

“Collective flow and two particle correlations at RHIC and LHC”

Phenomenology and Experiments at RHIC and LHC

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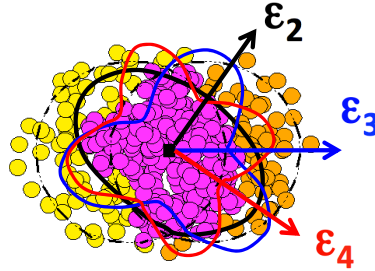
Collective flow

- ✧ EP correlations
- ✧ Event by event v_n
- ✧ N_q scaling
- ✧ v_2 in geometry controlled collisions
- ✧ Direct photon v_2
- ✧ High p_T & jet v_2

Event plane correlations

Measured planes : Ψ_n

True planes : Φ_n



Desired correlator

$$\langle \cos k(\Phi_n - \Phi_m) \rangle = \frac{\langle \cos k(\Psi_n - \Psi_m) \rangle}{\text{Res}\{k\Psi_n\} \text{Res}\{k\Psi_m\}}$$

Observed correlator

arXiv: 1105.3928
PHENIX but no
corrections for reso.

Resolution for individual planes

$$\text{Res}\{k\Psi_n\} = \langle \cos(k\Psi_n - k\Phi_n) \rangle$$

Can generalize into multi-plane correlations

Variable: $c_1\Phi_1 + 2c_2\Phi_2 \dots + lc_l\Phi_l$ satisfying: $c_1 + 2c_2 \dots + lc_l = 0$

arXiv:1104.4740,
Bhalerao, Luzum,
Ollitrault

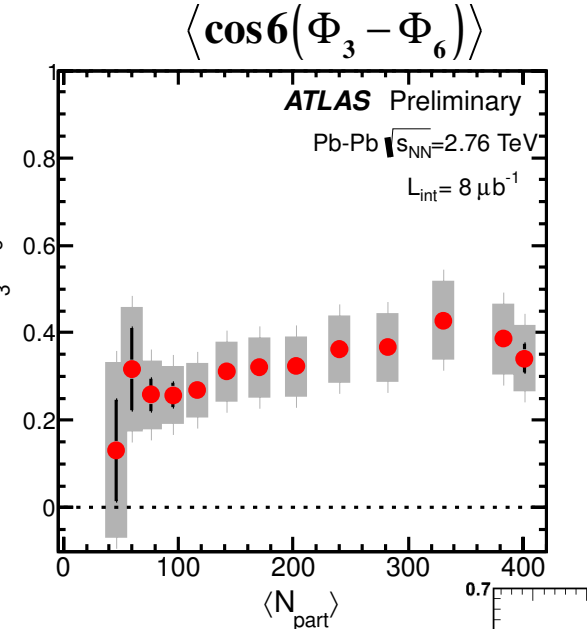
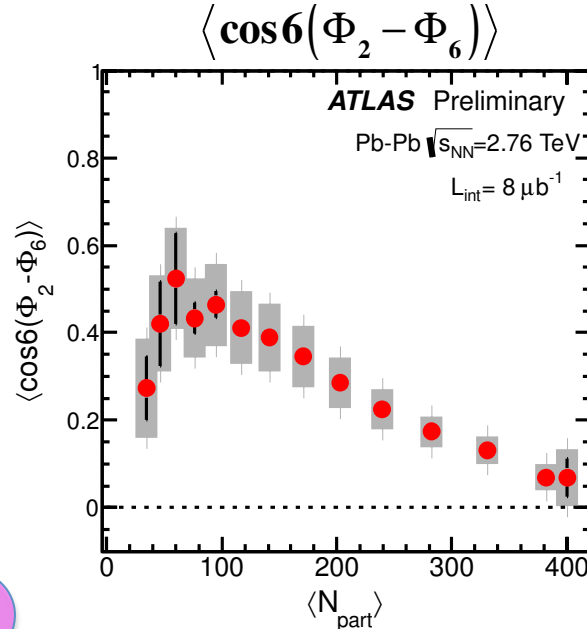
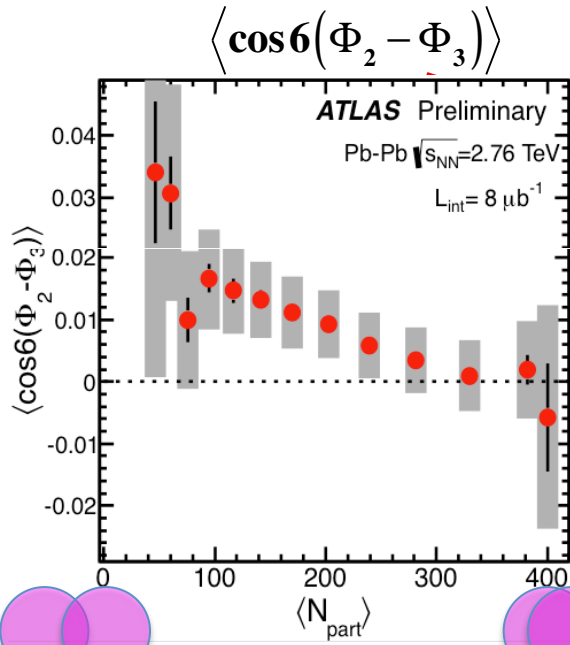
$$\langle \cos(c_1\Phi_1 + \dots + lc_l\Phi_l) \rangle = \frac{\langle \cos(c_1\Psi_1 + \dots + lc_l\Psi_l) \rangle}{\text{Res}\{c_1\Psi_1\} \dots \text{Res}\{lc_l\Psi_l\}}$$

$$\text{Res}\{c_n n \Psi_n\} = \langle \cos c_n n (\Psi_n - \Phi_n) \rangle$$

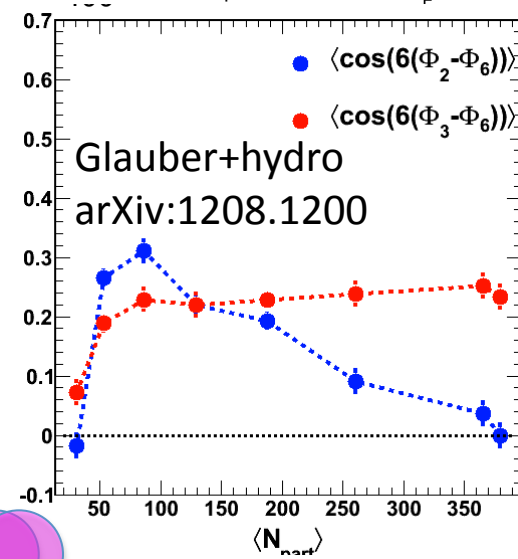
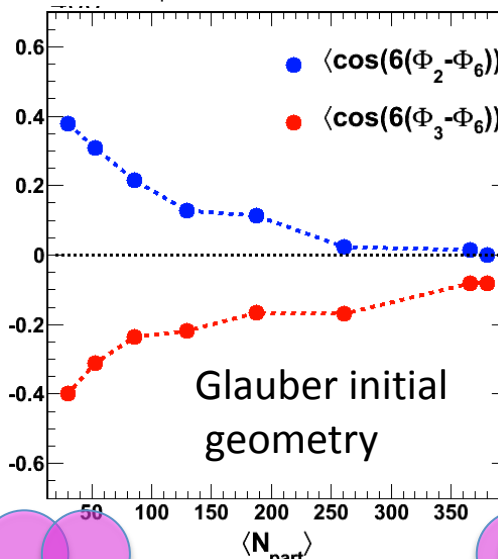
arXiv:1203.5095
1205.3585

$$\text{Res}\{(c_1\Psi_1 + \dots + lc_l\Psi_l)\} = \text{Res}\{c_1\Psi_1\} \dots \text{Res}\{lc_l\Psi_l\}$$

Two plane correlations

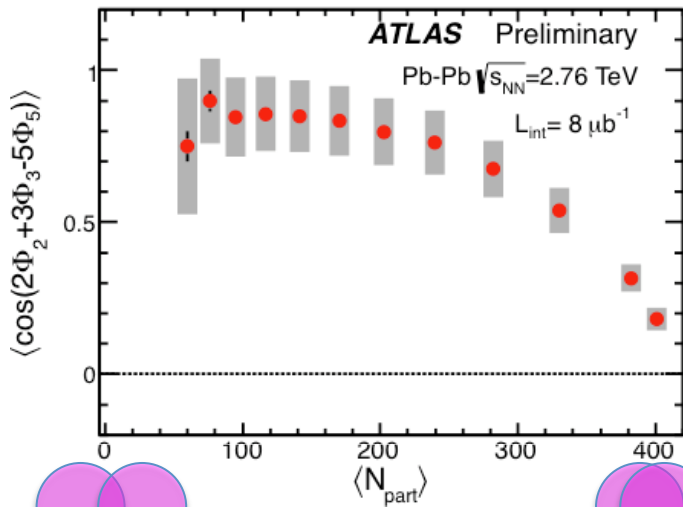


- ✧ $\Phi_{2,3}$ weakly correlated both strongly correlated with Φ_6
- Alignment between Φ_{23} & Φ_6
- ✧ Hydro. expansion qualitatively reproduce EP cor.
- Parameters in hydro. would also take main role in EP cor.

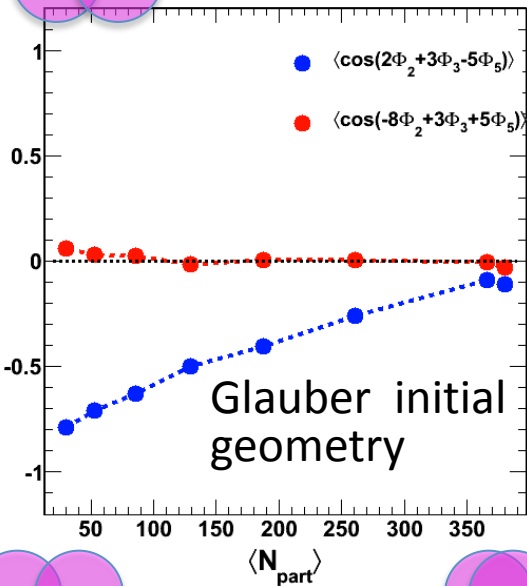
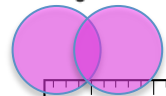
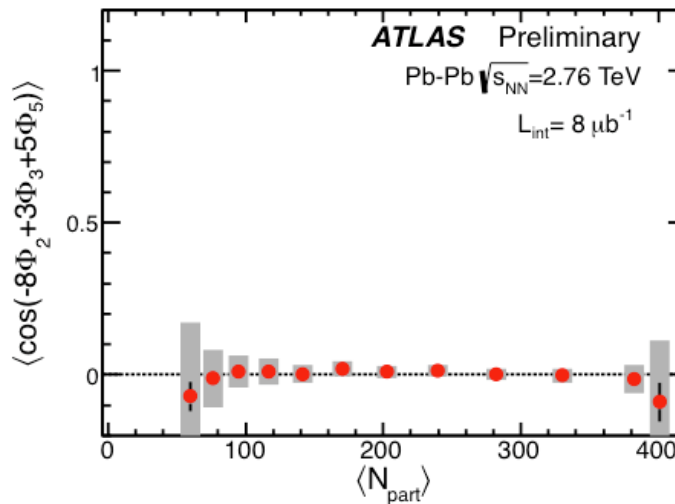


Three plane correlations

$$\langle \cos(2\Phi_2 + 3\Phi_3 - 5\Phi_5) \rangle$$



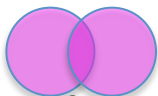
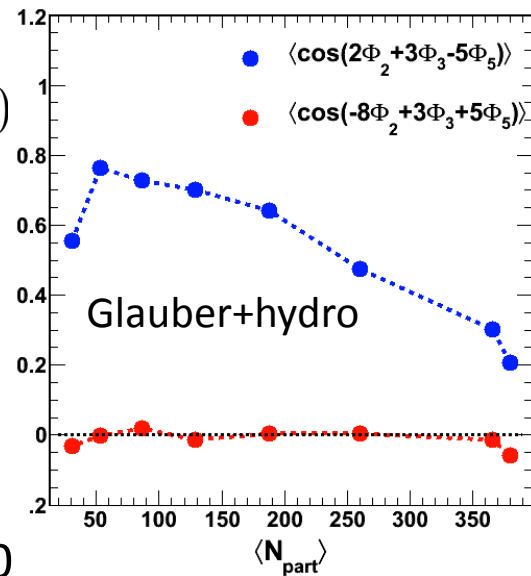
$$\langle \cos(-8\Phi_2 + 3\Phi_3 + 5\Phi_5) \rangle$$



Glauber geometry does not match the correlation

Hydro evolution qualitatively reproduces the centrality dependence

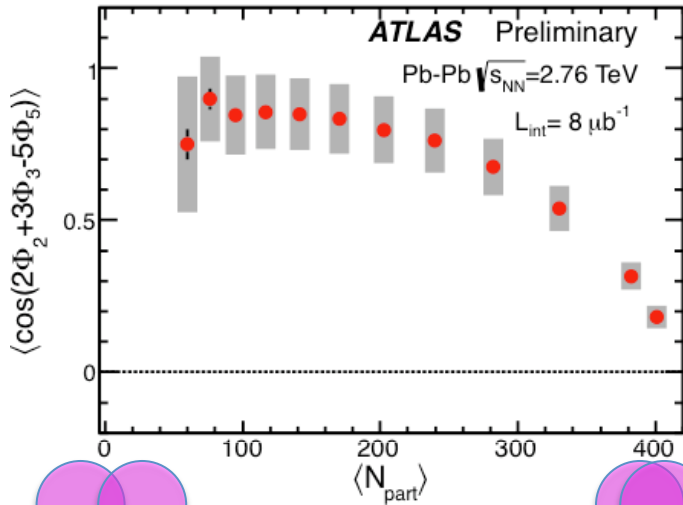
Glauber+hydro
arXiv:1208.1200



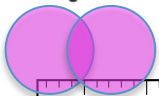
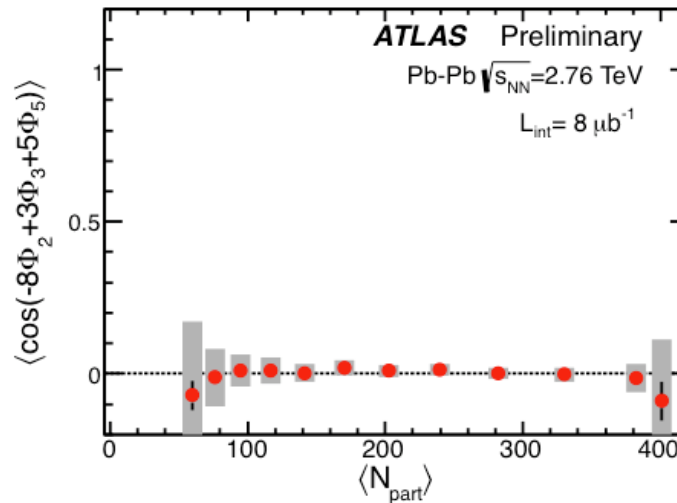
25 Sep 2012

Three plane correlations

$$\langle \cos(2\Phi_2 + 3\Phi_3 - 5\Phi_5) \rangle$$



$$\langle \cos(-8\Phi_2 + 3\Phi_3 + 5\Phi_5) \rangle$$



Glauber geometry does not

$$2\Phi_2 + 3\Phi_3 - 5\Phi_5 = 3(\Phi_3 - \Phi_2) - 5(\Phi_5 - \Phi_2)$$

$$-8\Phi_2 + 3\Phi_3 + 5\Phi_5 = 3(\Phi_3 - \Phi_2) + 5(\Phi_5 - \Phi_2)$$

$$\langle \sin 3(\Phi_3 - \Phi_2) \sin 5(\Phi_5 - \Phi_2) \rangle = \frac{1}{2} (\langle \cos 2\Phi_2 + 3\Phi_3 - 5\Phi_5 \rangle - \langle \cos -8\Phi_2 + 3\Phi_3 + 5\Phi_5 \rangle)$$

$$\langle \cos 3(\Phi_3 - \Phi_2) \cos 5(\Phi_5 - \Phi_2) \rangle = \frac{1}{2} (\langle \cos 2\Phi_2 + 3\Phi_3 - 5\Phi_5 \rangle + \langle \cos -8\Phi_2 + 3\Phi_3 + 5\Phi_5 \rangle)$$



