

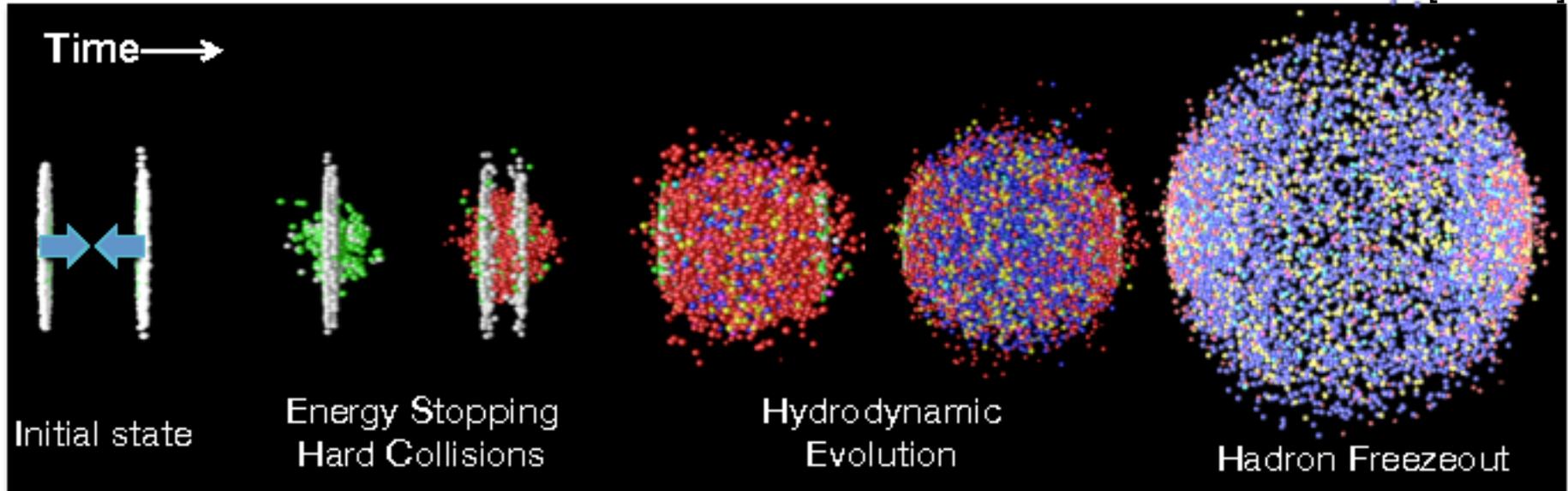
Azimuthal angle dependence of HBT radii with respect to the Event Plane in Au+Au collisions at PHENIX

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WPCF2013 @Acireale, Italy

Space-Time evolution in HI collisions

arXiv:1201.4264 [nucl-ex]



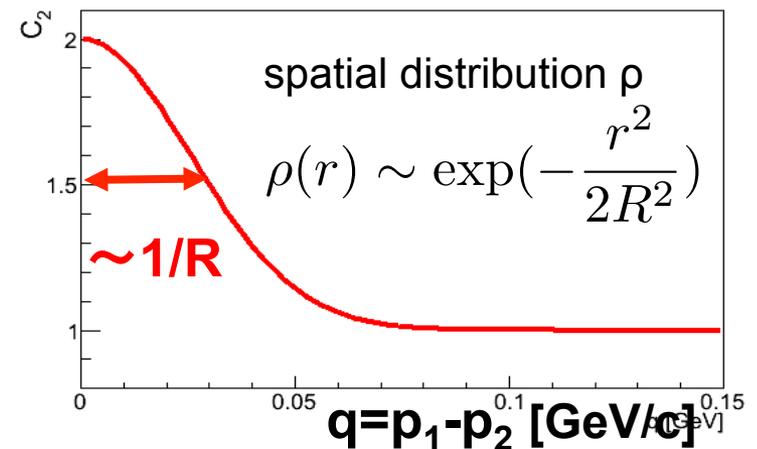
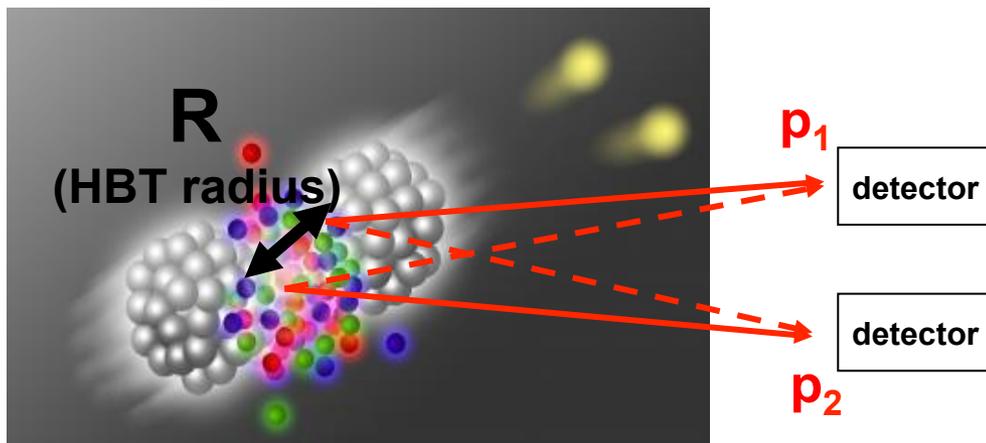
- Space-time extent at freeze-out reflects the characteristics of system evolution, such as the strength of the expansion, the expansion time, hadron rescattering, and so on.
- **HBT interferometry** is a powerful tool to study the space-time evolution in Heavy Ion collisions.

HBT Interferometry

- 1956s, R. Hanbury Brown and R. Twiss measured the angular diameter of Sirius.
- 1960, Goldhaber *et al.* correlation among identical pions in $p+\bar{p}$
- Quantum interference between two identical particles

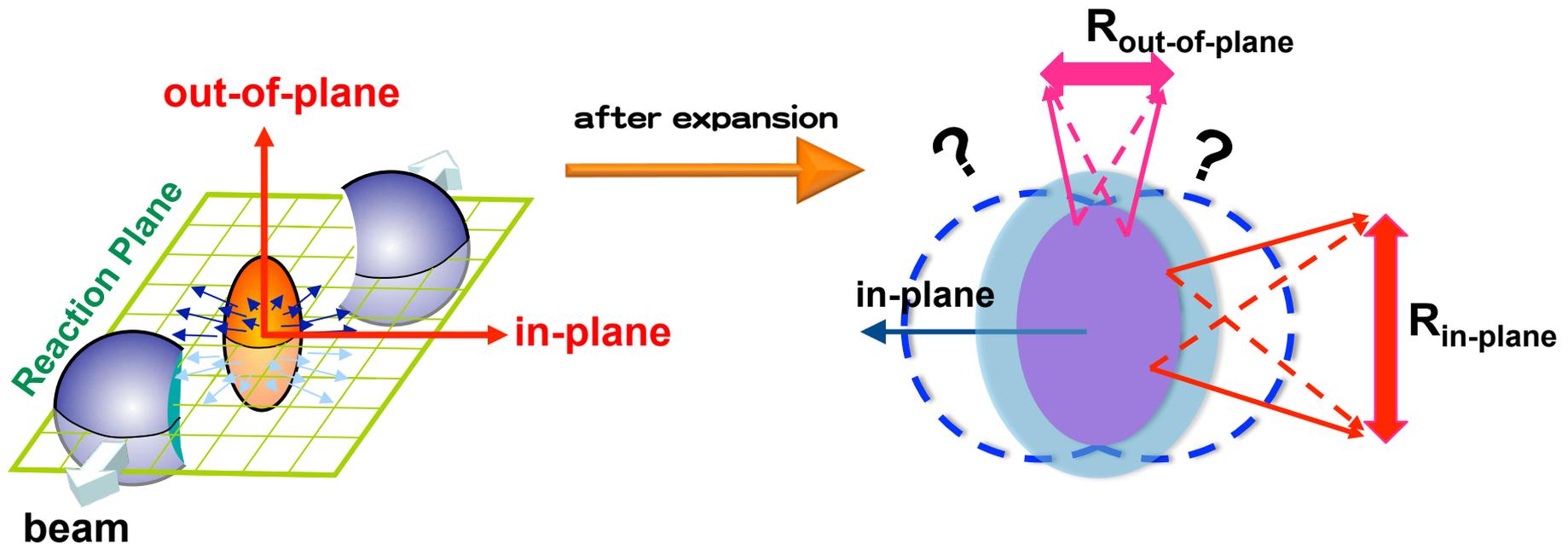
wave function for
2 bosons(fermions): $\Psi_{12} = \frac{1}{\sqrt{2}} [\Psi(x_1, p_1)\Psi(x_2, p_2) \pm \Psi(x_2, p_1)\Psi(x_1, p_2)]$

