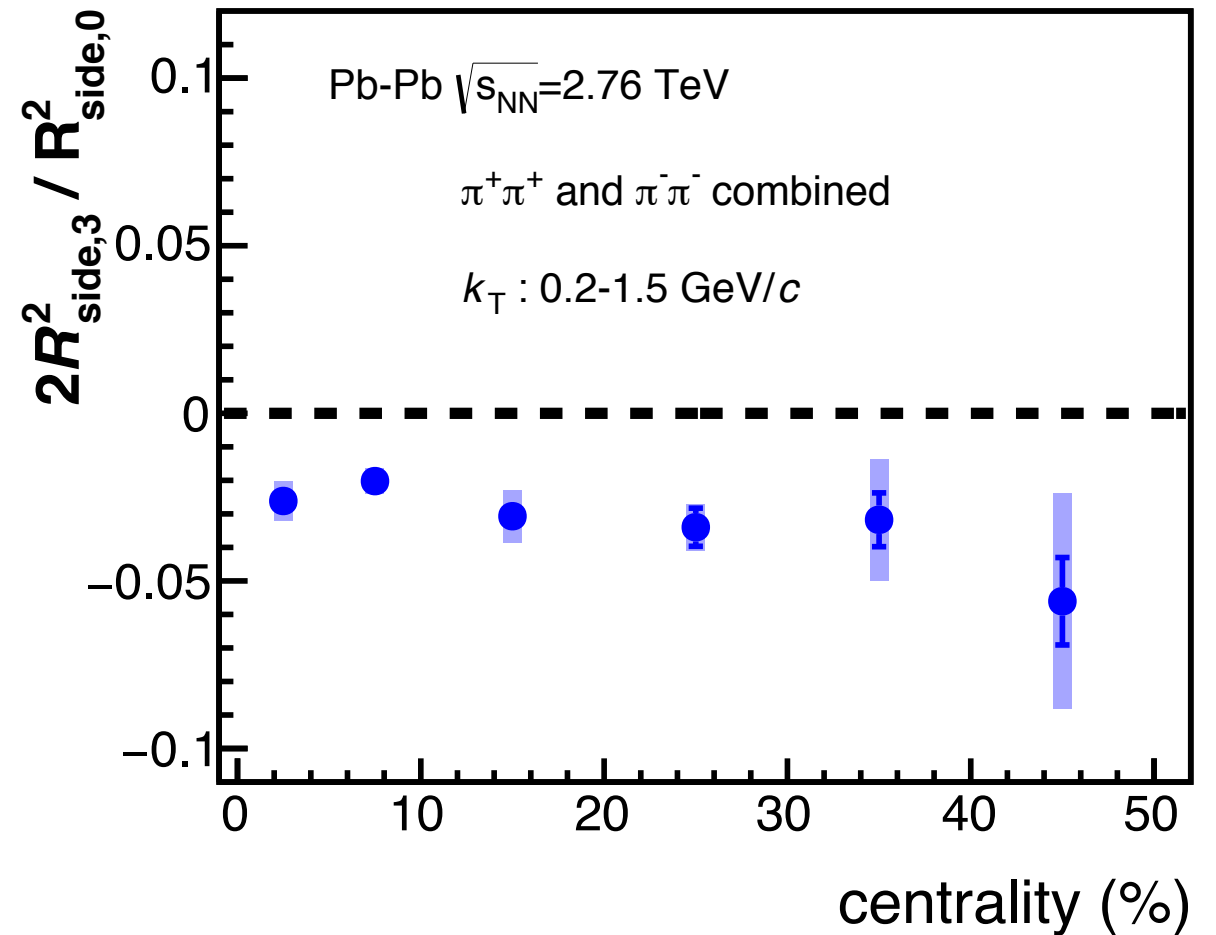
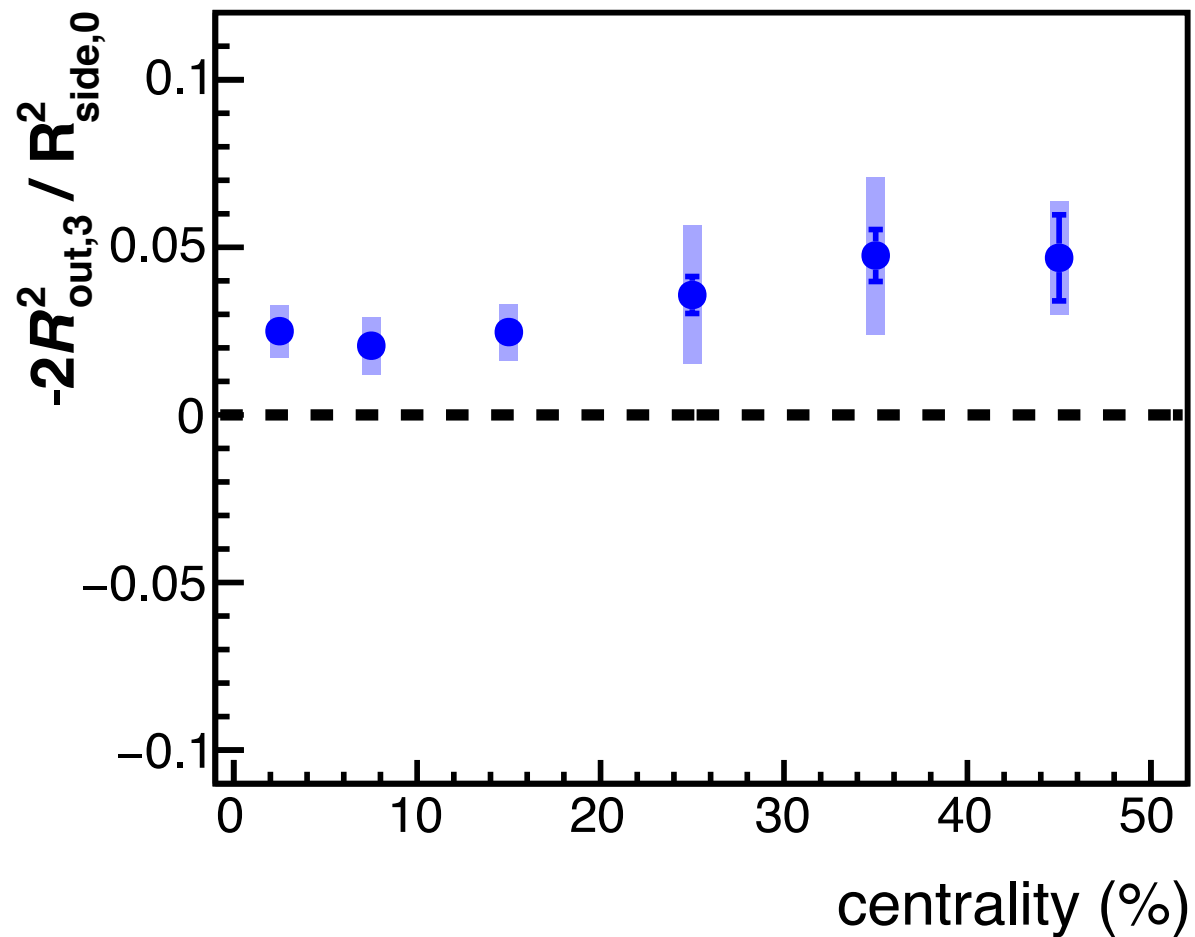


- Fit function
- $R_{\mu,0}^2 + 2 R_{\mu,3}^2 \cos(3(\phi_{\text{pair}} - \Psi_3))$
- $R_{\mu,0}^2$  : Average HBT radii,  $R_{\mu,3}^2$  : Oscillation amplitude



- Oscillations w.r.t.  $\Psi_3$  are observed in  $R_{\text{out}}$  and  $R_{\text{side}}$
- **$R_{\text{out}}$  and  $R_{\text{side}}$  oscillations have same sign**
  - Consistent to PHENIX result in Au+Au 200GeV collisions (PRL112.222301)
  - **Similar behaviour to HBT w.r.t.  $\Psi_2$  in most central smallest  $q_2$**
  - When the initial eccentricity is small, oscillation of  $R_{\text{out}}$  and  $R_{\text{side}}$  could have same sign.

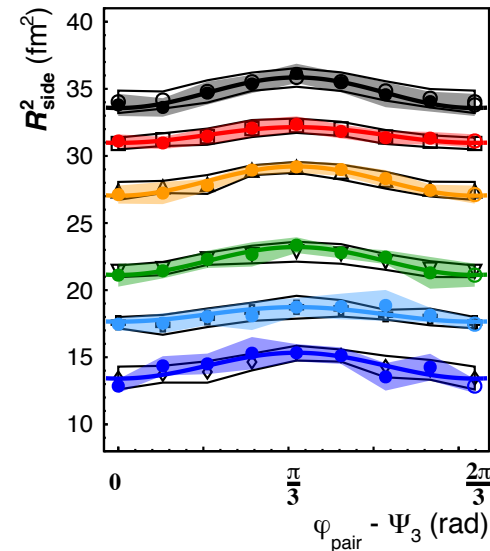
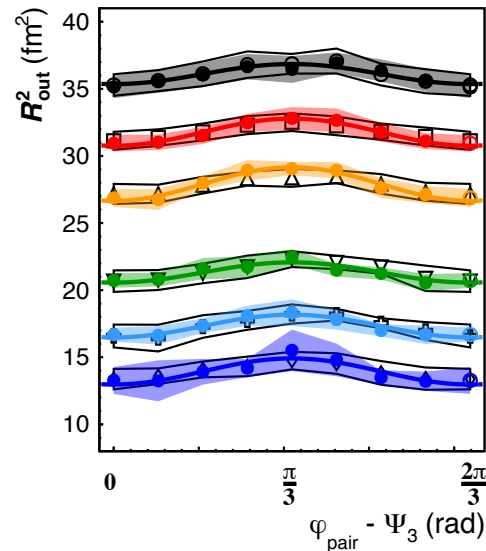
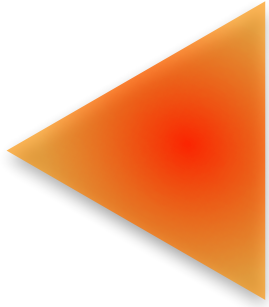
# 3<sup>rd</sup> harmonic oscillation of HBT radii



- ✓  $-2R^2_{out,3} / R^2_{side,0}$  has positive value in all centrality
- ✓  $2R^2_{side,3} / R^2_{side,0}$  has negative value in all centrality
- ✓  $R^2_{out,3} / R^2_{side,0}$  slightly increase with increasing centrality
- ✓  $R^2_{side,3} / R^2_{side,0}$  slightly becomes smaller from central to peripheral

# Azimuthal HBT w.r.t. $\Psi_3$ with ESE

Top 20%  $q_3$



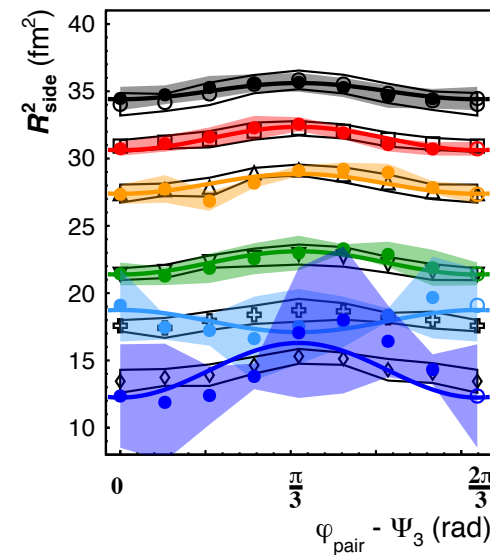
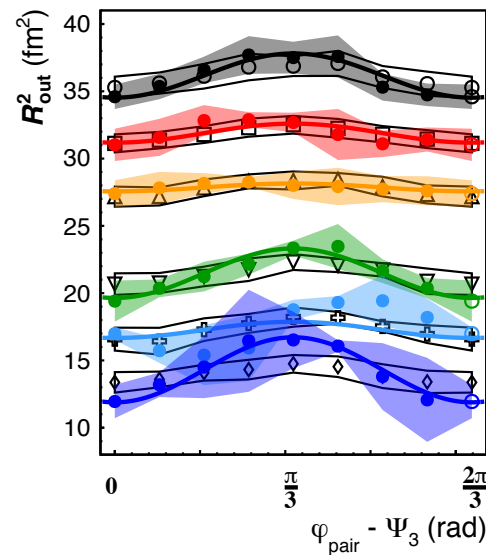
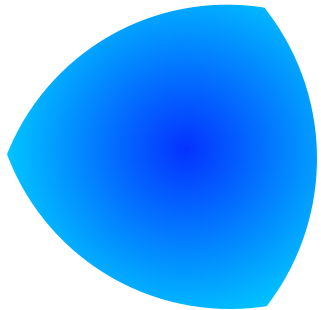
$q_3$  cut  
centrality

- 0-5%
- 5-10%
- 10-20%
- 20-30%
- 30-40%
- 40-50%

No  $q_3$  selection  
centrality

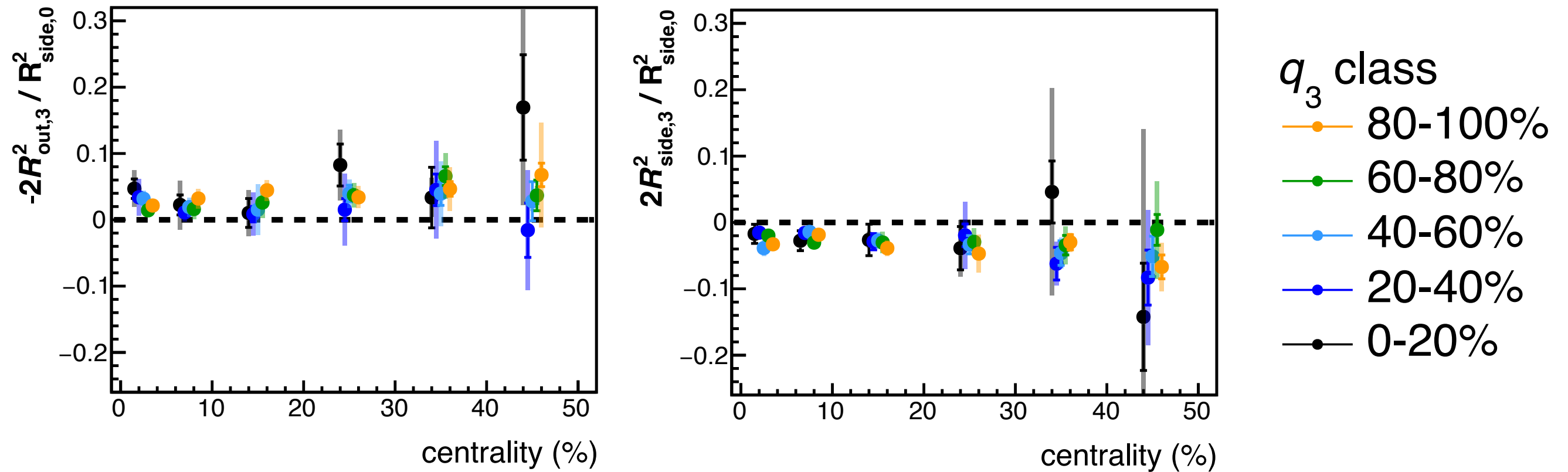
- 0-5%
- 5-10%
- △— 10-20%
- ▽— 20-30%
- ◇— 30-40%
- ◇— 40-50%

Bottom 20%  $q_3$



- Top(Bottom) 20%  $q_3$  vector selection is applied to HBT w.r.t.  $\Psi_3$
- No significant effect on the  $R_{out}$  oscillation can be observed by large  $q_3$  selection, though  $v_3$  changes with  $q_3$  selection

# Relative amplitude of HBT radii (3rd harmonics)



- ▶ **No significant change has been observed in relative amplitudes ( $R^2_{\text{out},3} / R^2_{\text{side},0}$  and  $R^2_{\text{side},3} / R^2_{\text{side},0}$ ), though  $v_3$  is enhanced  $\sim 15\%$** 
  - ➔ **Different behaviour to HBT w.r.t.  $\Psi_2 + q_2$  selection**
    - ▶ **Triangular shape at freeze-out seems to be saturated by radial flow and triangular flow**

# Summary-3

- ✦ **Azimuthal angle dependence of HBT relative to 3<sup>rd</sup> order event plane**
  - Small but finite oscillation can be found in  $R_{\text{out}}$ ,  $R_{\text{side}}$
  - Relative amplitude of  $R_{\text{out}}$  has positive and that of  $R_{\text{side}}$  has negative value
  - Both  $R_{\text{out},3}^2 / R_{\text{side},0}^2$   $R_{\text{side},3}^2 / R_{\text{side},0}^2$  has small centrality dependence
- ✦ **ESE applies to HBT measurements w.r.t. 3<sup>rd</sup> order event plane**
  - First measurement of  $q_3$  selection + HBT
  - No significant change can be found in relative amplitudes of  $R_{\text{out}}$  and  $R_{\text{side}}$  with  $q_3$  selection



# Conclusion

- ✦ **Azimuthal angle dependence of HBT relative to 2<sup>nd</sup>-order event plane**
  - ✦ Initial elliptic shape strongly diluted, but out-plane elongated elliptic shape still remains at freeze-out
  - ✦ Final eccentricity enhanced(suppressed) with  $q_2$  ( $\epsilon_2^{\text{initial}}$ ) selection
  - ✦  $q_2$  dependence could be different in centrality 20-40%
- ✦ **Azimuthal angle dependence of HBT relative to 3<sup>rd</sup> order event plane**
  - ✦  $-2R_{\text{out},3}^2 / R_{\text{side},0}^2 > 0$  and  $2R_{\text{side},3}^2 / R_{\text{side},0}^2 < 0$  in all centrality. This will constrain the freeze-out parameters
  - ✦ Relative amplitudes of HBT radii w.r.t.  $\Psi_3$  did not change with  $q_3$  selection. it might indicate freeze-out triangular shape saturates

# Back up

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# Event plane resolution

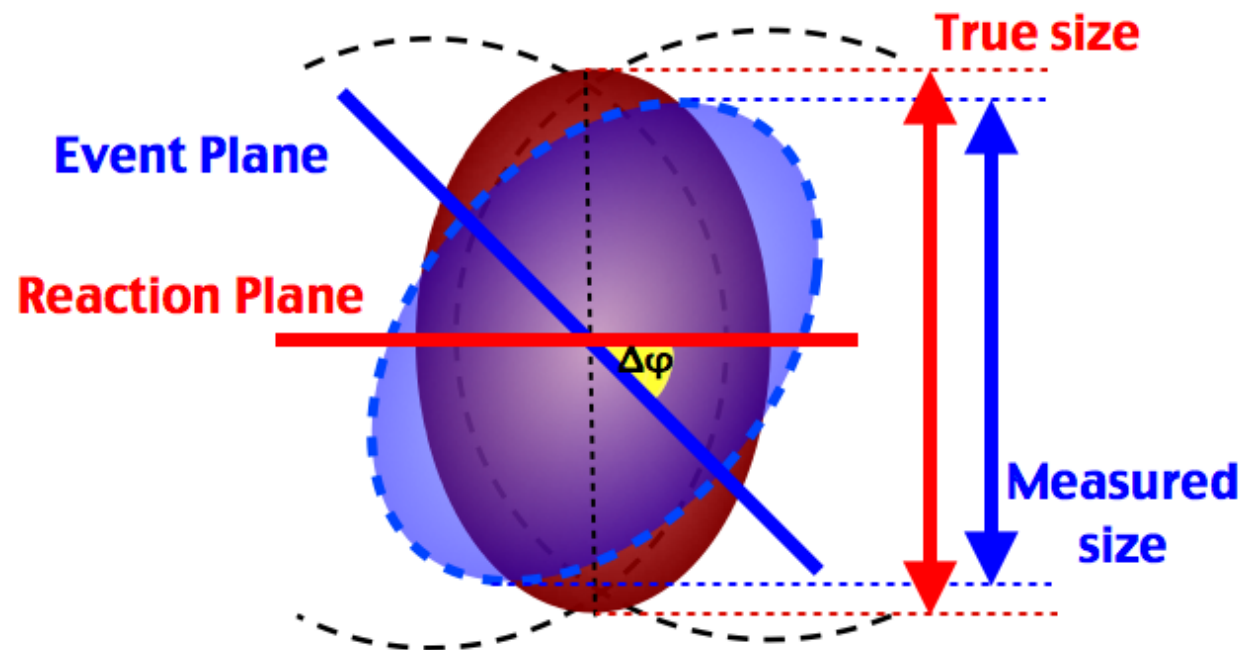
## ■ Event Plane Resolution Correction (Phys. Rev. C66, 044903 (2002) )

$$N(q, \phi_j) = N_{exp}(q, \phi_j) + 2 \sum_{n=1}^{n_{bins}} \xi_{n,m}(\Delta) [N_{c,n}^{exp}(q) \cos(n\phi_j) + N_{s,n}^{exp}(q) \sin(n\phi_j)]$$

$$N_{c,n}^{exp}(q) \cos(n\phi_j) = \langle N_{exp}(q, \phi_j) \cos(n\phi) \rangle = \frac{1}{n_{bins}} \sum_{n=1}^{n_{bins}} N_{exp}(q, \phi_j) \cos(n\phi_j)$$

$$N_{s,n}^{exp}(q) \sin(n\phi_j) = \langle N_{exp}(q, \phi_j) \sin(n\phi) \rangle = \frac{1}{n_{bins}} \sum_{n=1}^{n_{bins}} N_{exp}(q, \phi_j) \sin(n\phi_j)$$

$$\xi_{n,m}(\Delta) = \frac{n\Delta/2}{\sin(n\Delta/2) \langle \cos(n(\Psi_n^m - \Psi_n^{true})) \rangle} \rightarrow \text{event plane resolution}$$



