

# Hard Probes of the QGP: What have we learned and what can we still learn?

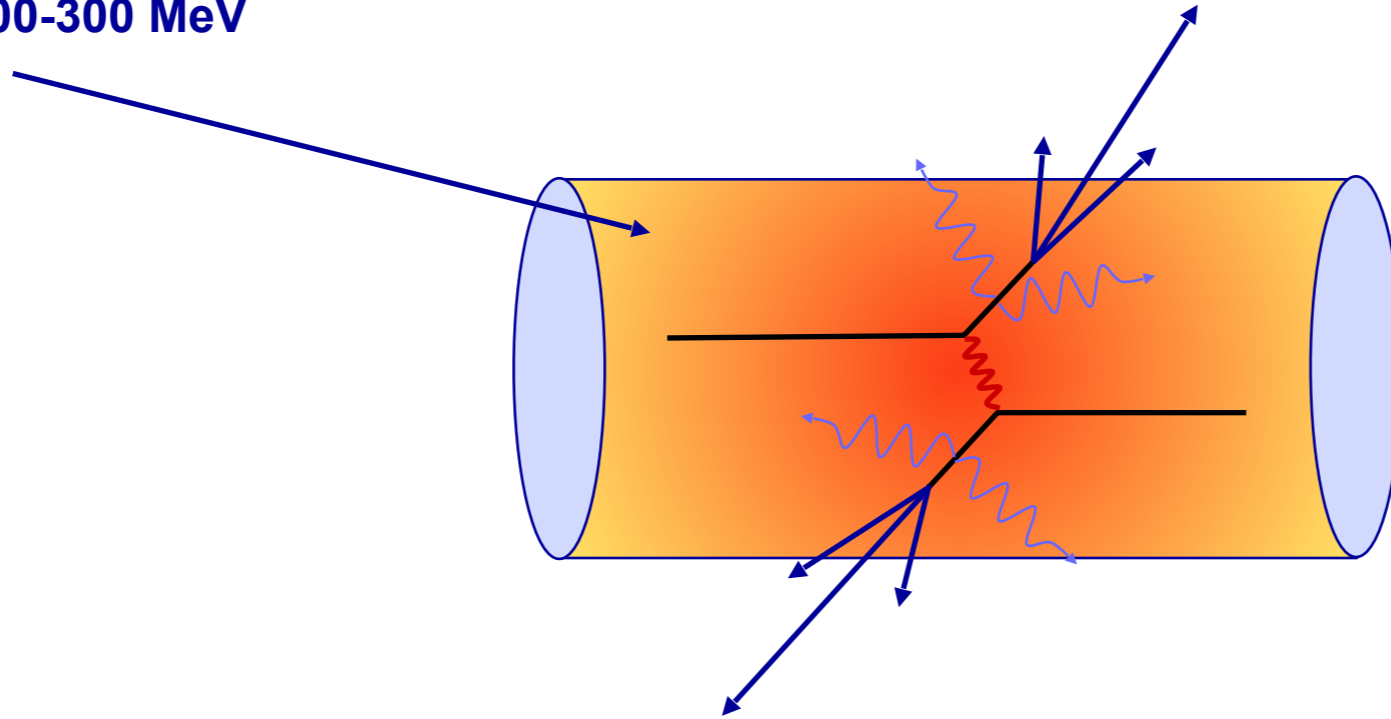
*Marco van Leeuwen,  
Nikhef and Utrecht University*

Heavy Ion Cafe, Tokyo  
27 September 2014



# Soft QCD matter and hard probes

Heavy-ion collisions produce  
QCD matter  
Dominated by soft partons  
 $p \sim T \sim 100\text{-}300\text{ MeV}$



Hard-scatterings produce 'quasi-free' partons  
 $\Rightarrow$  Initial-state production known from pQCD  
 $\Rightarrow$  Probe medium through energy loss

**'Hard Probes': sensitive to medium density, transport properties**

# Hard Probes of the Quark Gluon Plasma

## 1. Understand\* interactions between hard partons and the Quark Gluon Plasma

- Is LPM interference important?
- Is interference between successive parton emissions important?
- Is there a dead cone effect for heavy quarks?
- Are the quark/gluon differences driven by  $C_A/C_F$ , as expected?