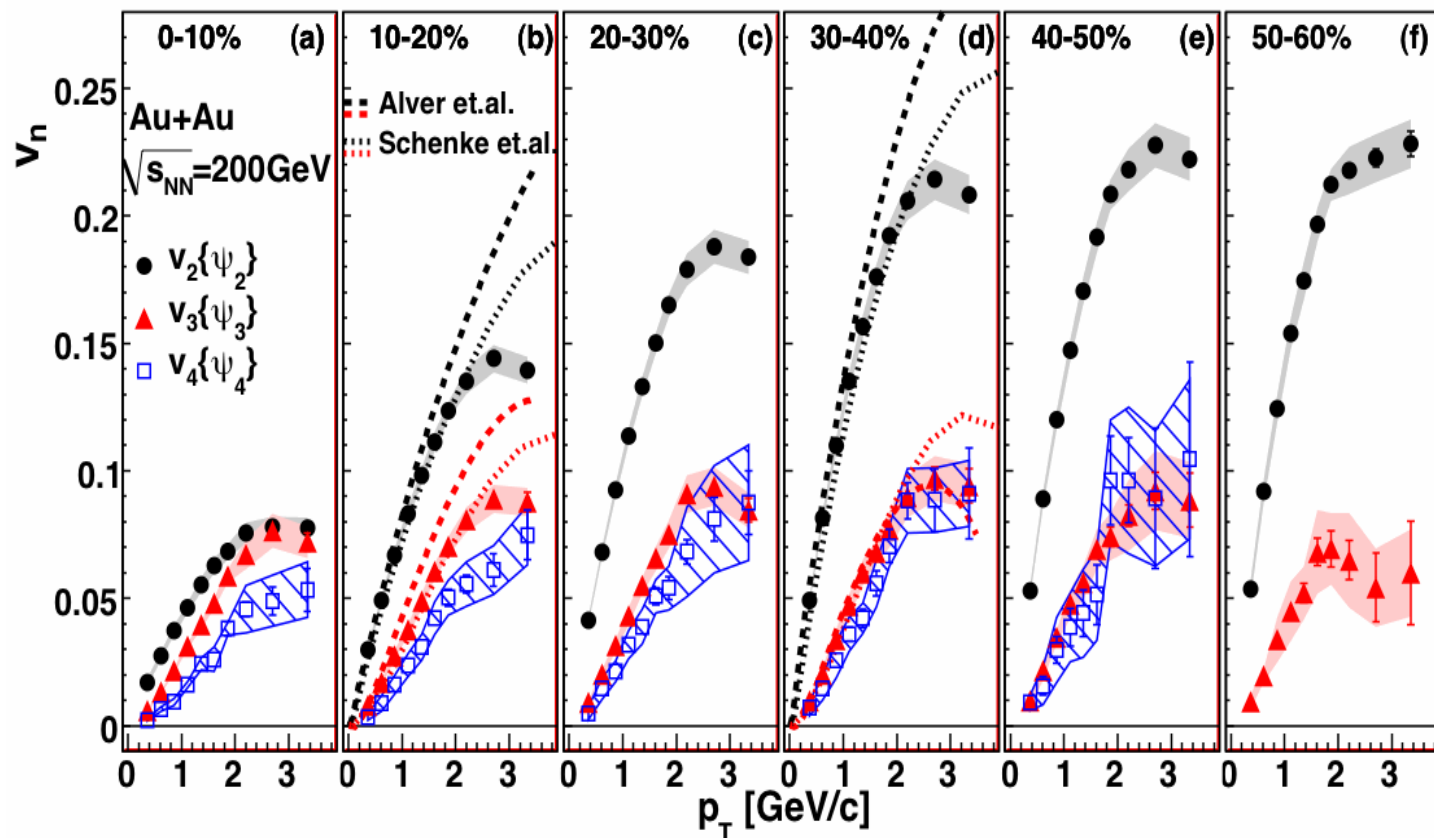
$\langle N_{part} \rangle$



arXIV:1208.1200

$\langle N_{part} \rangle$

p_T differential v_n at RHIC



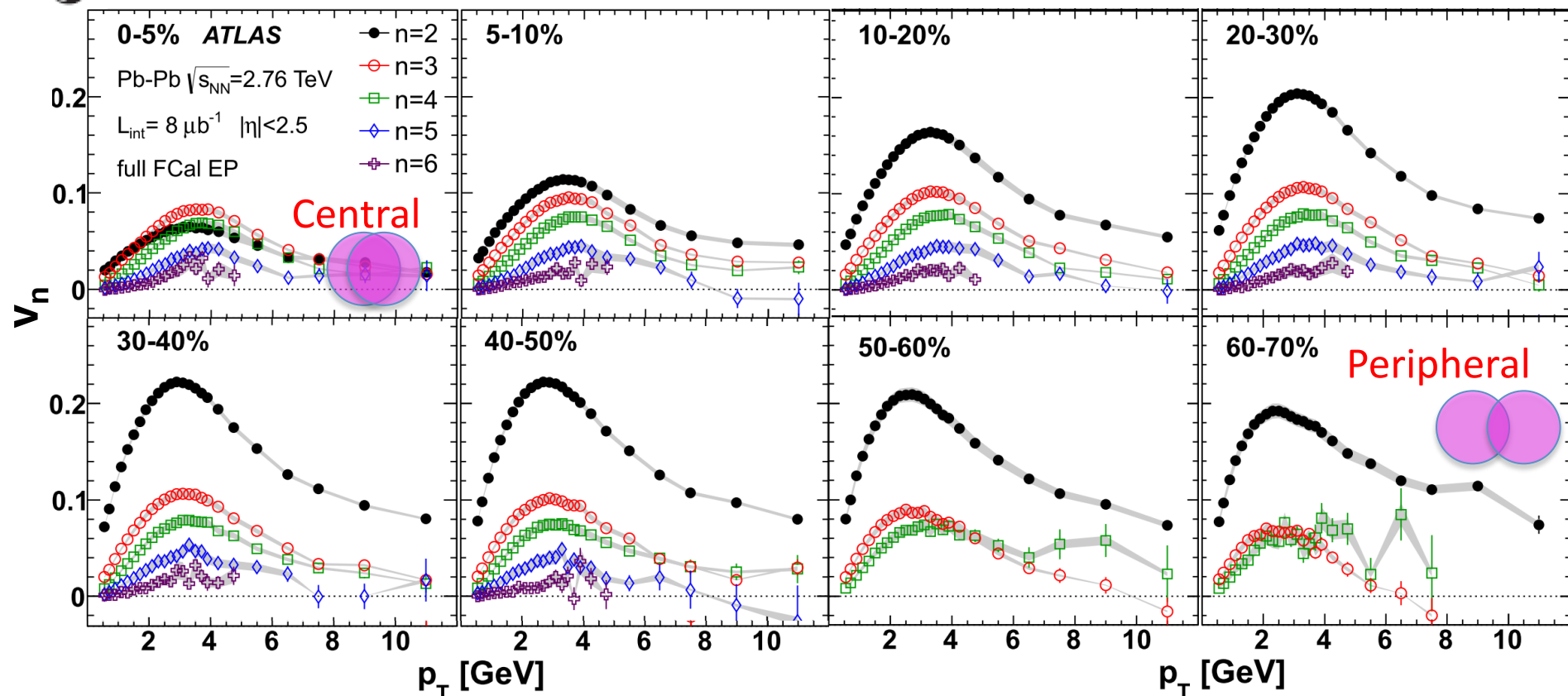
PRL.107.252301

Charged hadron v_n : $|\eta| < 0.35$
 Event plane Φ_n : $|\eta| = 1.0 \sim 2.8$

- ✧ v_3 & v_4 comparable to v_2 in most central
- ✧ Stronger centrality dependence of v_2

p_T differential v_n at LHC

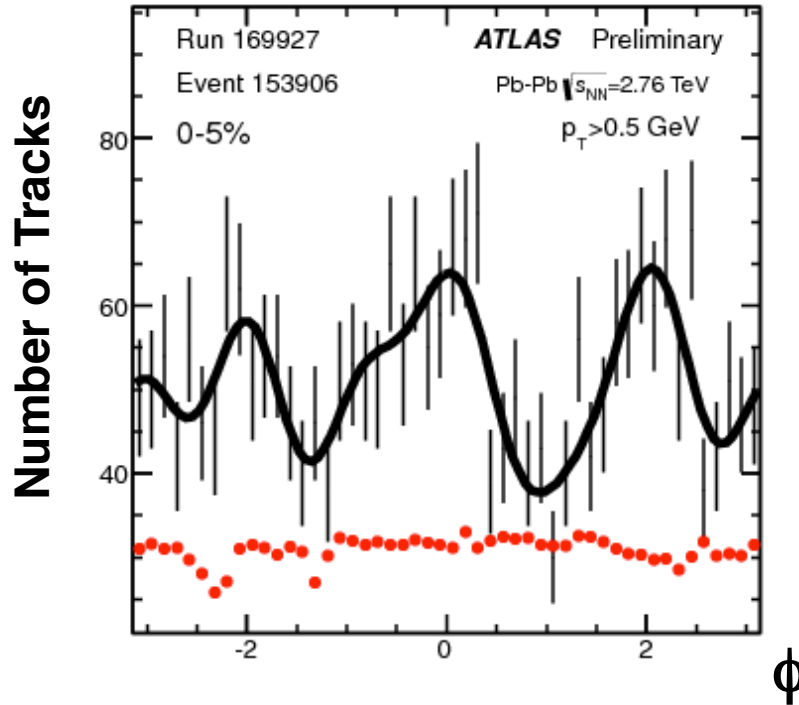
ATLAS, Phys. Rev. C 86, 014907 (2012)



- ✧ Significant v_n up to $n=6$
- ✧ In most central collisions(0-5%): v_3 & $v_4 > v_2$
- ✧ Stronger centrality dependence of v_2

Event-by-Event v_n

Singles



✧ Event by Event single particle distributions

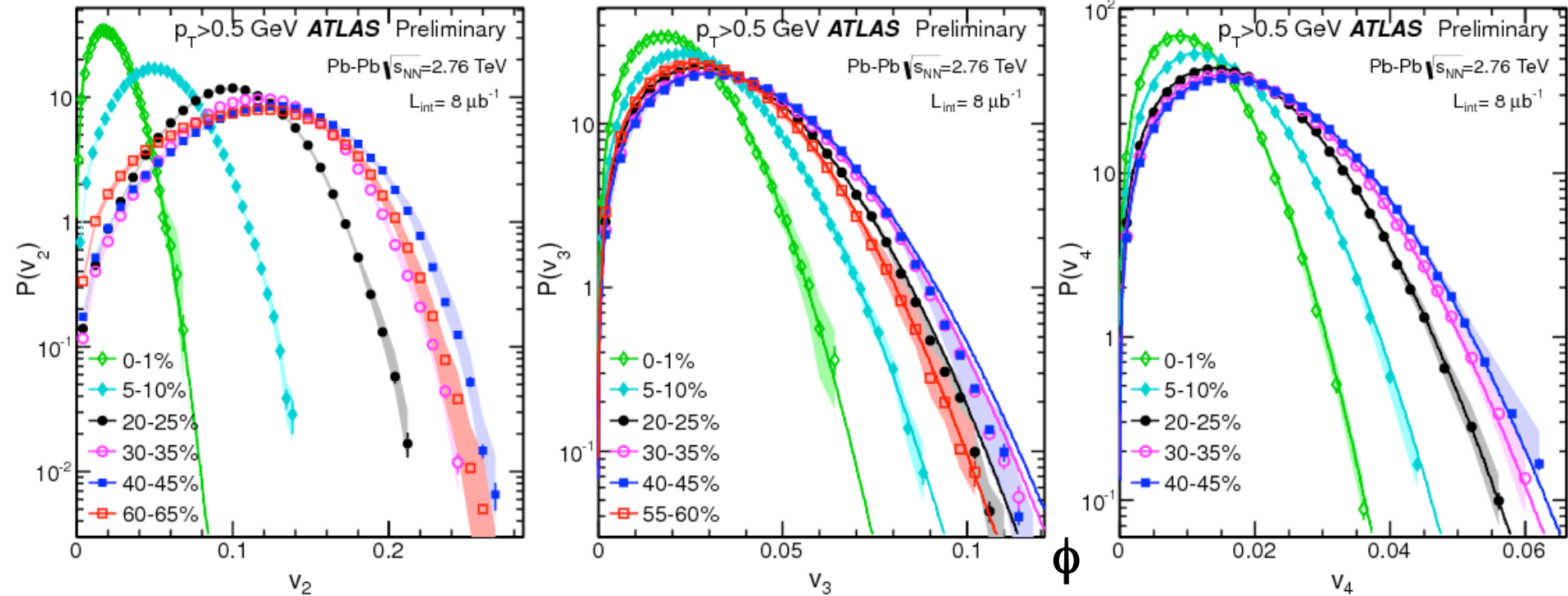
$$\frac{dN}{d\phi} \propto 1 + 2 \sum_{n=1}^{\infty} v_n^{\text{obs}} \cos n(\phi - \Psi_n^{\text{obs}}) = 1 + 2 \sum_{n=1}^{\infty} (v_{n,x}^{\text{obs}} \cos n\phi + v_{n,y}^{\text{obs}} \sin n\phi)$$

✧ Obtaining amplitude, Correction & unfolding on statistics

$$\vec{v}_n^{\text{obs}} = (v_{n,x}^{\text{obs}}, v_{n,y}^{\text{obs}})$$

✧ Provides constraints to model calculations

Event-by-Event v_n



✧ **Event by Event single particle distributions**

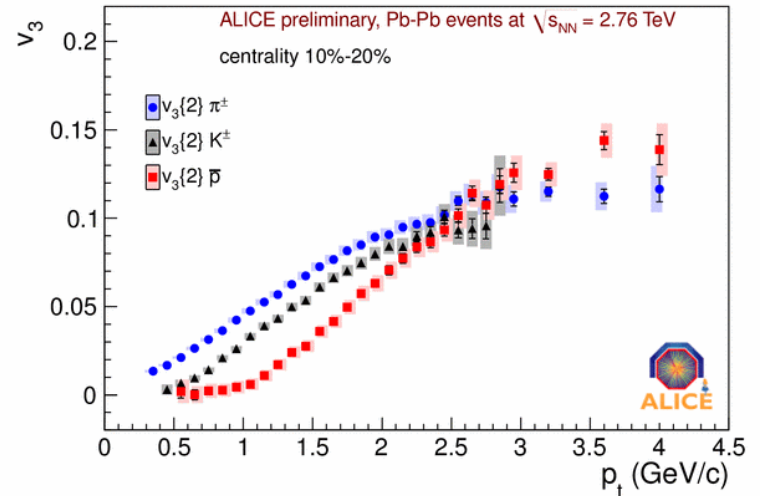
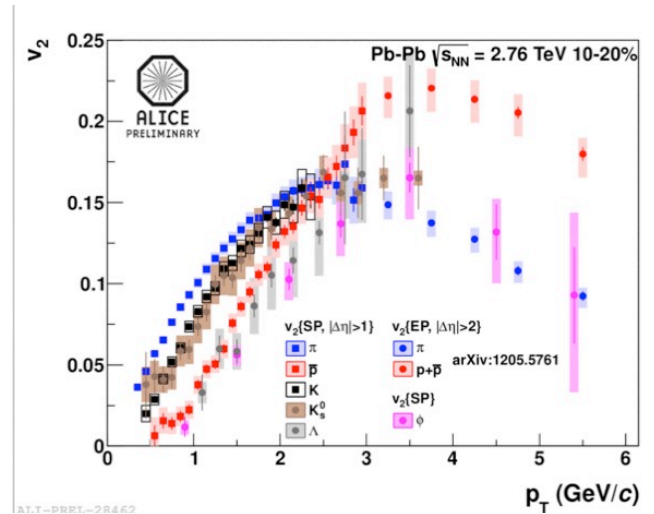
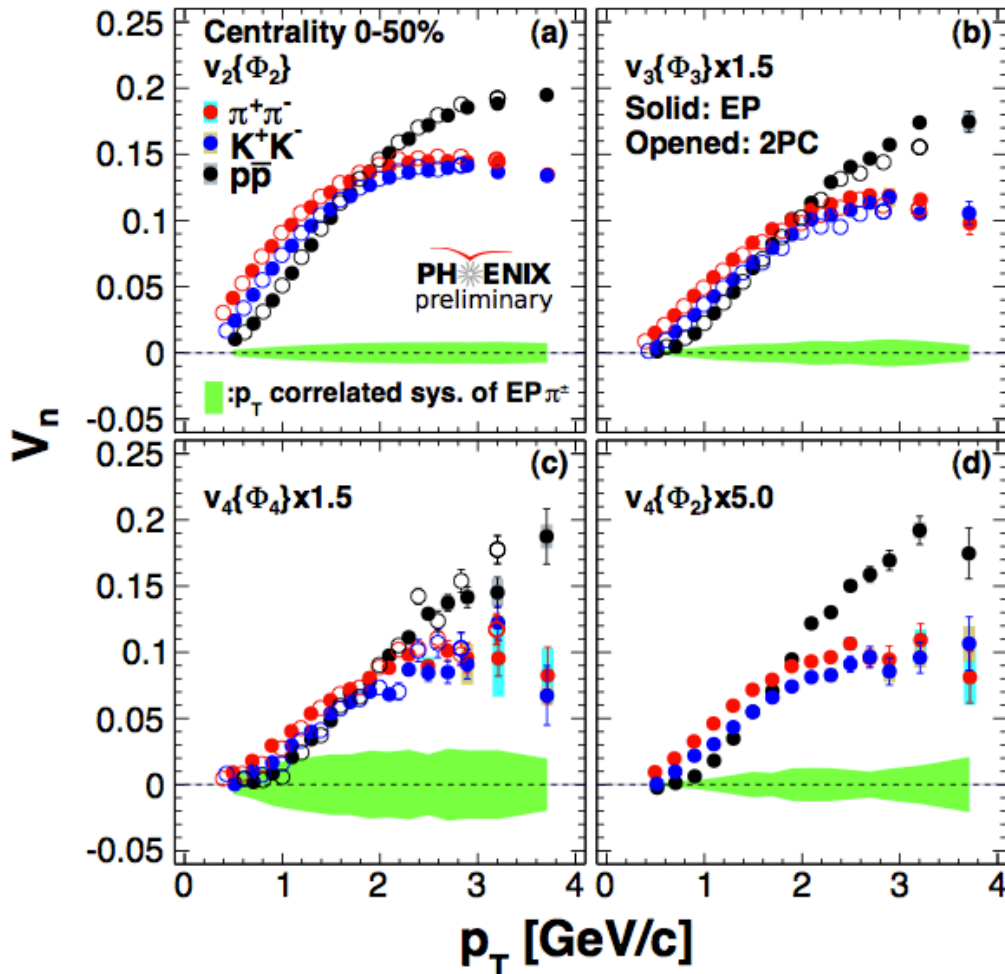
$$\frac{dN}{d\phi} \propto 1 + 2 \sum_{n=1}^{\infty} v_n^{\text{obs}} \cos n(\phi - \Psi_n^{\text{obs}}) = 1 + 2 \sum_{n=1}^{\infty} (v_{n,x}^{\text{obs}} \cos n\phi + v_{n,y}^{\text{obs}} \sin n\phi)$$