- correction for q-distribution with EP resolution

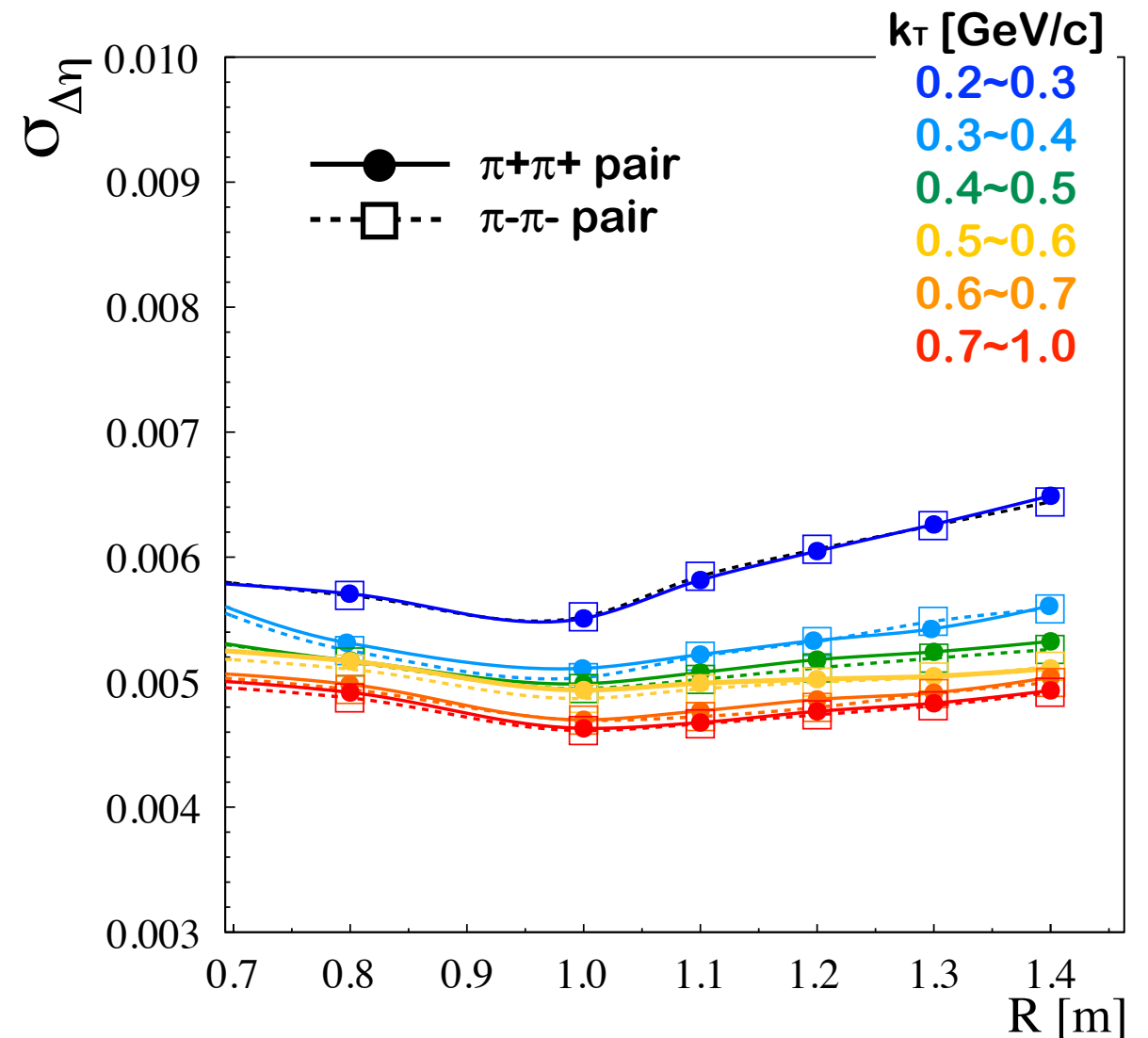
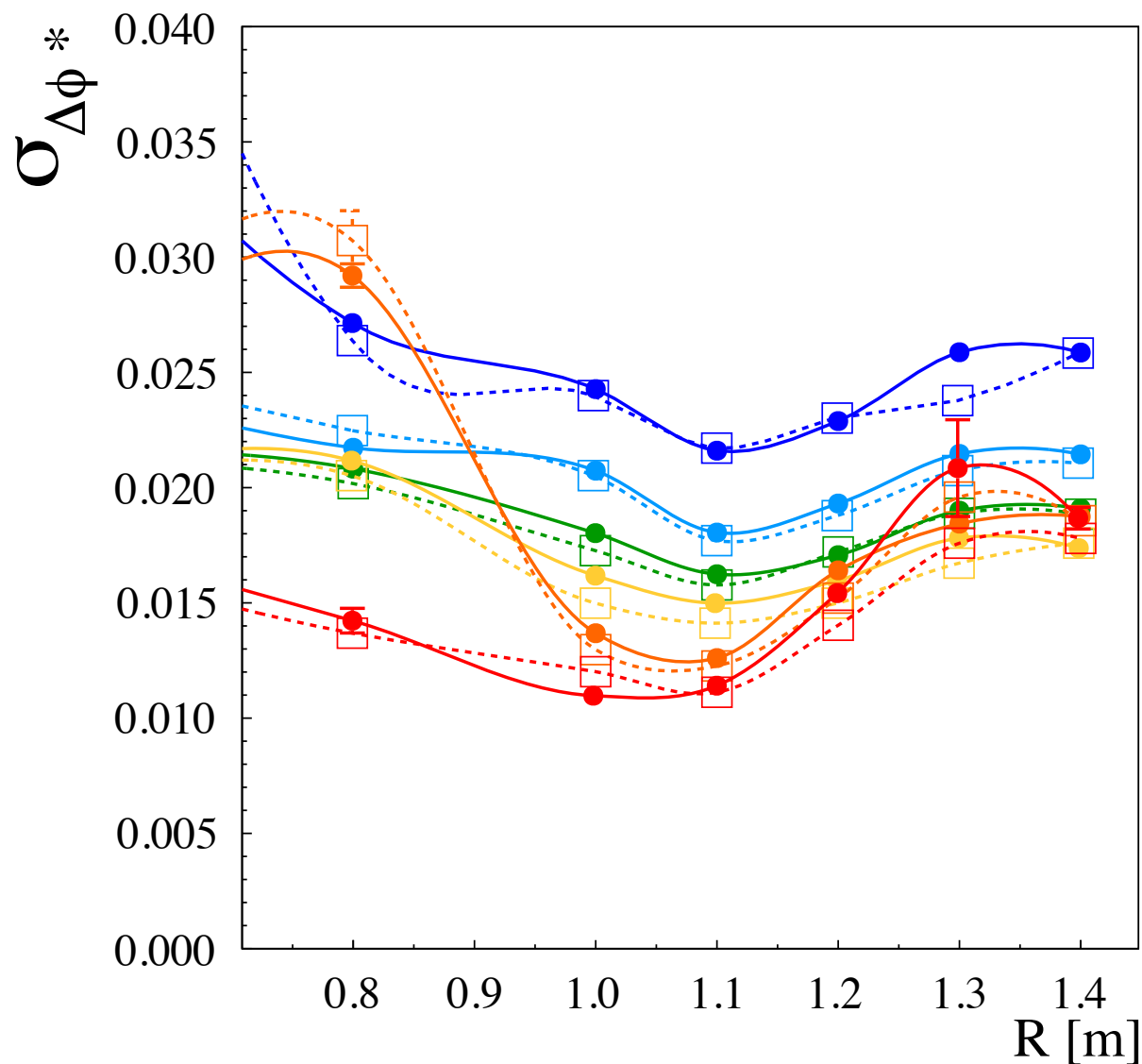
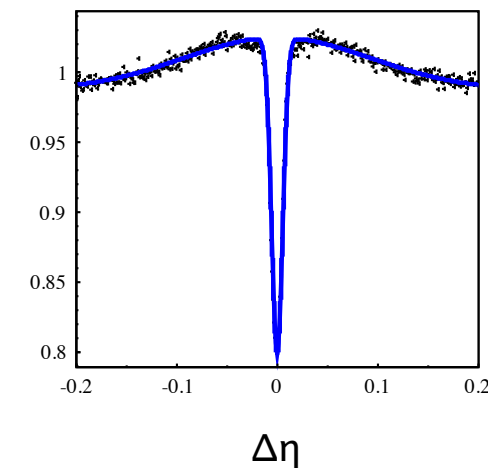
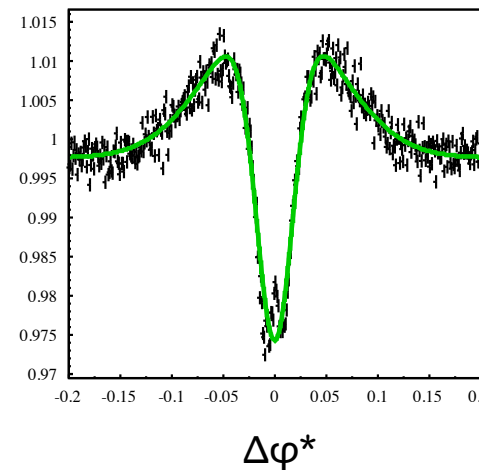
# Angular distance in $\Delta\varphi^* \Delta\eta$

## • Optimized Pair cut

■  $\Delta\varphi^*, \Delta\eta$  cut @  $R = 1.1$  [m]

-  $3\sigma$  of gaussian cut

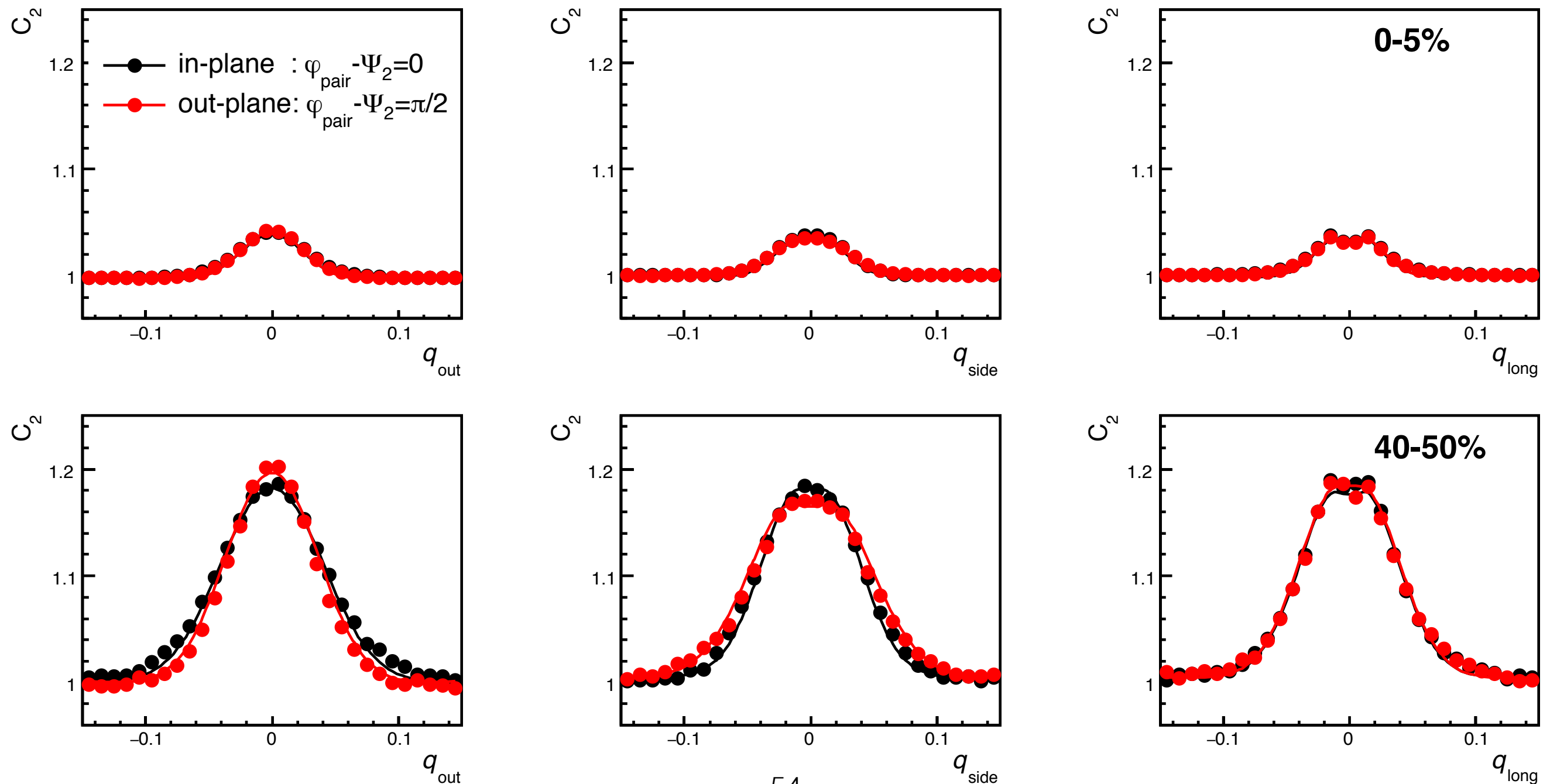
-  $|\Delta\varphi^*| < 0.066$  &&  $|\Delta\eta| < 0.018$



# Correlation function (HBT w.r.t. $\Psi_2$ )

## ◆ 1D projection of 3D correlation functions

- ▶ Projections of the other component within 50 MeV/c
- ▶ Different HBT radii can be found in peripheral collisions (oscillation of radii)

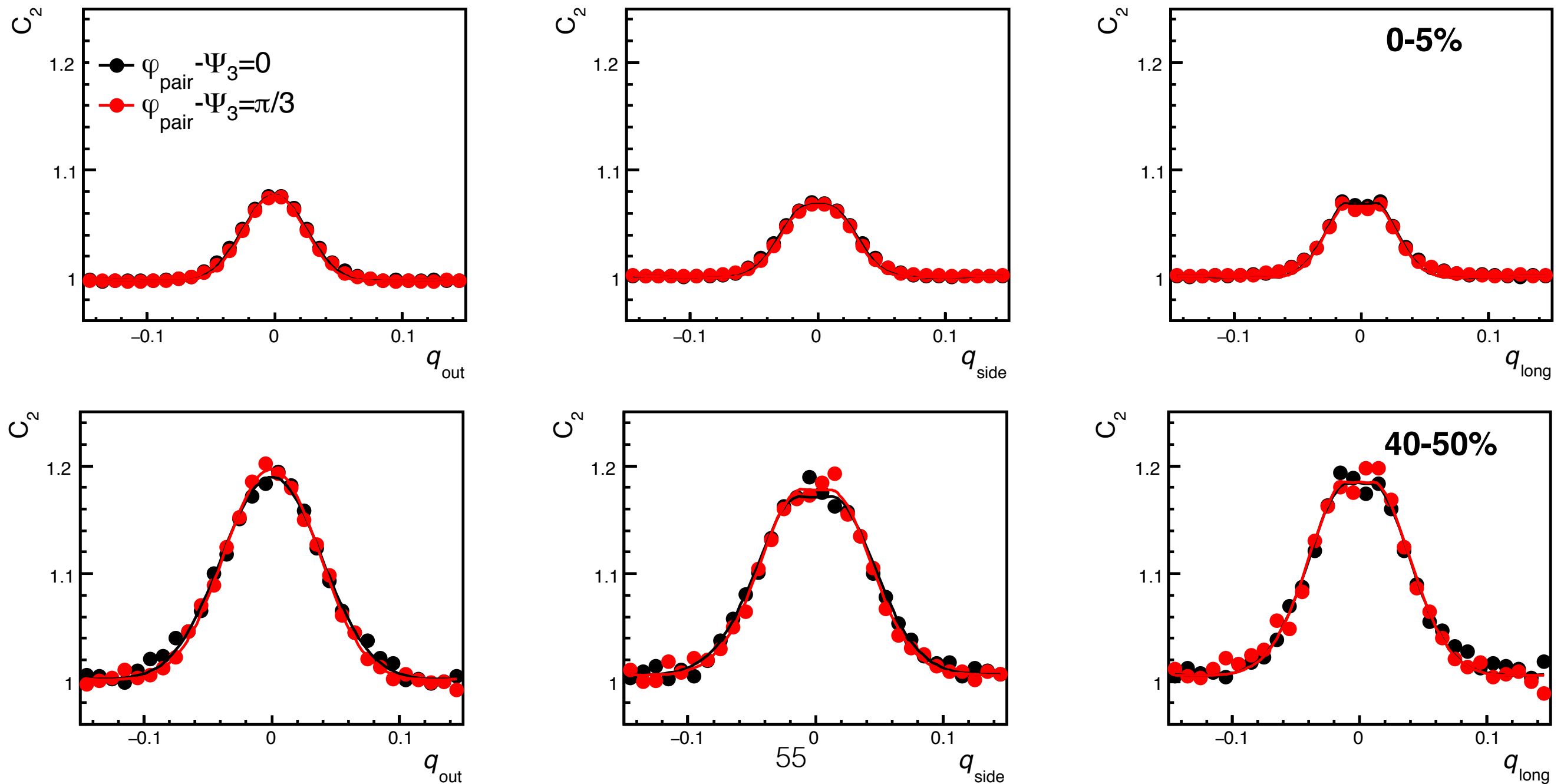




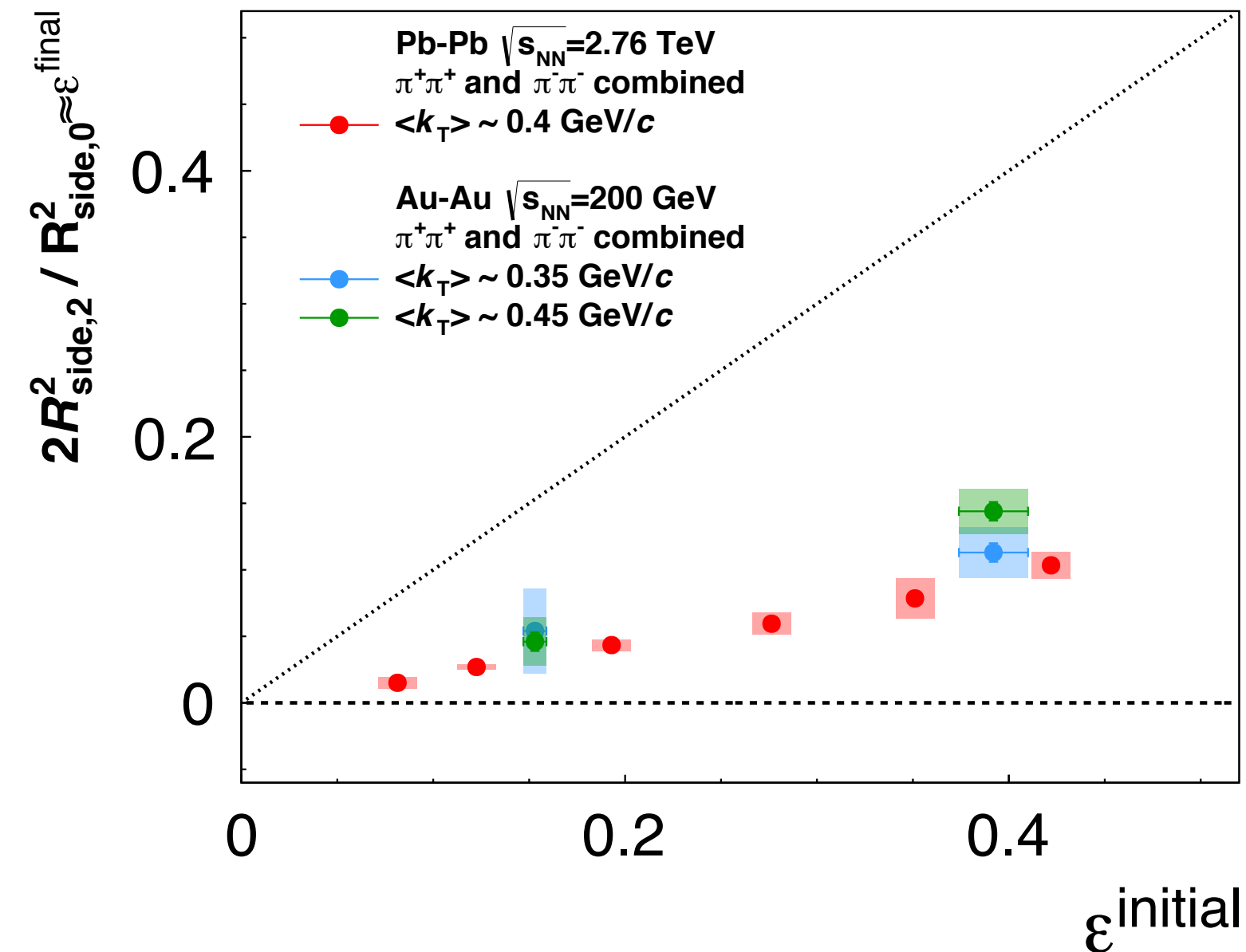
# Correlation function (HBT w.r.t. $\Psi_3$ )

## ◆ 1D projection of 3D correlation functions

- ▶ Projections of the other component within 50 MeV/c
- ▶ Different HBT radii can be found in peripheral collisions (oscillation of radii)

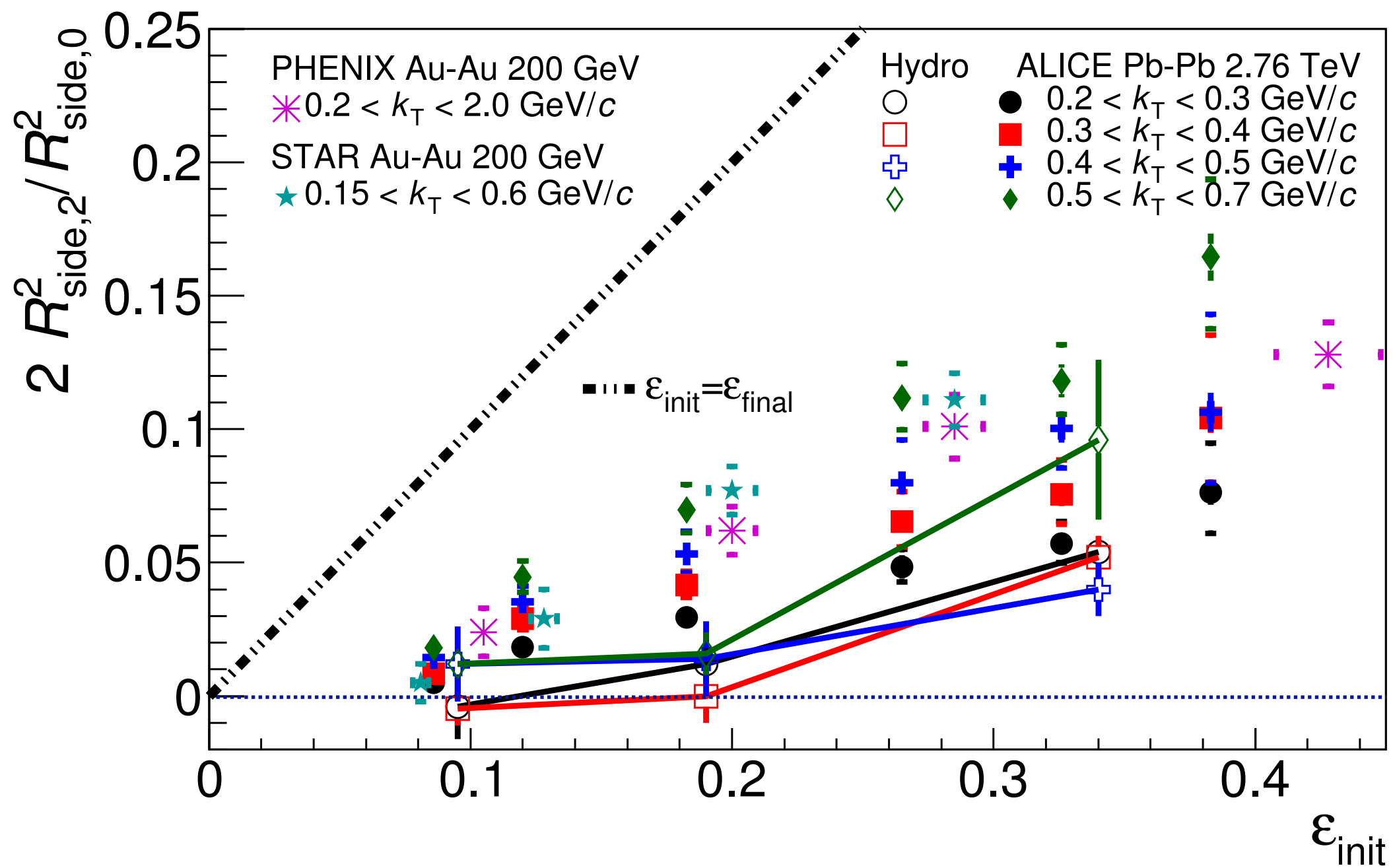


# Comparison with result in Au-Au 200GeV

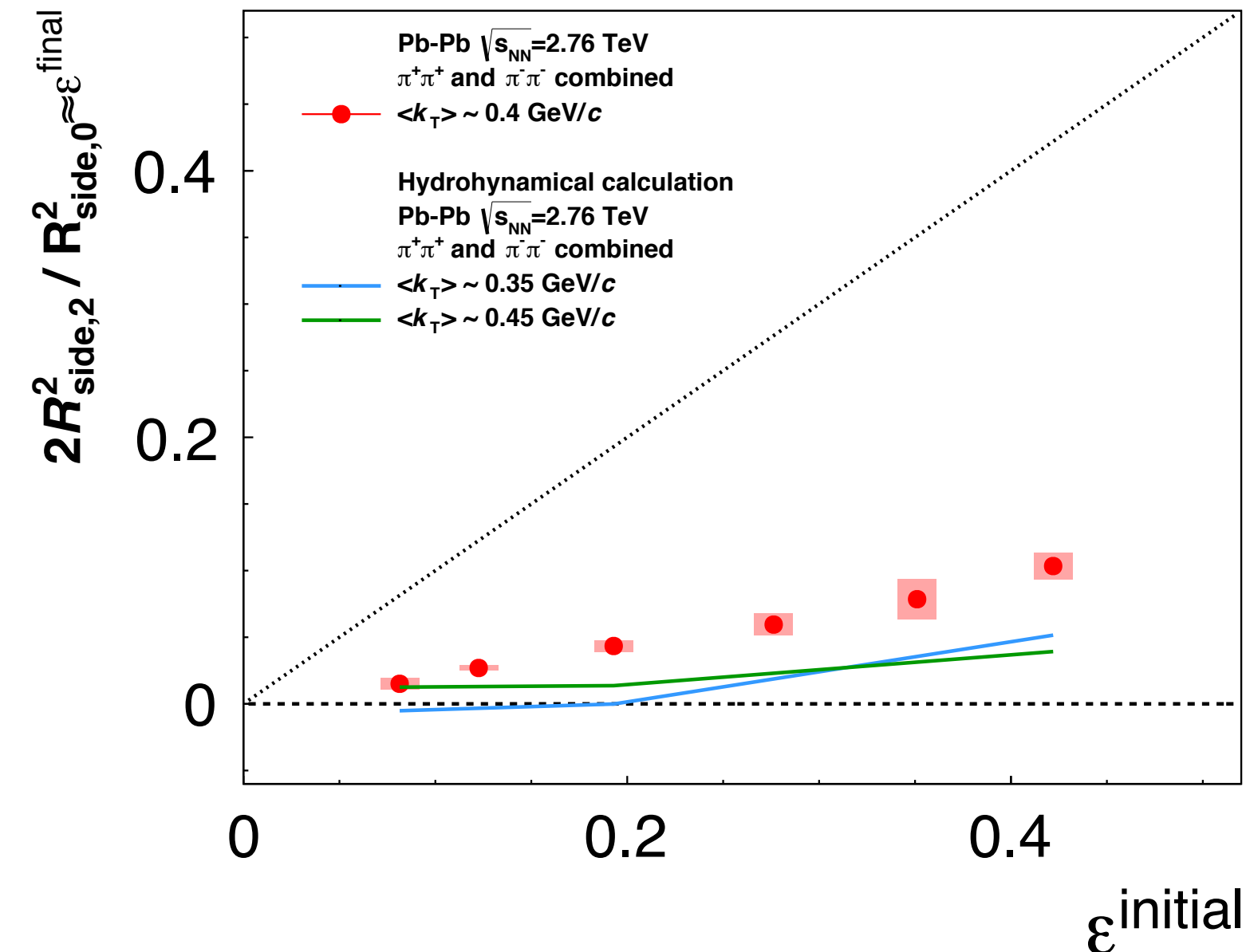


- Dilution effect at LHC is stronger than that at RHIC
  - Due to larger collective flow in LHC energy
- Difference between RHIC and LHC is remarkable at peripheral collisions