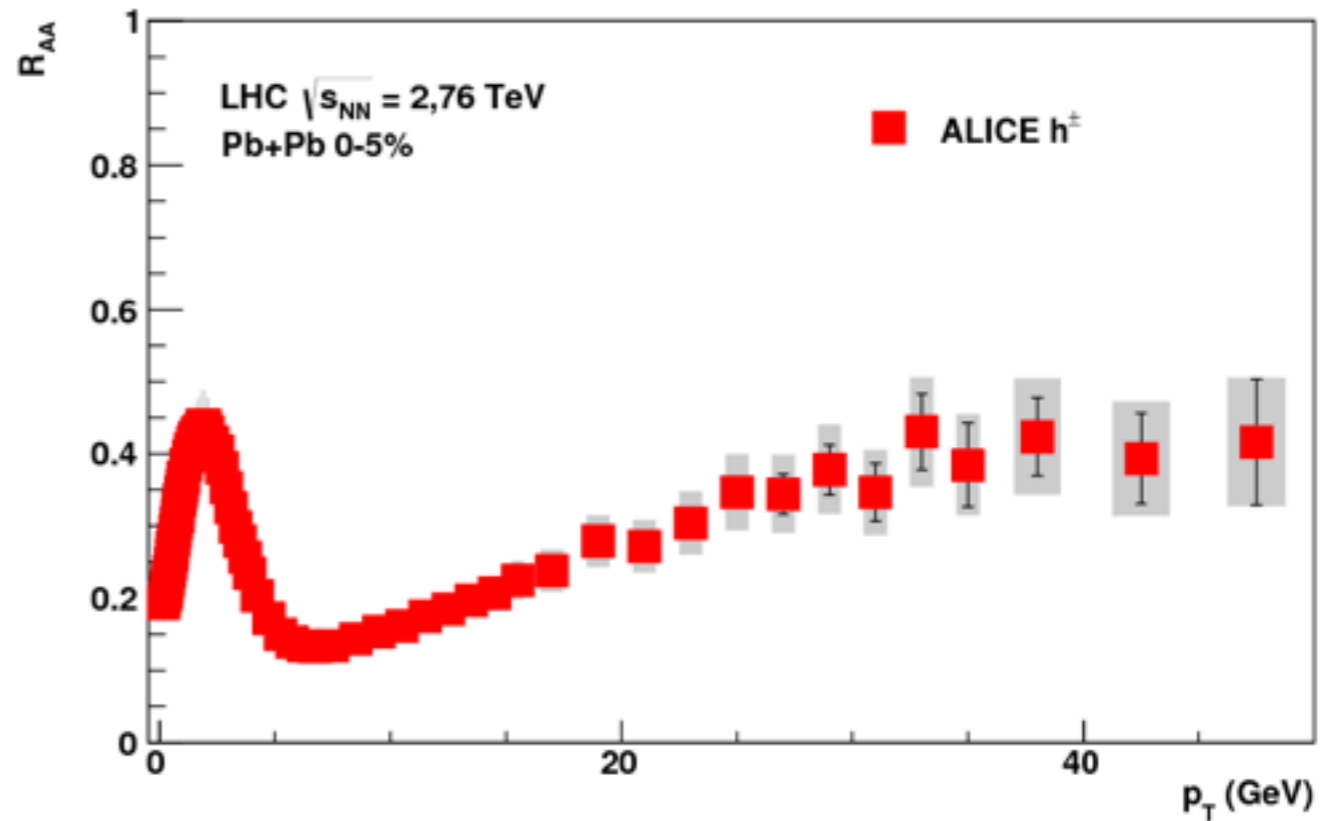
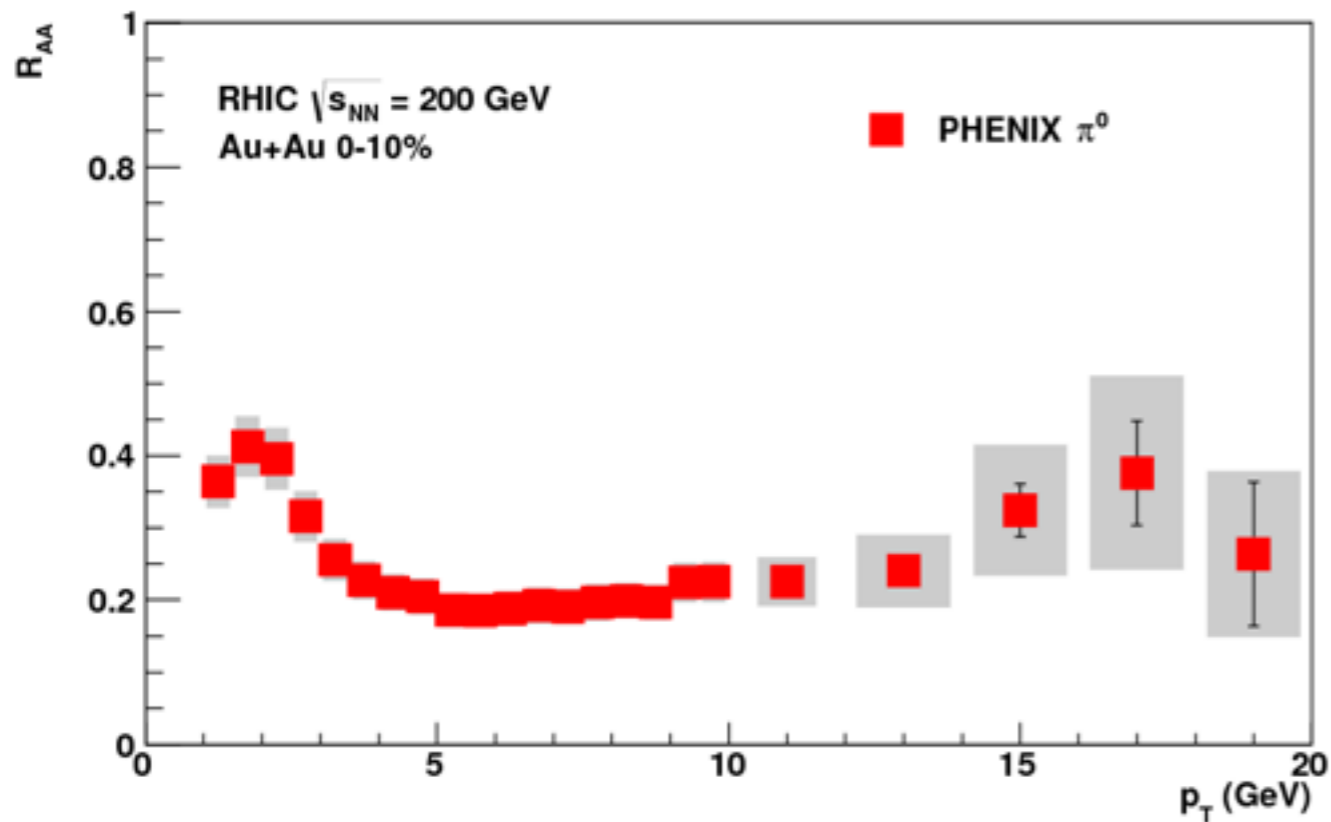
## 2. Use this to learn about the properties of the Quark Gluon Plasma