$$C_2 = \frac{P(p_1, p_2)}{P(p_1)P(p_2)} \approx 1 + |\tilde{\rho}(q)|^2 = 1 + \exp(-R^2 q^2)$$

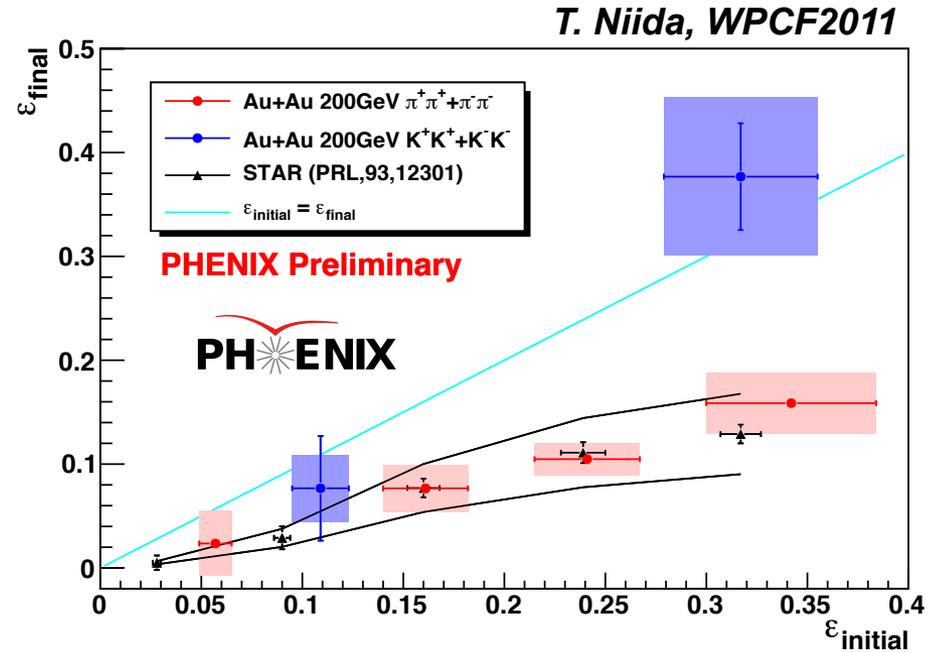
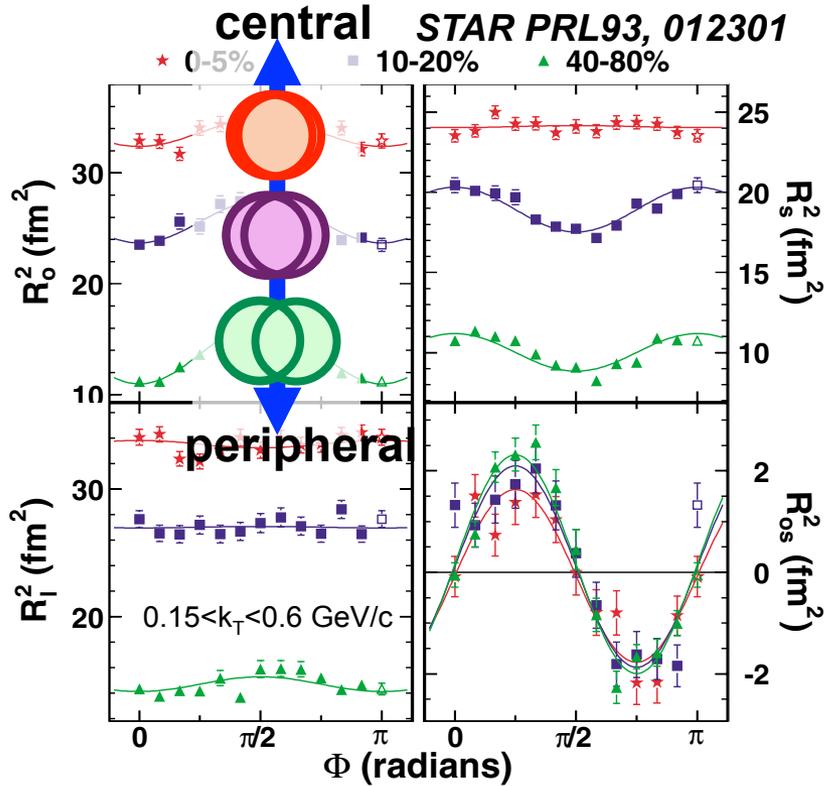


Azimuthal angle dependence

- Angle dependence of HBT radii relative to Reaction Plane reflects the source shape at kinetic freeze-out.
- Initial spatial anisotropy causes momentum anisotropy (flow anisotropy)
 - ✧ One may expect in-plane extended source at freeze-out
- Final source eccentricity will depend on initial eccentricity, flow profile, expansion time, and viscosity etc.



HBT radii w.r.t Reaction Plane at RHIC



PRC70, 044907 (2004)

$$R_{s,n}^2 = \langle R_{s,n}^2 (\Delta\phi) \cos(n\phi) \rangle$$

$$\epsilon_{final} = 2 \frac{R_{s,2}^2}{R_{s,0}^2}$$

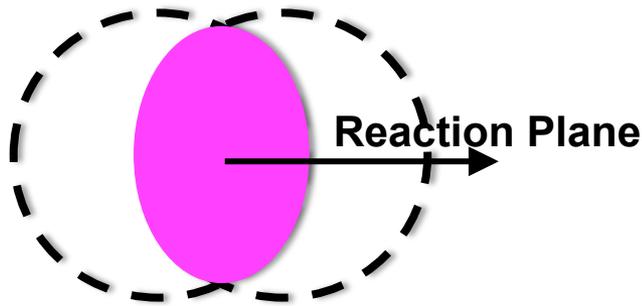
in-plane

- $\epsilon_{final} \approx \epsilon_{initial}/2$
- Strong expansion to in-plane, but still elliptical shape.