# $k_T$ dependence of $\varepsilon_2^{\text{final}}$ in Pb-Pb 2.76 TeV



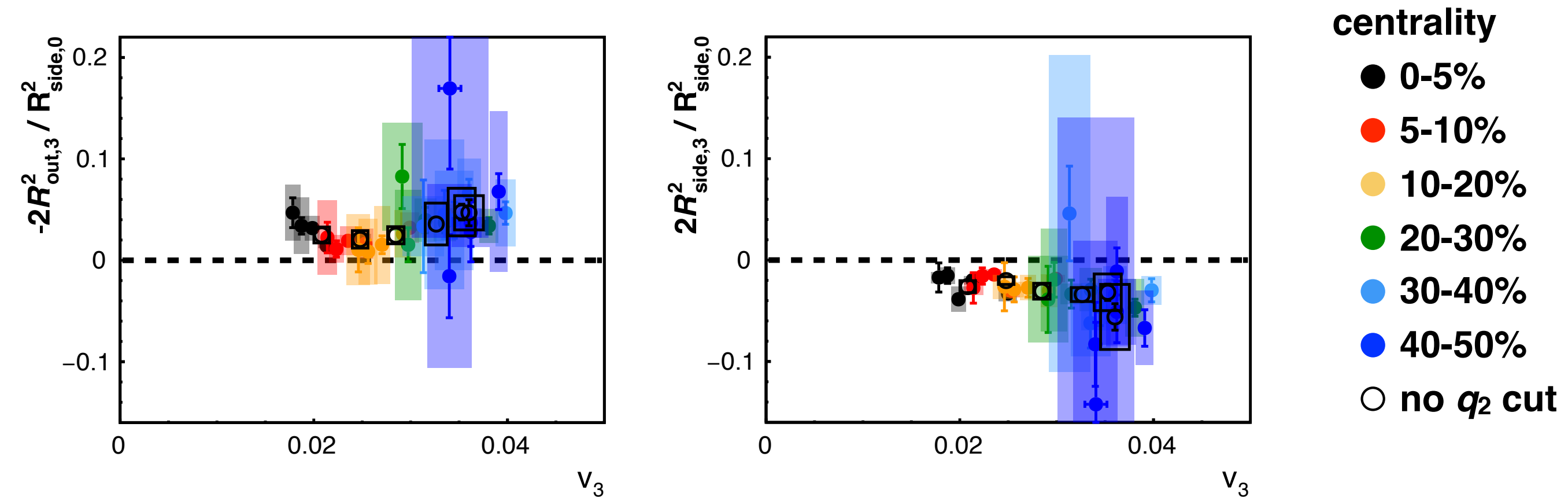
# Comparison with hydrodynamical calculation



- Hydrodynamical calculation is qualitatively consistent to data
- Final eccentricity at freeze-out of hydrodynamical prediction is slightly smaller than experimental result
- Difference between model and data is larger in peripheral than central collisions

# $v_3$ scaling to Relative amplitude of HBT radii

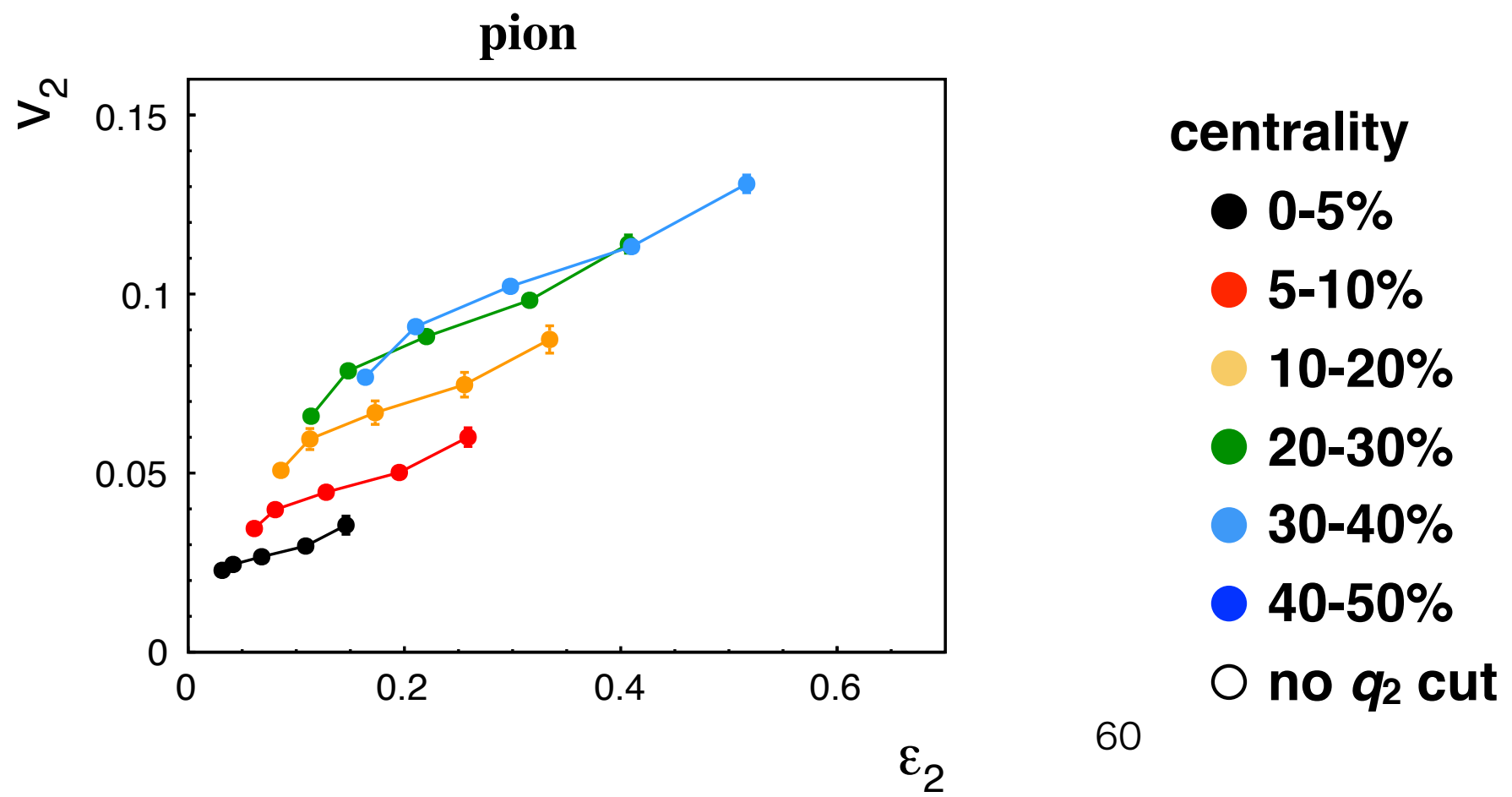
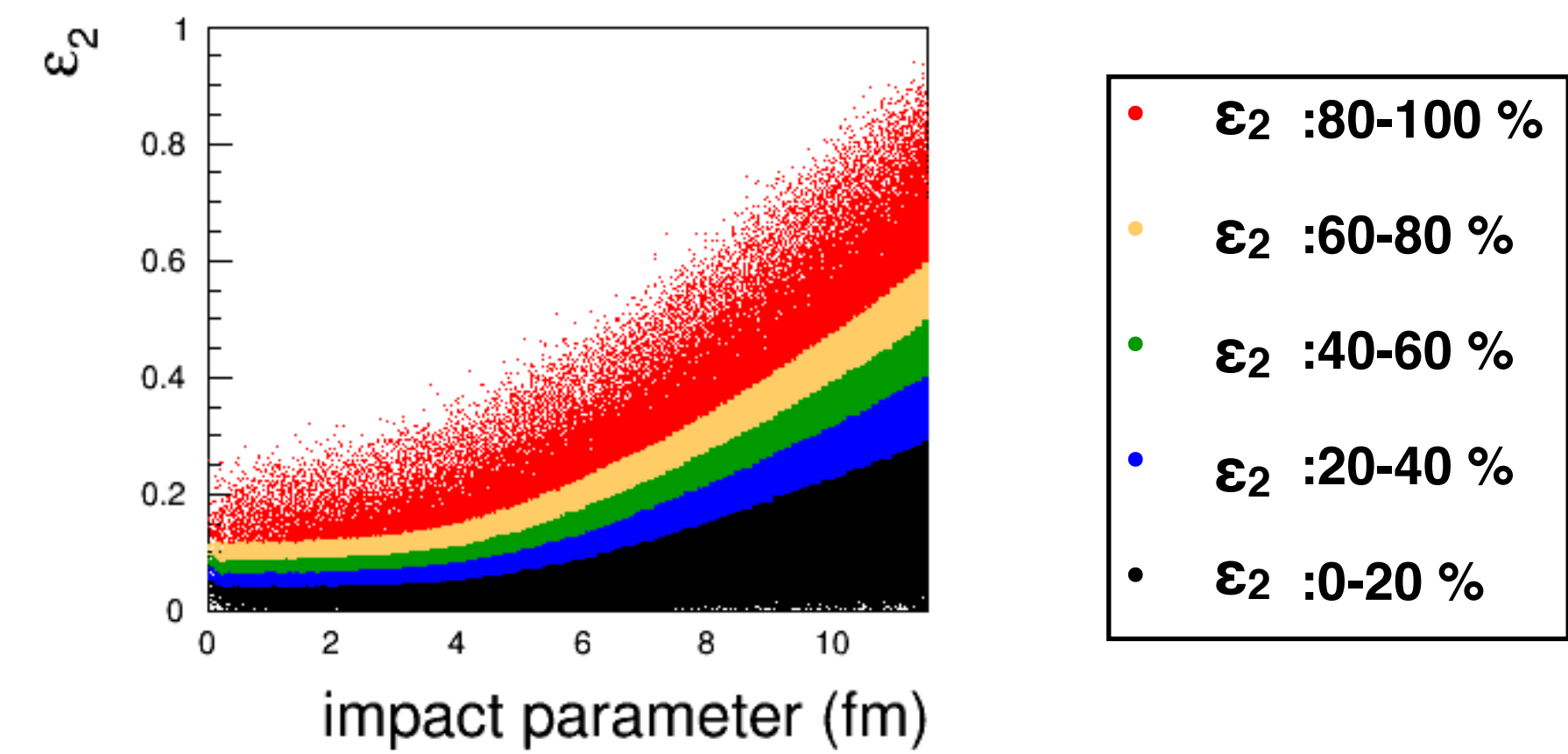
- ✓ Difference of event by event initial geometry fluctuation can not be reflected to “centrality”
- ✓ More sensitive probe is necessary !



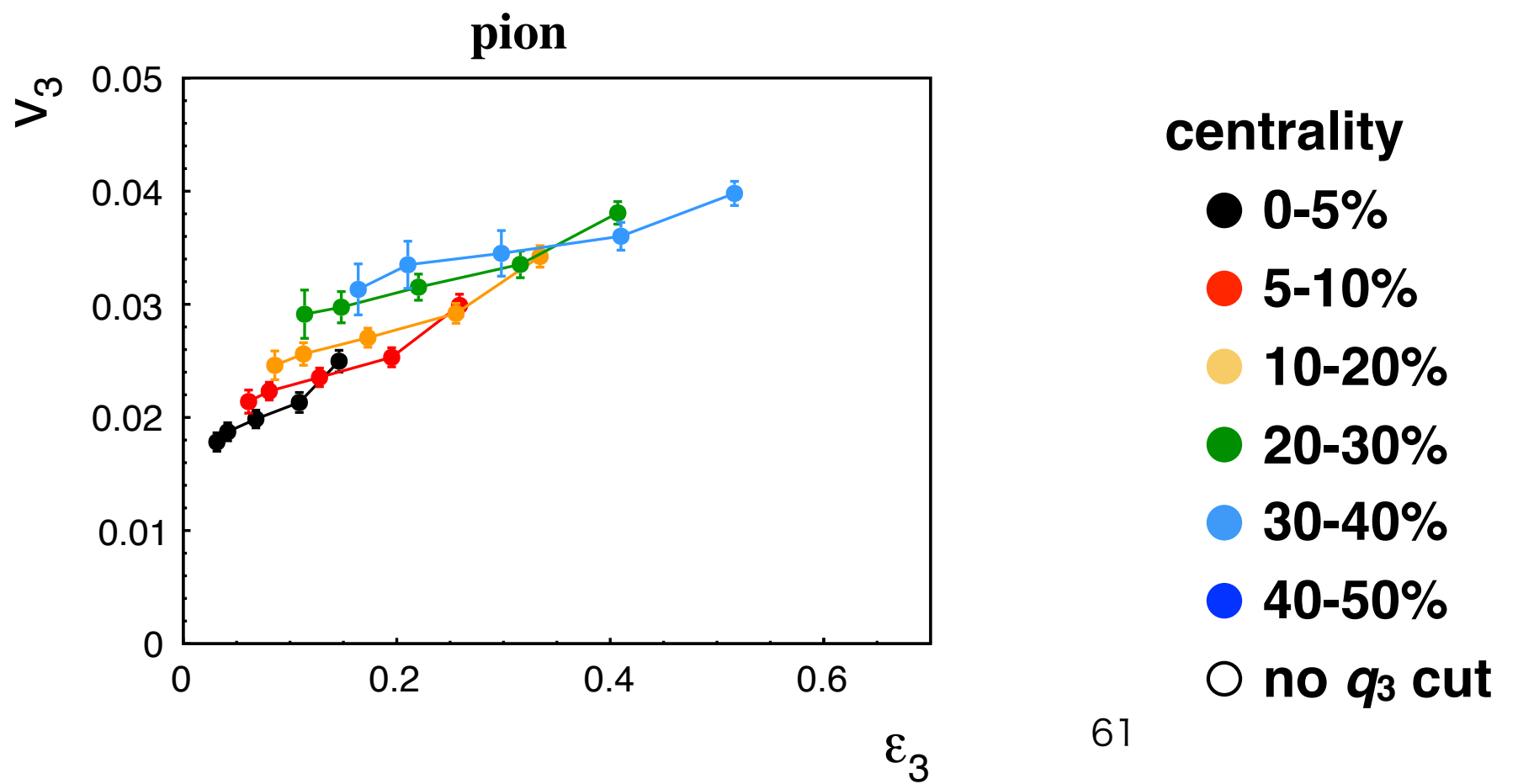
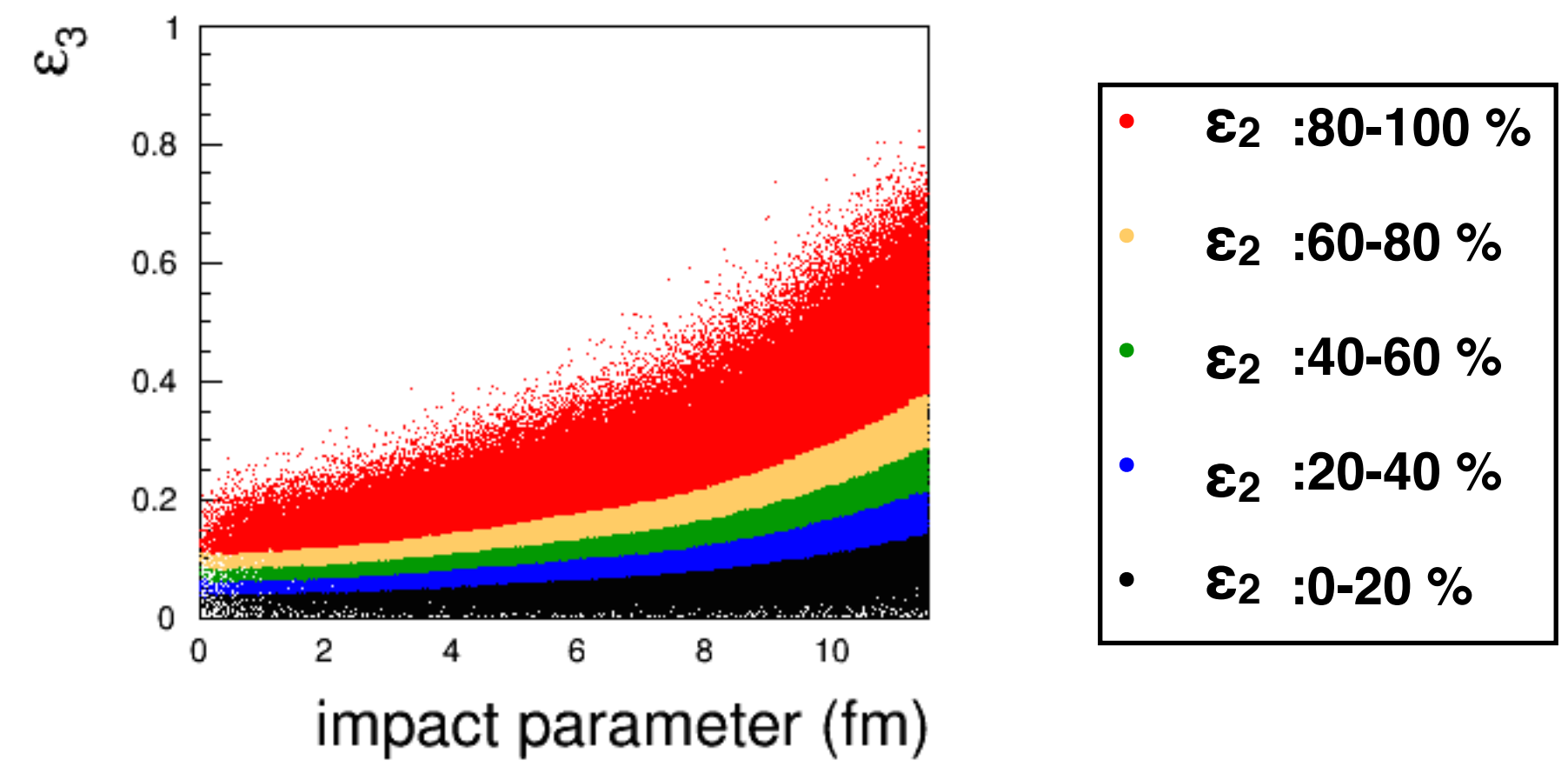
- ✓ Both relative amplitudes of  $R_{out}$  and  $R_{side}$  are scaled with  $v_3$
- ✓ Non linear correlation between  $-2R^2_{out,3} / R^2_{side,0}$  and  $v_3$
- ✓ No significant correlation can be found between  $-2R^2_{side,2} / R^2_{side,0}$  and  $v_3$



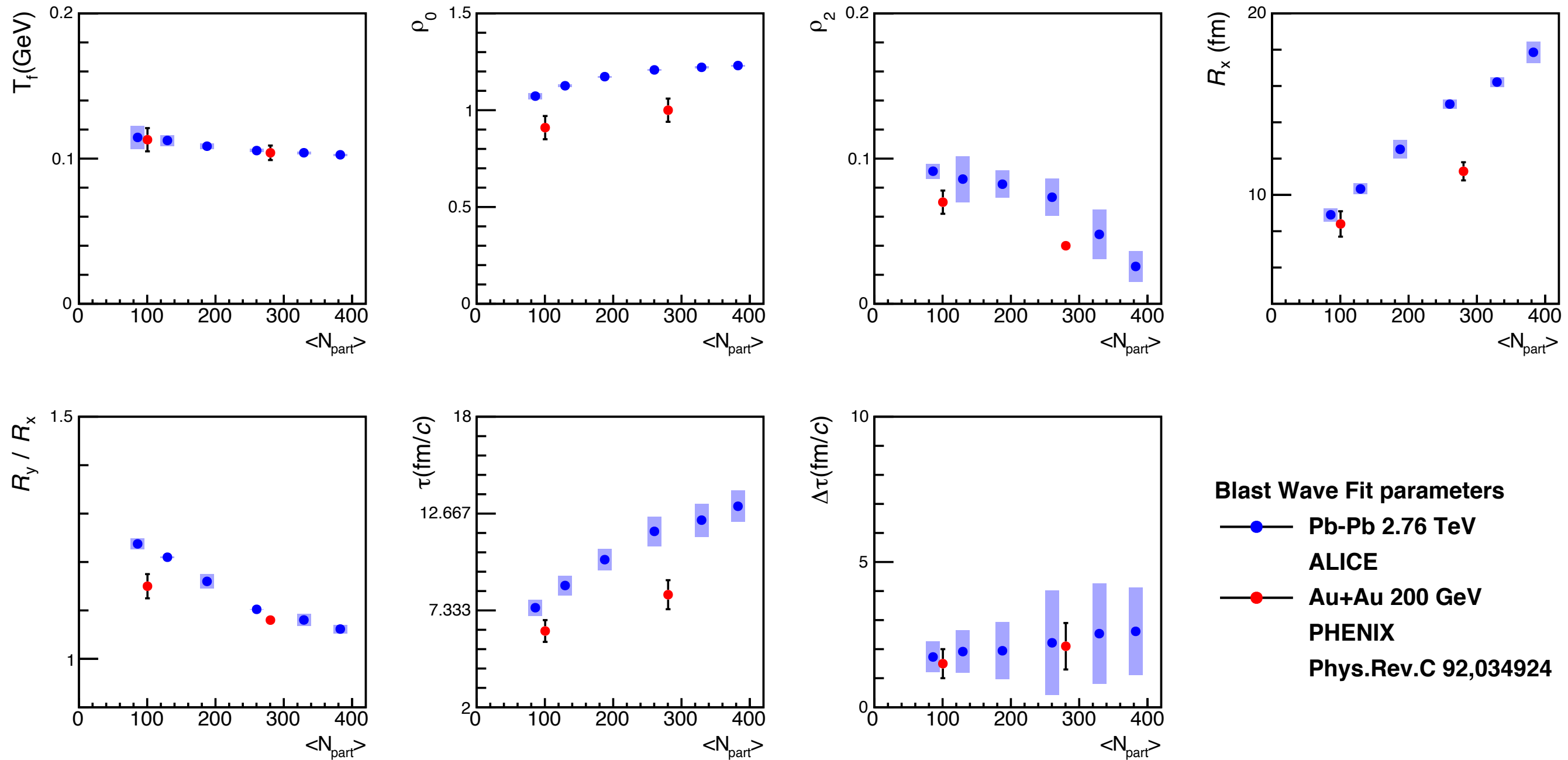
# Correlation between $v_2$ and $\epsilon_2^{\text{initial}}$ (Glauber)