- General properties: nature of the interactions: scattering centers or fields (strong coupling), effective degrees of freedom? etc
- Specific properties: e.g. density/temperature at RHIC vs LHC

**\*As usual: there is some freedom in defining the question, e.g. we can decide that certain aspects are not tractable and/or uninteresting**

# Nuclear modification factor

$$R_{AA} = \frac{dN / dp_T |_{Pb+Pb}}{N_{coll} dN / dp_T |_{p+p}}$$



Suppression factor 2-6  
Significant  $p_T$ -dependence  
Similar at RHIC and LHC?

**So what does it mean?**

# From RHIC to LHC

RHIC: 200 GeV per nucleon pair  
 LHC: 2.76 TeV

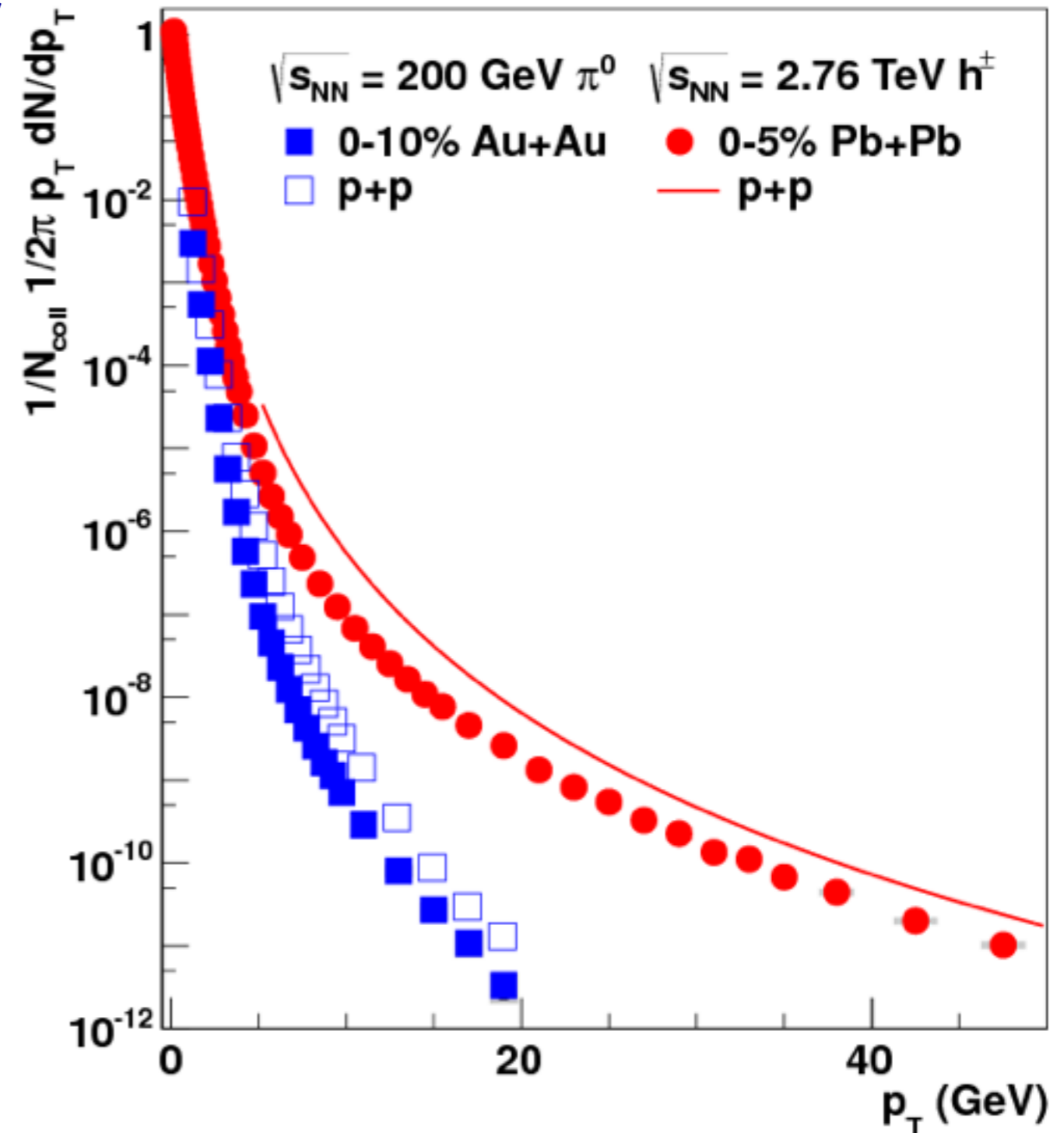
Energy ~14 x higher

LHC: spectrum less steep,  
 larger  $p_T$  reach

$$\frac{1}{2\pi p_T} \frac{dN}{dp_T} \propto p_T^{-n}$$

RHIC:  $n \sim 8.2$

LHC:  $n \sim 6.4$



# Back-of-the envelope considerations

Just to get a sense of the numbers:

- Take the hadron spectra and apply ‘energy loss’

$$\frac{1}{2\pi p_T} \frac{dN}{dp_T} \propto p_T^{-n}$$

- Two scenarios:

- Constant relative energy loss  $\Delta E/E$

- $R_{AA}$  constant for a power law spectrum  $R_{AA} = \left(1 - \frac{\Delta E}{E}\right)^{n-2}$