✧ **Obtaining amplitude, Correction & unfolding on statistics**

$$\vec{v}_n^{\text{obs}} = (v_{n,x}^{\text{obs}}, v_{n,y}^{\text{obs}})$$

✧ **Provides constraints to model calculations**

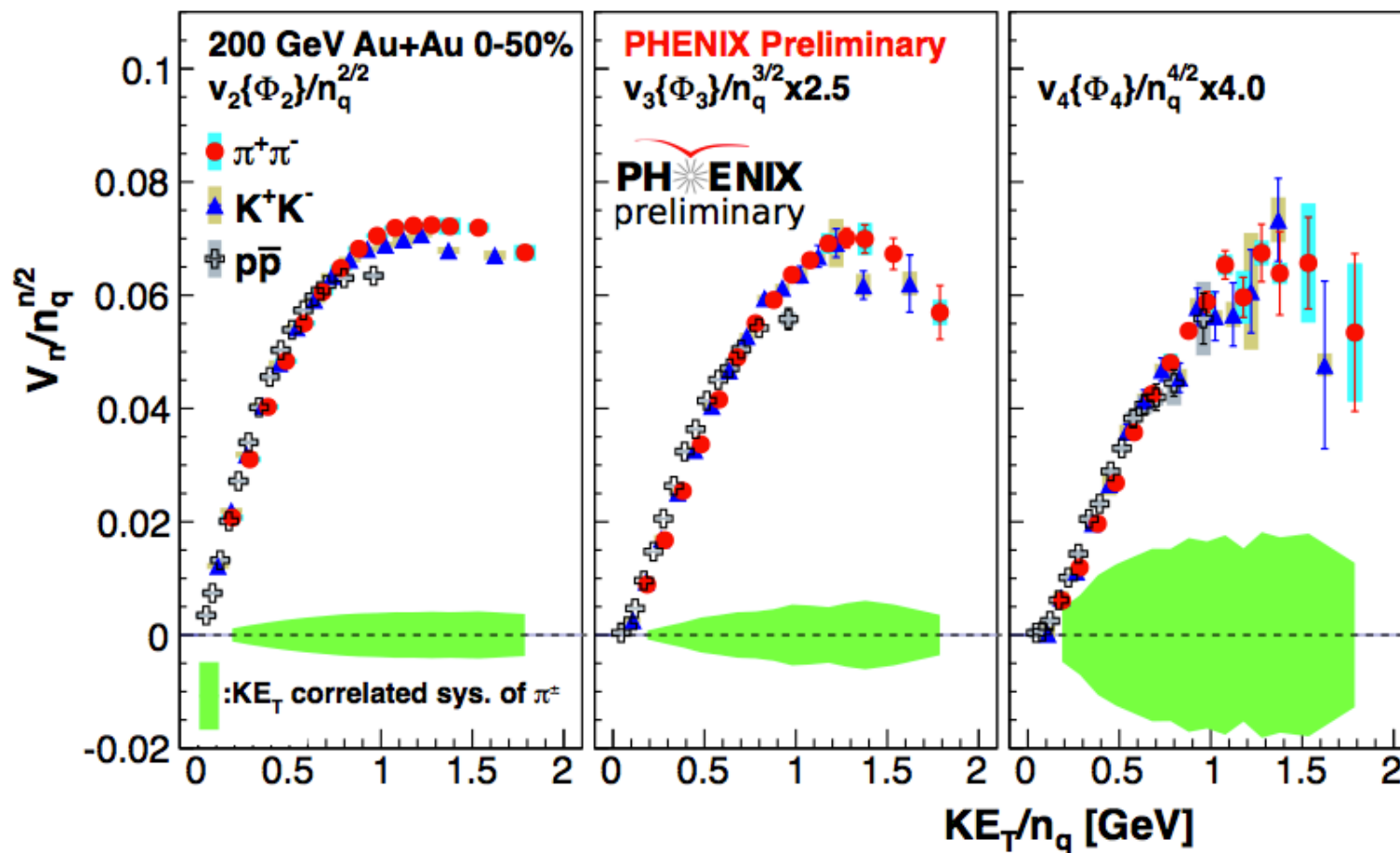
Identified particle v_n



✧ Mass ordering at low p_T

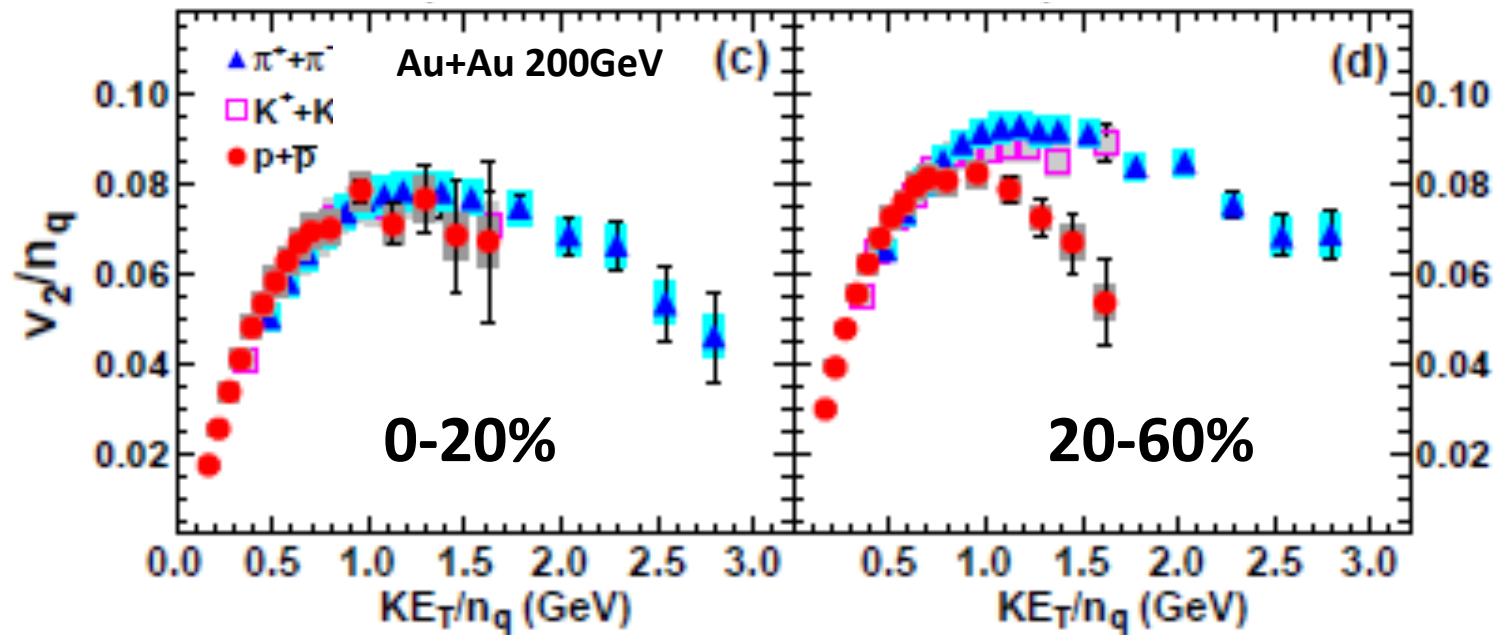
✧ Coalescence at intermediate p_T

N_q scaling of v_n



✧ N_q scaling up to $KE_T/n_q = 0.7$ GeV for v_2 , v_3 , and v_4

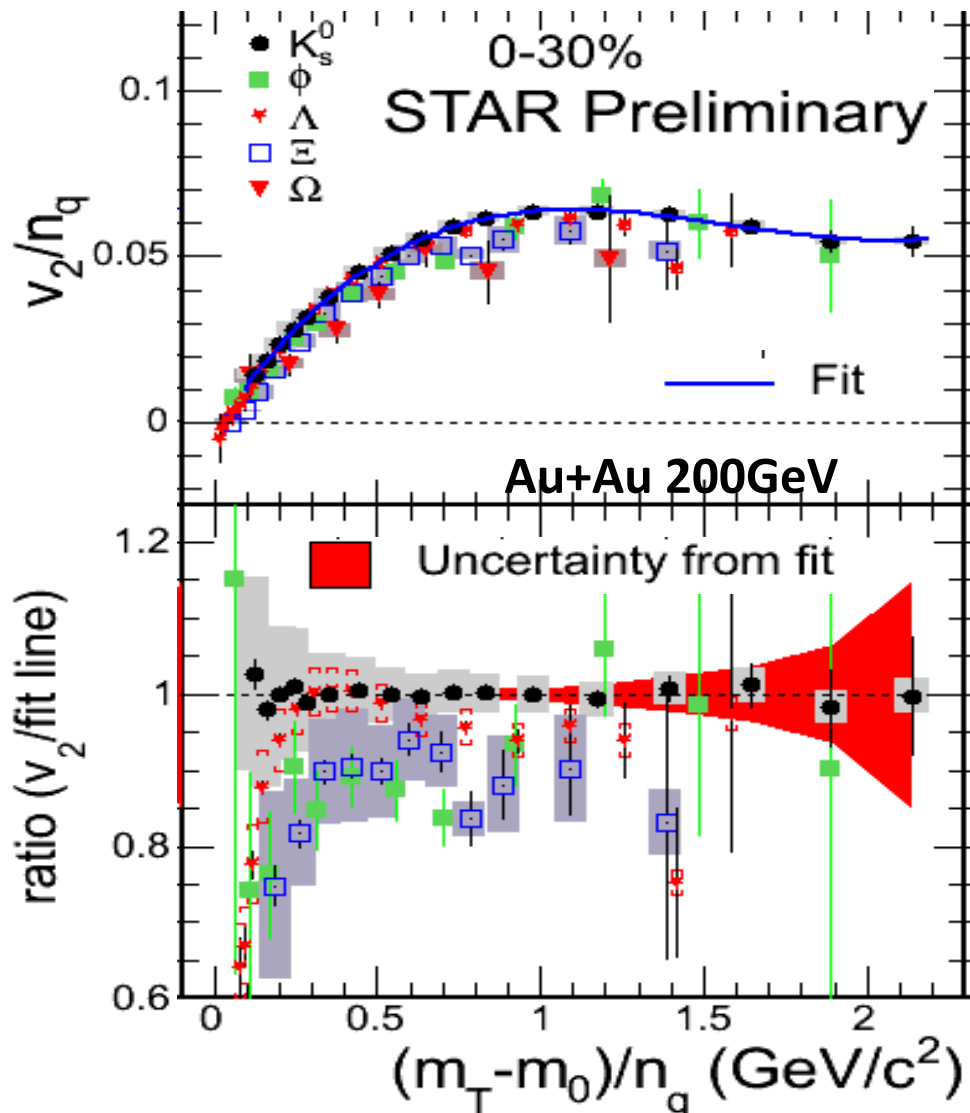
Break of N_q scaling of v_2 at high p_T



PHENIX PRC 85, 064914 (2012)

- ✧ In the 0-20%, scaling is still roughly kept.
- ✧ In 20-60% n_q scaling is broken at $KE_T > 0.7$ GeV.
- ✧ Different mechanisms for pion and proton production at intermediate p_T for different centralities

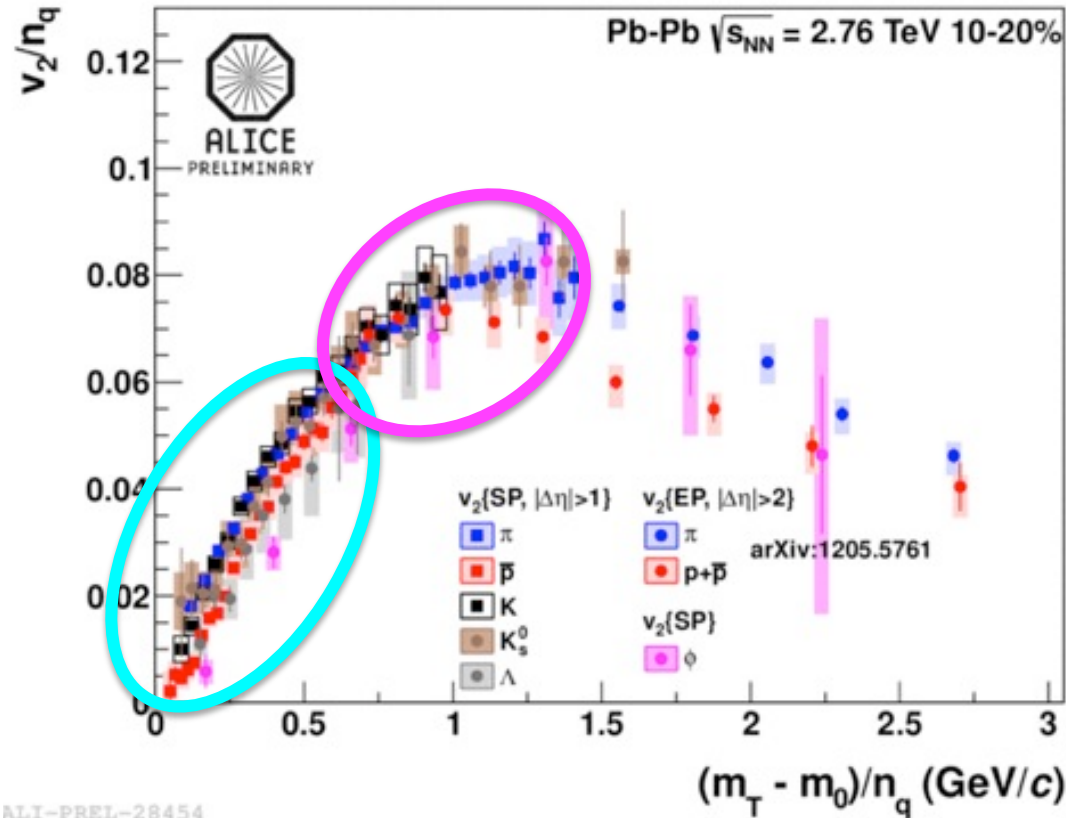
N_q scaling of strange hadron v_2



✧ K_s^0 follows scaling curve of π , K, & P

✧ Multi-strangeness hadrons deviate from K_s^0

N_q scaling of v_2 at LHC

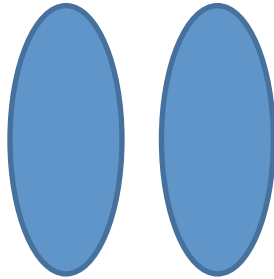


- ✧ P, Λ, ϕ deviate from π, K at low p_T
 - Might be due to stronger radial flow at LHC than RHIC
 - Realistic parameter describes radial flow effects to hadrons
- ✧ N_q scaling survives at intermediate p_T