# Correlation between $v_3$ and $\epsilon_3^{\text{initial}}$ (Glauber)

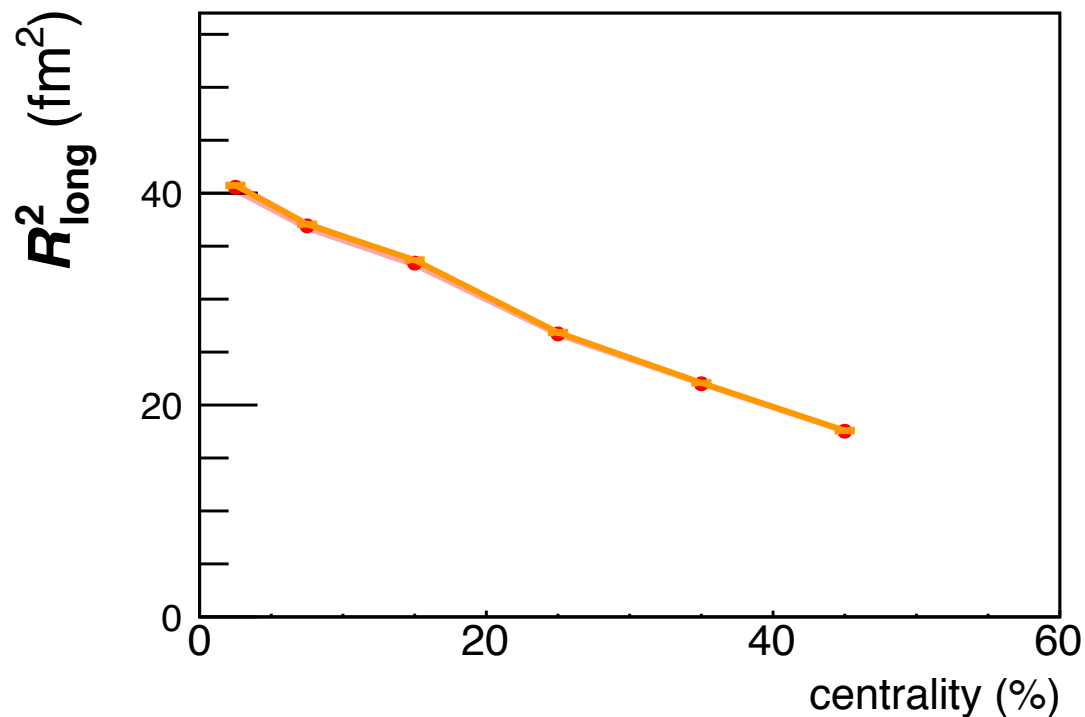
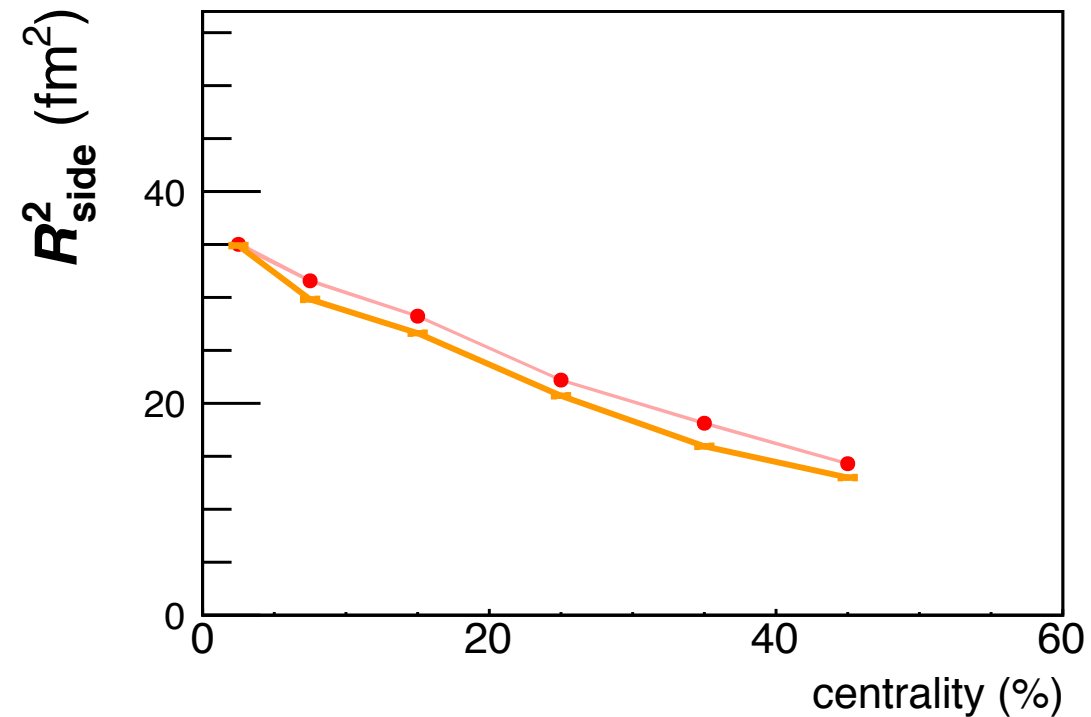
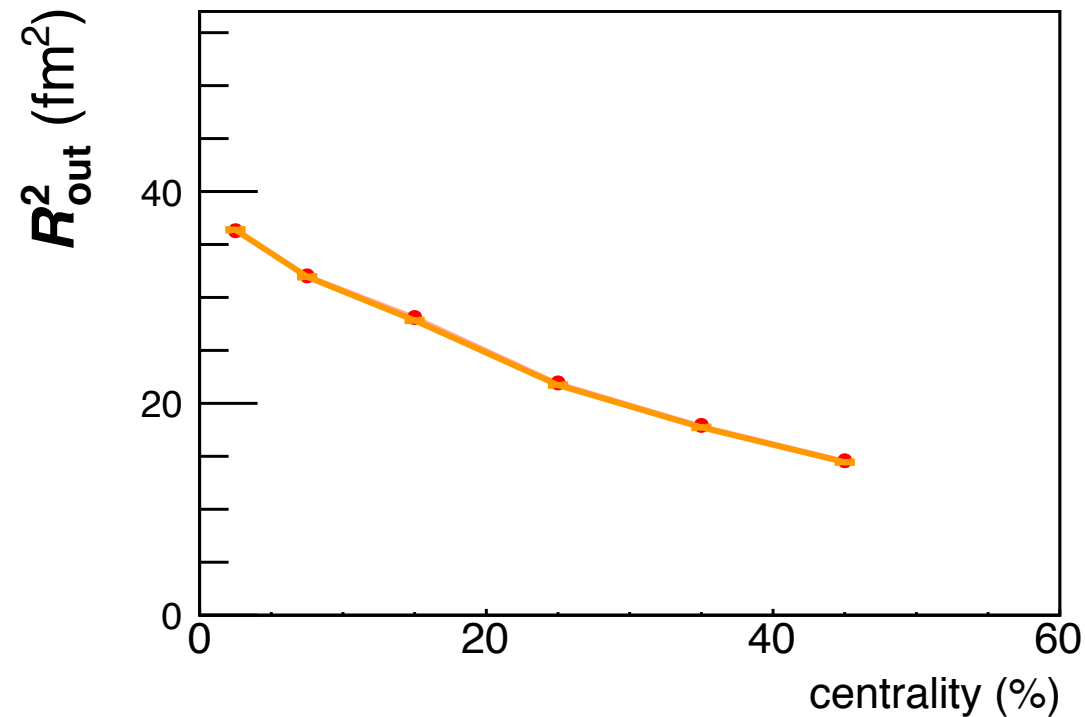


# Blast-wave parameters (comparison with PHENIX)



- ◆ Freeze out temperature( $T_f$ ), eccentricity( $R_y/R_x$ ), duration( $\Delta\tau$ ) : ALICE ~ PHENIX
- ◆ Flow velocity ( $\rho_0$  and  $\rho_2$ ) and system life time : ALICE > PHENIX

# Comparison with Blast-wave model (average HBT radii)



**Pb-Pb  $\sqrt{s_{\text{NN}}}=2.76$  TeV**

**$\pi^+\pi^+$  and  $\pi^-\pi^-$  combined**

**$k_{\text{T}} : 0.2-1.5$  GeV/ $c$**

**• Data**

**— Blast-wave fit**

◆  $R_{\text{out}}$  and  $R_{\text{long}}$  of Blast-wave fit is consistent to that of Data

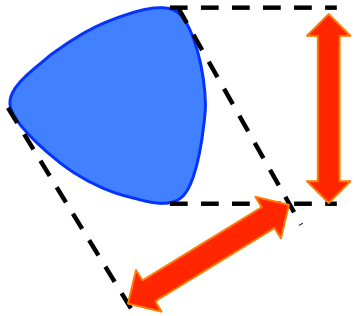
◆  $R_{\text{side}}$  of Blast-wave fit is slightly smaller than that of Data

# Final source **triangular shape** and HBT w.r.t. $\Psi_3$

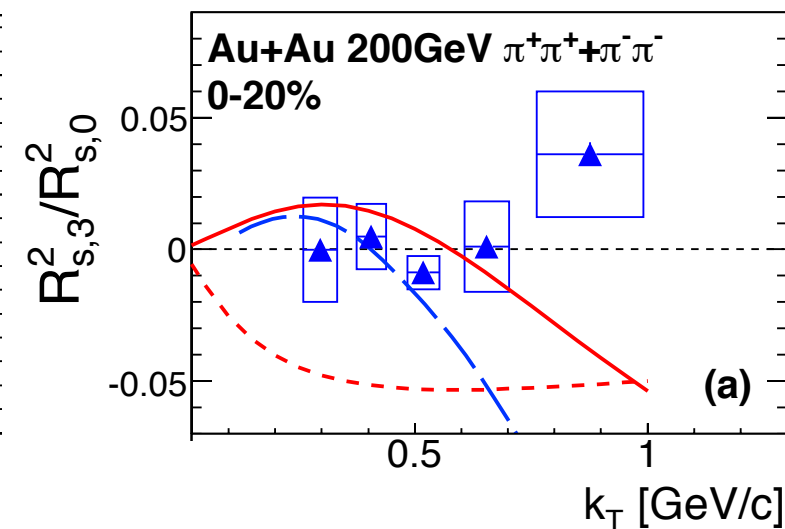
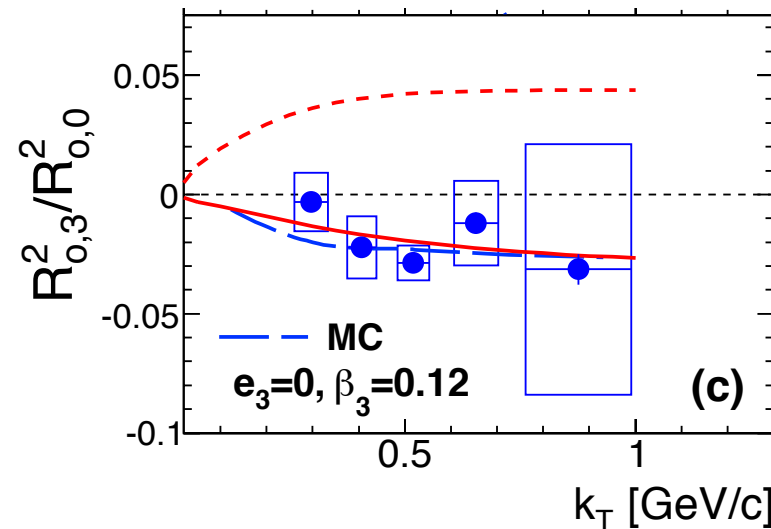
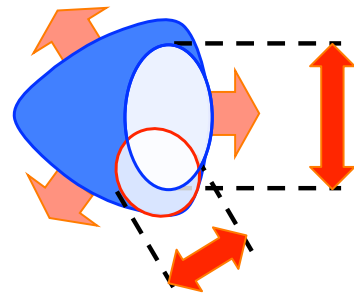
## ► **Triangularity cannot be directly obtained from HBT w.r.t. $\Psi_3$**

→ Both triangular flow and geometrical triangularity make 3rd order oscillation of HBT radii

### • Static source



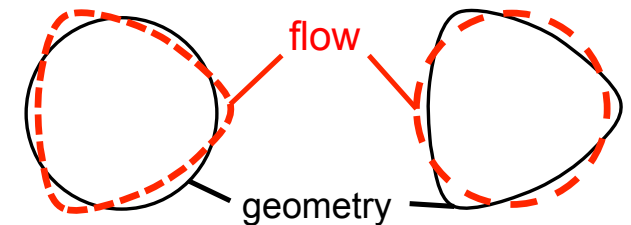
### • Dynamic source



## ► **HBT w.r.t. $\Psi_3$ in Au+Au 200GeV collisions**

- A. Adare et al., PRL112.222301
- MC simulation of two extreme case
- HBT oscillation could be explained by “deformed flow” at RHIC

—  $\bar{\epsilon}_3=0, \bar{v}_3=0.25$  deformed flow  
 - - -  $\bar{\epsilon}_3=0.25, \bar{v}_3=0$  deformed geometry



PRC88,044914

→ Any hint of sign change of  $\epsilon_3$  under larger collective flow at LHC ??

## ☑ Detailed analysis is necessary for understanding final source triangularity

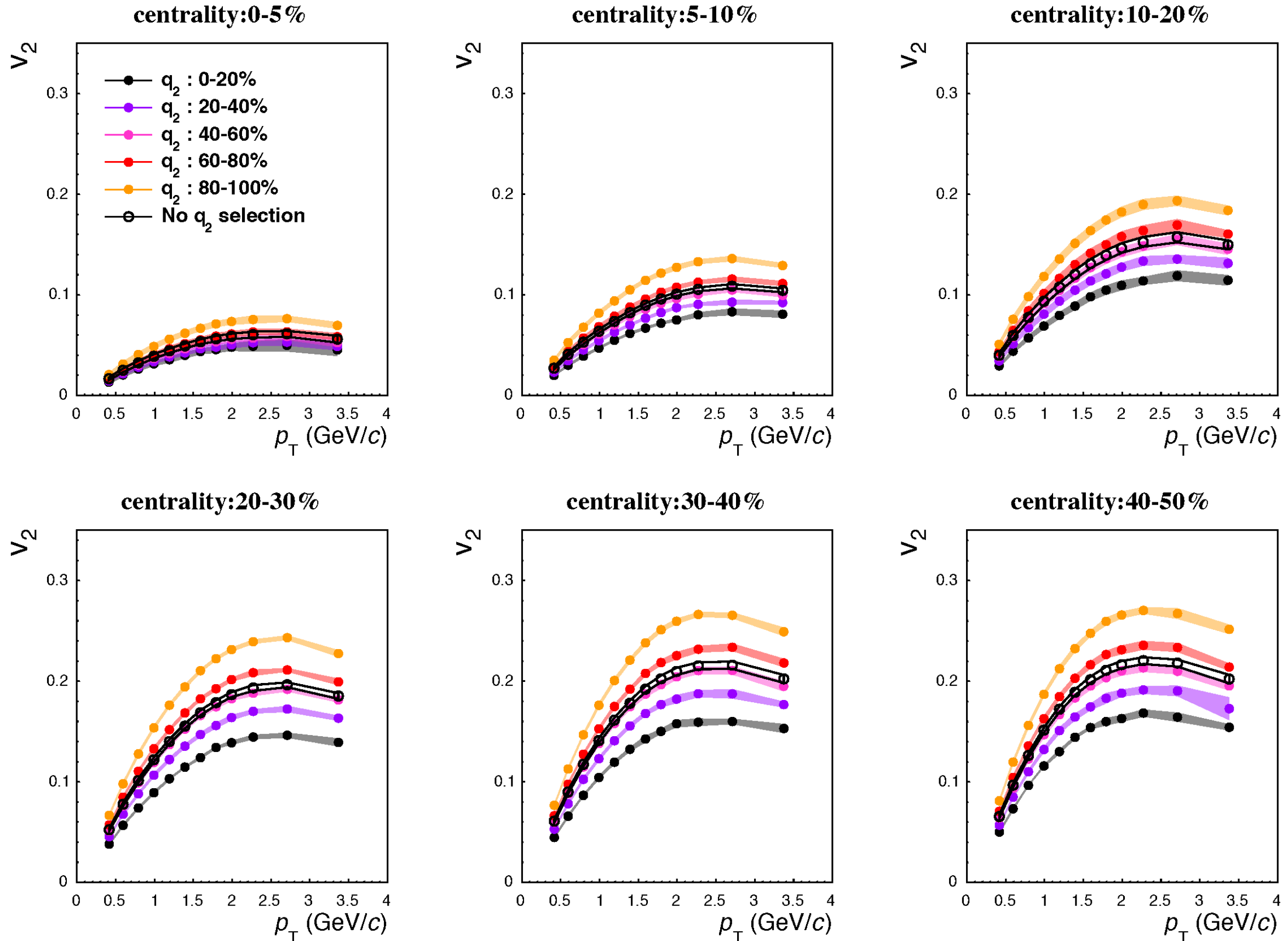
◆  $k_T$  dependence of Azimuthally differential femtoscopy w.r.t.  $\Psi_3$

→ **High multiplicity and good E.P. resolution in ALICE Pb-Pb collisions !**

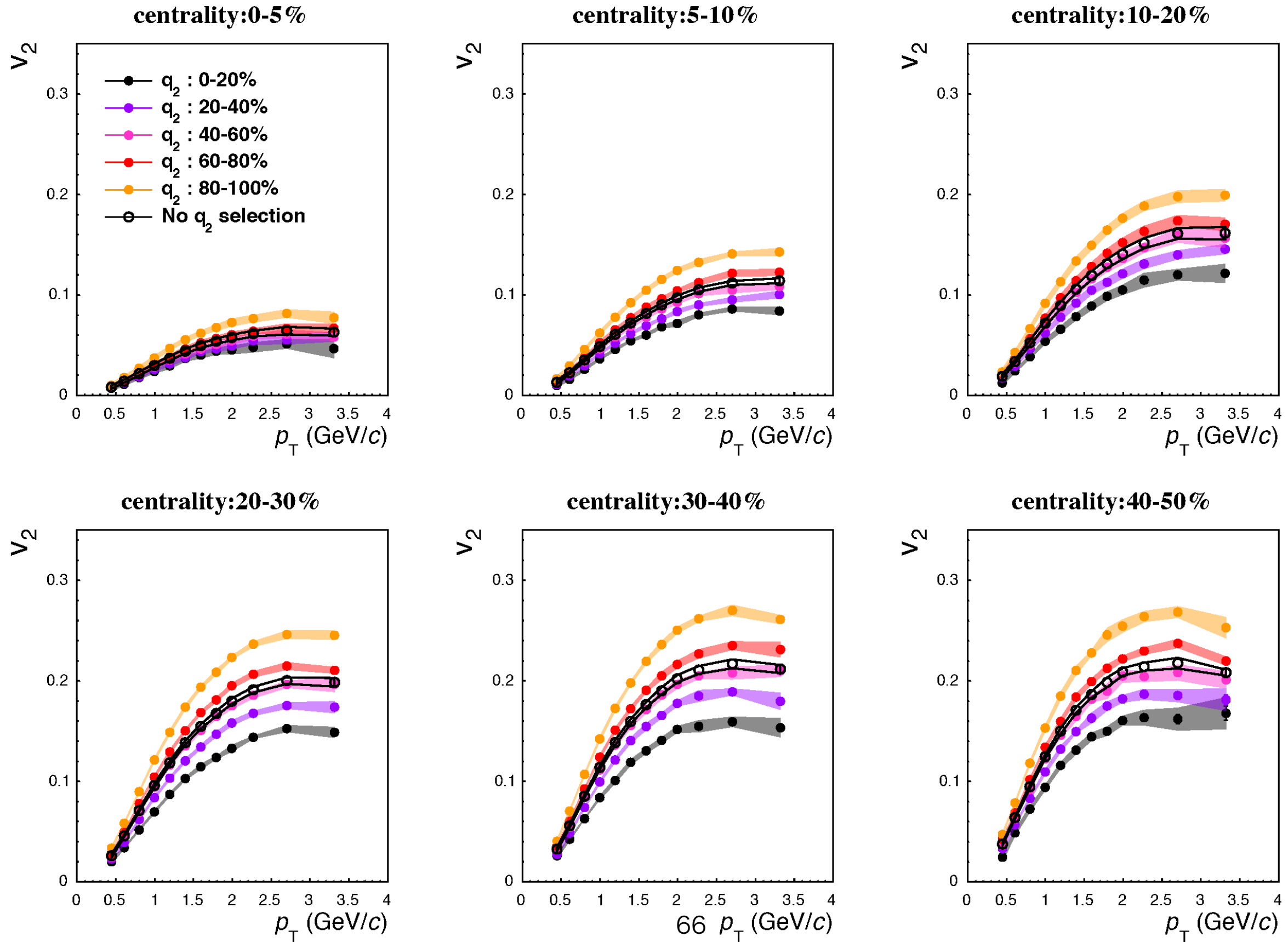
◆ **Direct measurement of correlation between geometrical and flow information**



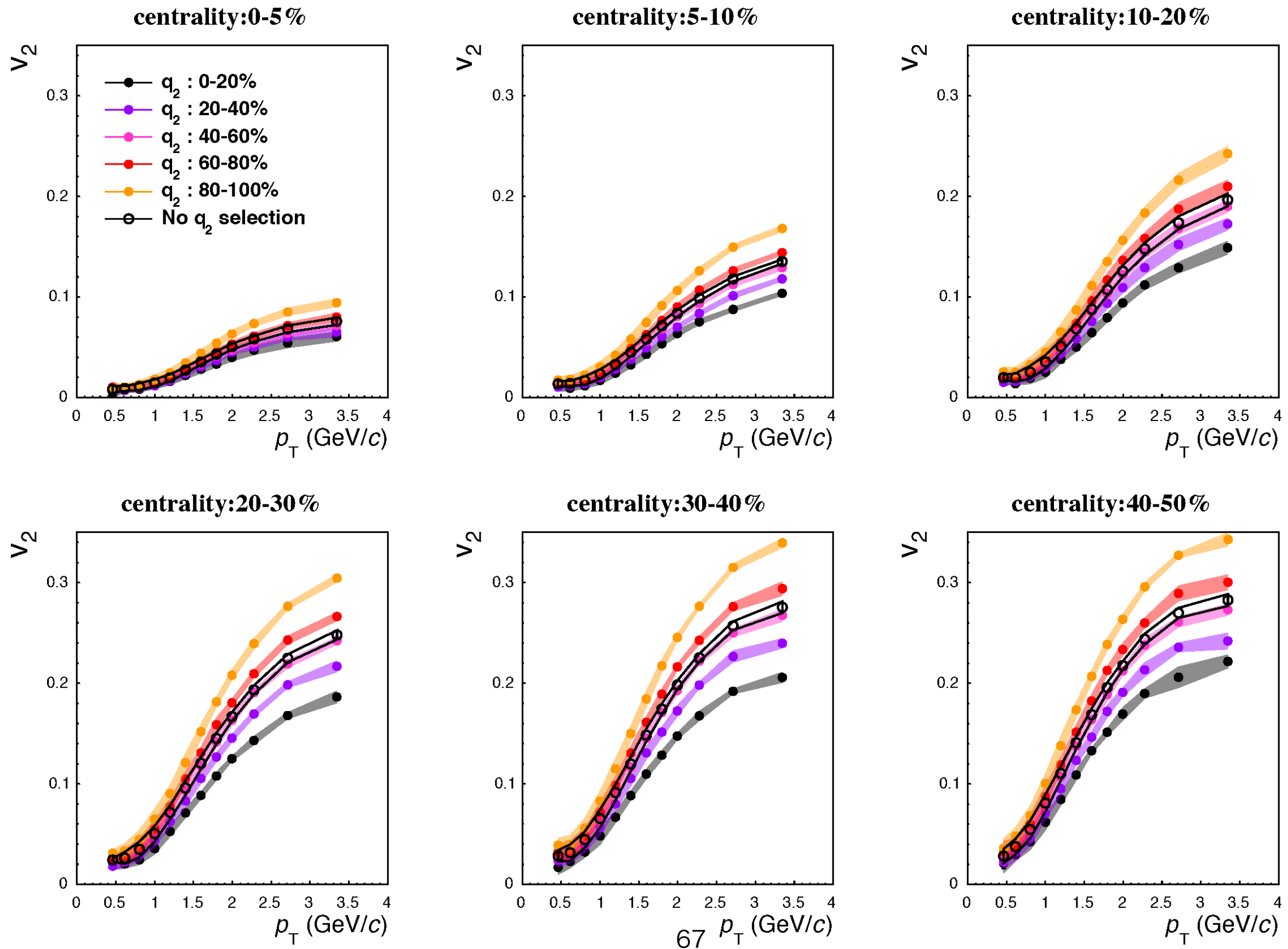
# $v_2$ ( $p_T$ dependence ) for each 20% $q_2$ selection (pion)