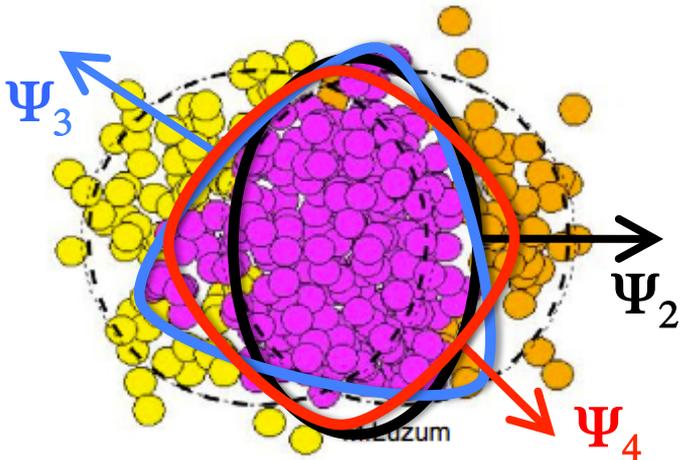
Higher Harmonic Flow and Event Plane

- Initial density fluctuations cause higher harmonic flow v_n
- Azimuthal distribution of emitted particles:

smooth picture



fluctuating picture



$$\frac{dN}{d\phi} \propto 1 + 2v_2 \cos 2(\phi - \Psi_2) + 2v_3 \cos 3(\phi - \Psi_3) + 2v_4 \cos 4(\phi - \Psi_4)$$

$$v_n = \langle \cos n(\phi - \Psi_n) \rangle$$

v_n : strength of higher harmonic flow
 Ψ_n : higher harmonic event plane
 ϕ : azimuthal angle of emitted particles

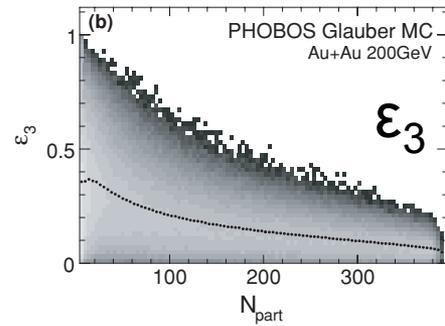
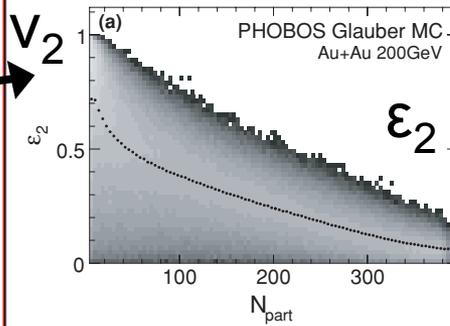
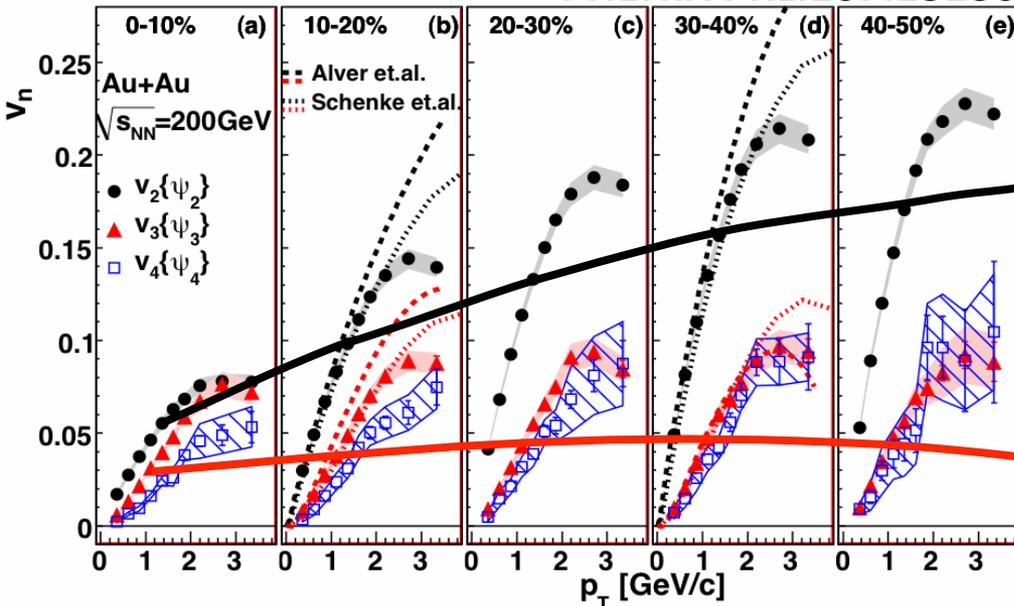
Centrality dependence of v_n and initial ϵ_n

Higher harmonic flow v_n

Initial source anisotropy ϵ_n

PHENIX PRL.107.252301

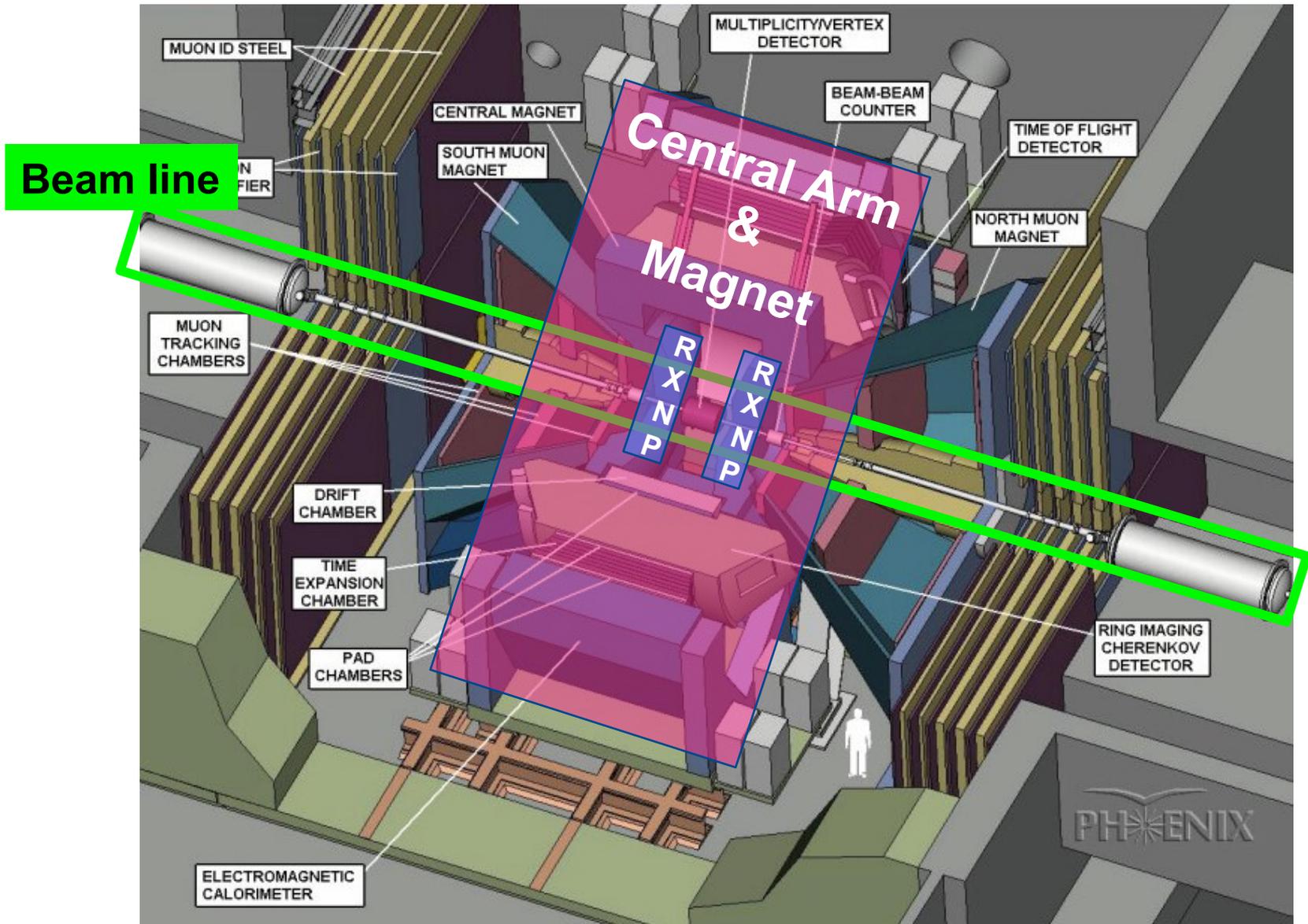
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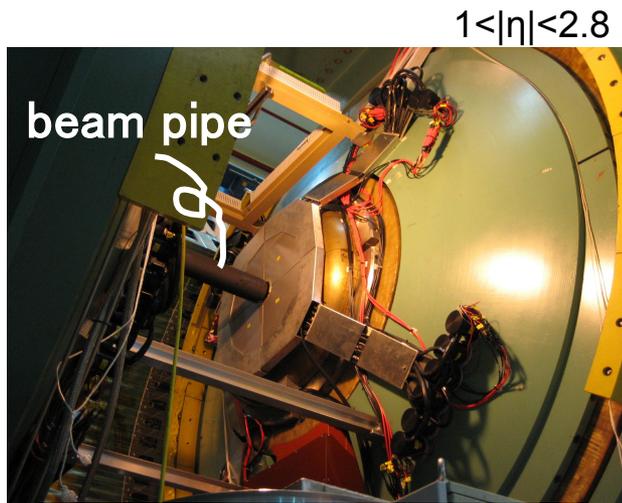
v_3
($p_T=1.1 \text{ GeV}/c$)