- Constant energy loss  $\Delta E$

- $R_{AA}$  increases with  $p_T$  for a power law spectrum

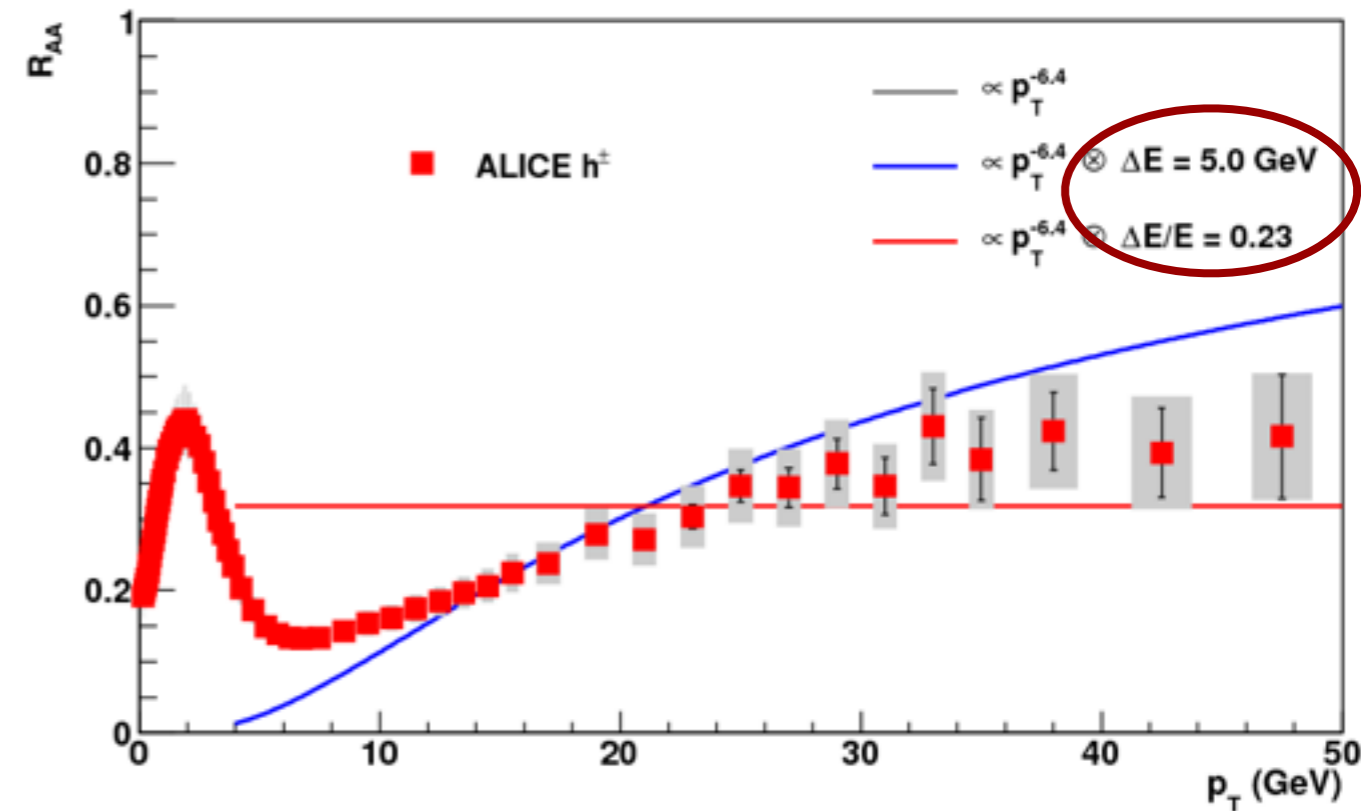