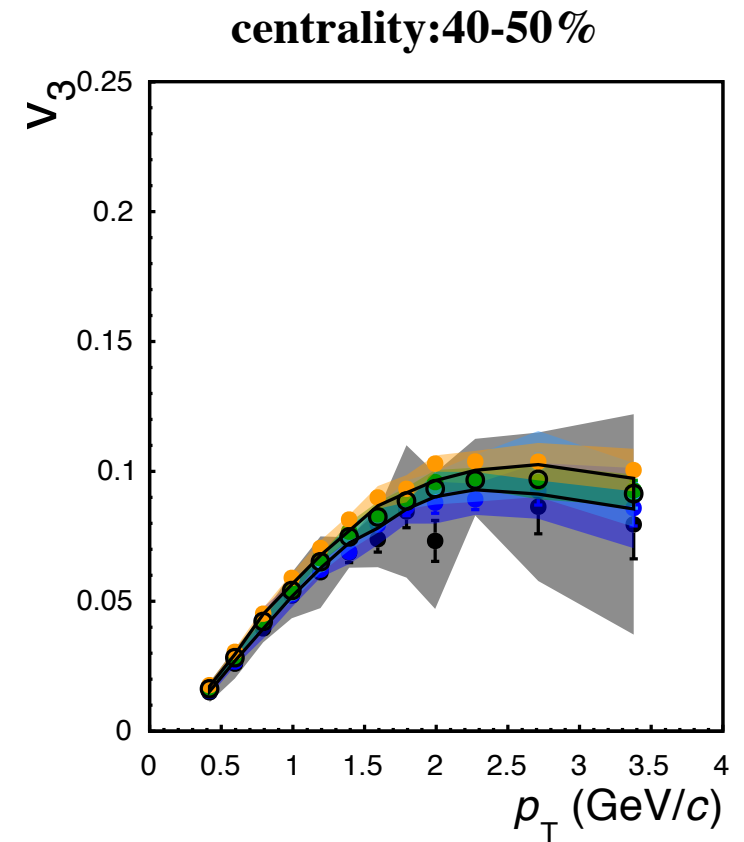
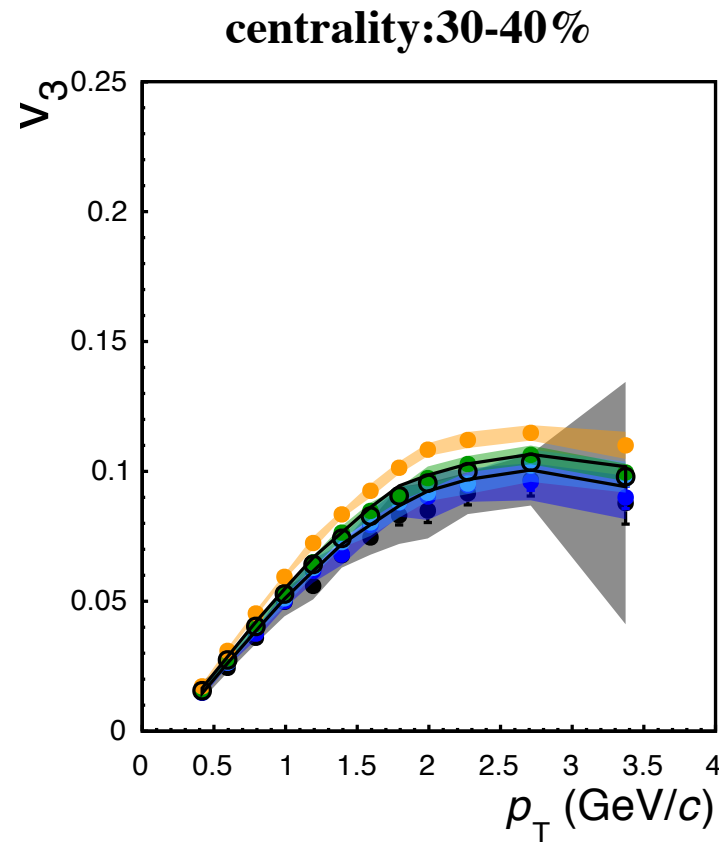
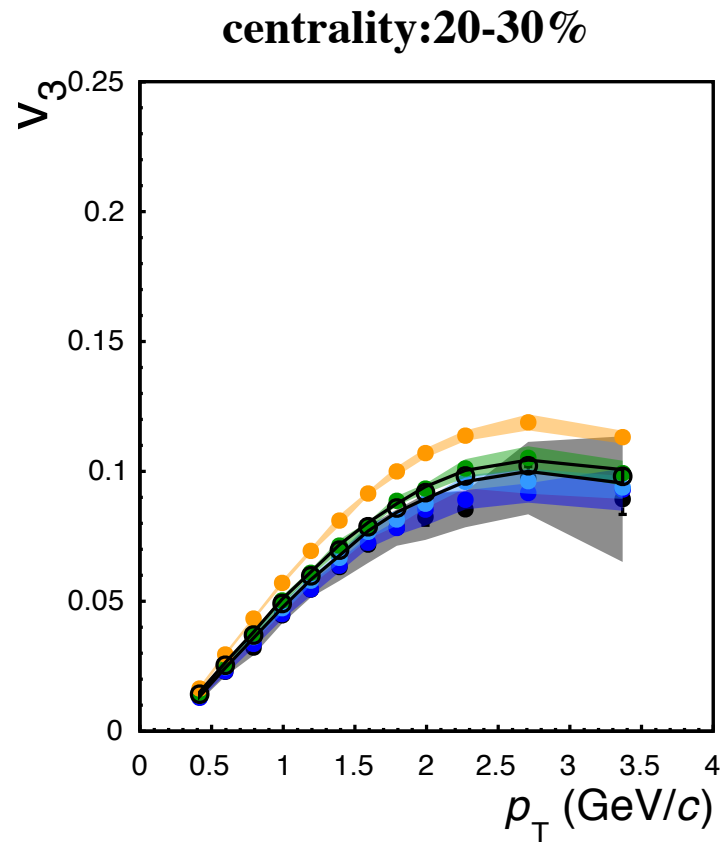
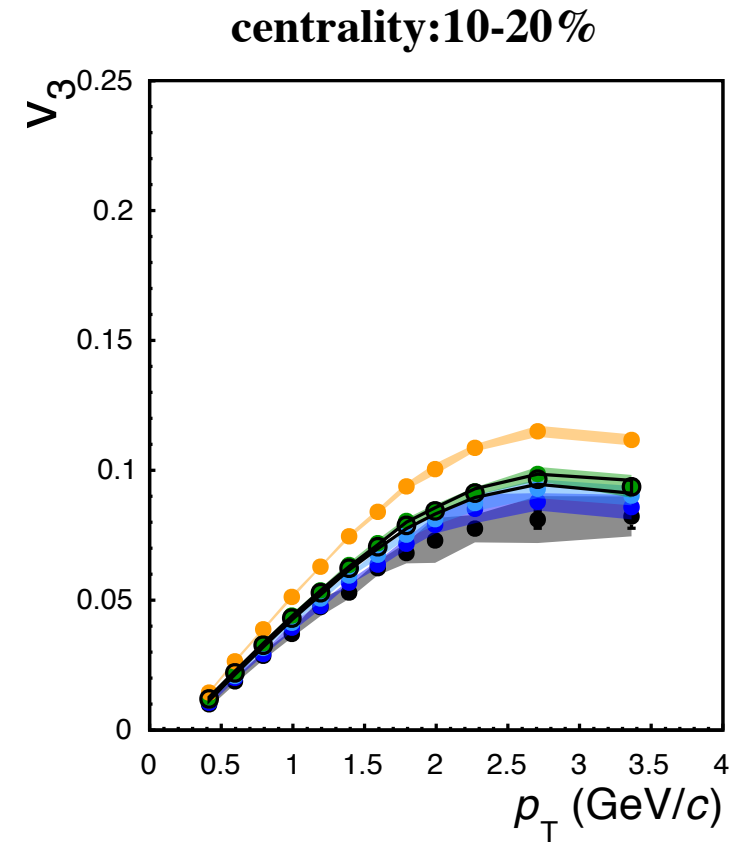
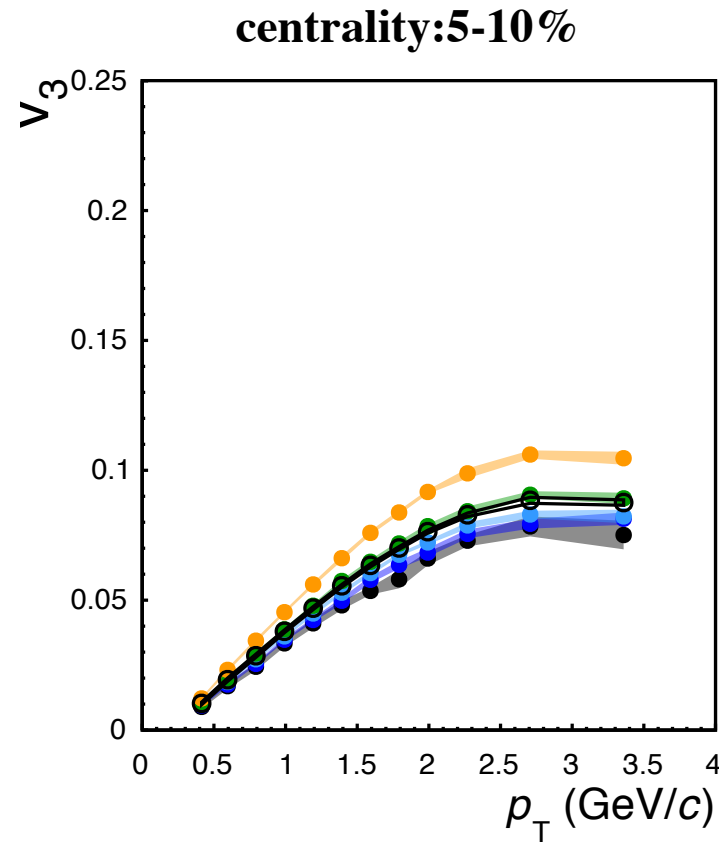
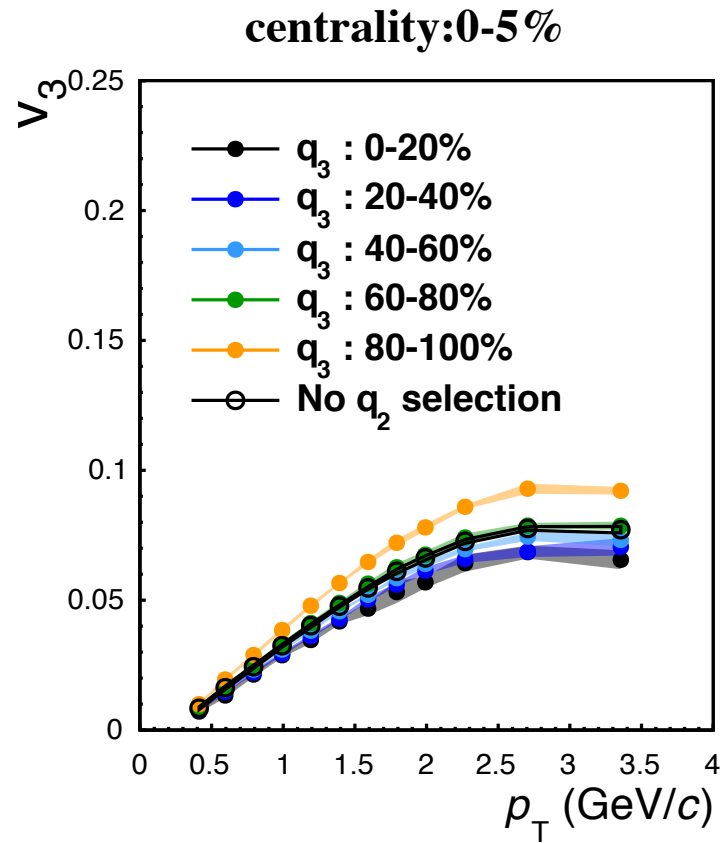
# $v_2$ ( $p_T$ dependence ) for each 20% $q_2$ selection (kaon)



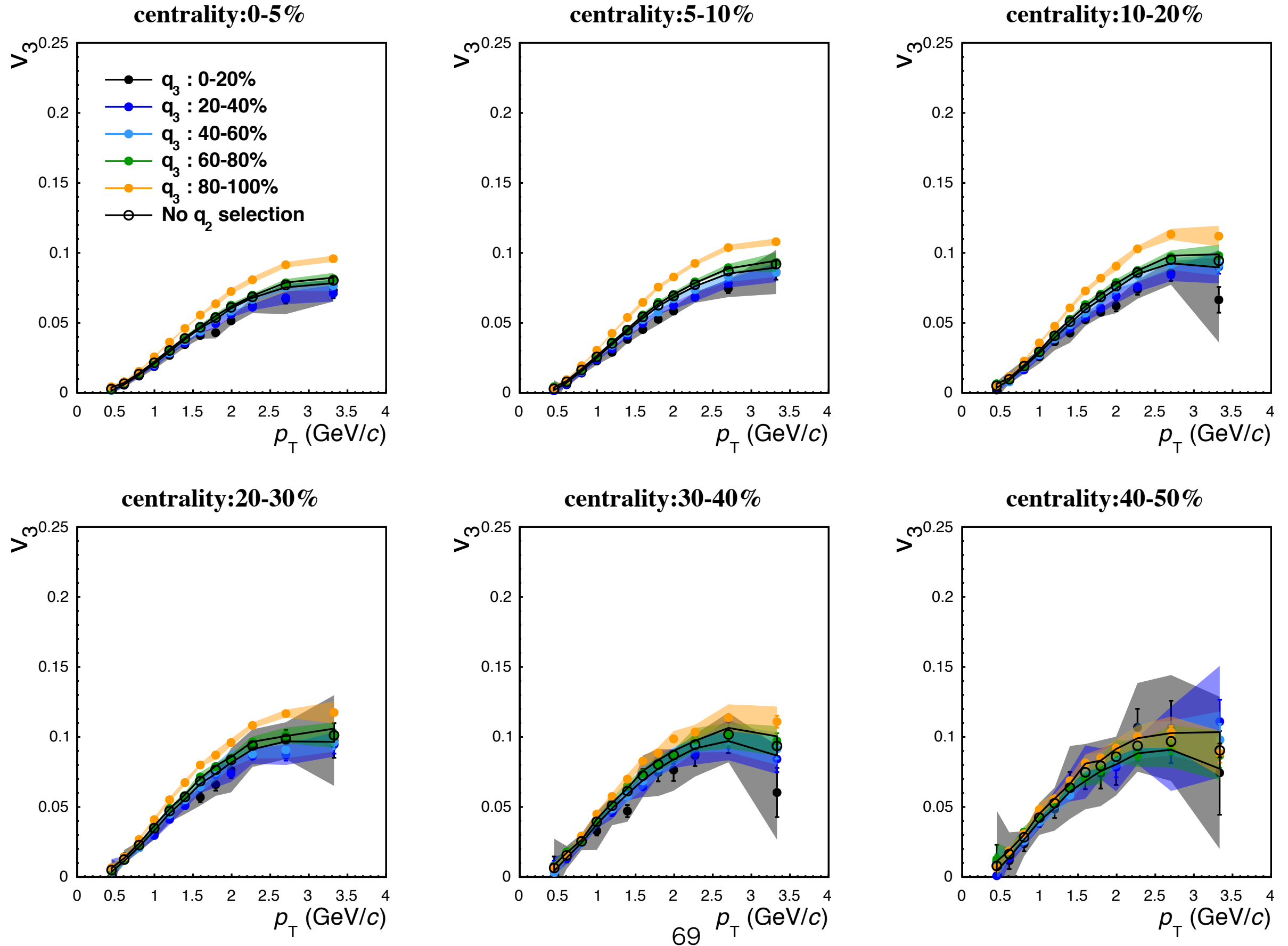
# $v_2$ ( $p_T$ dependence ) for each 20% $q_2$ selection (proton)



# $v_2$ ( $p_T$ dependence ) for each 20% $q_2$ selection (pion)

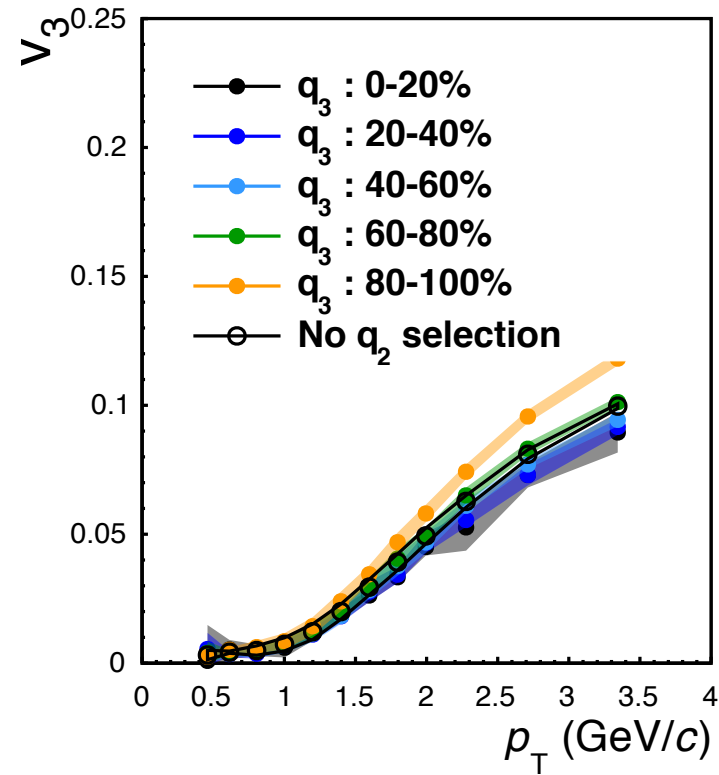


# $v_2$ ( $p_T$ dependence ) for each 20% $q_2$ selection (kaon)

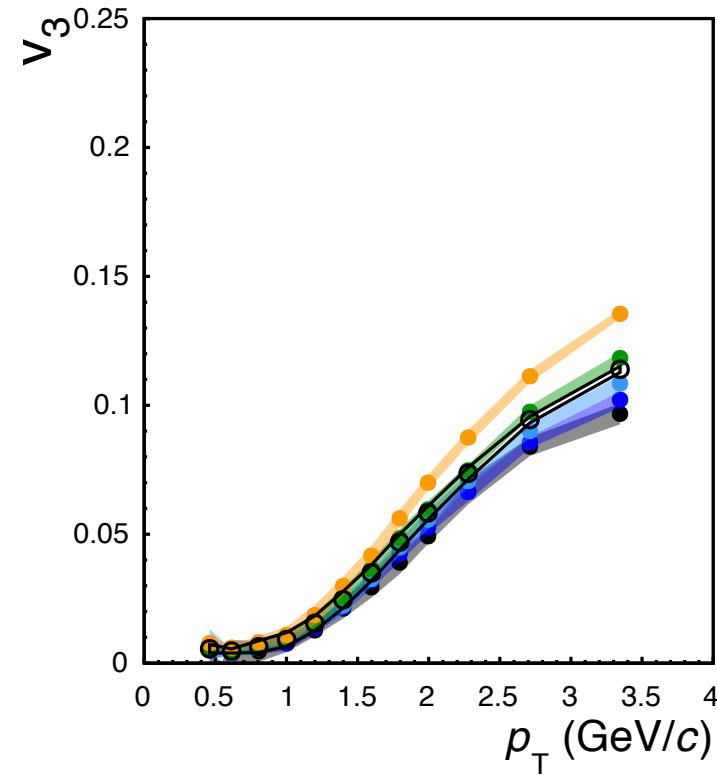


# $v_2$ ( $p_T$ dependence ) for each 20% $q_2$ selection (proton)

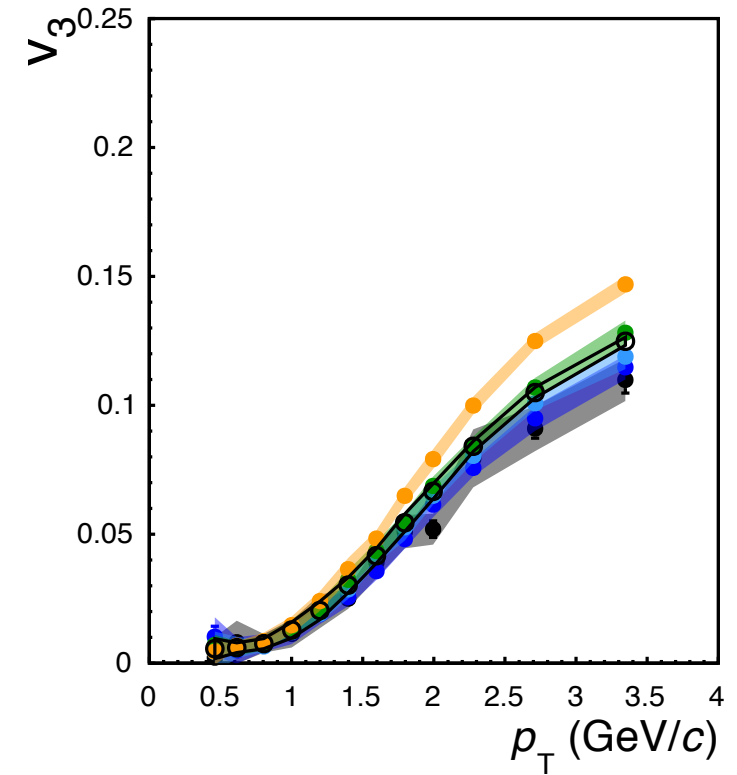
centrality:0-5%



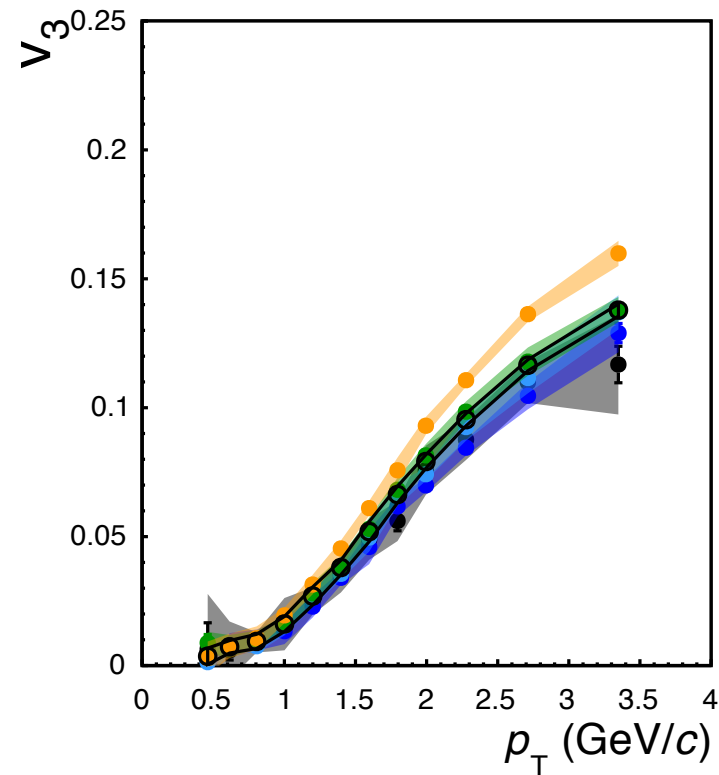
centrality:5-10%



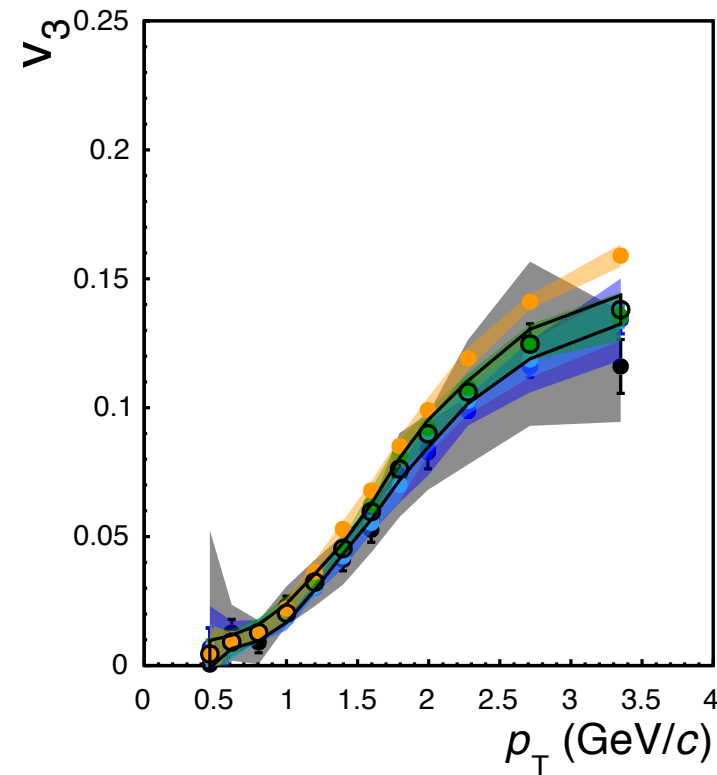
centrality:10-20%



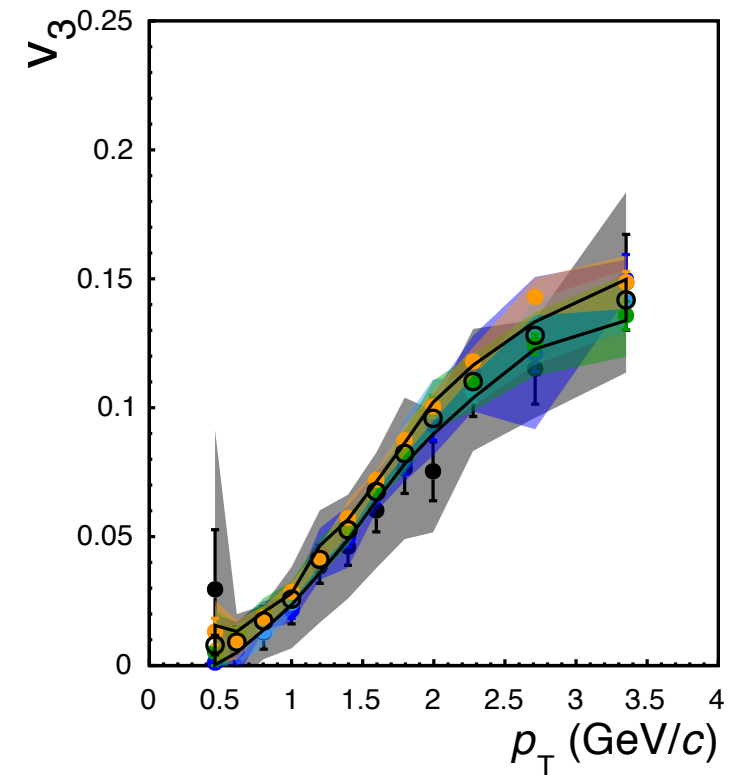
centrality:20-30%



centrality:30-40%



centrality:40-50%





# Blast wave fit for $\pi$ , K, p Spectra

## ★ Fitting for pT spectra

- positive and negative particle
- $\pi$ , K, p
- 6 particles pT spectra (simultaneous)