- Weak centrality dependence of v_3 unlike v_2
- Initial ϵ_3 has finite values and weaker centrality dependence than ϵ_2
- ▲ **Triangular component in source shape exists at final state?**
➔ Measurement of HBT radii relative to Ψ_3

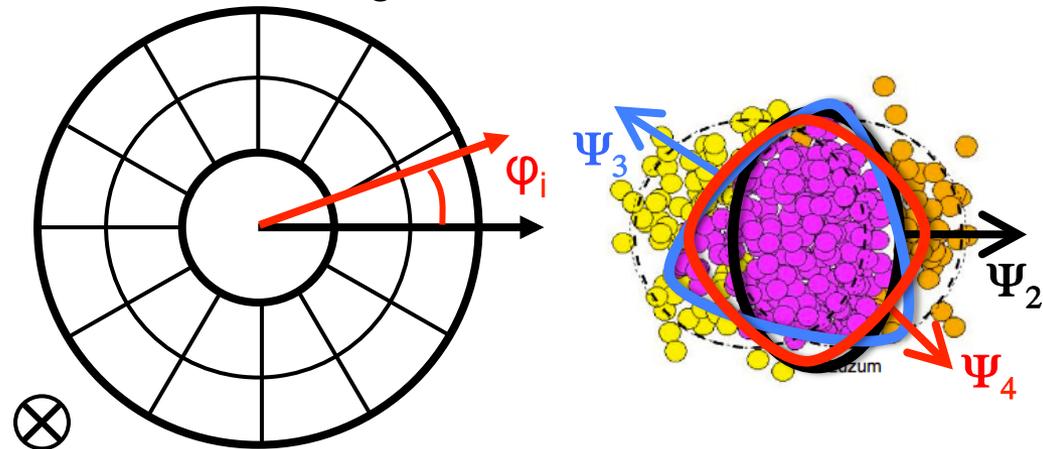
PHENIX Experiment



Event Plane Determination

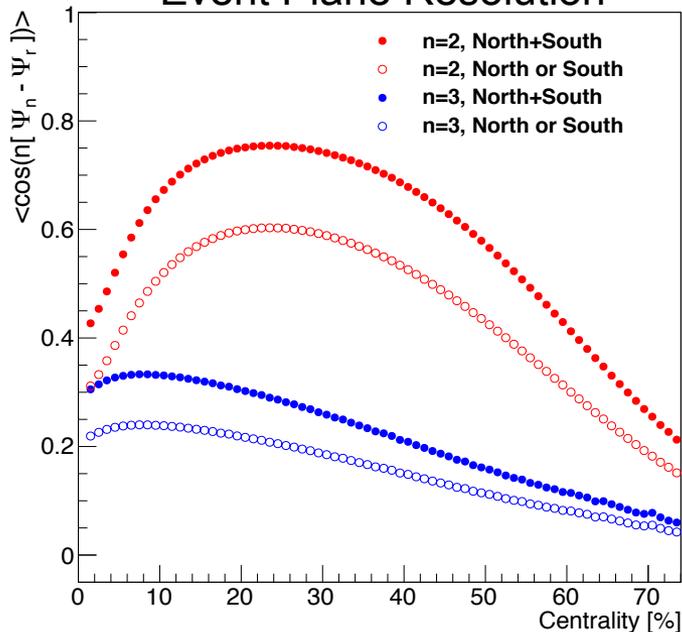


24 scintillator segments



beam axis

Event Plane Resolution



■ Determined by anisotropic flow itself

$$\Psi_n = \frac{1}{n} \tan^{-1} \left(\frac{\sum w_i \cos(n\phi_i)}{\sum w_i \sin(n\phi_i)} \right)$$

■ Event plane is determined by Reaction Plane Detector (RXNP)

✧ Resolution: $\langle \cos(n(\Psi_n - \Psi_{\text{real}})) \rangle$

n=2 : ~ 0.75

n=3 : ~ 0.34

Particle Identification

- **EMC-PbSc is used.**

- ✧ timing resolution ~ 600 ps

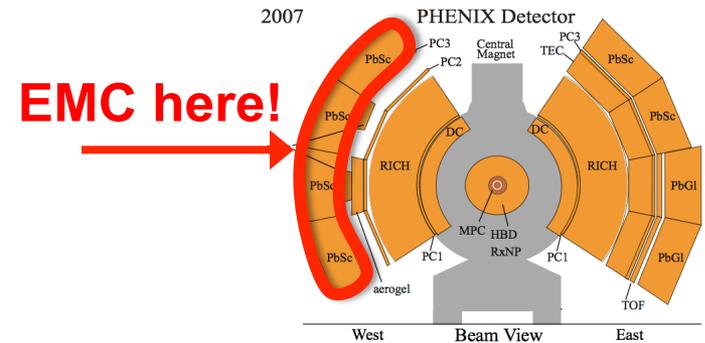
- **Time-Of-Flight method**

$$m^2 = p^2 \left(\left(\frac{ct}{L} \right)^2 - 1 \right)$$

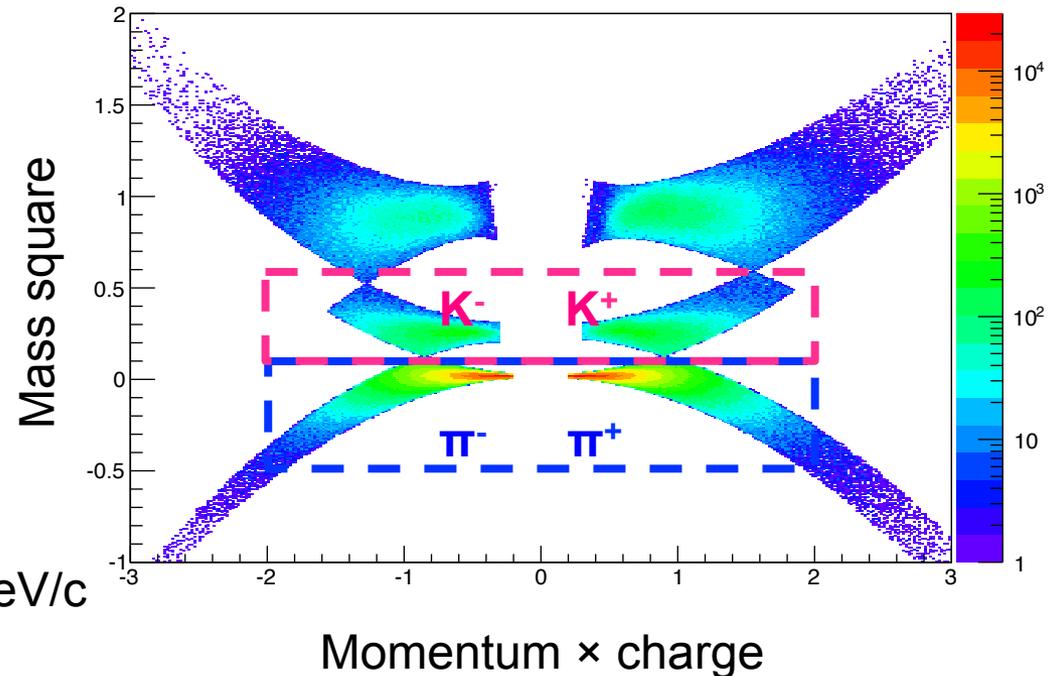
p: momentum L: flight path length
t: time of flight