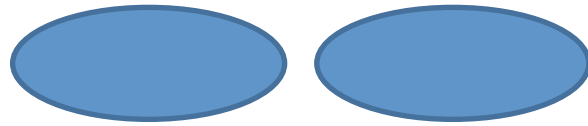
Geometry controlled collision systems

4A, Huang

U+U collisions

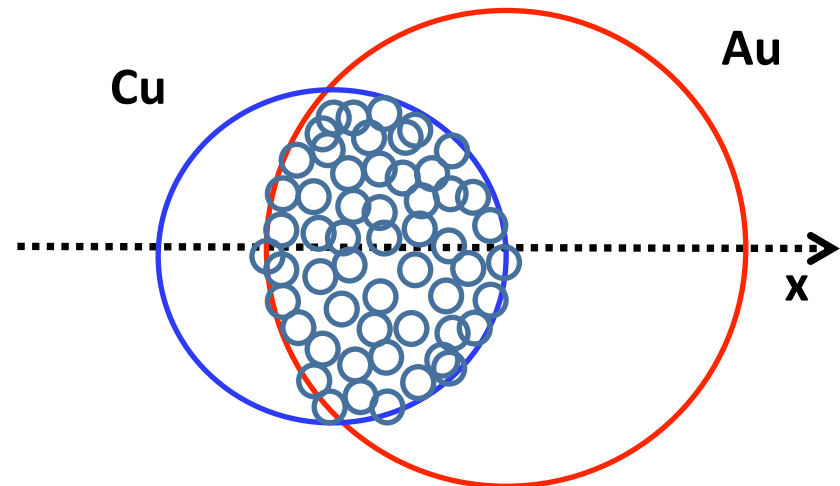


Body-body



Tip-tip

Cu+Au collisions

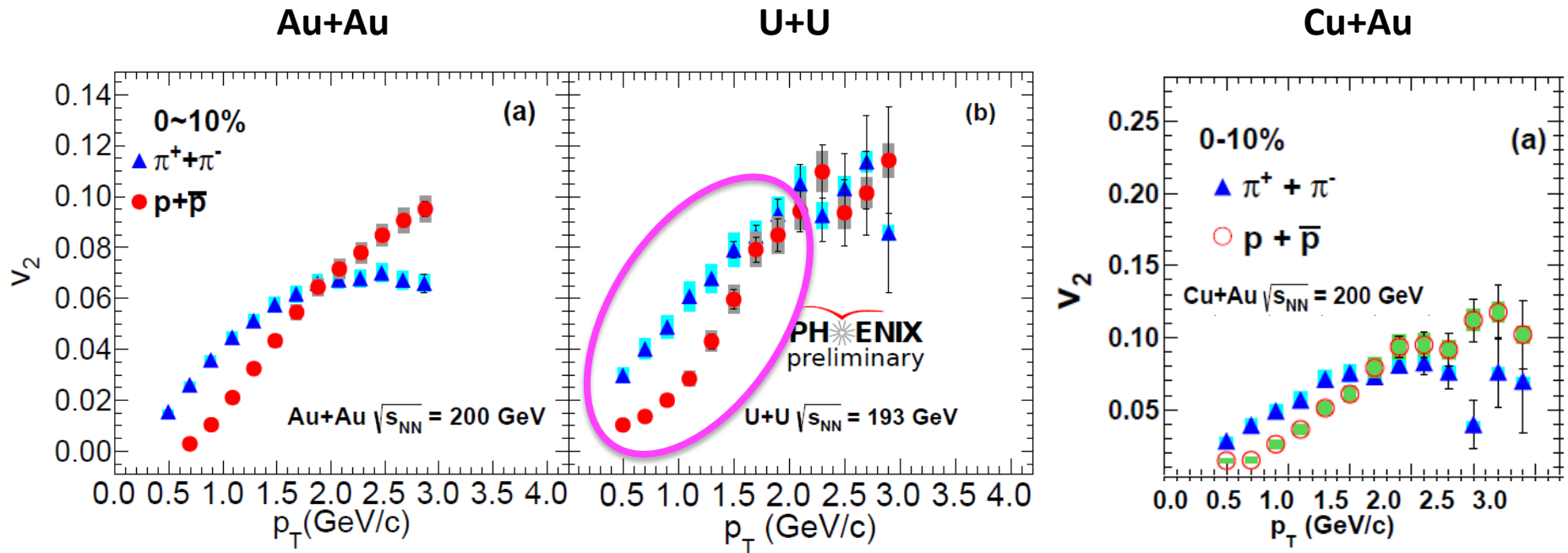


✧ **Various collision geometry**

✧ **The geometry separation in progress**

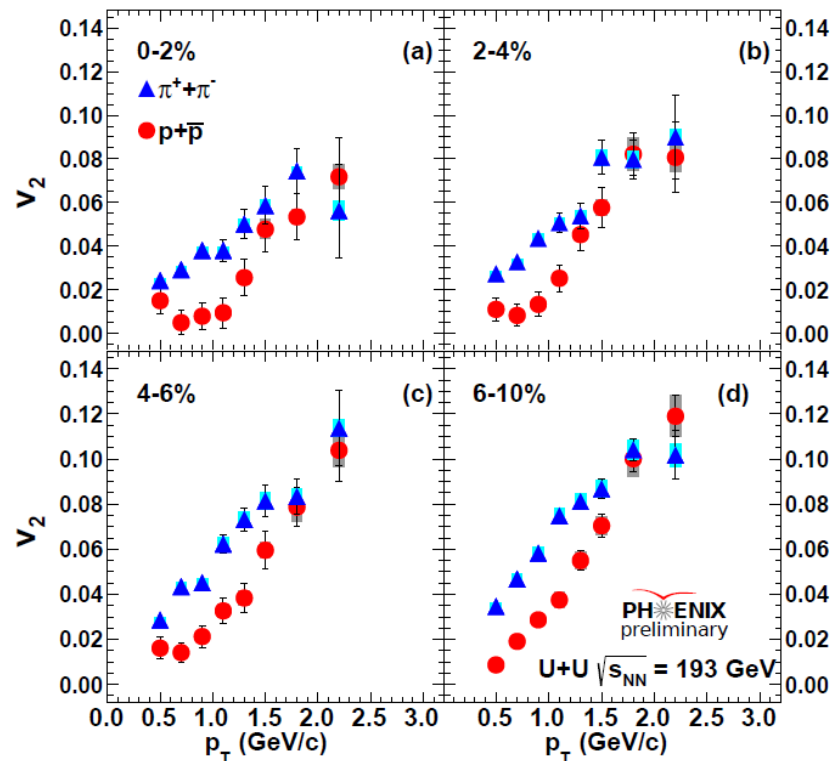
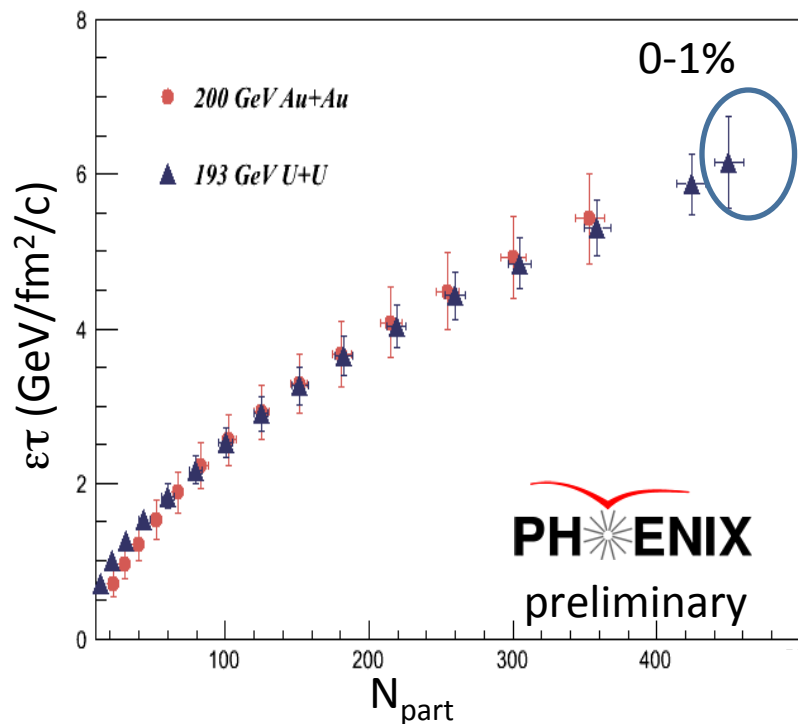
- **This time only centrality is selected**

Stronger mass ordering in central U+U collisions



✧ Not seen in other centrality and collision systems

π & p v_2 in 0-6% central U + U collision



✧ From 0-10% Au+Au to 0-1% U+U collisions

✧ $\varepsilon\tau$ increase about 20%

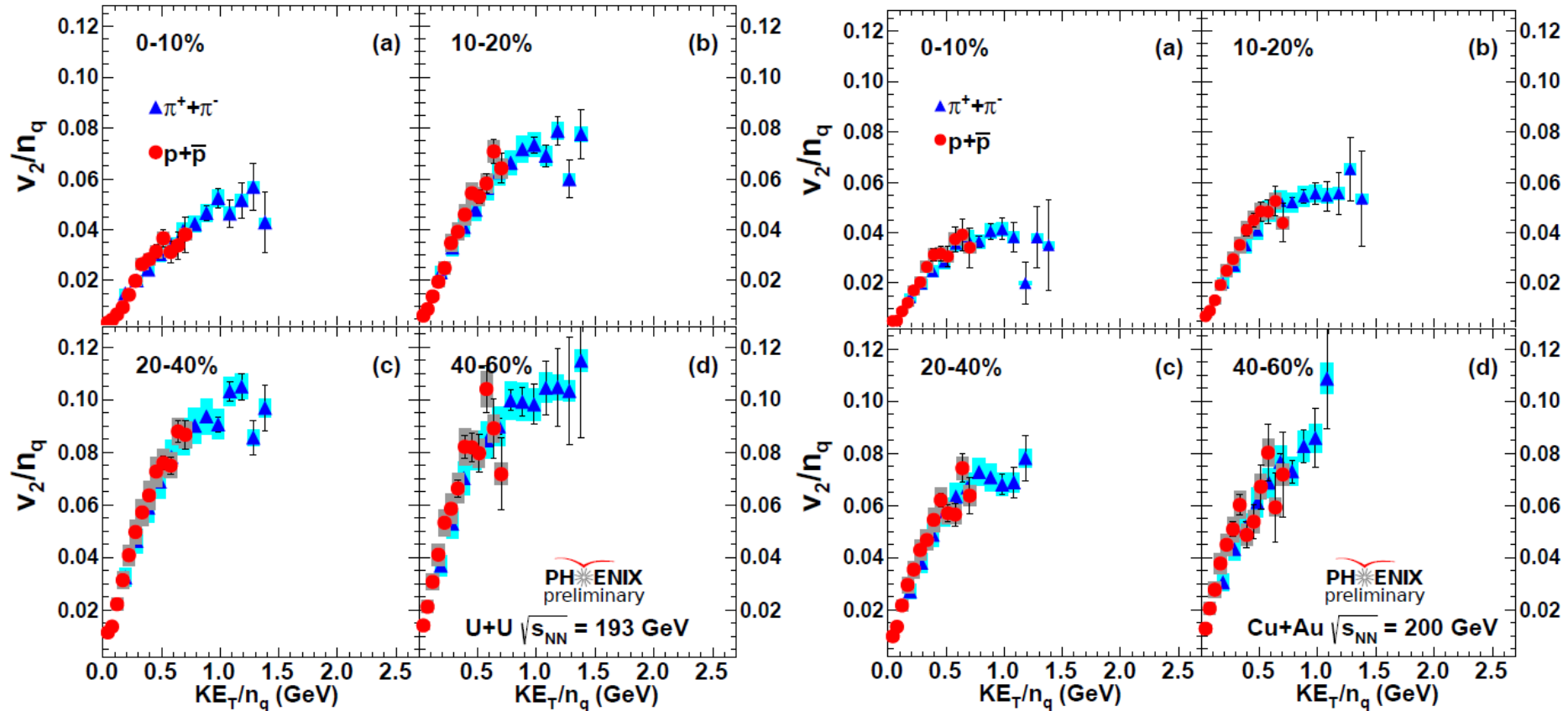
✧ Strong mass ordering in 0-6% centrality despite of relatively small increase of $\varepsilon\tau$.

✧ Radial flow or collision geometry?

N_q scaling in U+U and Cu+Au collisions

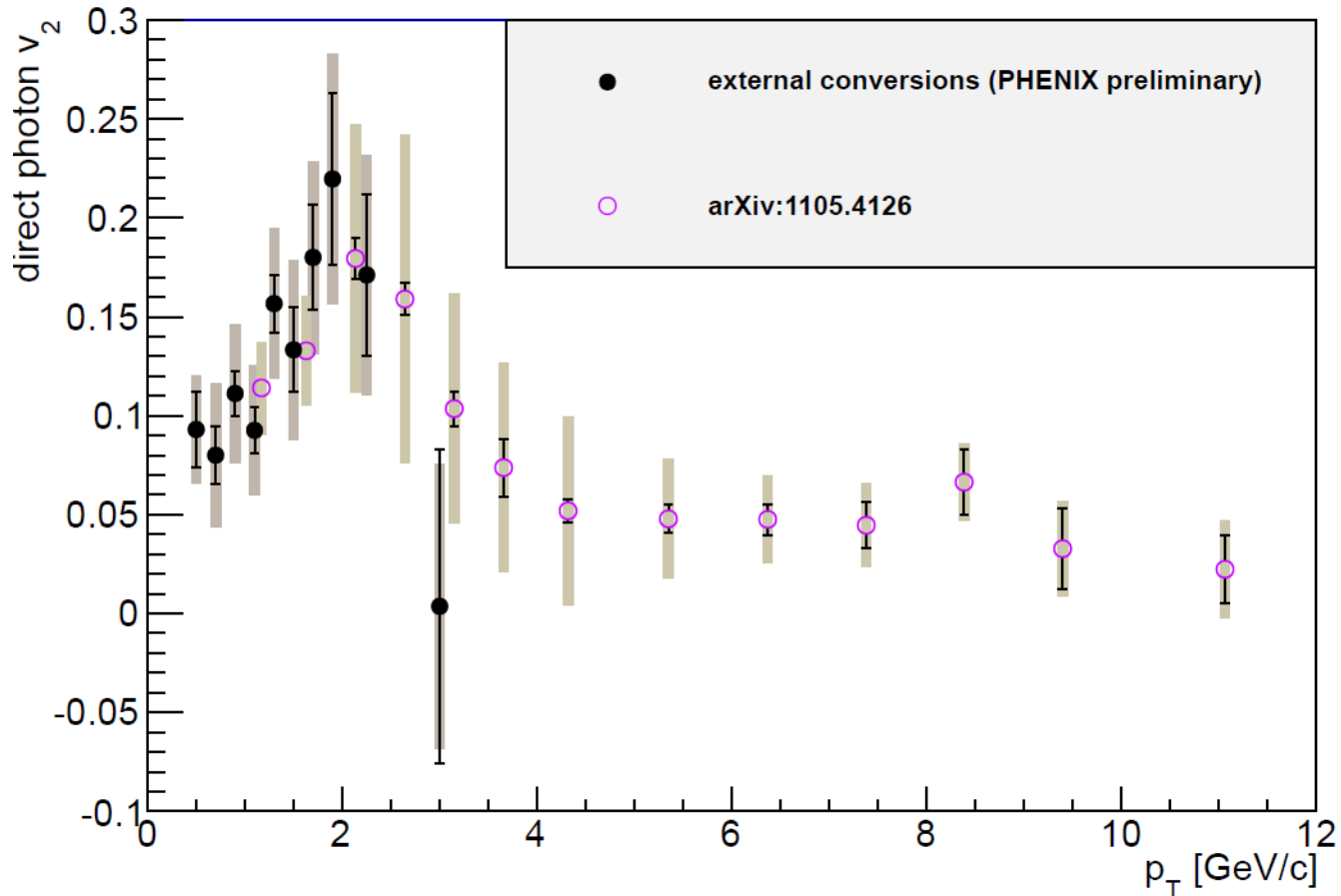
U+U

Cu+Au



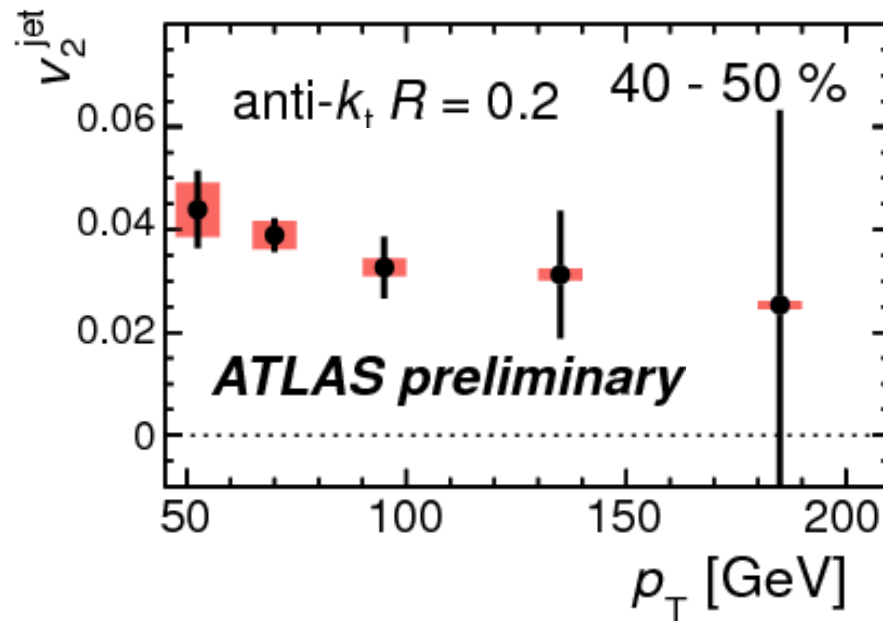
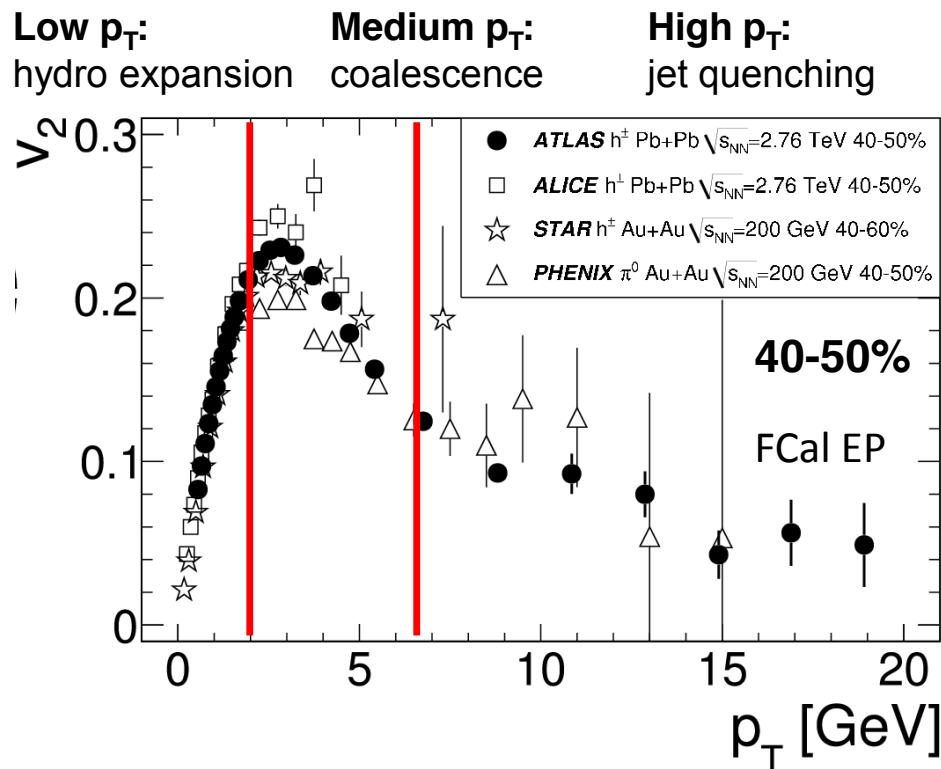
✧ N_q scaling works for U+U and Cu+Au for π , P