- pion
- Kaon
- proton

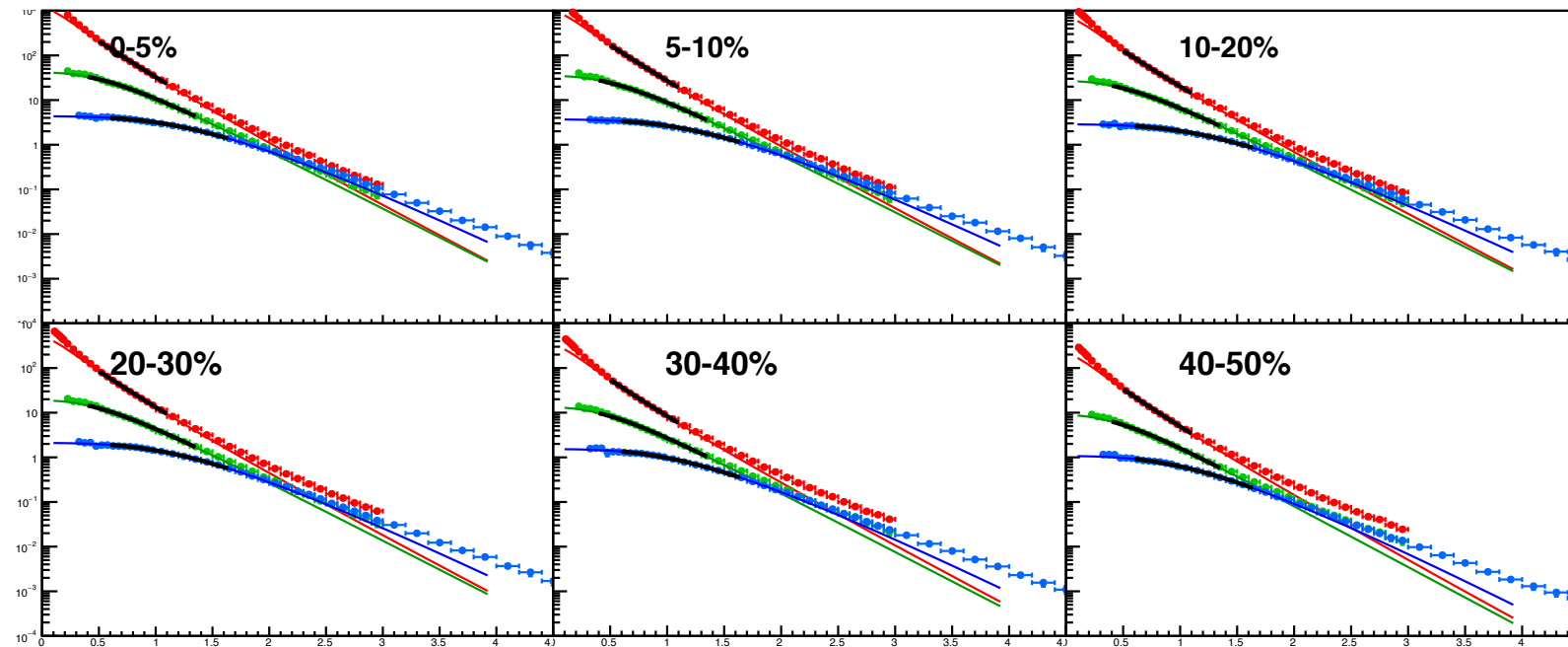
## ★ 2 Parameters

- $T_f$  : Kinetic freeze out temperature
- $p_0$  : Transverse rapidity
- $p_2$  : 2nd order modulation
- $\tau_0$  : Freeze out time
- $\Delta\tau$  : Emission duration

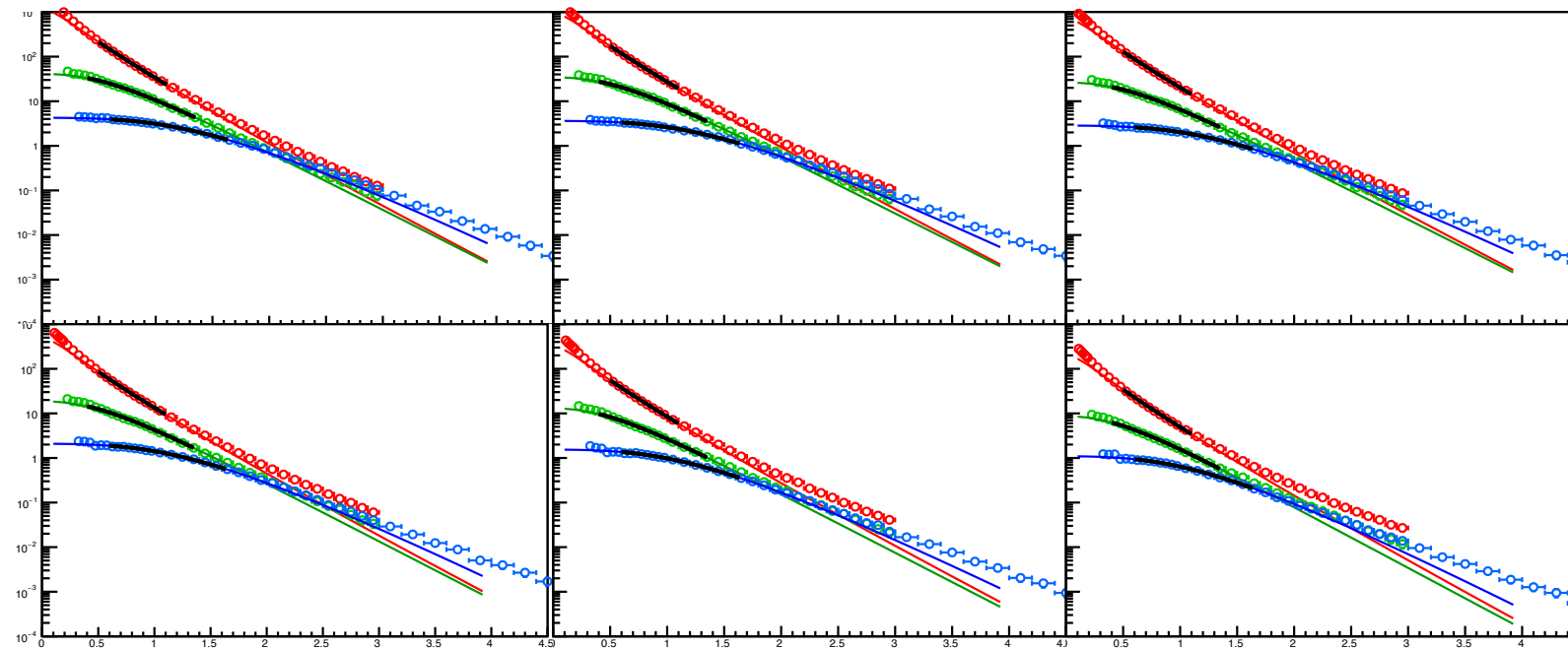
## ★ Fit function for spectra

$$\frac{dN}{p_T dp_T} = 2(2\pi)^{3/2} \tau_0 \Delta\tau m_T \int_0^{2\pi} d\phi_s \int_0^\infty r dr \Omega(r, \phi_s) I_0(\alpha) K_1(\beta)$$

### ★ Positive



### ★ Negative



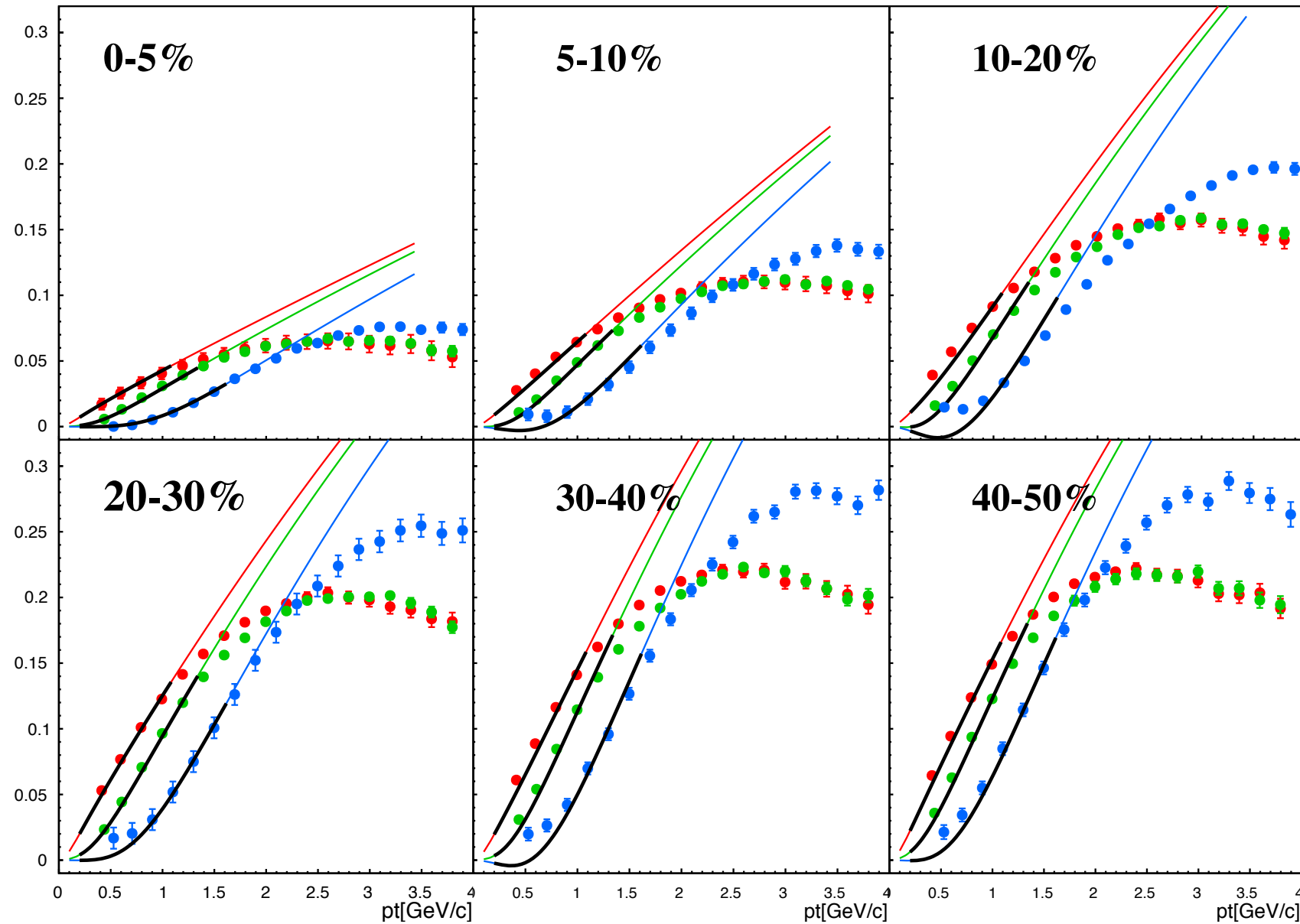
# Blast wave fit for PID $v_2$

## ★ Fitting for pT dependence of $\pi$ , K, p $v_2$

- pion
- Kaon
- proton

## ★ 4 Parameters

- $T_f$  : Kinetic freeze out temperature
- $p_0$  : Transverse rapidity
- $p_2$  : 2nd order modulation
- $R_x, R_y$  : Transverse size



## ★ Fit function for $v_2$

$$v_2(p_T, m) = \frac{\int_0^{2\pi} d\phi_p \int_0^\infty r dr \Omega(r, \phi_s) K_1(\beta) \cos(2\phi_b) I_2(\alpha)}{\int_0^{2\pi} d\phi_s \int_0^\infty r dr \Omega(r, \phi_s) I_{0/2}(\alpha) K_1(\beta)}.$$

# Blast wave fit for HBT radii

## ✓ HBT radii relative to $\Psi_2$

### ★ 7 Parameters

- **Tf** : Kinetic freeze out temperature
- **p0** : Transverse rapidity
- **p2** : 2nd order modulation in transverse flow
- **Rx, Ry** : Transverse size of the source
- **τ0** : Freeze out time
- **Δτ** : Emission duration

$$\langle f(x) \rangle = \frac{\int d^4x f(x) S(x, K)}{\int d^4x S(x, K)},$$
$$\tilde{x}^\mu = x^\mu - \langle x^\mu \rangle,$$

### ★ Fit function for HBT

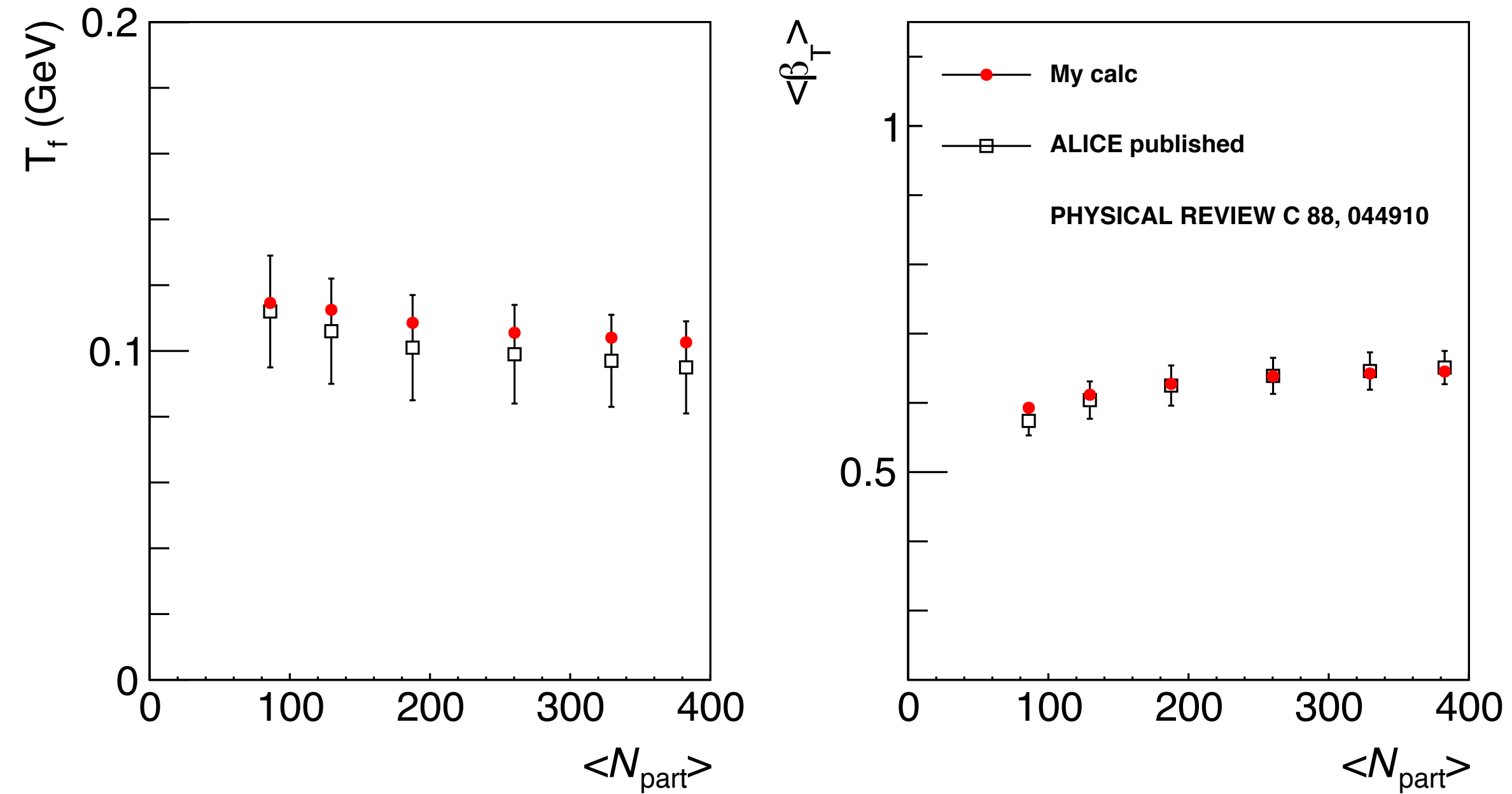
$$R_s^2 = \frac{1}{2}(\langle \tilde{x}^2 \rangle + \langle \tilde{y}^2 \rangle) - \frac{1}{2}(\langle \tilde{x}^2 \rangle - \langle \tilde{y}^2 \rangle) \cos(2\phi_p) - \langle \tilde{x}\tilde{y} \rangle \sin(2\phi_p),$$

$$R_o^2 = \frac{1}{2}(\langle \tilde{x}^2 \rangle + \langle \tilde{y}^2 \rangle) + \frac{1}{2}(\langle \tilde{x}^2 \rangle - \langle \tilde{y}^2 \rangle) \cos(2\phi_p) + \langle \tilde{x}\tilde{y} \rangle \sin(2\phi_p),$$
$$-2\beta_T(\langle \tilde{t}\tilde{x} \rangle \cos \phi_p + \langle \tilde{t}\tilde{y} \rangle \sin \phi_p) + \beta_T^2 \langle \tilde{t}^2 \rangle,$$

$$R_{os}^2 = \langle \tilde{x}\tilde{y} \rangle \cos(2\phi_p) - \frac{1}{2}(\langle \tilde{x}^2 \rangle - \langle \tilde{y}^2 \rangle) \sin(2\phi_p) + \beta_T(\langle \tilde{t}\tilde{x} \rangle \sin \phi_p - \langle \tilde{t}\tilde{y} \rangle \cos \phi_p),$$

$$R_l^2 = \langle \tilde{z}^2 \rangle - 2\beta_l \langle \tilde{t}\tilde{z} \rangle + \beta_l^2 \langle \tilde{t}^2 \rangle,$$
$$= \langle \tilde{z}^2 \rangle,$$

# Blast Wave parameters (comparison with ALICE published)

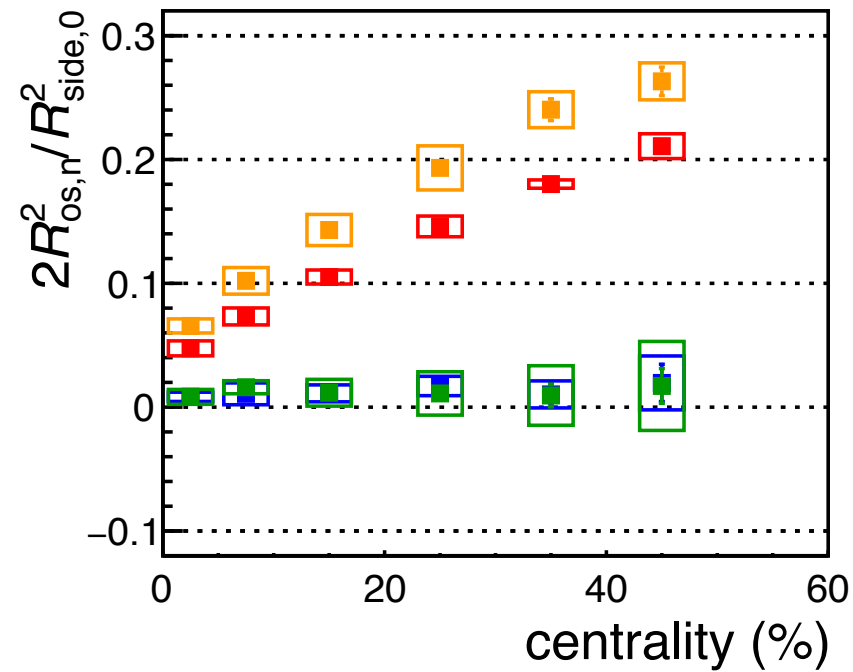
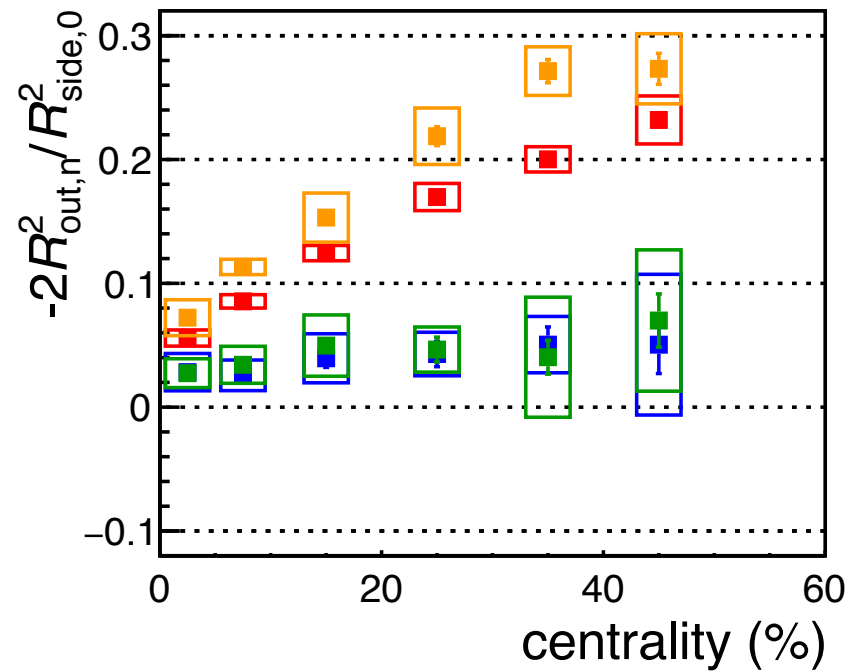
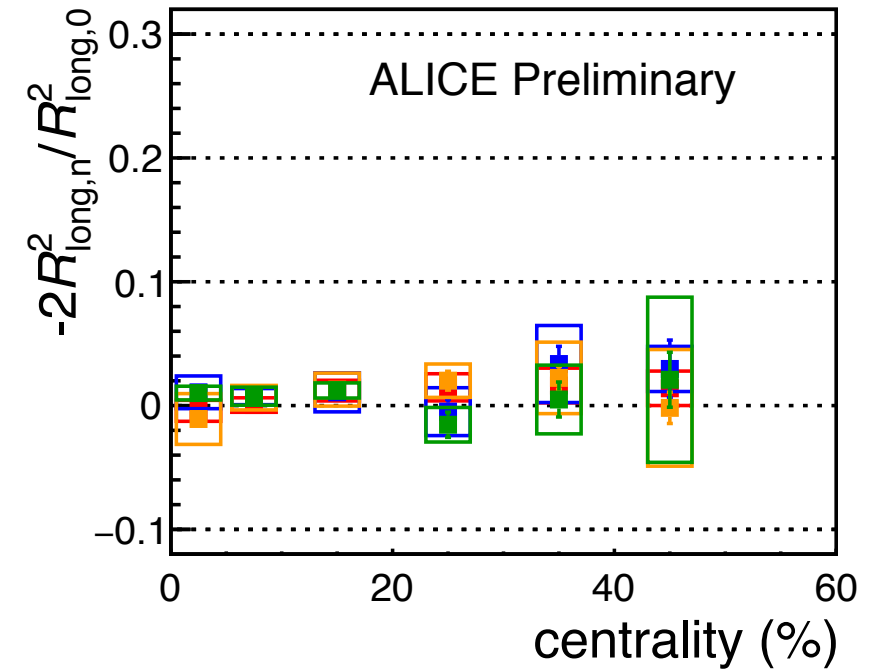
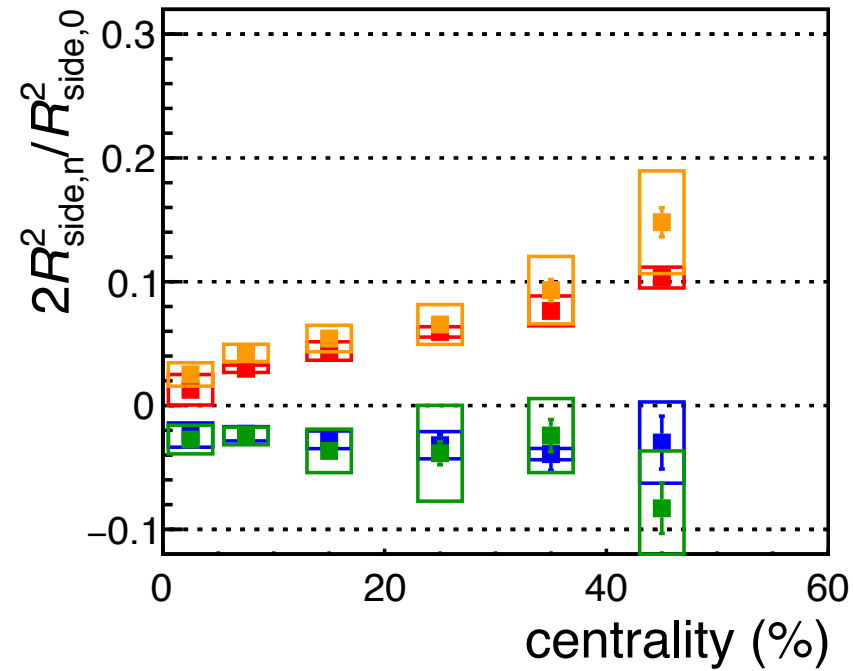
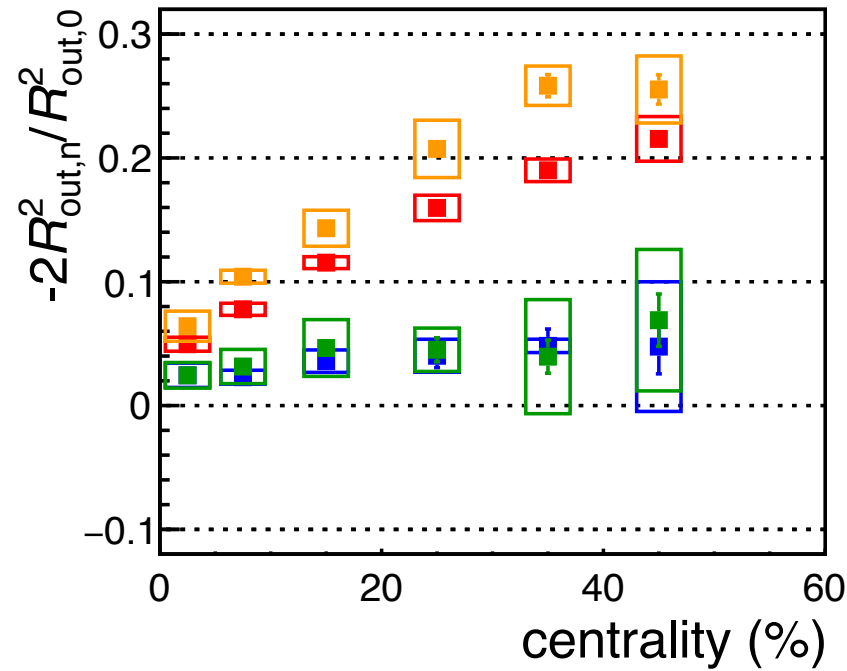