- **Charged π within 2σ**

- ✧ π/K separation up to ~ 1 GeV/c



Particle Identification by PbSc-EMC



3D-Analysis

■ “Out-Side-Long” frame

- ✧ Bertsch-Pratt parameterization
- ✧ Longitudinal Center of Mass System ($p_{z1}=p_{z2}$)

$$C_2 = 1 + \lambda G \quad \lambda : \text{chaoticity} \quad R_\mu : \text{HBT radii}$$

$$\begin{aligned} G &= \exp(-\mathbf{R}^2 \mathbf{q}^2) \\ &= \exp(-R_x^2 q_x^2 - R_y^2 q_y^2 - R_z^2 q_z^2 - \Delta\tau^2 q_0^2) \\ &= \exp(-R_s^2 q_s^2 - R_o^{*2} q_o^2 - R_l^2 q_l^2 - \Delta\tau^2 q_0^2) \\ &\stackrel{\text{LCMS}}{\approx} \exp(-R_s^2 q_s^2 - \underbrace{(R_o^{*2} + \beta_T^2 \Delta\tau^2)}_{=\mathbf{R}_o^2} q_o^2 - R_l^2 q_l^2) \end{aligned}$$

including cross term

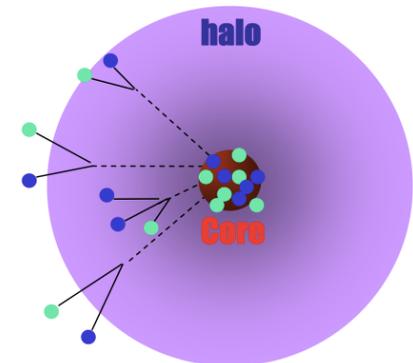
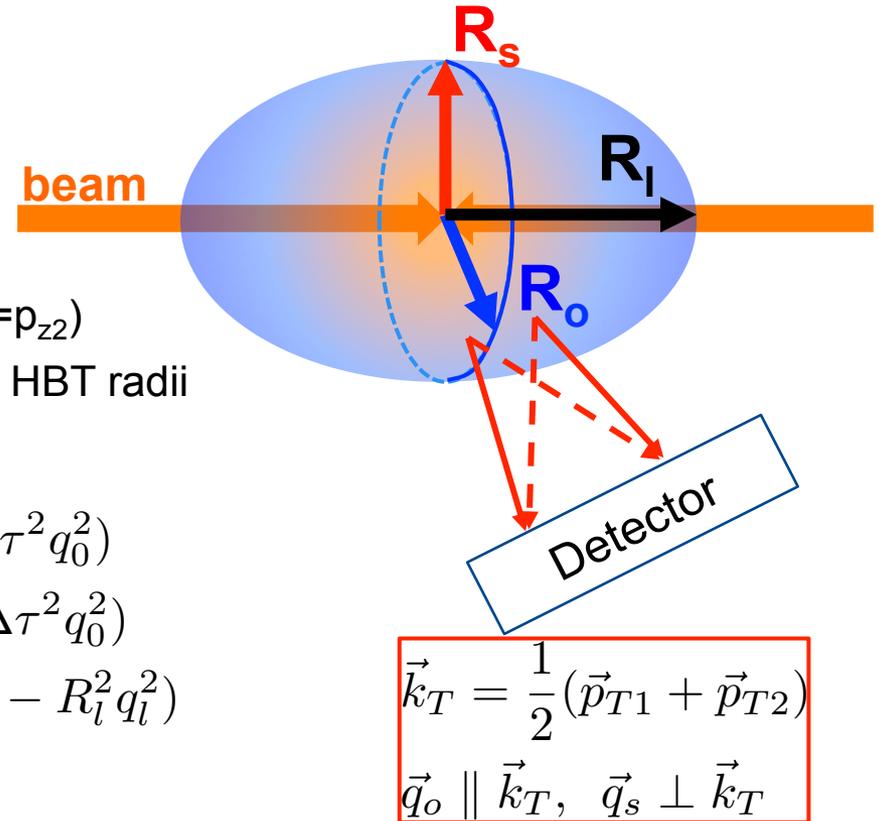
$$G = \exp(-R_s^2 q_s^2 - R_o^2 q_o^2 - R_l^2 q_l^2 - 2R_{os}^2 q_s q_o)$$

■ Core-Halo model

$$\begin{aligned} C_2 &= C_2^{\text{core}} + C_2^{\text{halo}} \\ &= N[\lambda(1 + G)F_{\text{coul}}] + [1 - \lambda] \end{aligned}$$

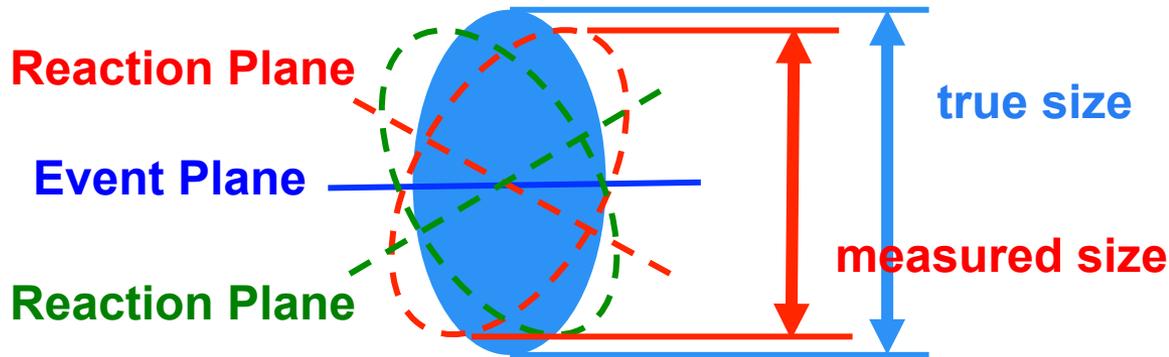
N: normalization factor

F_{coul} : Coulomb correction factor



Correction of Event Plane Resolution

- Smearing effect by finite resolution of the event plane



- Correction for q-distribution $A_{corr}(q, \Phi_j) = A_{uncorr}(q, \Phi_j)$

✧ PRC.66, 044903(2002)

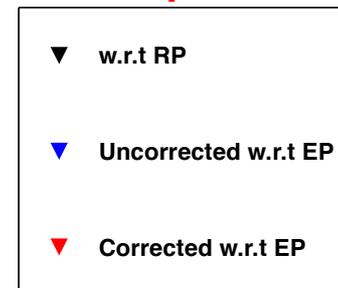
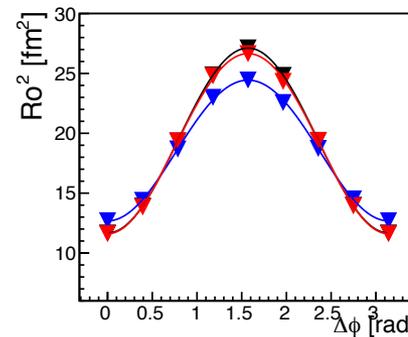
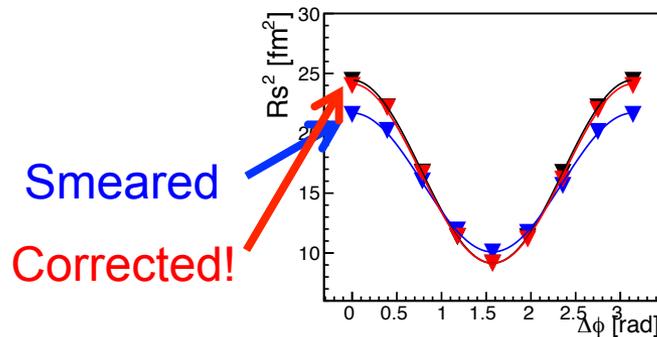
✓ model-independent correction