Direct Photon v_2



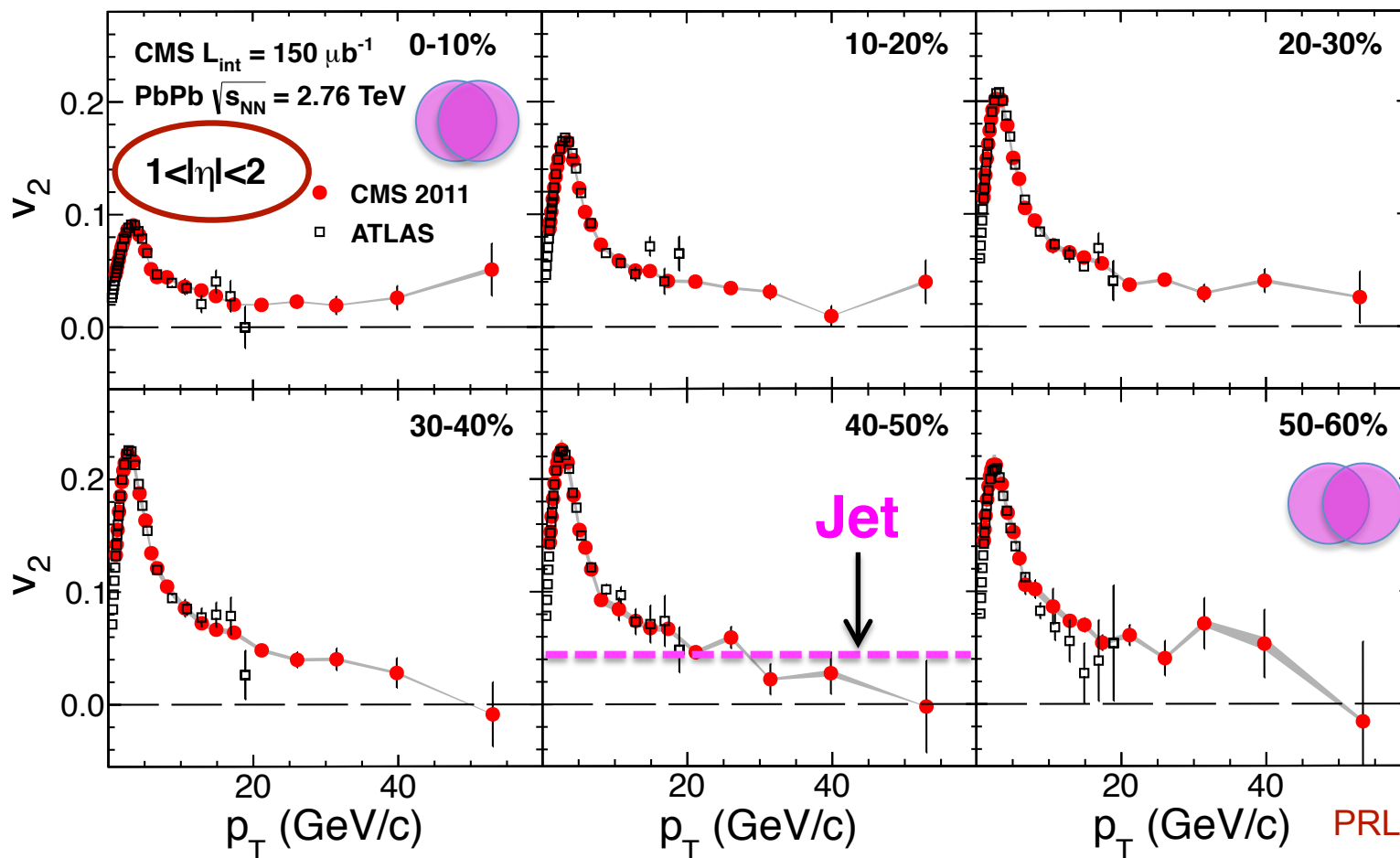
- ✧ v_2 down to 0.5 GeV via external conversion di-electron pairs
- ✧ Consistency check with previous measurements via photon
- ✧ Agreement up to 2 GeV, None-zero v_2 is conclusive

High p_T single hadron and jet v_2



- ✧ None-zero v_2 of single hadrons at high p_T
- ✧ Jet v_2 is qualitatively consistent with hadron v_2
 - Path length dependence of parton energy loss

Very high p_T v_2 via 2PC

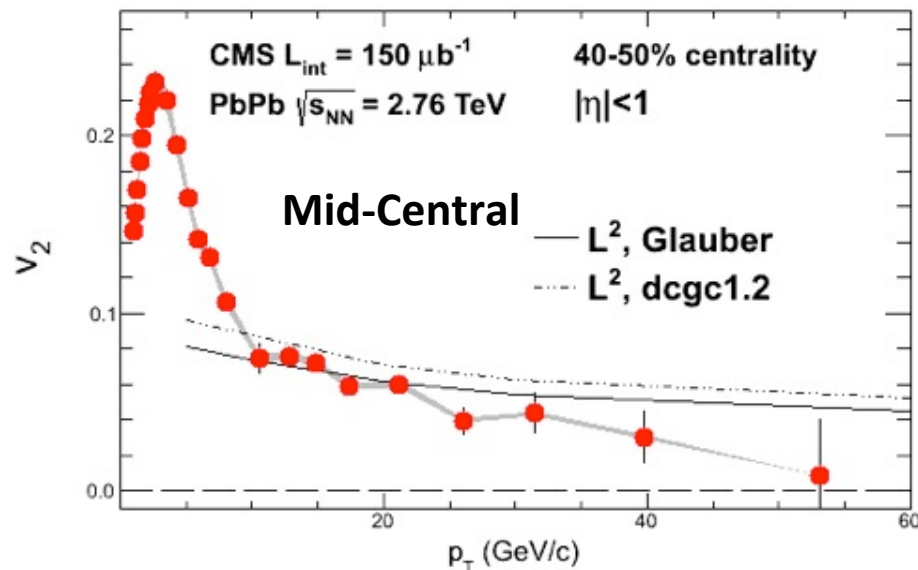
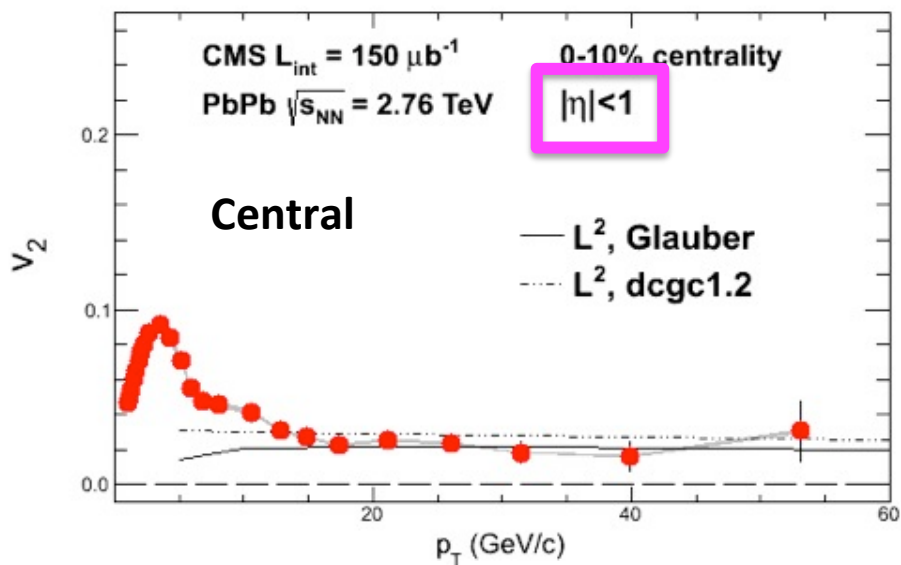


✧ None zero v_2 up to p_T 40 GeV/c

✧ Comparable to jet v_2 above 20 GeV/c

Theory Comparison

Data: PRL 109.022301(2012)



Theory: B.Betz,M.Gyulassy;arXiv:1201.0281

- Data can constrain different theoretical scenarios
- ✧ RHIC data supports L^3 dependence

Two-particle correlations

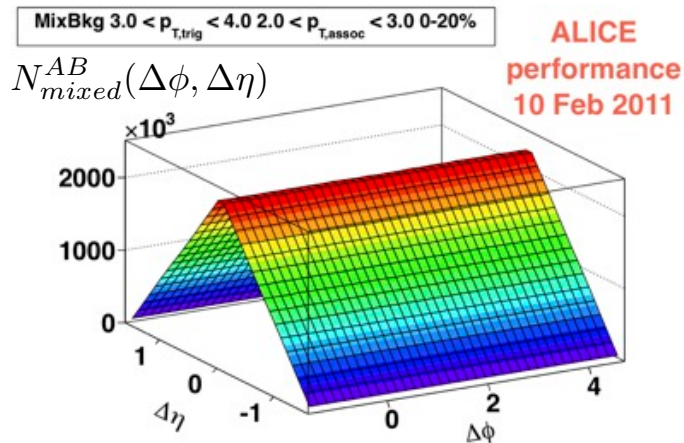
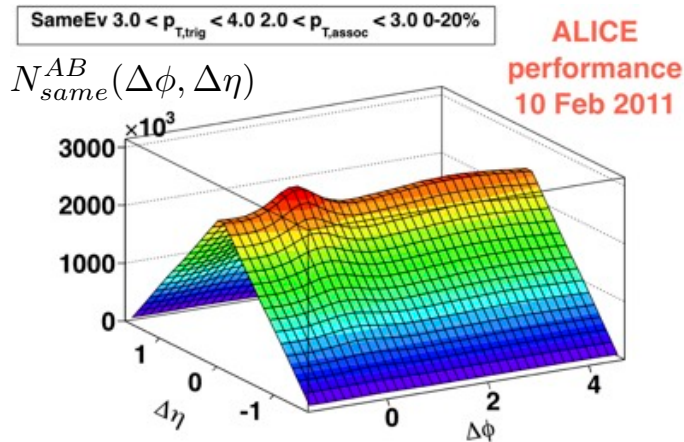
✧ **Correlations with v_n background subtractions**

✧ **Correlations with respect to Ψ_2 & Ψ_3**

Two-particle correlations

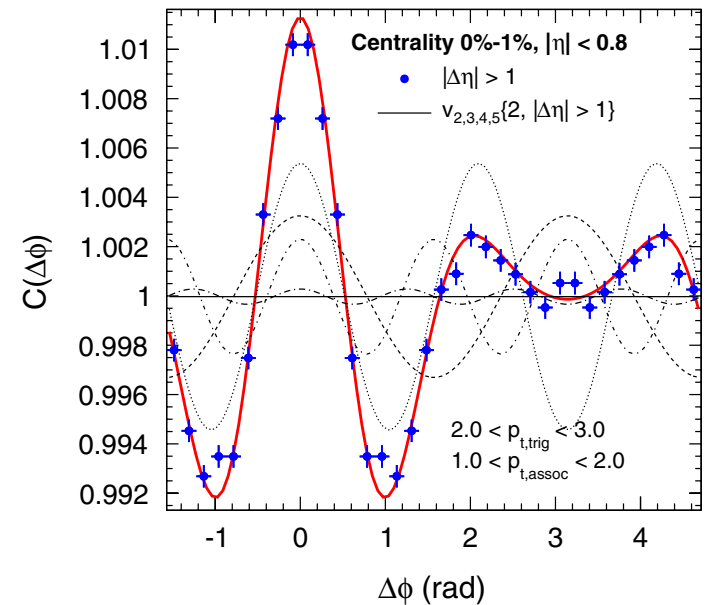
Pair distributions in real & mixed events

$$\Delta\phi = \phi^a - \phi^t, \Delta\eta = \eta^a - \eta^t$$



Correlation functions

$$C(\Delta\phi) \equiv \frac{N_{\text{mixed}}}{N_{\text{real}}} \cdot \frac{N_{\text{real}}/d\Delta\phi}{N_{\text{mixed}}/d\Delta\phi}$$



Flow backgrounds in correlations

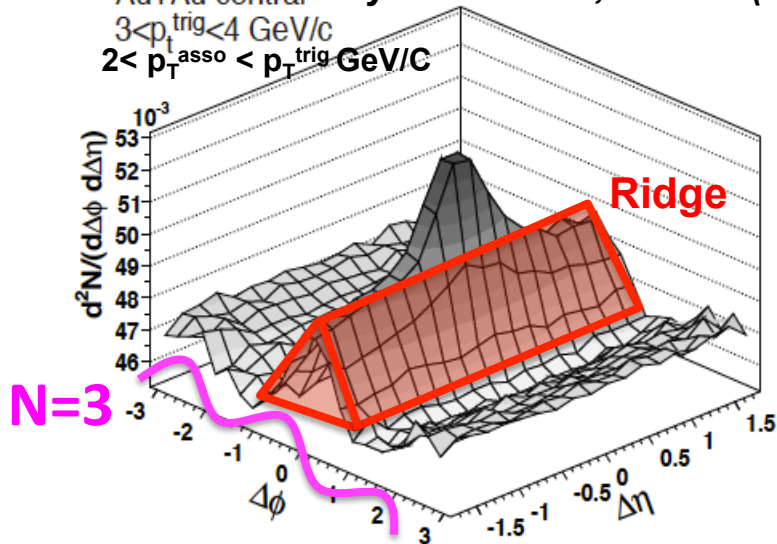
$$F(\Delta\phi) = b_0 \left[1 + \sum_{n=1} 2v_n^t v_n^a \cos(n\Delta\phi) \right]$$

Motivations

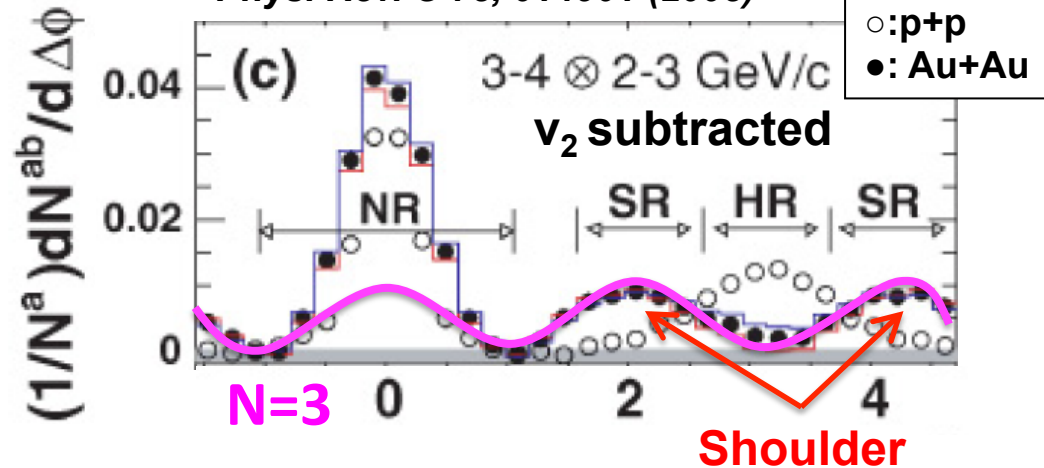
Au+Au central *Phys. Rev. C* 80, 064912 (2009)

$3 < p_T^{\text{trig}} < 4 \text{ GeV}/c$

$2 < p_T^{\text{asso}} < p_T^{\text{trig}} \text{ GeV}/c$



Phys. Rev. C 78, 014901 (2008)

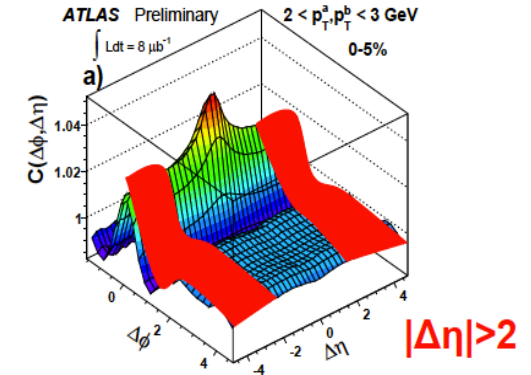
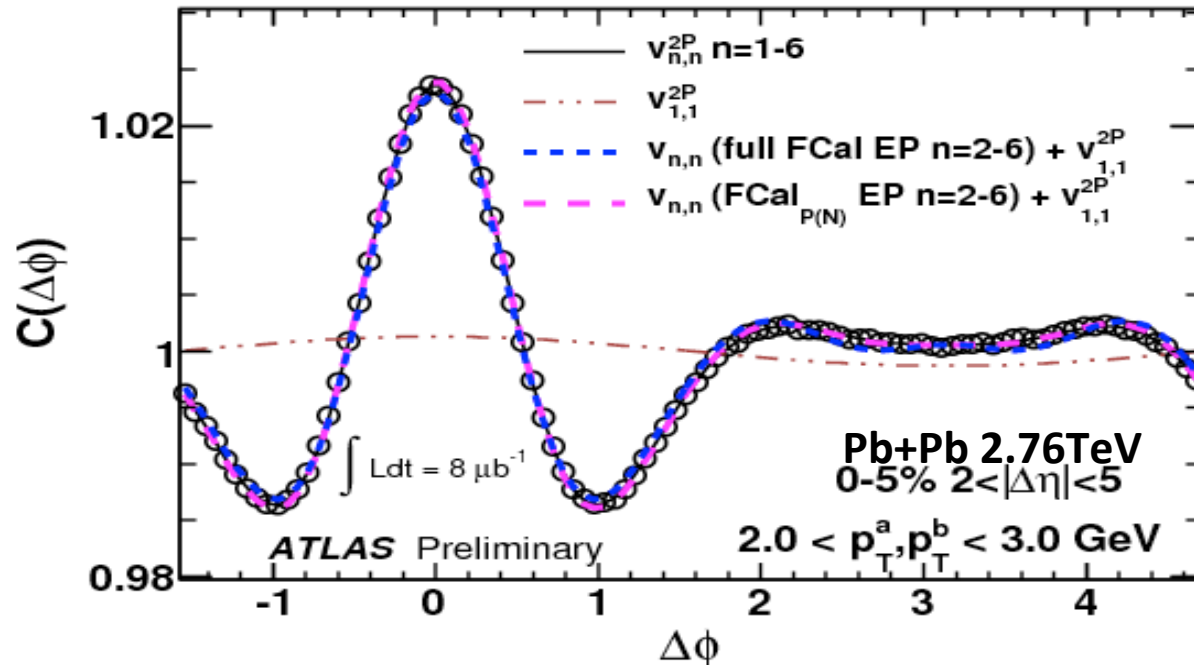