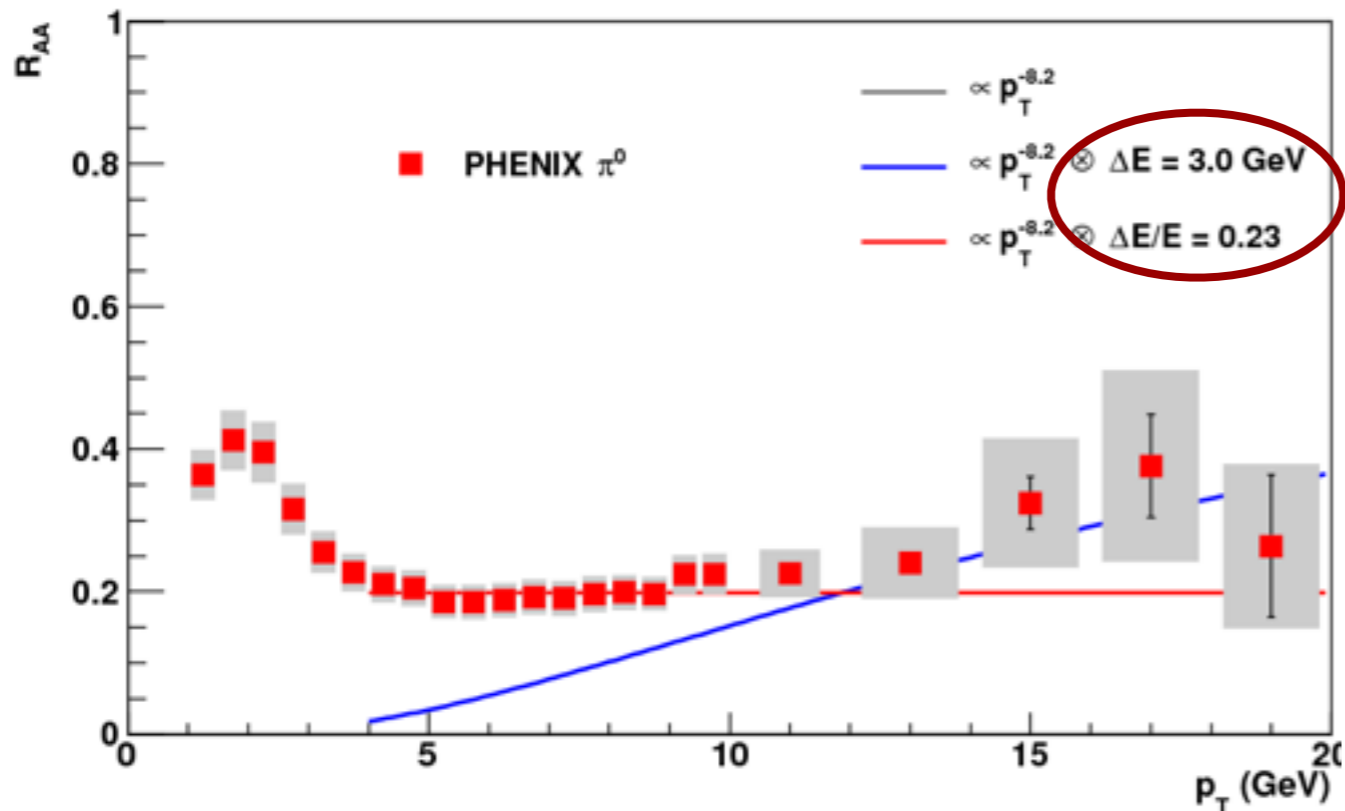
**$R_{AA}$  depends on  $n$ , steeper spectra, smaller  $R_{AA}$**