◆ Fully consistent within the systematic uncertainties

$$\langle \beta_T \rangle = \int_0^{2\pi} d\phi \int_0^1 dr \tanh((\rho_0 + \rho_2 \cos(2\phi)) r^n) r (1 + 2s_2 \cos(2\phi))$$

$$s_2 = \frac{1}{2} \frac{(R_y/R_x)^2 - 1}{(R_y/R_x)^2 + 1}$$

# HBT relative to $\Psi_n$ with ESE( $q_n$ cut)



Pb-Pb  $\sqrt{s_{NN}}=2.76$  TeV

$\pi^+\pi^+$  and  $\pi^-\pi^-$  pair combined

$k_T: 0.2-1.5$  (GeV/c)

q vector cut via FMD A+C side

—■— 20% large  $q_2$  cut,  $n=2$

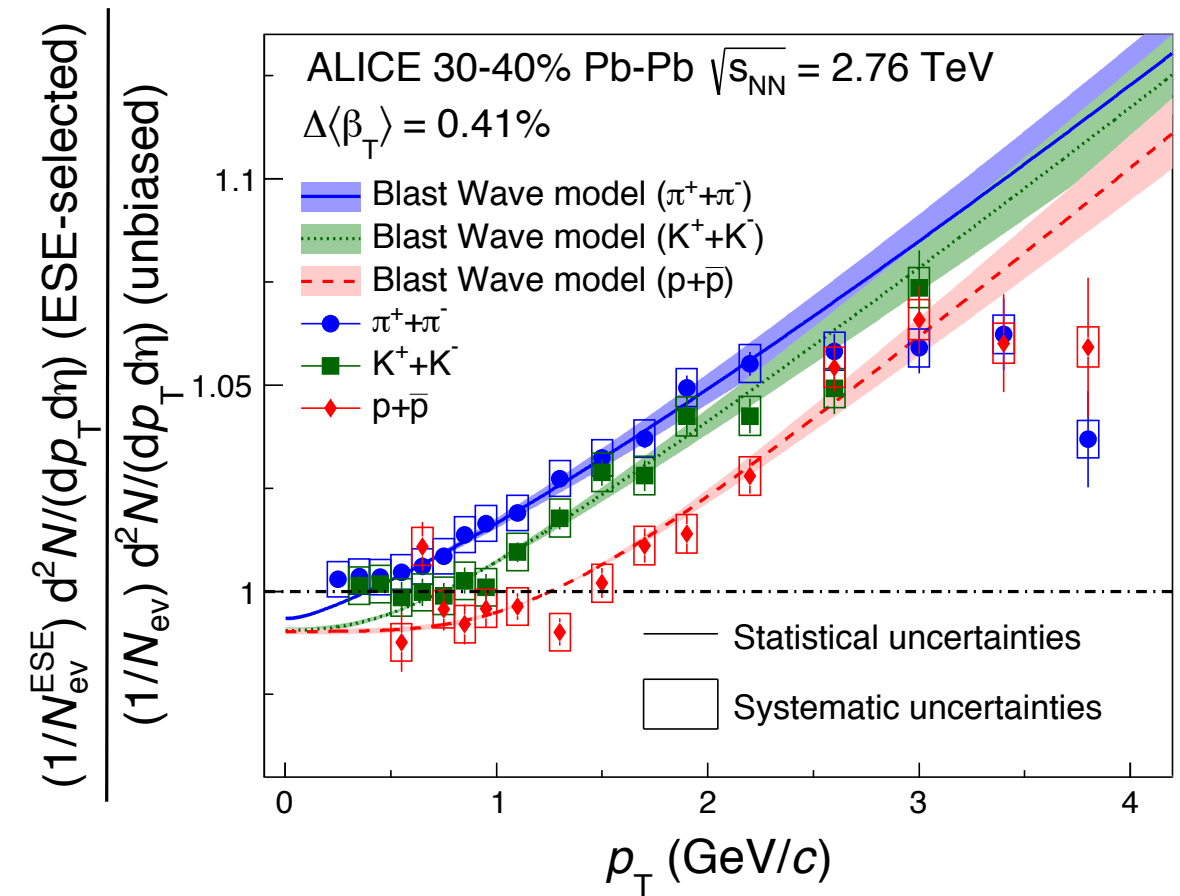
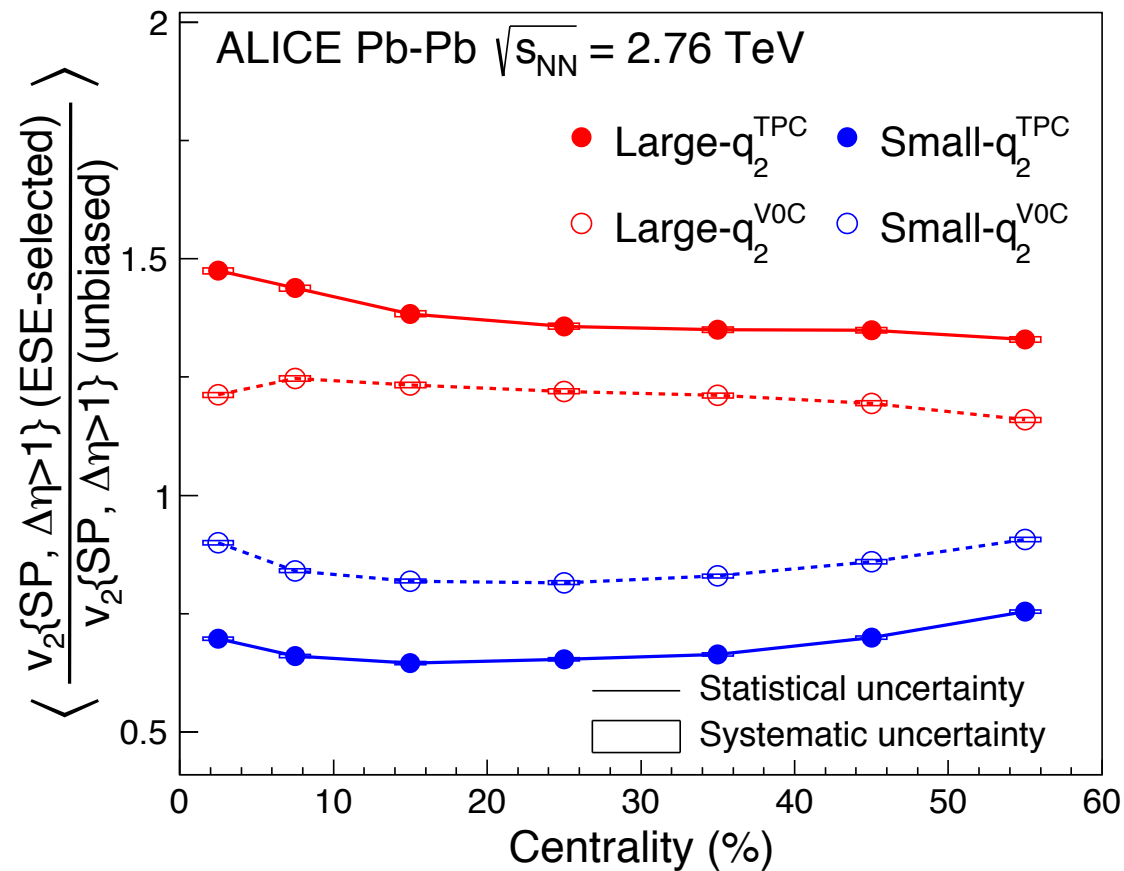
—■— No  $q_2$  cut,  $n=2$

—■— 20% large  $q_3$  cut,  $n=3$

—■— No  $q_3$  cut,  $n=3$

# Spectra + Event shape engineering

## ◆ Positive correlation between $\langle v_2 \rangle$ and $\langle p_T \rangle$

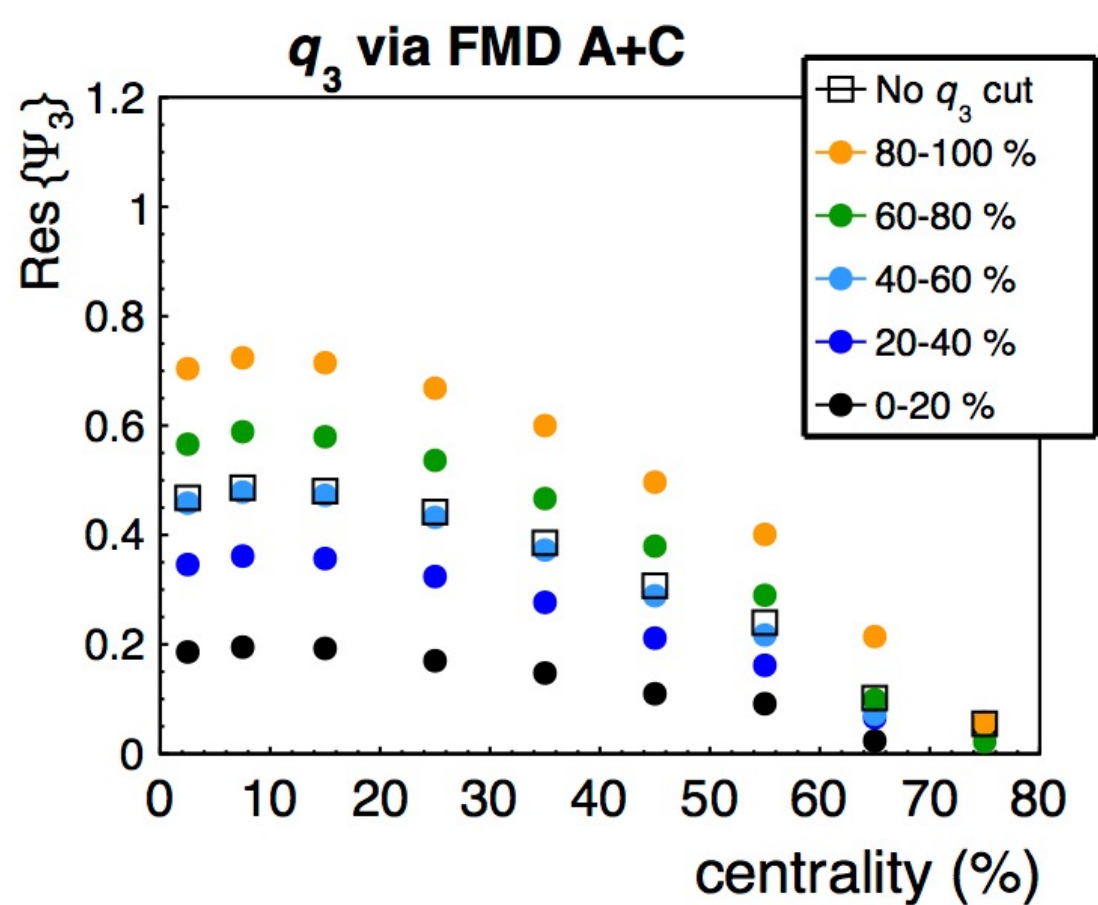
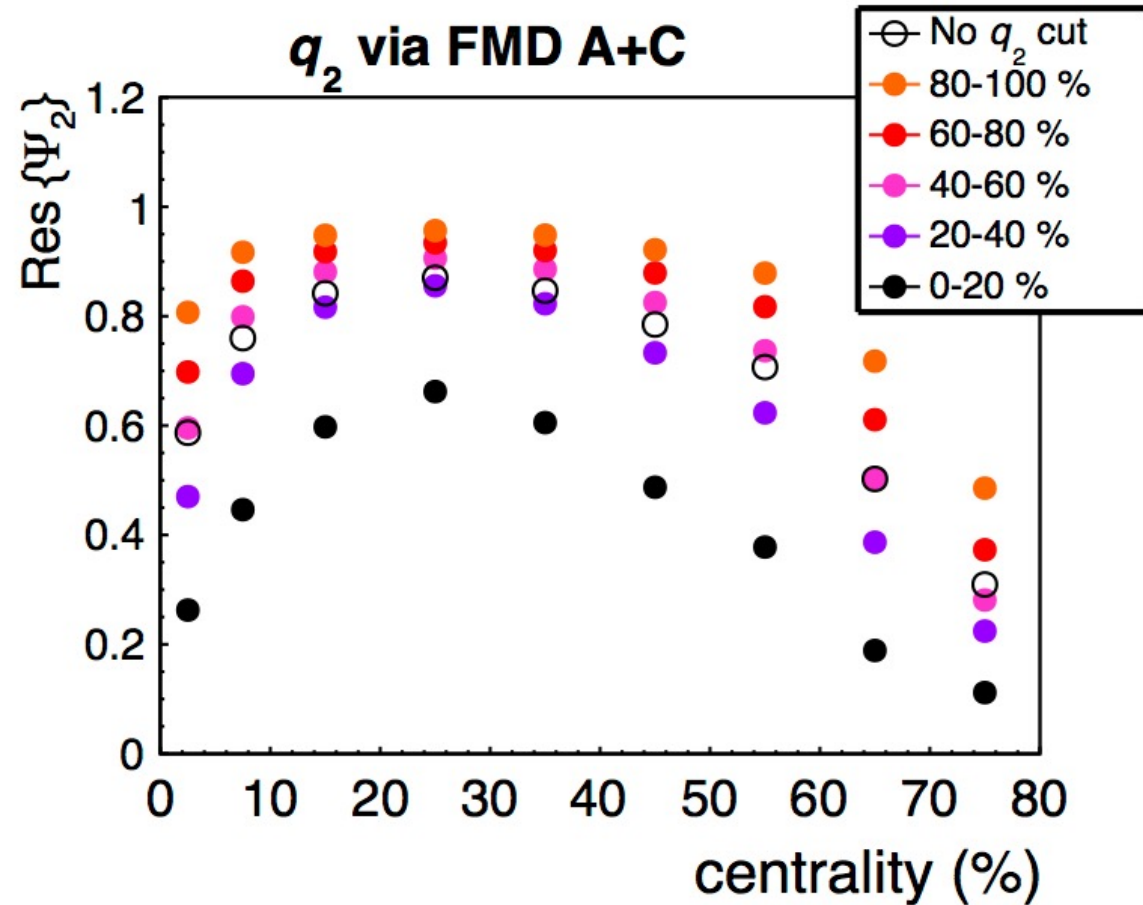
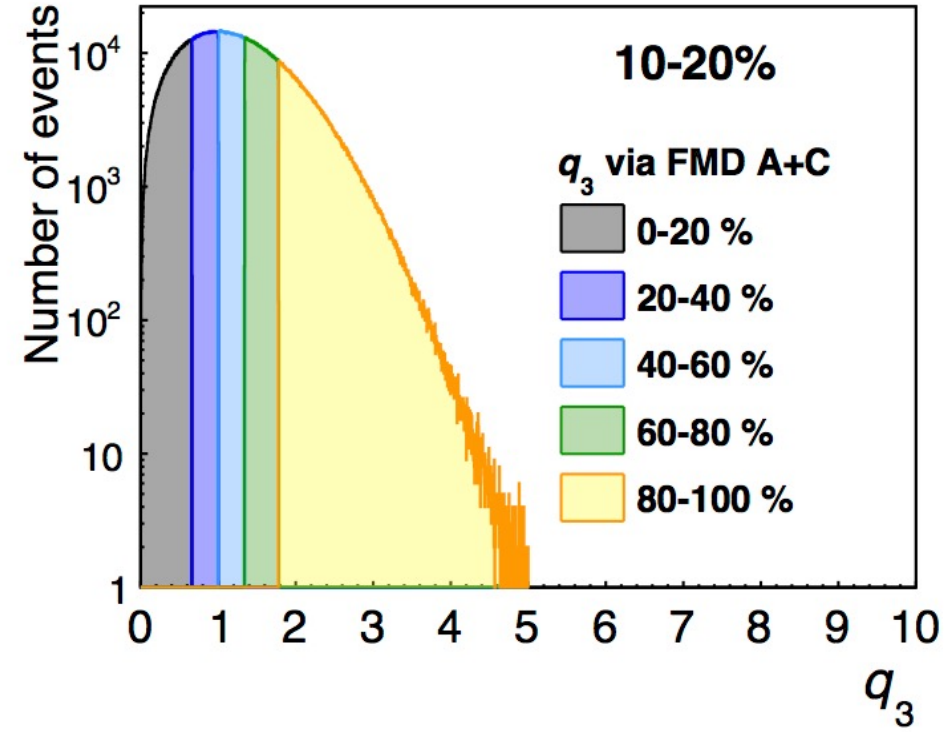
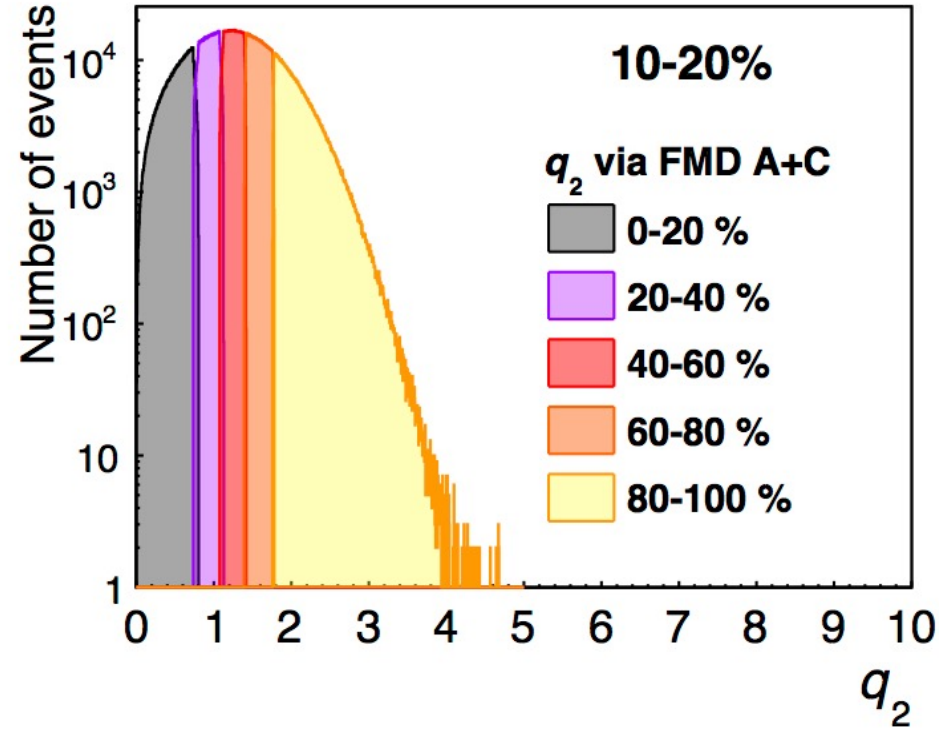


- ◆  $v_2$  ratio with  $q_2$  large(small) cut
  - ✓ large  $q_2^{TPC}$  top10% (bottom10%)
  - ✓ large  $q_2^{VZERO}$  top10%(bottom10%)

- ◆ Ratio of  $p_T$  distribution of  $\pi$ ,  $K$ ,  $p$
- ◆  $q_2^{TPC}$  top 10% cut ( $|\ln| < 0.4$ )
- ◆ Blast wave model comparison
  - ✓  $\Delta\langle\beta_T\rangle = +0.41\%$

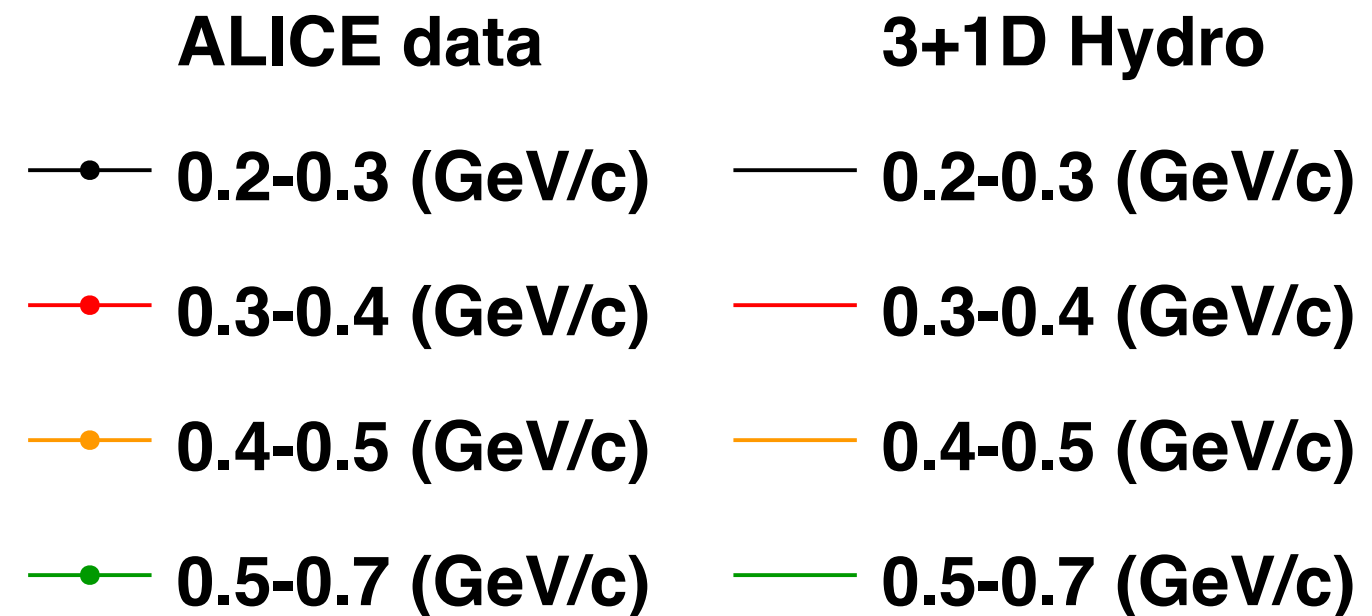
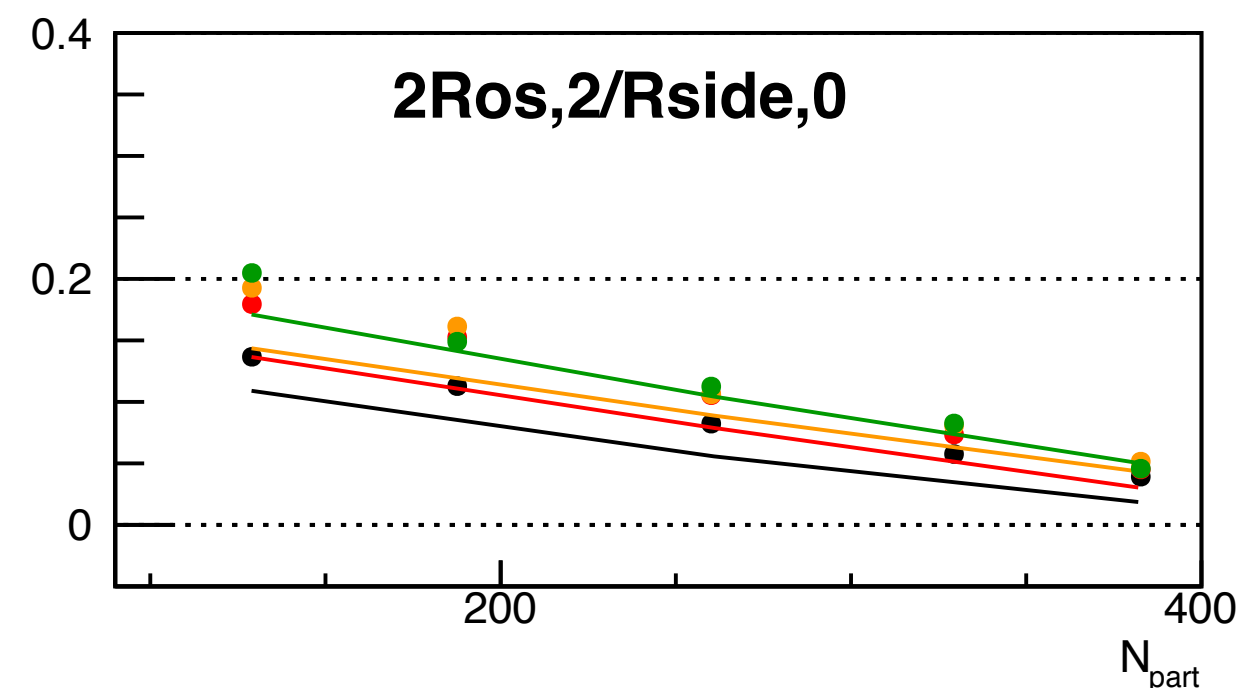
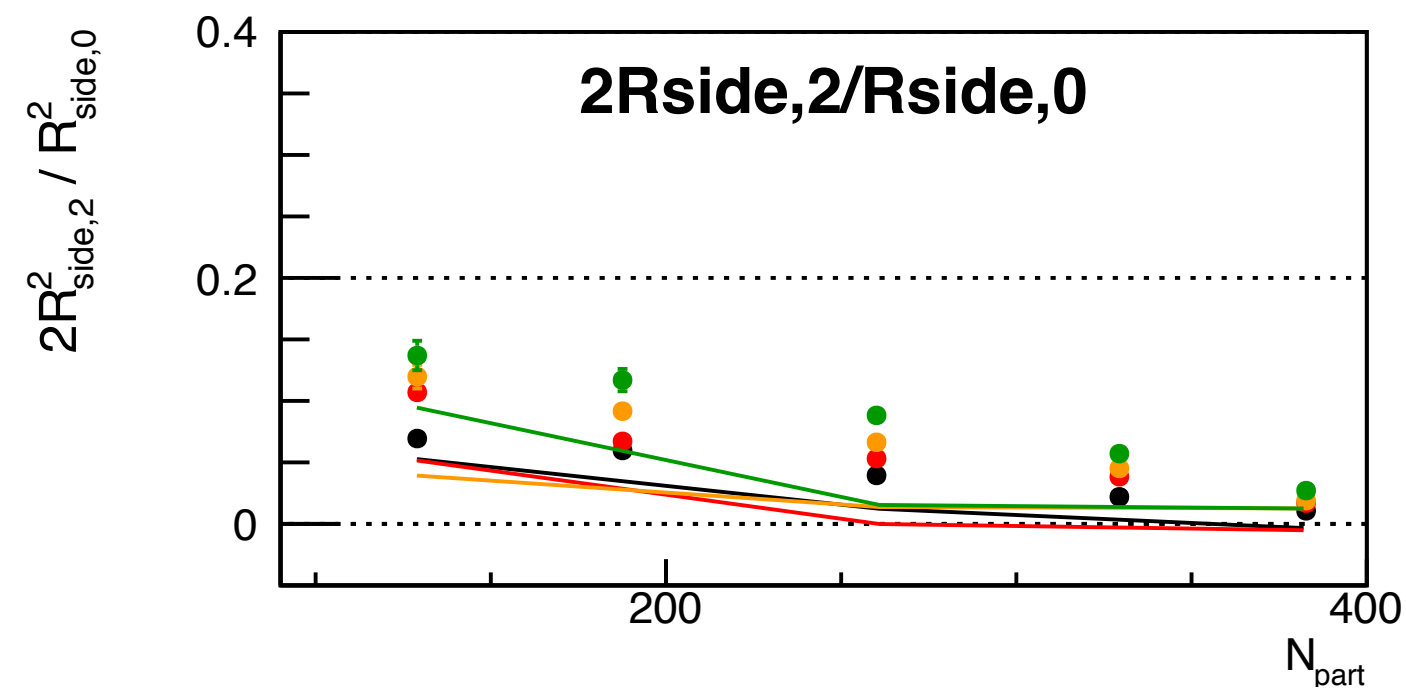
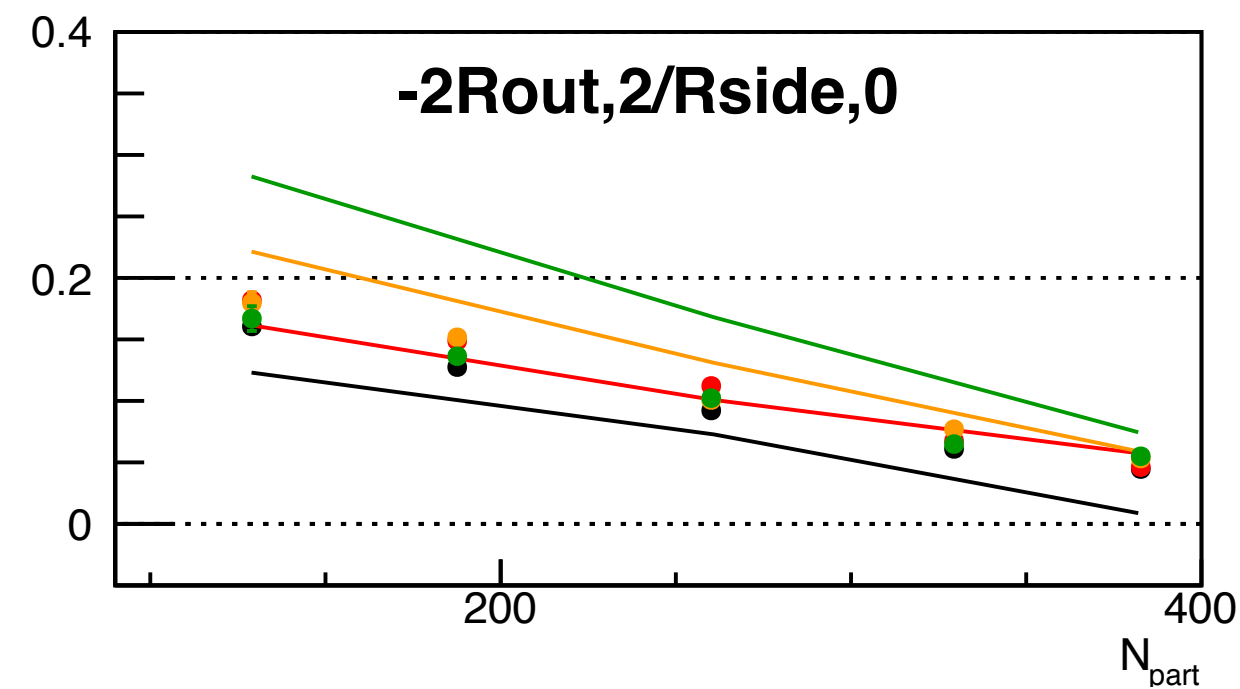