- ✧ Dissect interplay of hard-scattered partons and medium
- ✧ Definitive answer what remains after v_n subtractions
 - Whether Ridge and shoulder survives?
- ✧ Test path length dependence of parton energy loss
 - Correlations with respect to event planes

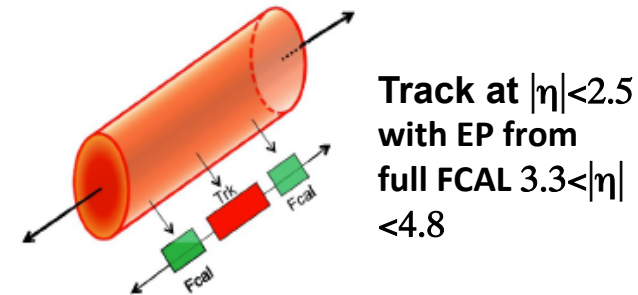
Correlations with large $\Delta\eta$ gap

$$C(\Delta\phi) = b^{2P} (1 + 2v_{1,1}^{2P} \cos\Delta\phi + 2 \sum_{n=2}^6 v_n^{EP} v_n^{EP} \cos n\Delta\phi)$$

From 2PC method From EP method



v_n with EP Method

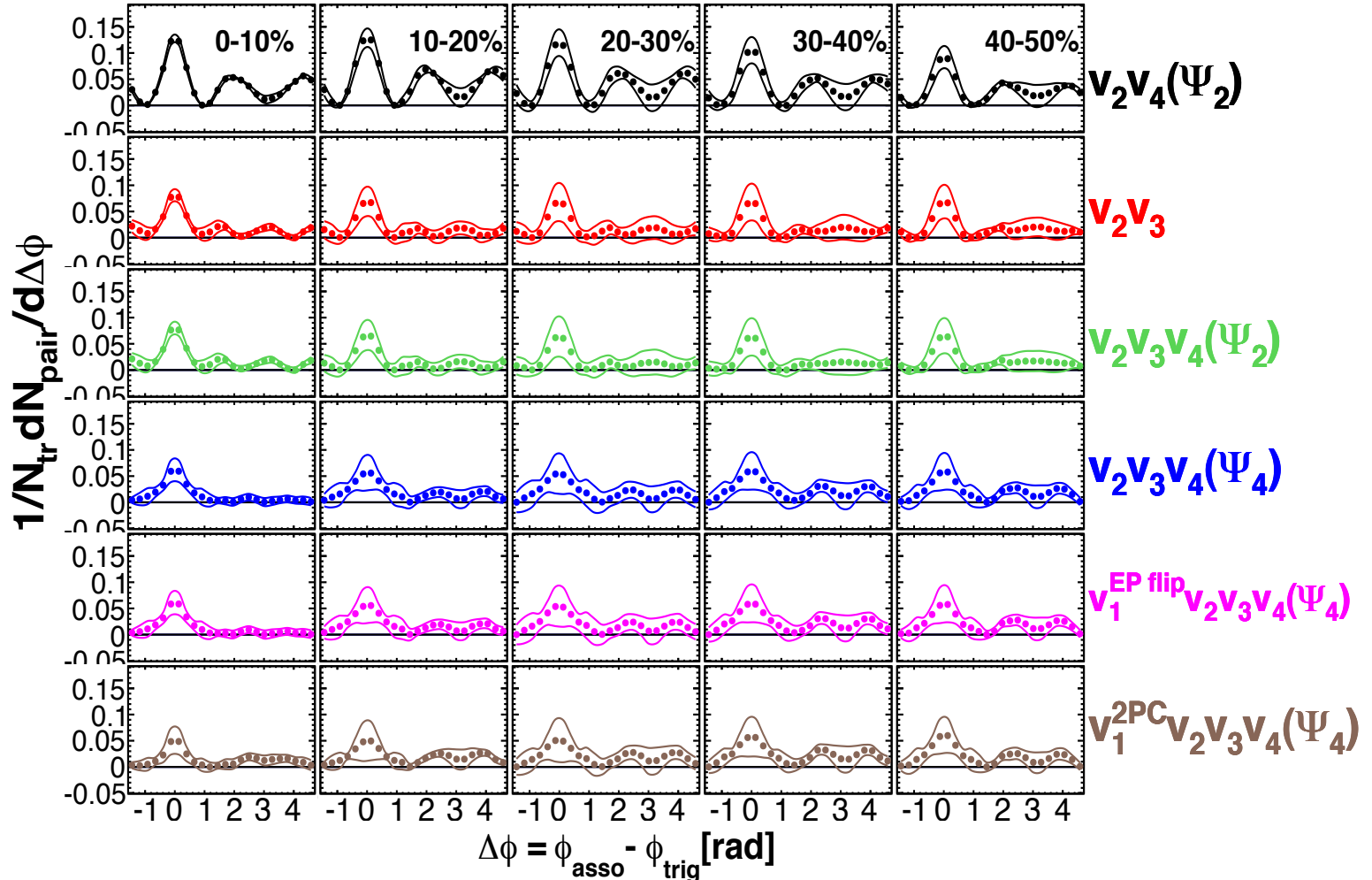


- ✧ Ridge & Shoulder well reproduced at 0-5%
- ✧ Caveat! Correlation and v_n have similar long rapidity gap, very similar information!
- ✧ Consider correlations small rapidity gap where jet contribution survives

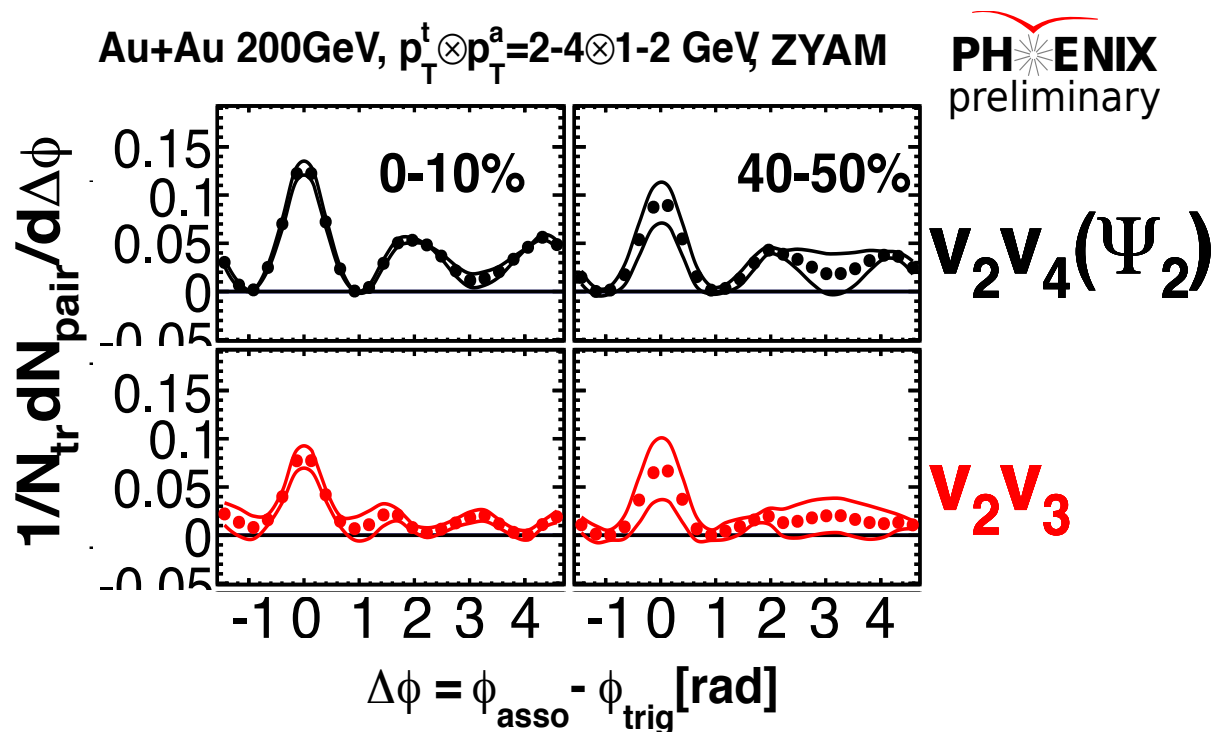
Correlations with small $\Delta\eta$ gap in wide centrality with various v_n background subtractions by ZYAM

Au+Au 200GeV, $p_T^t \otimes p_T^a = 2-4 \otimes 1-2$ GeV

PHENIX
preliminary



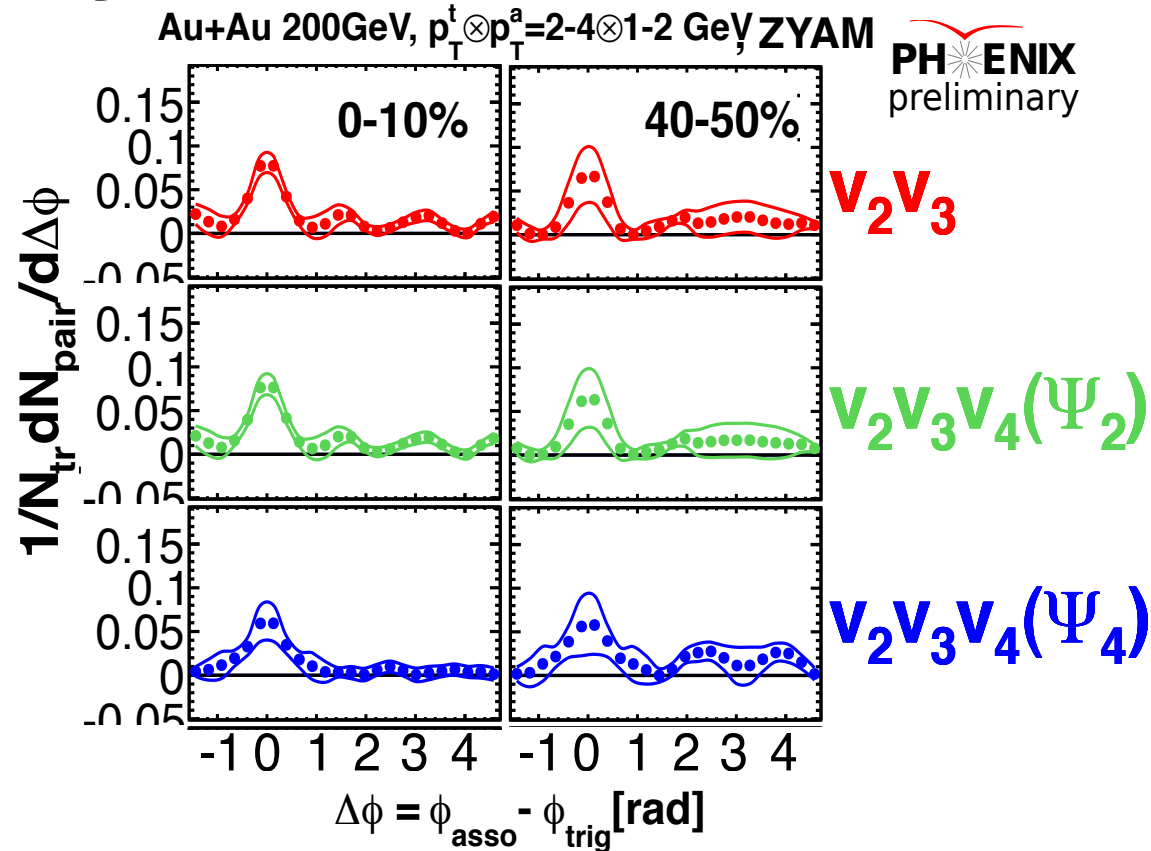
Impact of v_3 to away side residual



✧ v_3 largely reduce away-side shoulder

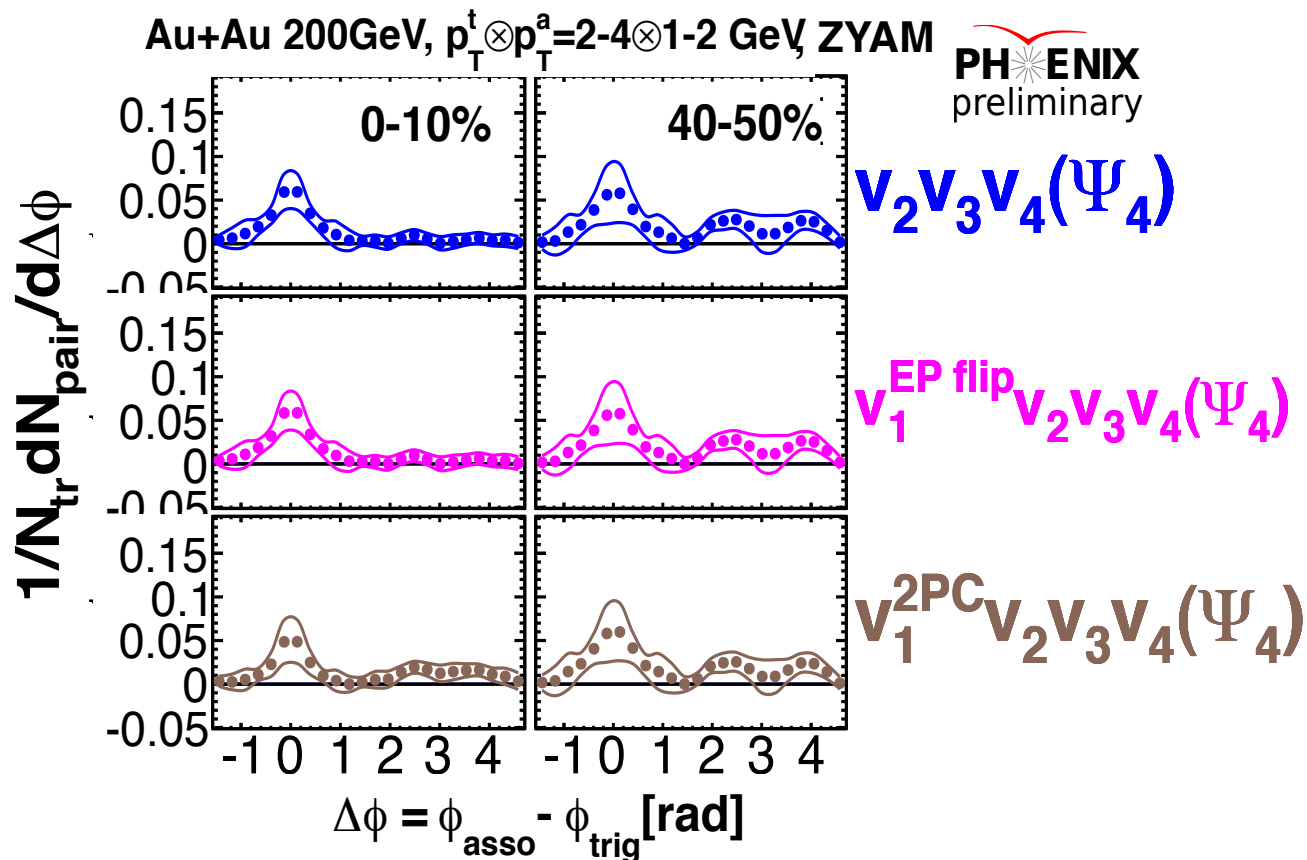
- Small residual at away side in most central
- Double hump almost gone in mid central

Sensitivity of away-side residual to v_4



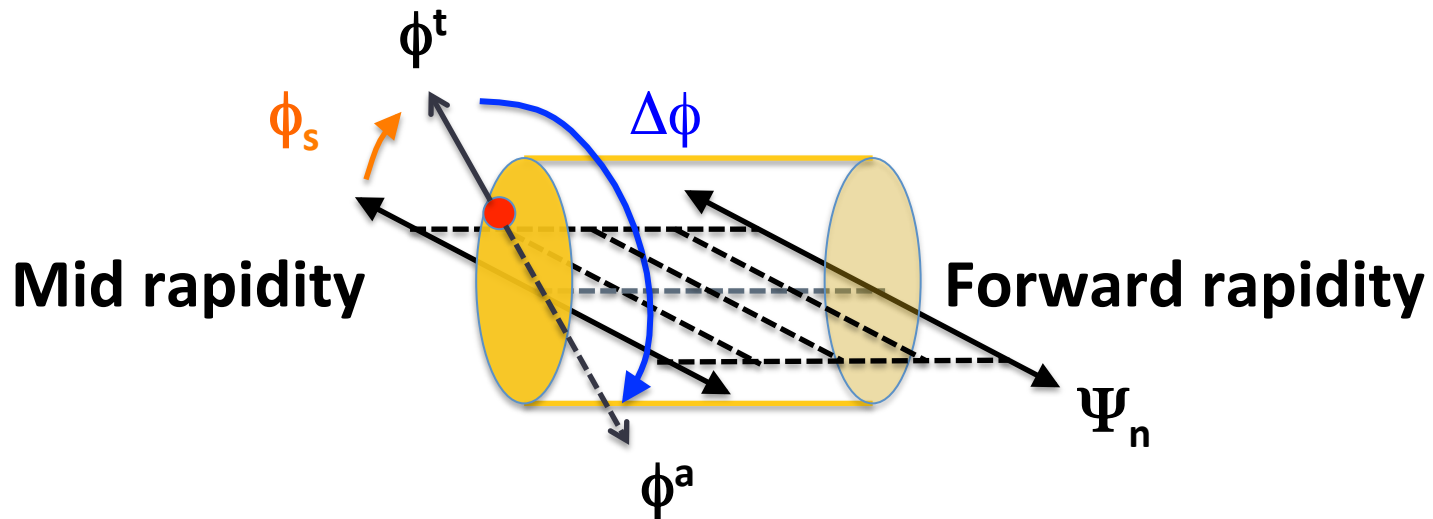
- ✧ $v_4(\Psi_2)$ doesn't change away-side trends
- ✧ $v_4(\Psi_4)$ removes away-side residual in central
 - reproduce double hump in mid-central
- ✧ Mach-cone is possibly induced by jet?