✧ Checked by MC-simulation

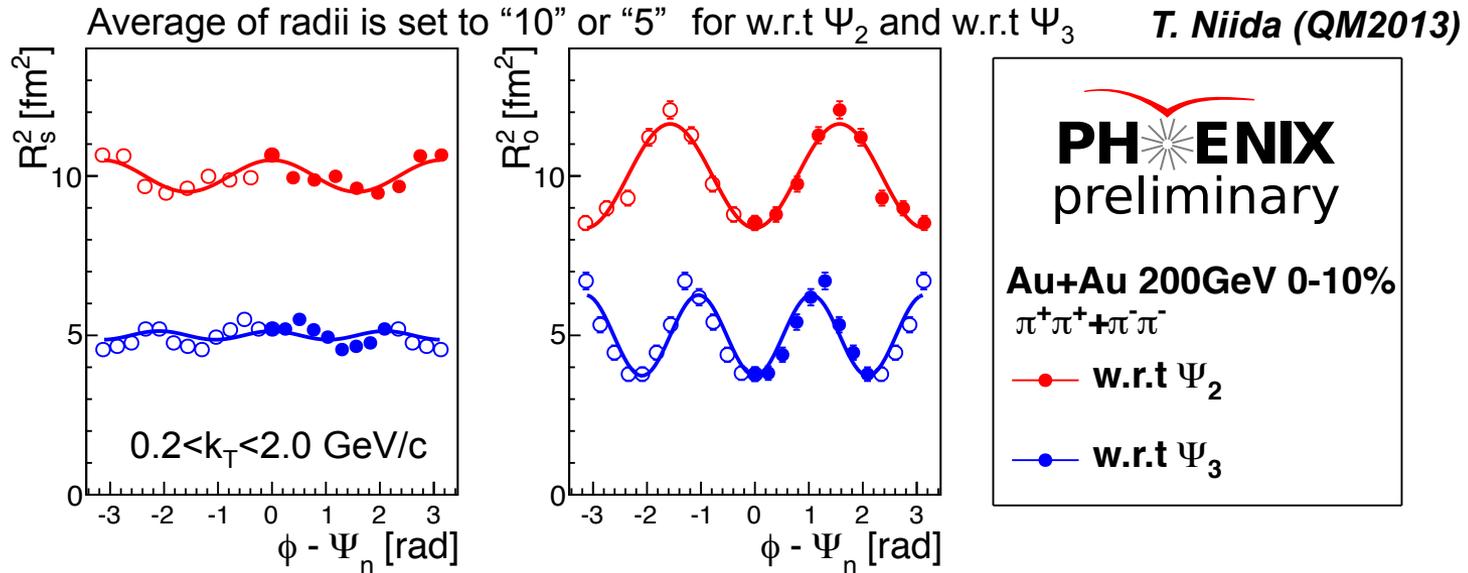
$$+ 2 \sum \zeta_{n,m} [A_c \cos(n\Phi_j) + A_s \sin(n\Phi_j)]$$

$$\zeta_{n,m} = \frac{n\Delta/2}{\sin(n\Delta/2) \langle \cos(n(\Psi_m - \Psi_{real})) \rangle}$$

event plane resolution



HBT radii w.r.t 3rd-order event plane



- R_o clearly shows a finite oscillation w.r.t Ψ_3 in most central event, while R_s does not show such a oscillation.

- What makes this R_o oscillation?

□ $\Delta\tau$ depends on azimuthal angle?

Note: R_o is sensitive to $\Delta\tau$ & β_T

$$C_2 = 1 + \lambda \exp(-R_s^2 q_s^2 - R_o^2 q_o^2 - R_l^2 q_l^2 - 2R_{os}^2 q_o q_s)$$

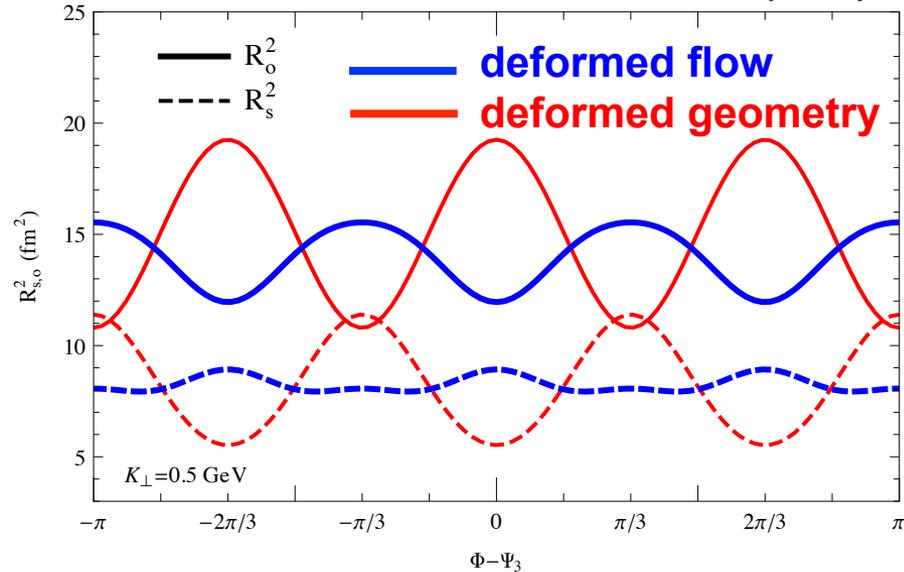
$$R_o^2 = R_o^{*2} + \beta_T^2 \Delta\tau^2$$

□ effect of flow anisotropy?

□ difference of “width” and “thickness”?

Possible explanation

PRC88, 044914 (2013)



■ HBT radii w.r.t Ψ_3 with Gaussian model

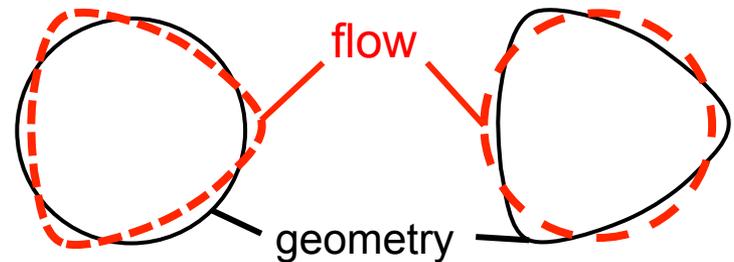
◇ C. Plumberg *et al.*, PRC88, 044914 (2013)