# E.P. resolution with $q_n$ cut



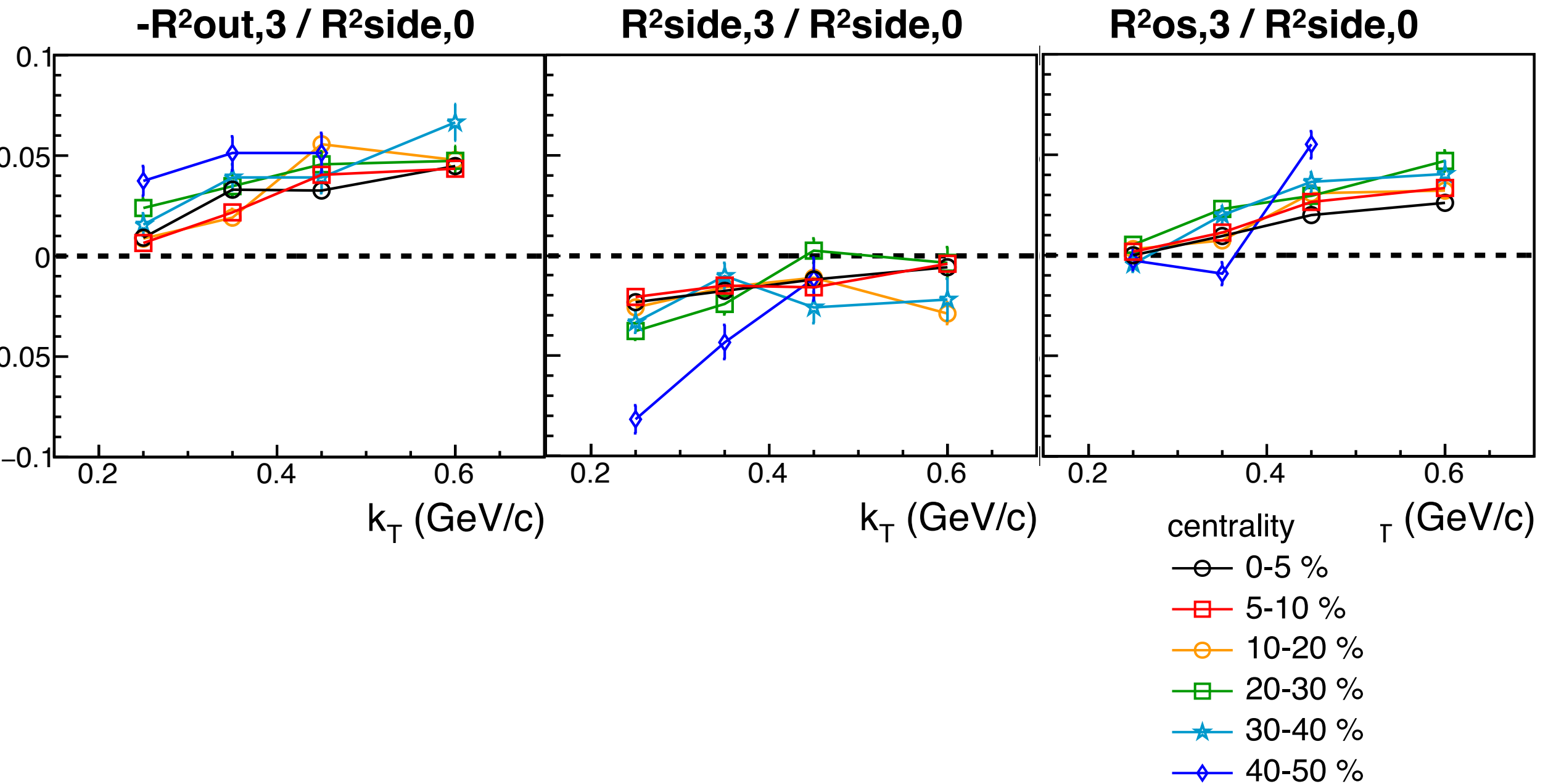
# 2nd harmonic oscillation amplitude of HBT radii

(P. Bozek, J. Phys. G38, 124097)



- ◆ Hydro calculation cannot reproduce  $R_{out,2}^2 / R_{side,0}^2$  small  $k_T$  dependence
  - ◆  $N_{part}$  dependence of  $R_{out,2}^2 / R_{side,0}^2$  is very similar though
- ◆  $R_{out,2}^2 / R_{side,0}^2$  in lowest  $k_T$  is consistent but not in high  $k_T$  (under estimate)
- ◆  $R_{os,2}^2 / R_{side,0}^2$  is well reproduced

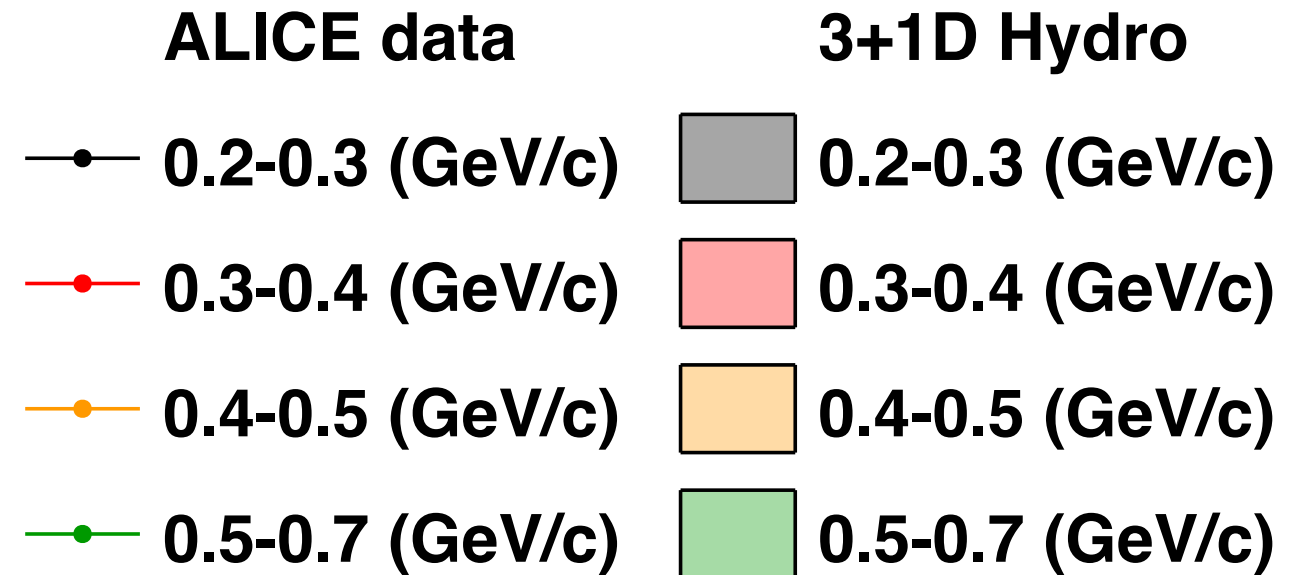
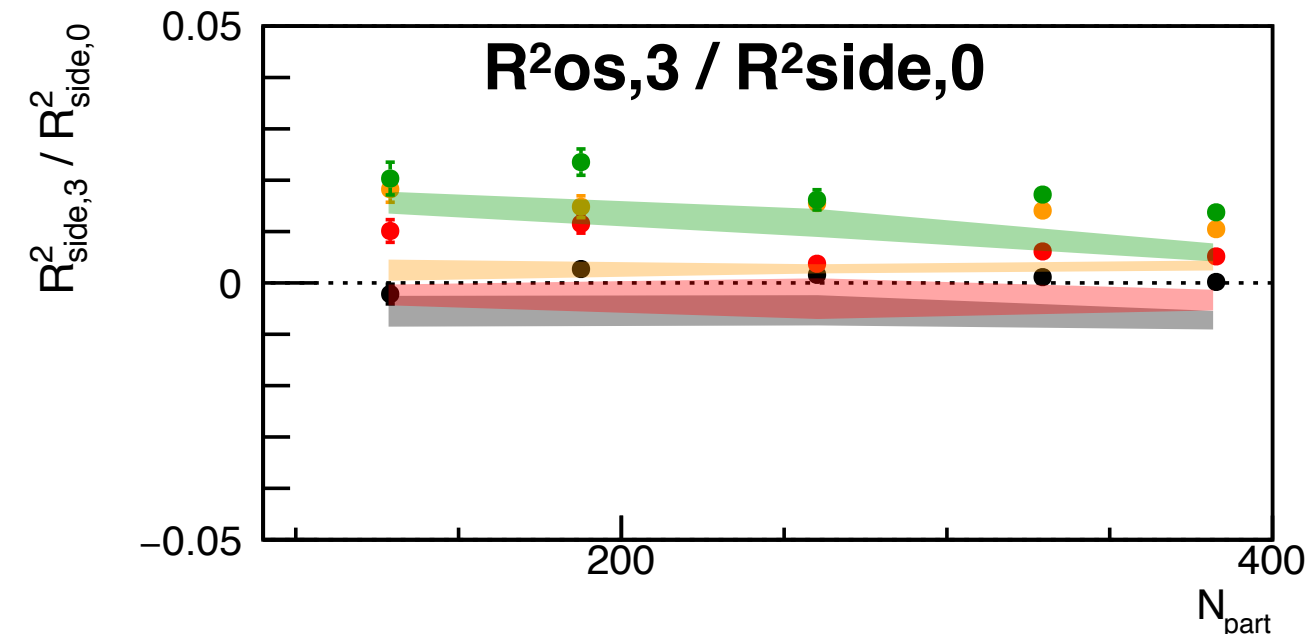
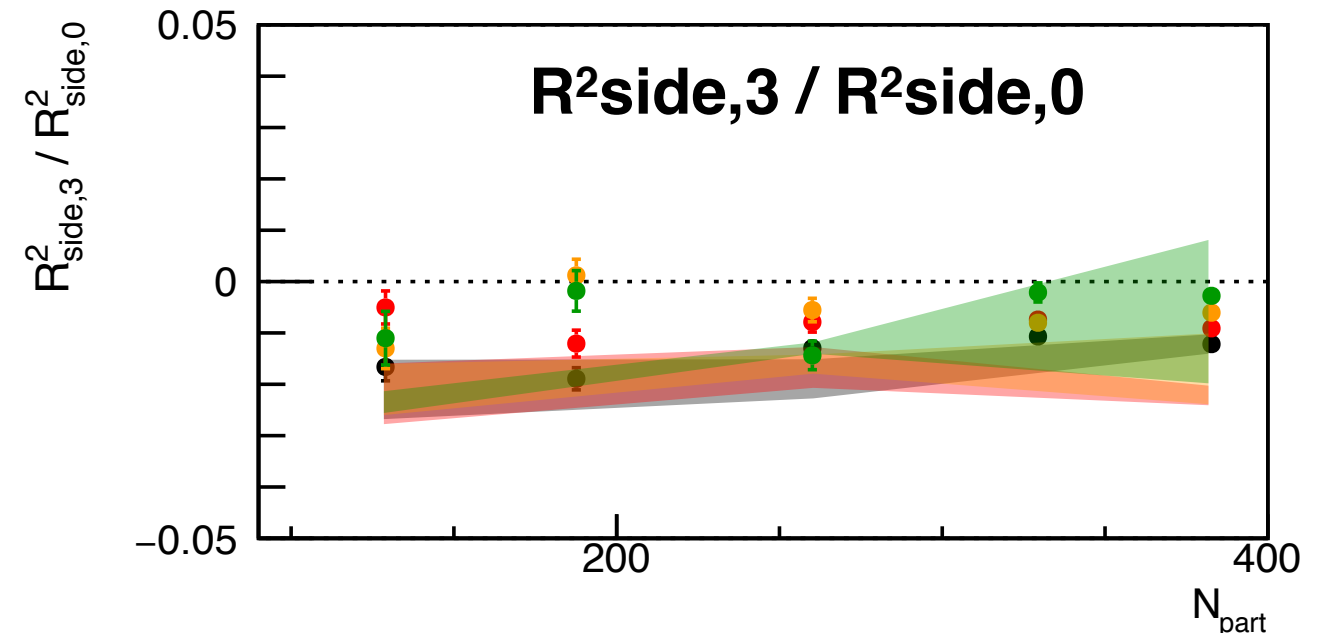
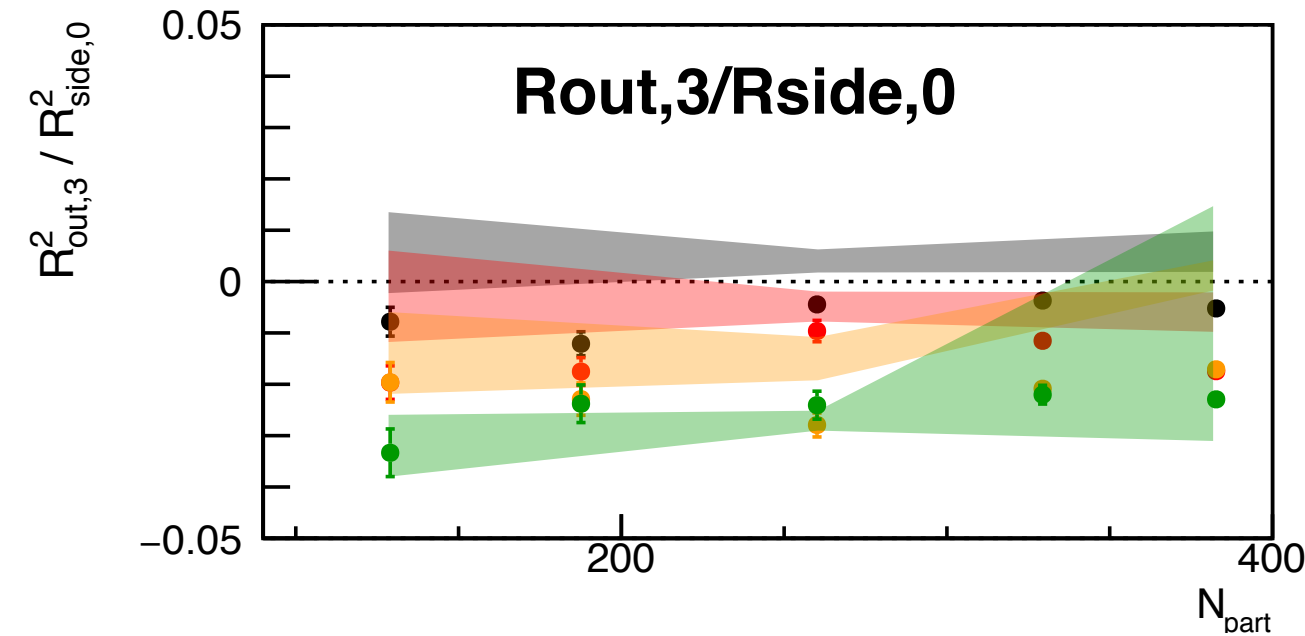
# Relative amplitude of HBT radii w.r.t. $\Psi_3$ $k_T$ dependence



- ✓ Relative amplitude of  $R_{out}$  becomes larger with increasing  $k_T$
- ✓  $R_{side}$  oscillation decreases from low  $k_T$  to high  $k_T$
- ✓  $R_{os}$  shows explicit  $k_T$  dependence and  $R_{os}$  oscillation is 0 at  $k_T=0$

# 3rd harmonic oscillation amplitude of HBT radii

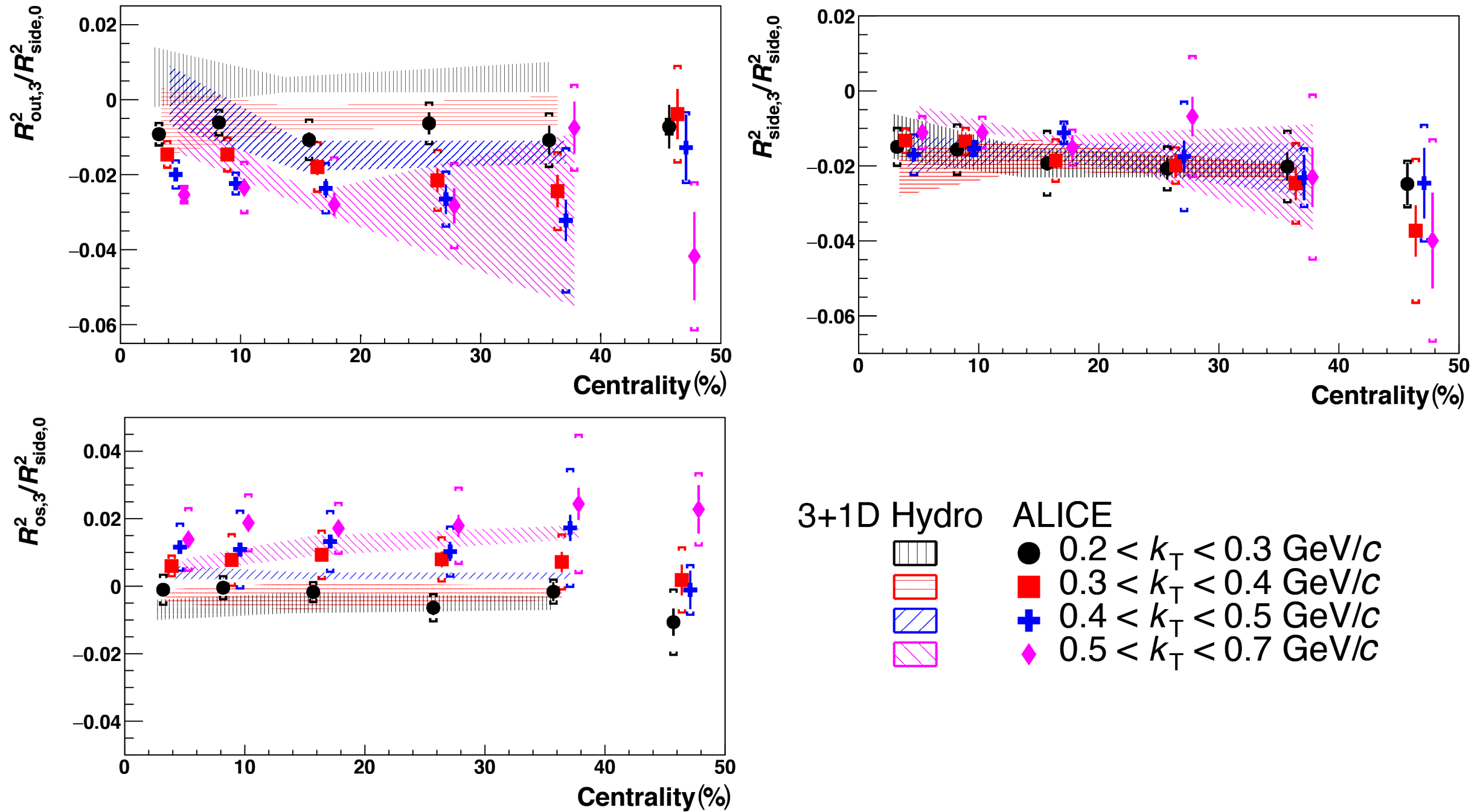
(P. Bozek, J. Phys. G38, 124097)



- ◆  $N_{part}$  dependence in Hydro calc. and Data are qualitative consistent
- ◆  $R^2_{out}$  oscillation is consistent in high  $k_T$  (Hydro calc. at low  $p_T$  is opposite sign)
- ◆  $R^2_{side}$  oscillation is consistent in low  $k_T$  (Hydro calc. can't reproduce  $k_T$  dependence)
- ◆ Low  $k_T$  of  $R_{os}$  oscillation with Hydro calc is underestimate

# 3rd harmonic oscillation amplitude of HBT radii

(P. Bozek, J. Phys. G38, 124097)



- ◆  $N_{\text{part}}$  dependence in Hydro calc. and Data are qualitatively consistent
- ◆  $R^2_{\text{out}}$  oscillation is consistent in high  $k_T$  (Hydro calc. at low  $p_T$  is opposite sign)
- ◆  $R^2_{\text{side}}$  oscillation is consistent in low  $k_T$