v_n ($n=1,2,3,4$) subtracted correlations



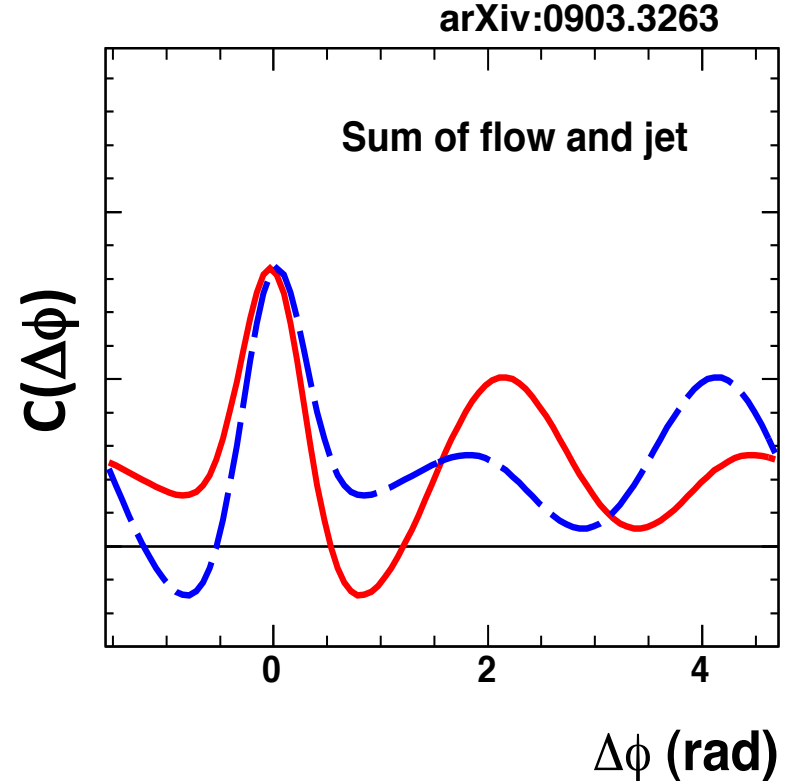
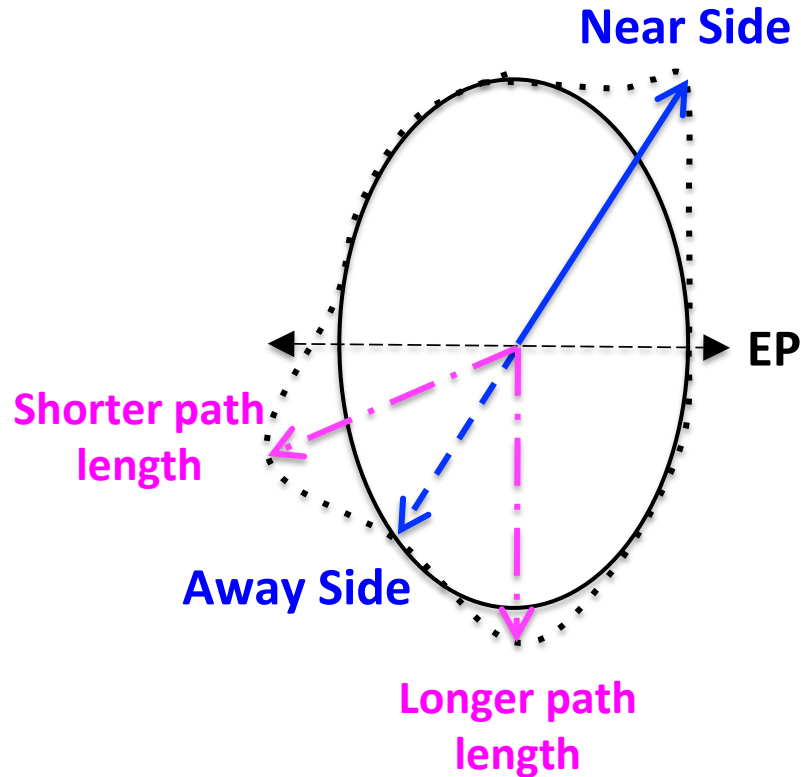
- ✧ Subtraction of v_1 term doesn't change correlations
- ✧ Away side double humps in mid-central collision are conclusive

Correlations relative to Ψ_2 & Ψ_3



- ✧ **Control parton path length (mainly Ψ_2)**
 - In-plane : shorter path length
 - Out-of-plane : longer path length
- ✧ **Sensitivity of correlations to different harmonic event planes**

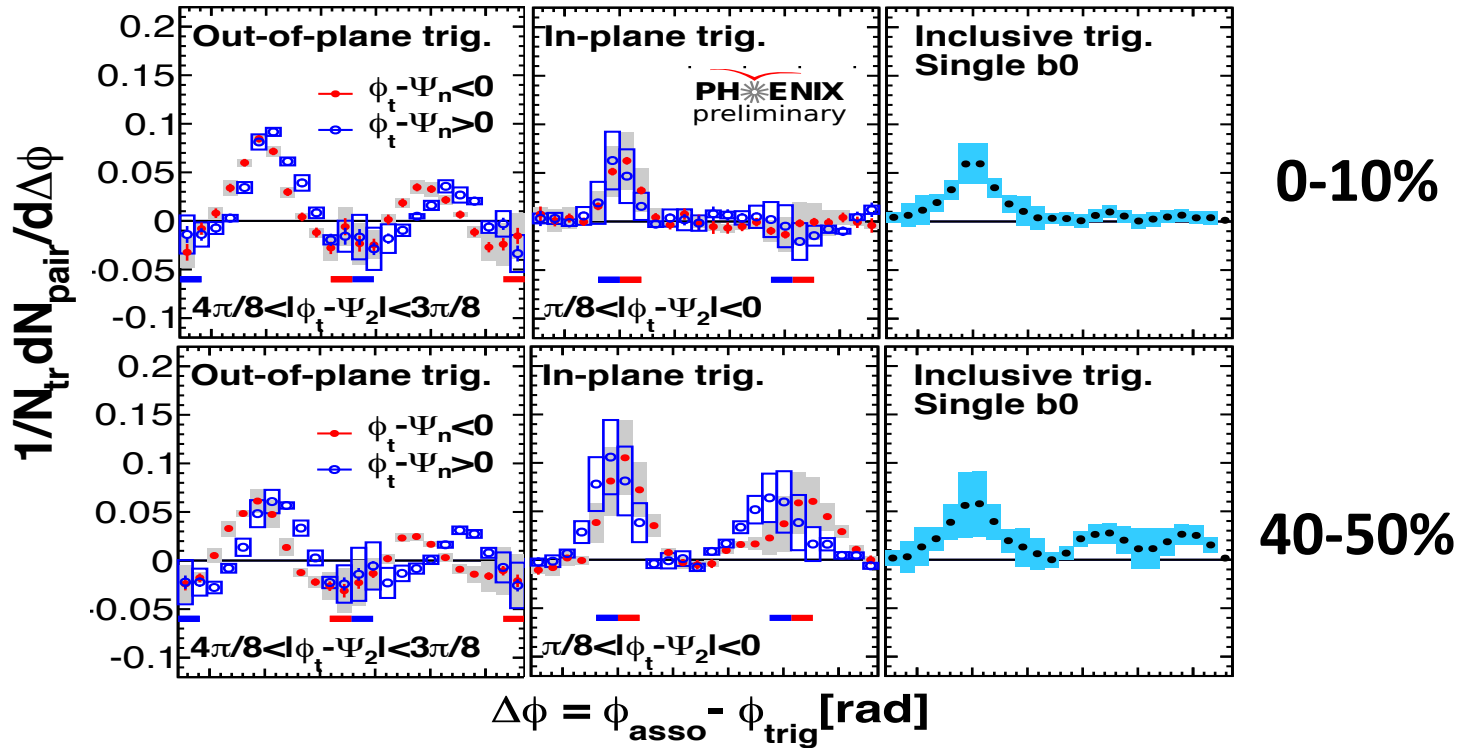
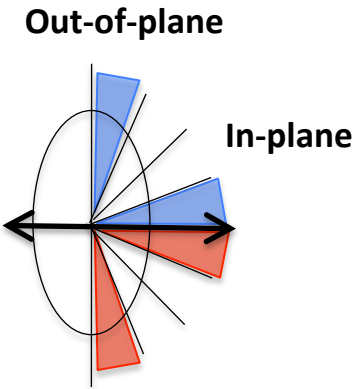
Parton path length in **Left/Right** correlations



- ✧ **Left/Right** trigger selection relative to event plane results in non-uniform path length at away-side
- ✧ Expect the modification of away-side as **Left/Right** asymmetry

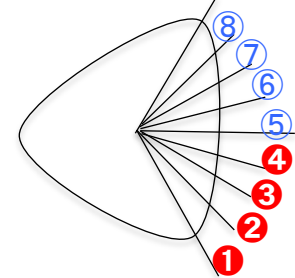
Correlations relative to Ψ_2

2-4 \otimes 1-2 GeV, $v_2 v_3 v_4(\Psi_4)$ subtracted with $\langle \cos 4(\Psi_2 - \Psi_4) \rangle = v_4(\Psi_2)/v_4(\Psi_4)$ by ZYAM

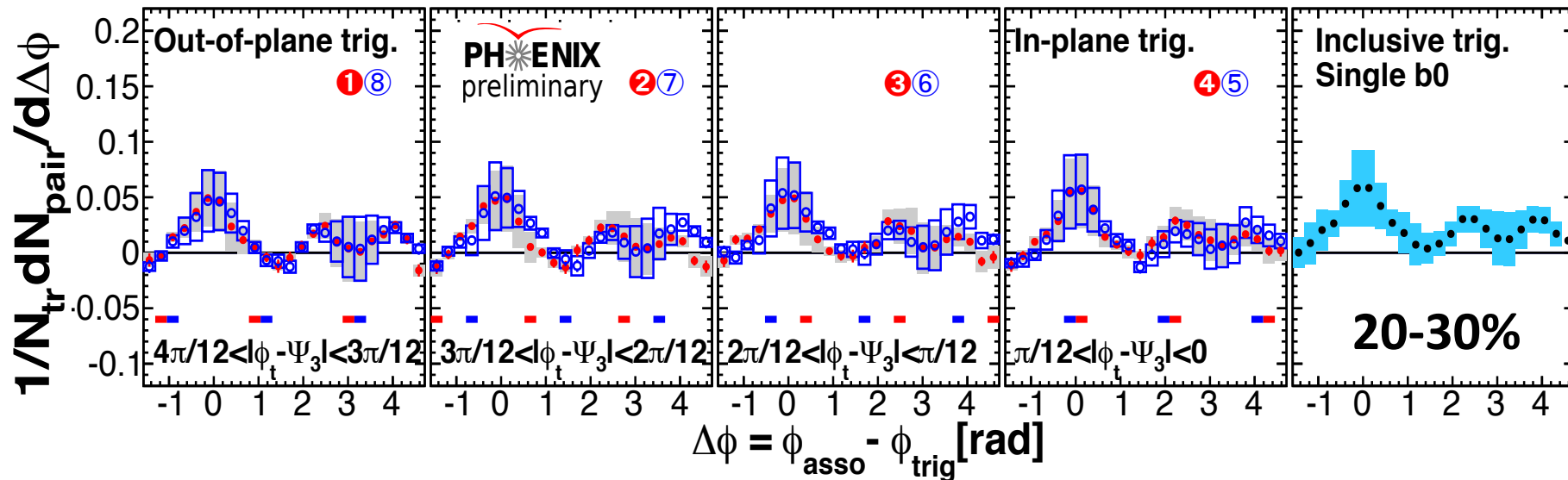


- ✧ Single background level doesn't work
- ✧ Ψ_2 dependence is observed
- ✧ **Left/Right** asymmetry more pronounced in mid-central
- ✧ Jets pull down v_2 in central collisions
- ✧ Jets push up v_2 in peripheral collisions

Correlations relative to Ψ_3



2-4 \times 1-2 GeV, $v_2 v_3 v_4(\Psi_4)$ subtracted with $\langle \cos 4(\Psi_2 - \Psi_4) \rangle = v_4(\Psi_2) / v_4(\Psi_4)$ by ZYAM



- ✧ Single background level works
- ✧ Correlations are independent of Ψ_3 within systematics
- ✧ **Left/Right** correlations are consistent within systematics

Summary

Collective flow

- ✧ EP correlations & event by event v_n provides more constraints to Hydro-models
- ✧ N_q scaling from various aspects
- ✧ v_2 in geometry controlled collisions systems
- ✧ None zero direct photon v_2
- ✧ None zero high p_T hadron & jet v_2

Two-particle correlations

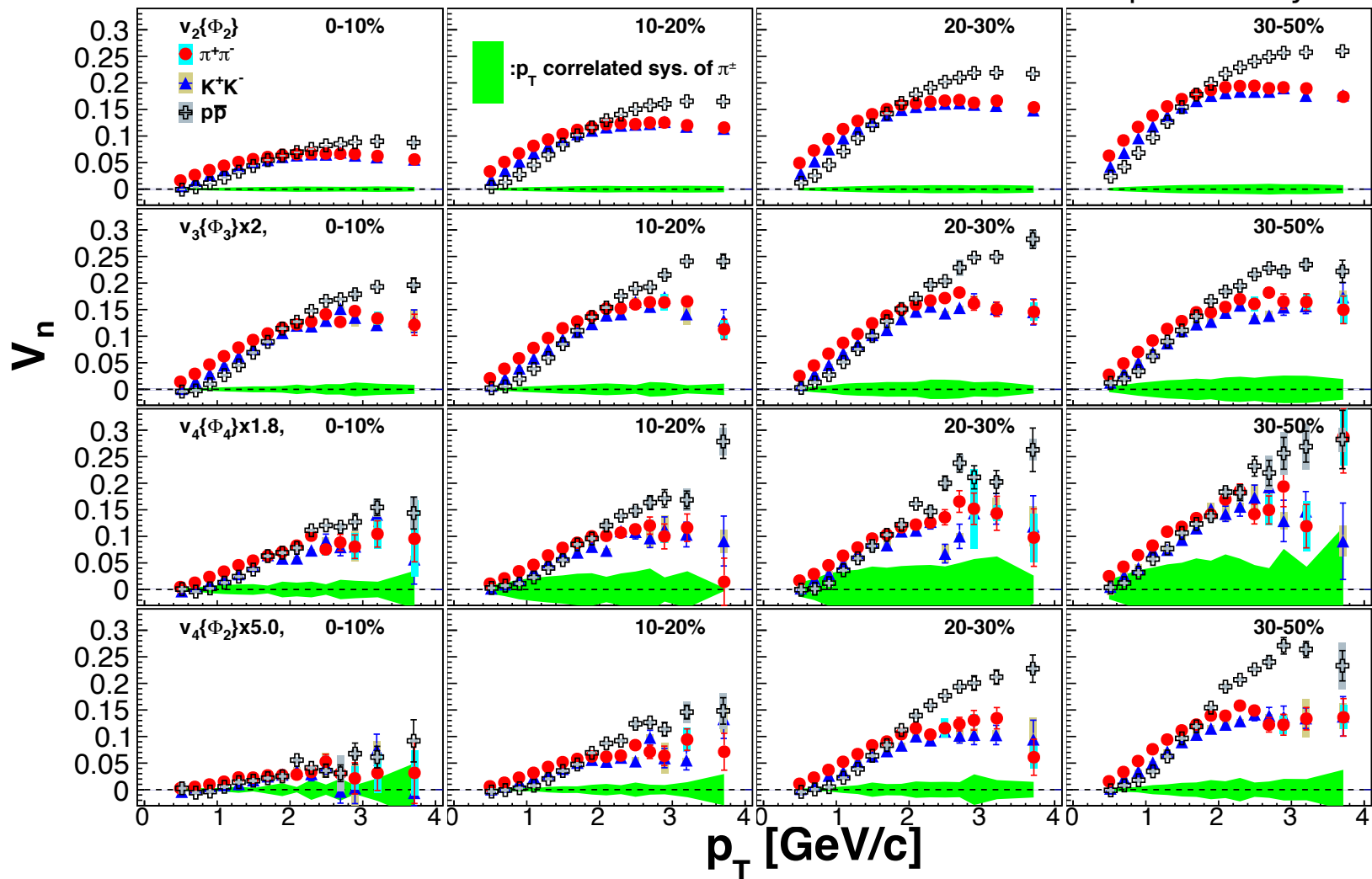
- ✧ Mach-cone like structure is conclusive
 - Difficult to explain by v_n
 - Possibly induced by jet
- ✧ Correlations have different sensitivity to Ψ_2 & Ψ_3