◇ Next talk: C. Plumberg

■ with/without triangularly deformed flow/geometry

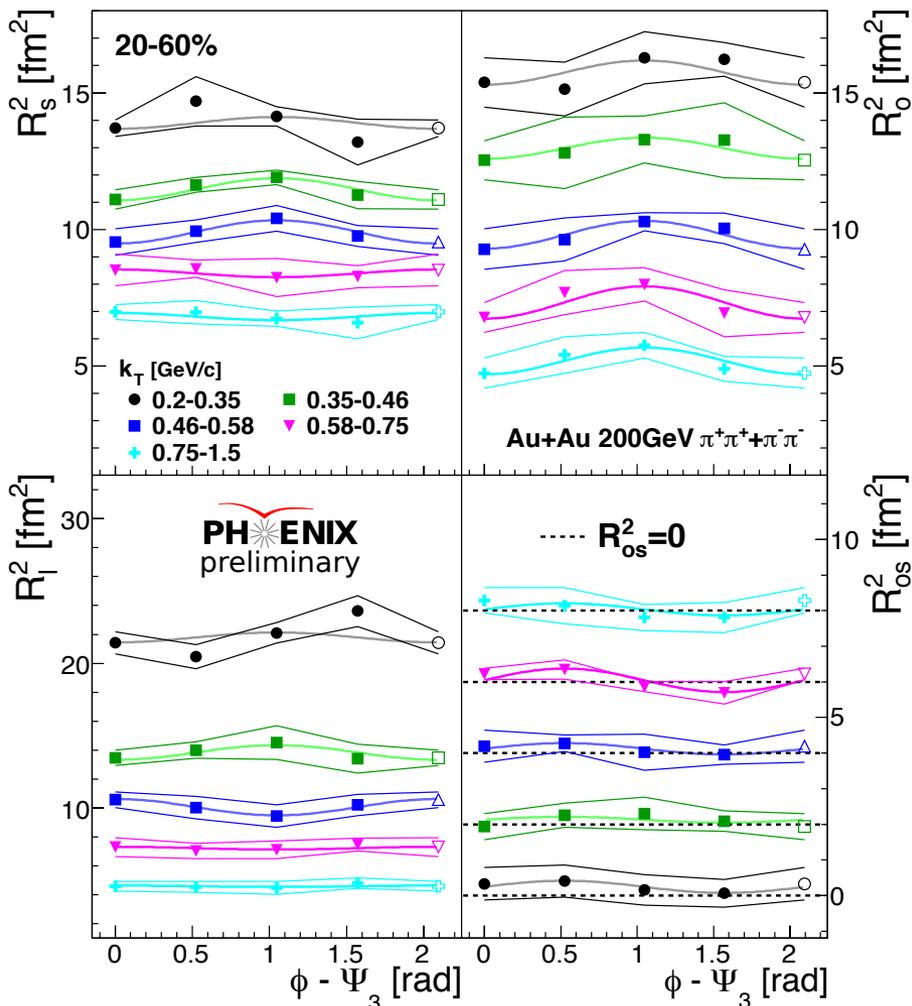
deformed flow

deformed geometry



- “Deformed flow” shows finite R_o oscillation and very small R_s oscillation
- Qualitatively agreement with the data seen in most-central collisions

k_T dependence of HBT radii w.r.t Ψ_3



■ Charged pions in Au+Au 200 GeV

◆ 20-60% centrality

◆ 5 k_T bins within 0.2-1.5 GeV/c

■ Fitted with the following Eq.:

$$R_\mu^2 = R_{\mu,0}^2 + 2R_{\mu,3}^2 \cos[3(\phi - \Psi_3)]$$

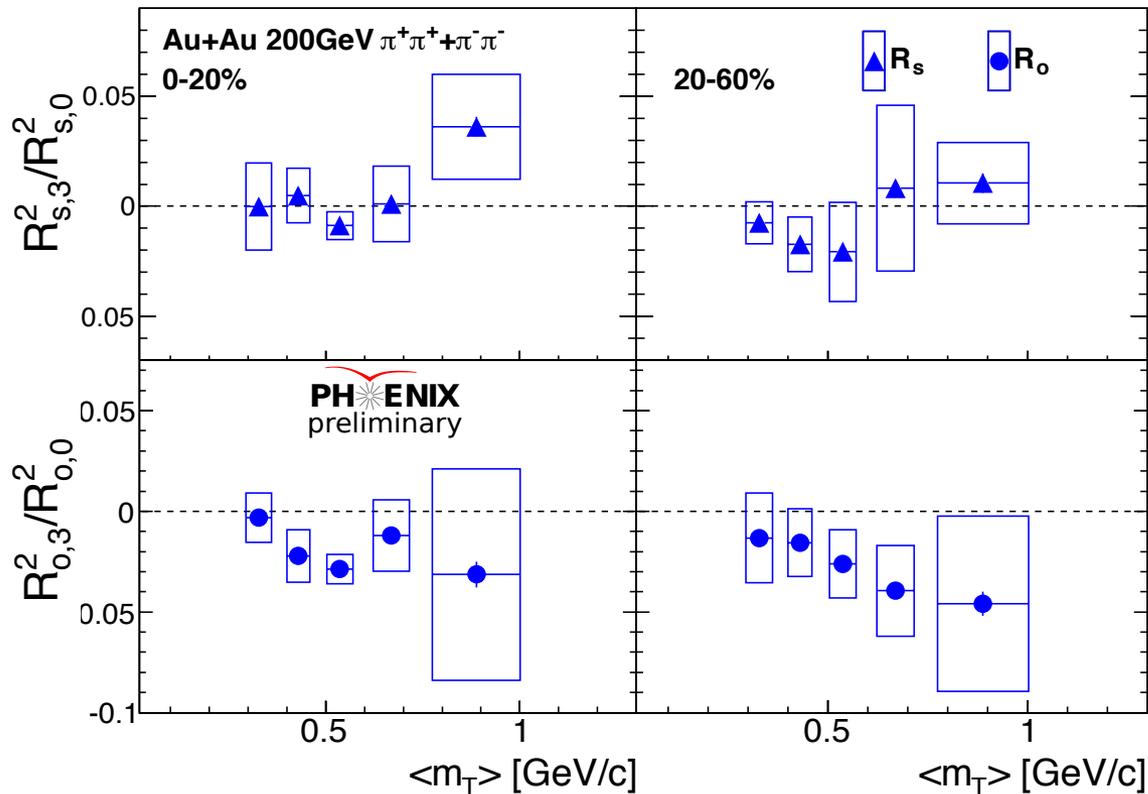
$$R_{os}^2 = 2R_{os,3}^2 \sin[3(\phi - \Psi_3)]$$