Back Up Slides

Identified particle v_n

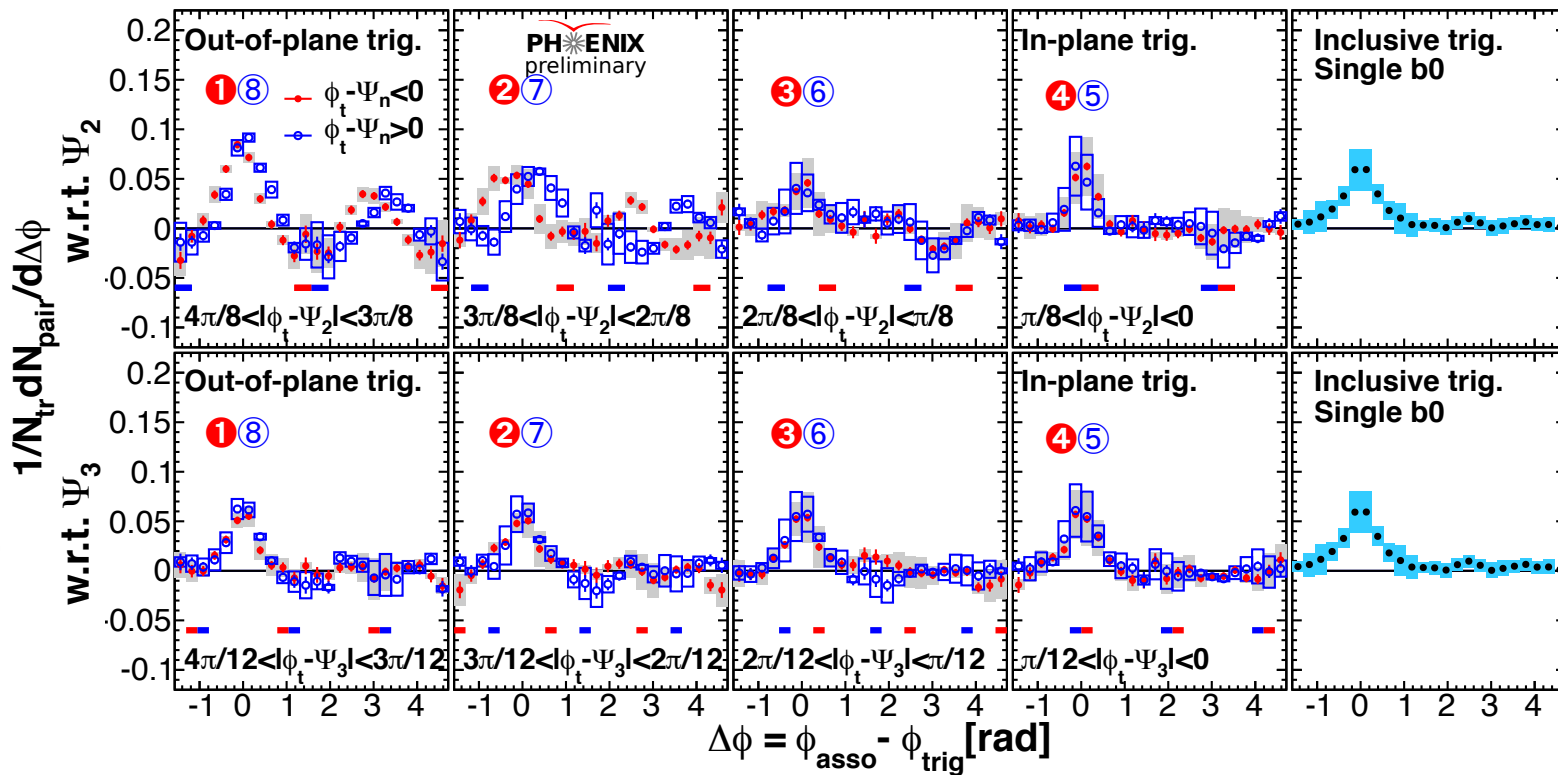
Au+Au $\sqrt{s_{NN}}=200$ GeV PHENIX Preliminary

PHENIX preliminary



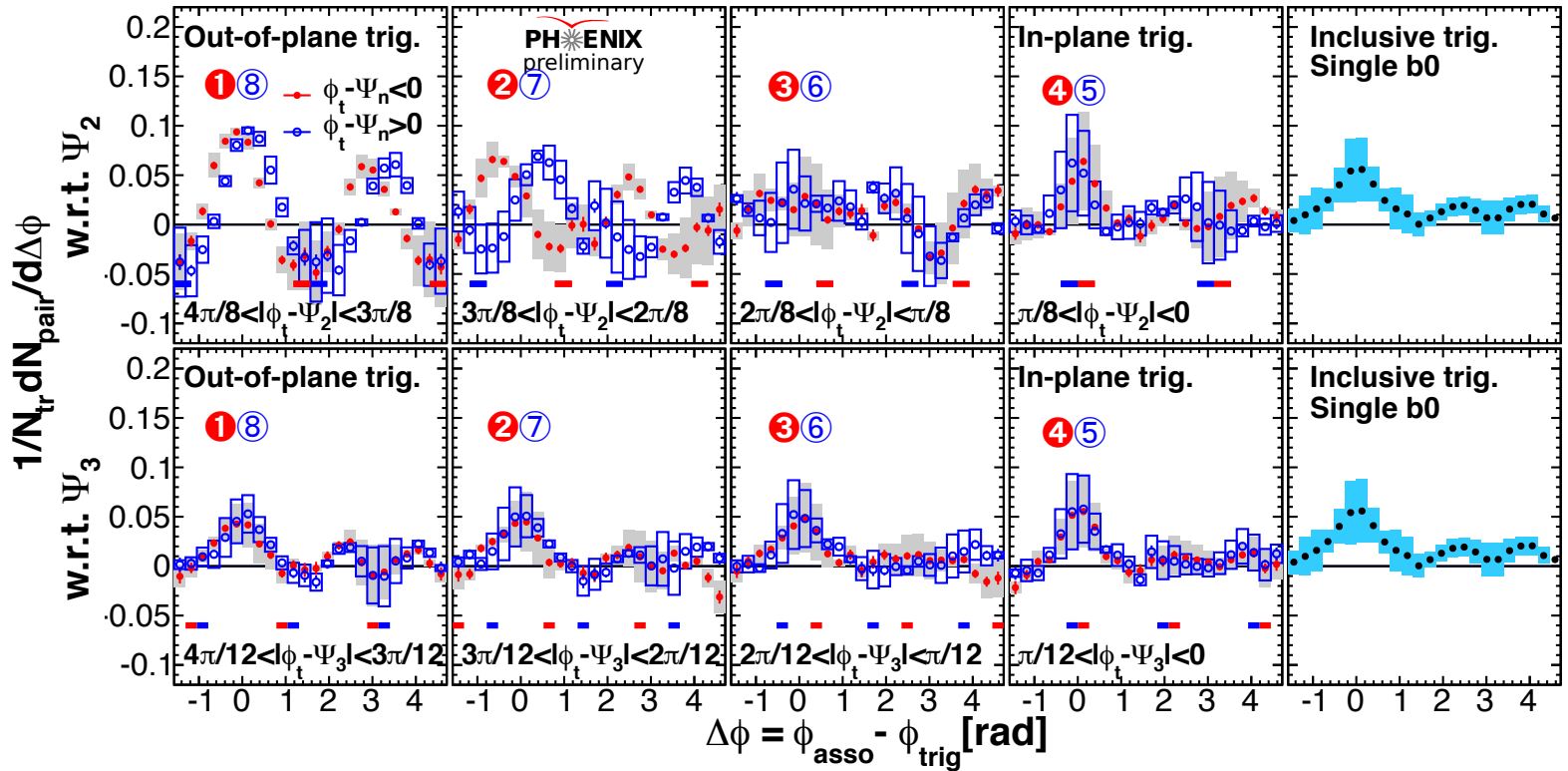
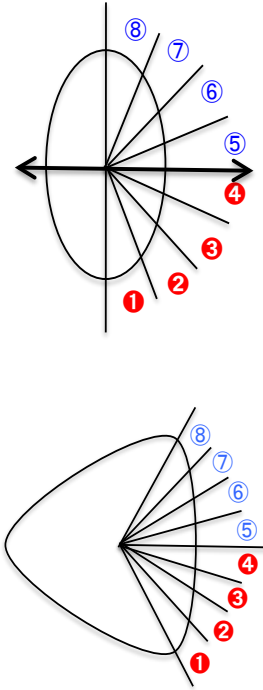
Correlations relative to Ψ_2 & Ψ_3 , 0-10%

Au+Au 200GeV, 0-10%, 2-4 \times 1-2 GeV, $v_2 v_3 v_4(\Psi_4)$ subtracted with $\langle \cos 4(\Psi_2 - \Psi_4) \rangle = v_4(\Psi_2)/v_4(\Psi_4)$ by ZYAM



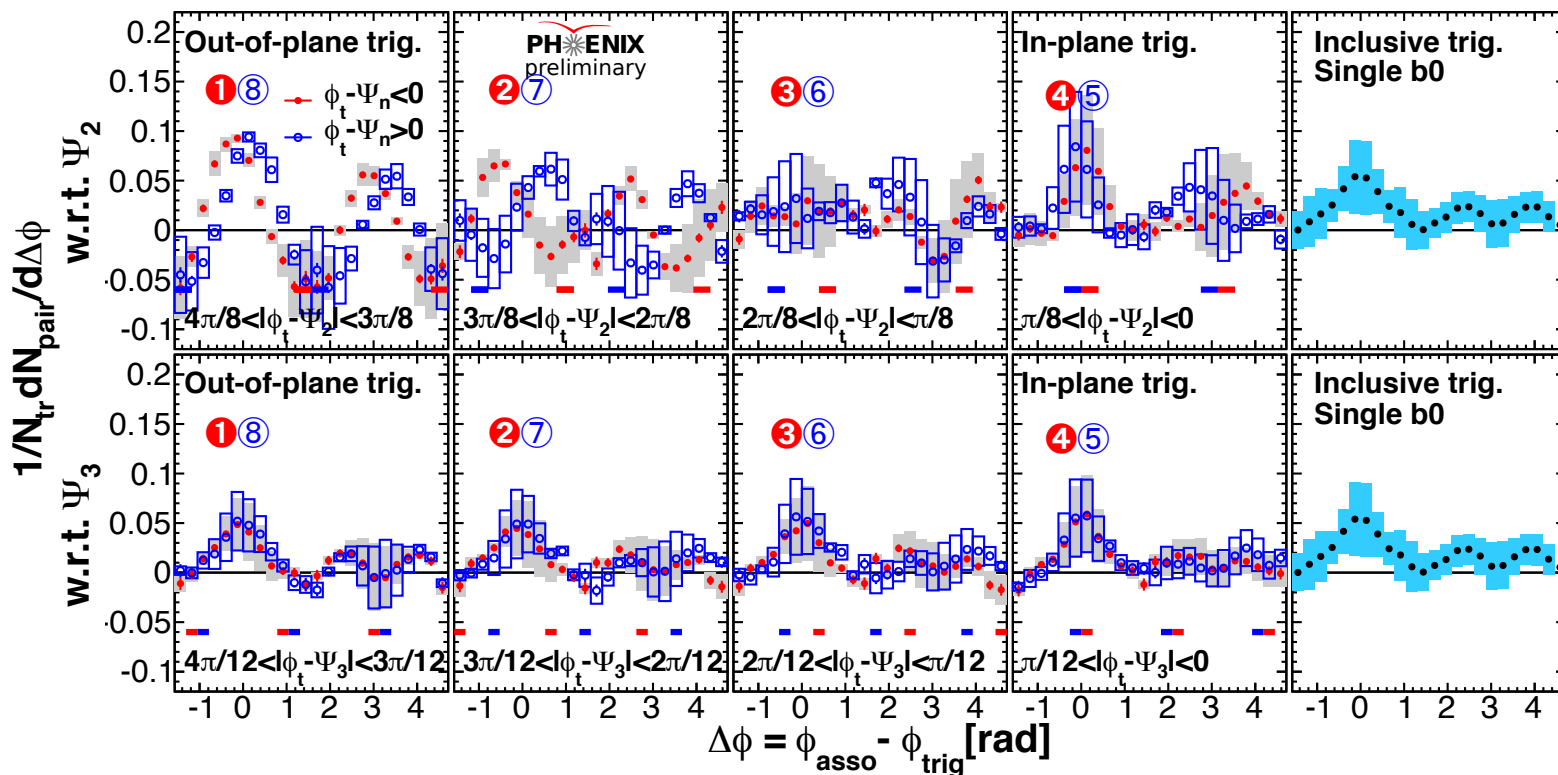
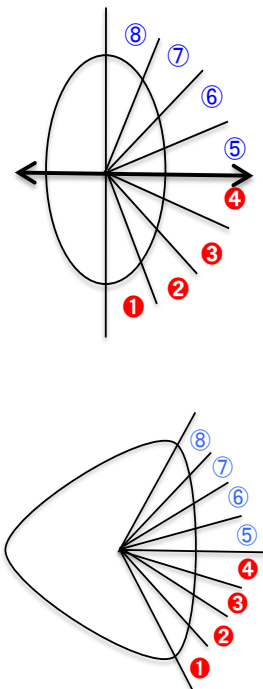
Correlations relative to Ψ_2 & Ψ_3 10-20%

Au+Au 200GeV, 10-20%, 2-4 \otimes 1-2 GeV, $v_2 v_3 v_4(\Psi_4)$ subtracted with $\langle \cos 4(\Psi_2 - \Psi_4) \rangle = v_4(\Psi_2)/v_4(\Psi_4)$ by ZYAM



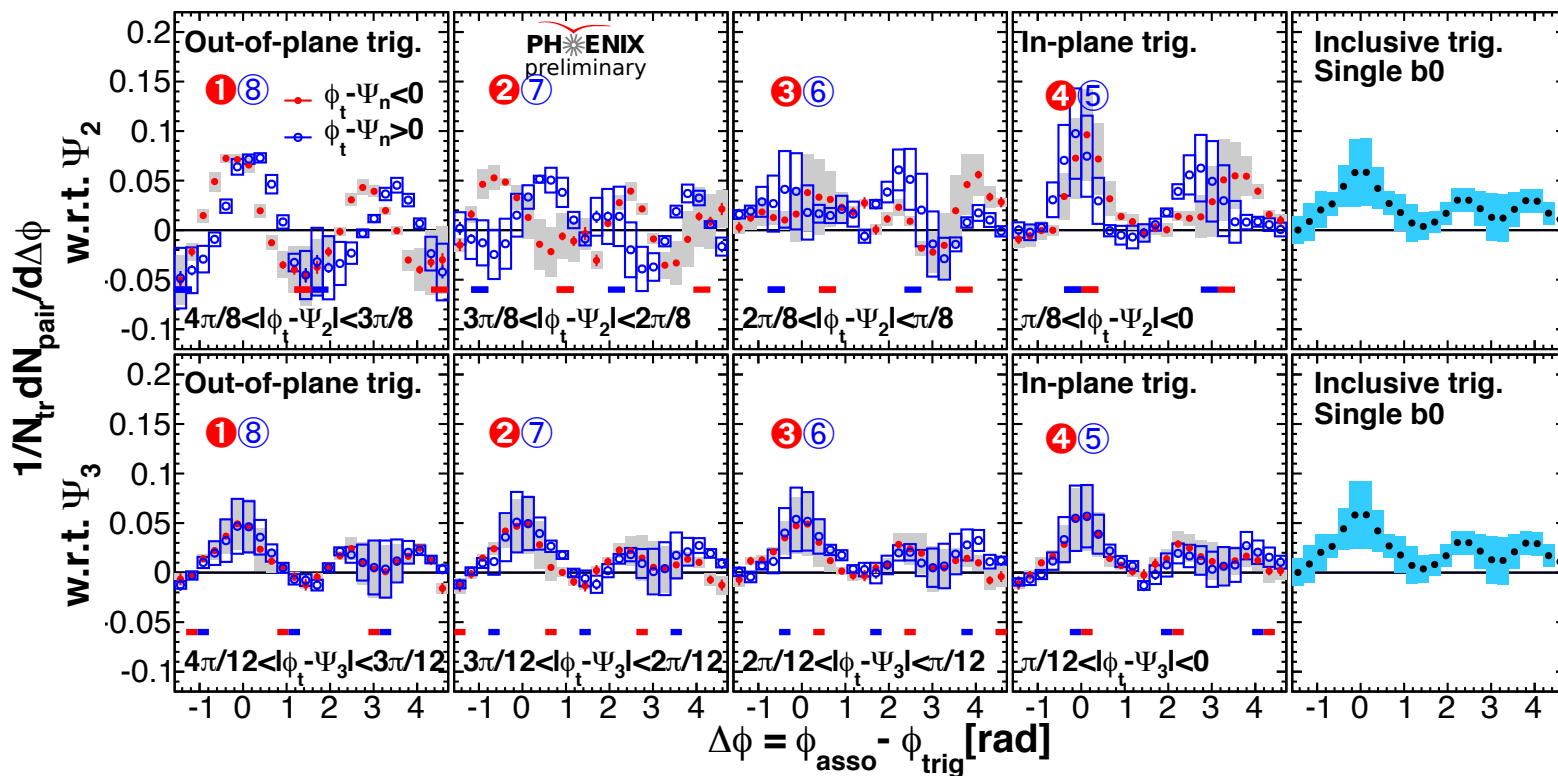
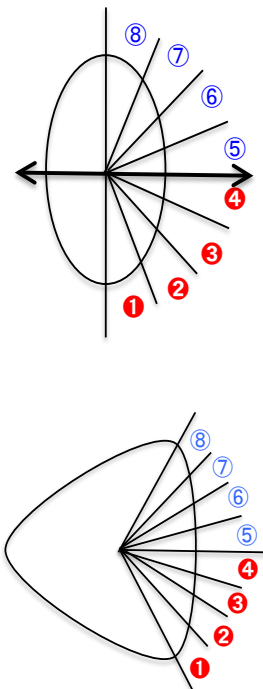
Correlations relative to Ψ_2 & Ψ_3 20-30%

Au+Au 200GeV, 20-30%, 2-4 \otimes 1-2 GeV, $v_2 v_3 v_4(\Psi_4)$ subtracted with $\langle \cos 4(\Psi_2 - \Psi_4) \rangle = v_4(\Psi_2)/v_4(\Psi_4)$ by ZYAM



Correlations relative to Ψ_2 & Ψ_3 30-40%

Au+Au 200GeV, 30-40%, 2-4 \times 1-2 GeV, $v_2 v_3 v_4(\Psi_4)$ subtracted with $\langle \cos 4(\Psi_2 - \Psi_4) \rangle = v_4(\Psi_2)/v_4(\Psi_4)$ by ZYAM



Correlations relative to Ψ_2 & Ψ_3 , 40-50%

Au+Au 200GeV, 40-50%, $2-4 \times 1-2$ GeV, $v_2 v_3 v_4(\Psi_4)$ subtracted with $\langle \cos 4(\Psi_2 - \Psi_4) \rangle = v_4(\Psi_2)/v_4(\Psi_4)$ by ZYAM