$$\mu = s, o, l$$

■ No clear k_T dependence for R_s

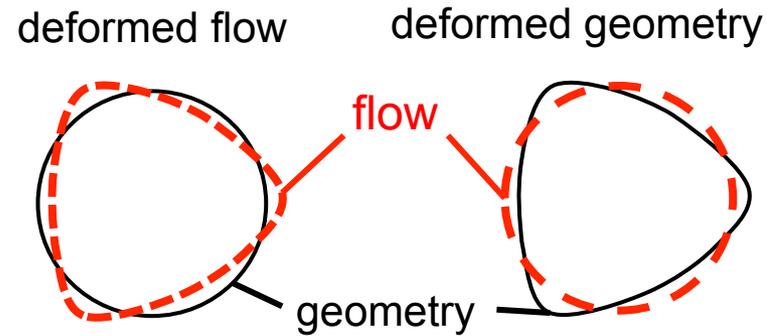
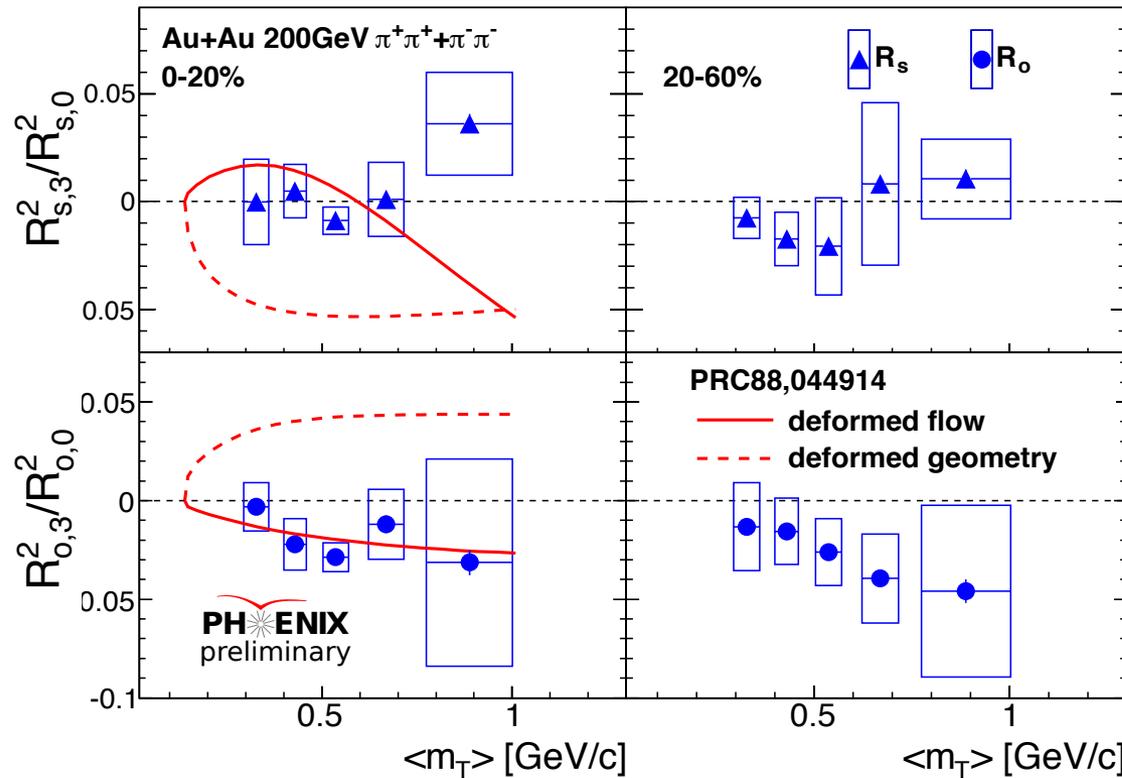
■ Same sign of the R_o oscillation in all k_T bins

m_T dependence of 3rd-order oscillation amplitudes



- $R_{s,3}^2$ are around zero, and does not show any clear m_T dependence.
- $R_{o,3}^2$ has finite negative values in both centrality
 - ✧ In 20-60%, it seems to decrease with m_T .

Comparison with the 3rd-order Gaussian model



- Trend of $R_{o,3}^2$ seems to be explained by “deformed flow” in both centralities.
- ✧ Note that model curves are scaled by 0.3 for the comparison with the data
- $R_{s,3}^2$ seems to show a slight opposite trend to “deformed flow”.
- ✧ Zero~negative value at low m_T , and goes up to positive value at higher m_T
- Contribution from spatial anisotropy seems to be small.

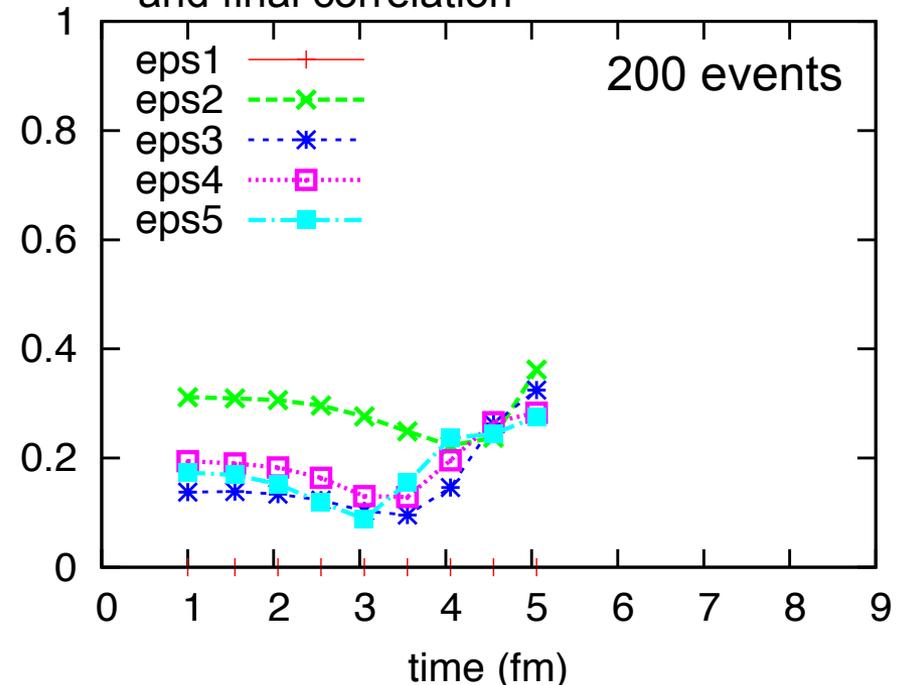
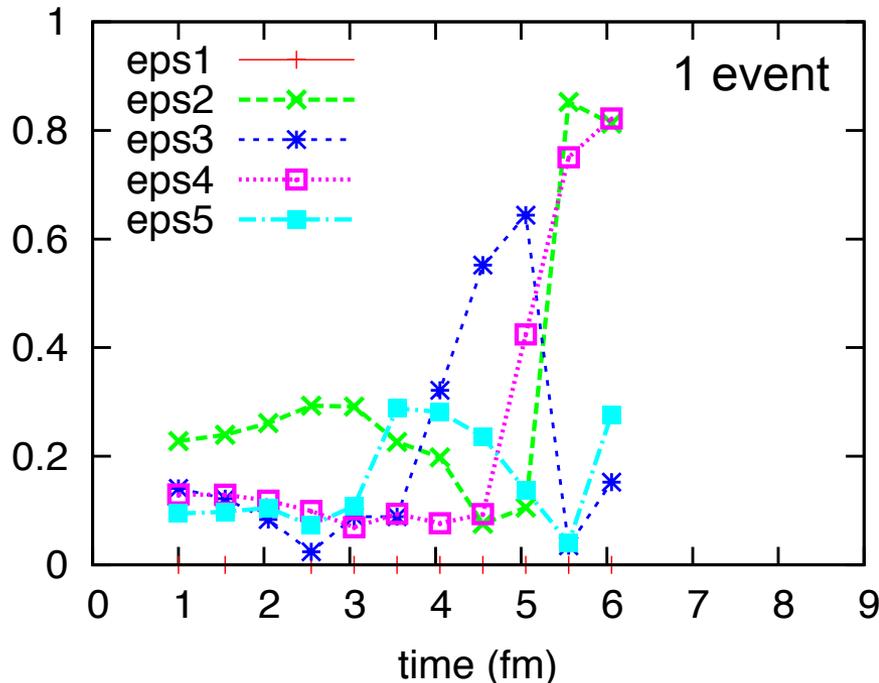
Time evolution of spatial anisotropy

■ MC-KLN + Hydrodynamic model

✧ Parameters are not tuned.

■ 15-20% centrality

C. Nonaka, Aug. 2013,
@2nd workshop on initial fluctuations
and final correlation



- ▲ Inflection points represent that the n^{th} -order deformation of the source turns over.
- ▲ Interesting that ϵ_3 turns over earlier than ϵ_2 .

Summary

- **Azimuthal angle dependence of HBT radii with respect to 3rd-order event plane have been presented.**
- ✧ Finite oscillation of R_o^2 and very weak oscillation of R_s^2 seen in most central event may be explained by the triangular flow anisotropy rather than spatial anisotropy.
- ✧ $R_{o,3}^2$ shows a monotonic decrease with m_T .
 - ✓ Similar trend to “deformed flow” model
- ✧ $R_{s,3}^2$ does not show any clear m_T dependence, but seems to have opposite trend to “deformed flow” model.
- **The result indicate that initial triangularity may be significantly diluted.**

Thank you for your attention!