# From RHIC to LHC

## Back-of-the envelope considerations

**RHIC**

**LHC**



**RHIC:  $n \sim 8.2$**

**LHC:  $n \sim 6.4$**

$$(1 - 0.23)^{6.2} = 0.20$$

$$(1 - 0.23)^{4.4} = 0.32$$

Qualitative lessons:

- 1) Similar  $R_{AA}$  at LHC means larger energy loss
- 2) Increase of  $R_{AA}$  with  $p_T$ : relative energy loss not constant  
Expect: constant  $\Delta E$ , or log increase + kinematic limits

# Towards a more complete picture

- Energy loss not single-valued, but a distribution
- Geometry: density profile; path length distribution
- Energy loss is partonic, not hadronic
  - Full modeling: medium modified shower
  - Simple ansatz for leading hadrons: energy loss followed by fragmentation
  - Quark/gluon differences



# First generation models

Parton spectrum **Energy loss distribution** Fragmentation (function)

$$\left. \frac{dN}{dp_T} \right|_{hadr} = \left[ \left. \frac{dN}{dE} \right|_{jets} \right] \otimes P(\Delta E) \otimes D(p_{T,hadr} / E_{jet})$$

known pQCDxPDF      extract      'known' from e<sup>+</sup>e<sup>-</sup>

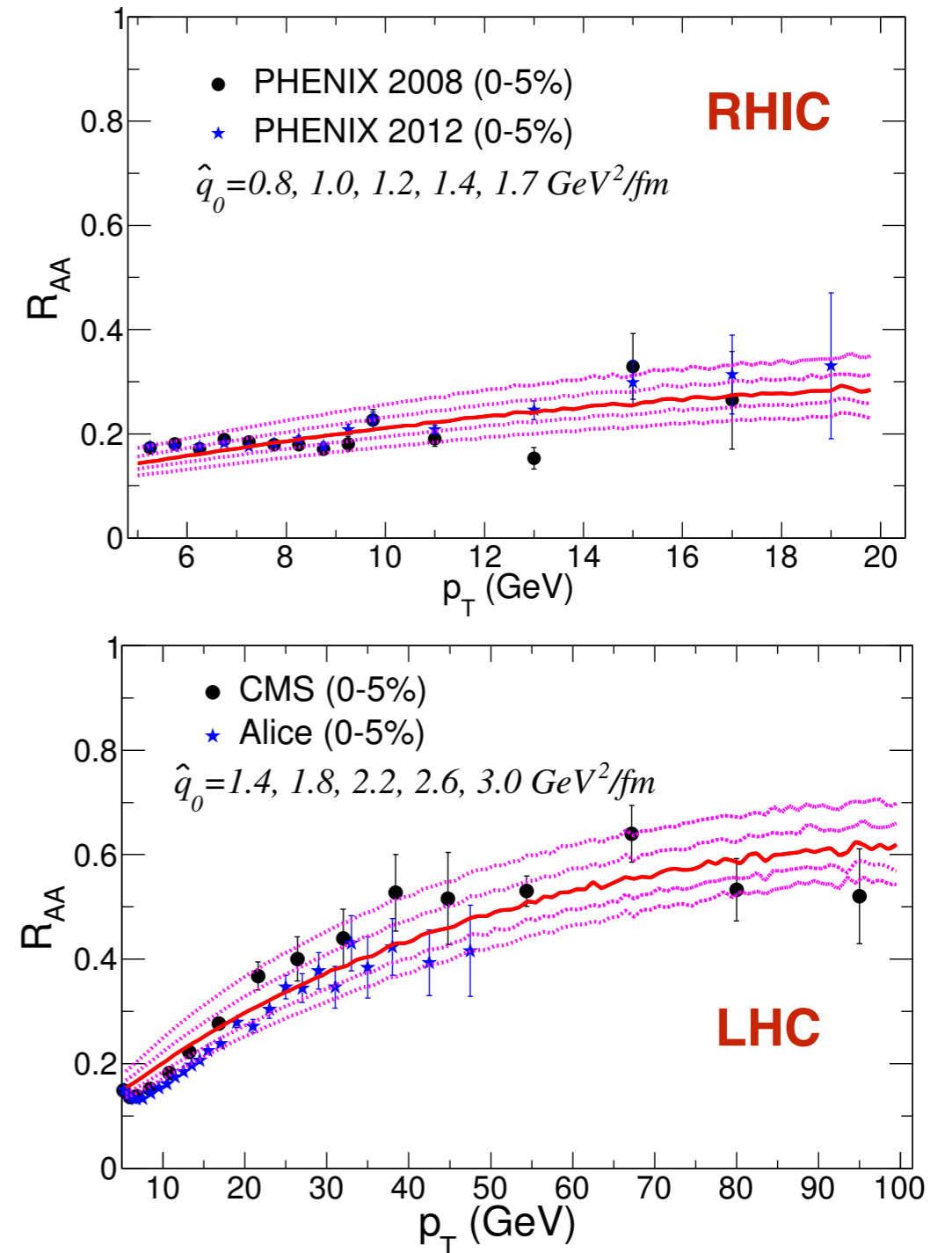
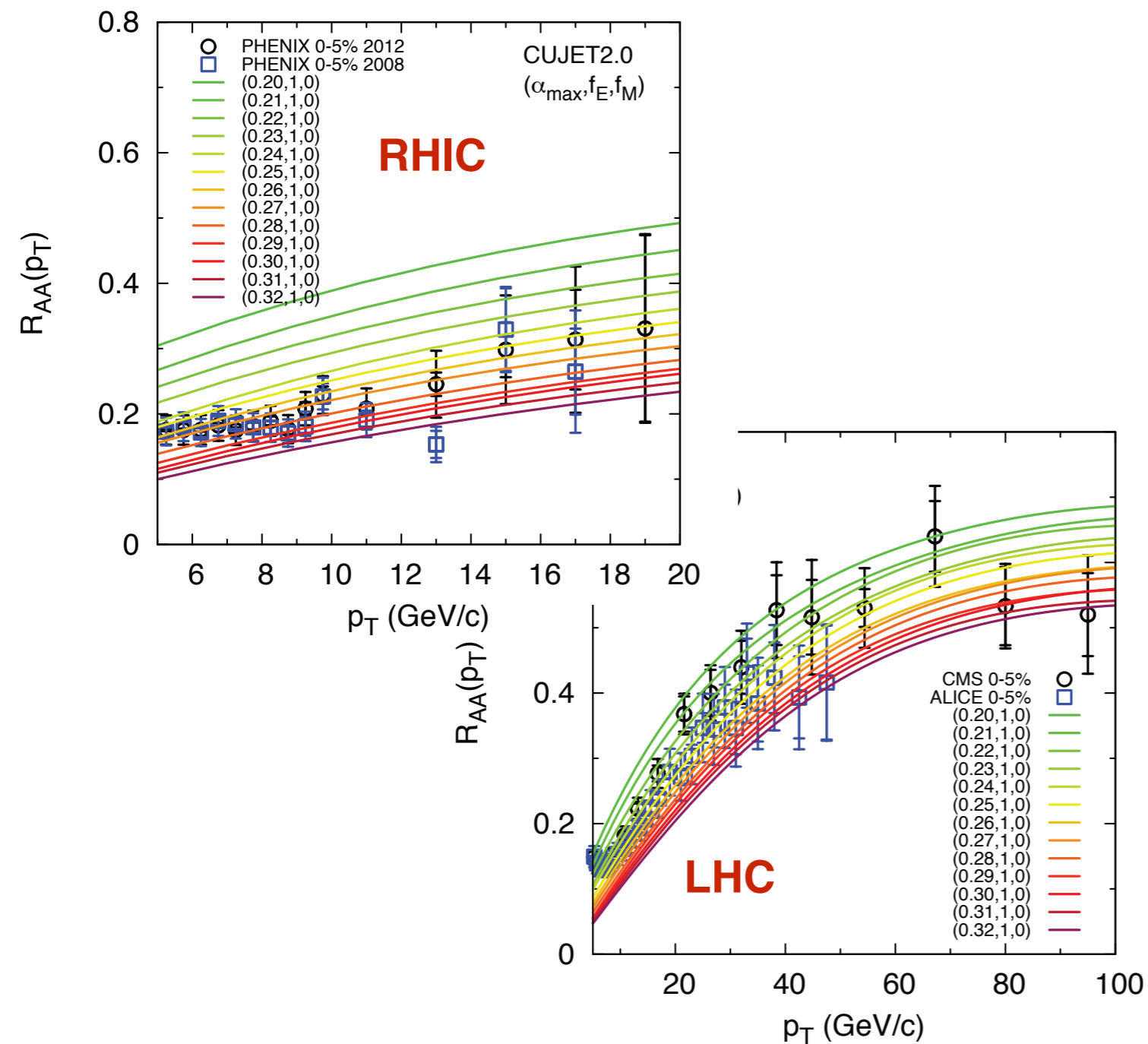
**This is where the information about the medium is**

$P(\Delta E)$  combines geometry  
with the intrinsic process  
– Unavoidable for many observables

Notes:

- This is the simplest ansatz – most calculation to date use it (except some MCs)
- Jet,  $\gamma$ -jet measurements 'fix' E, removing one of the convolutions

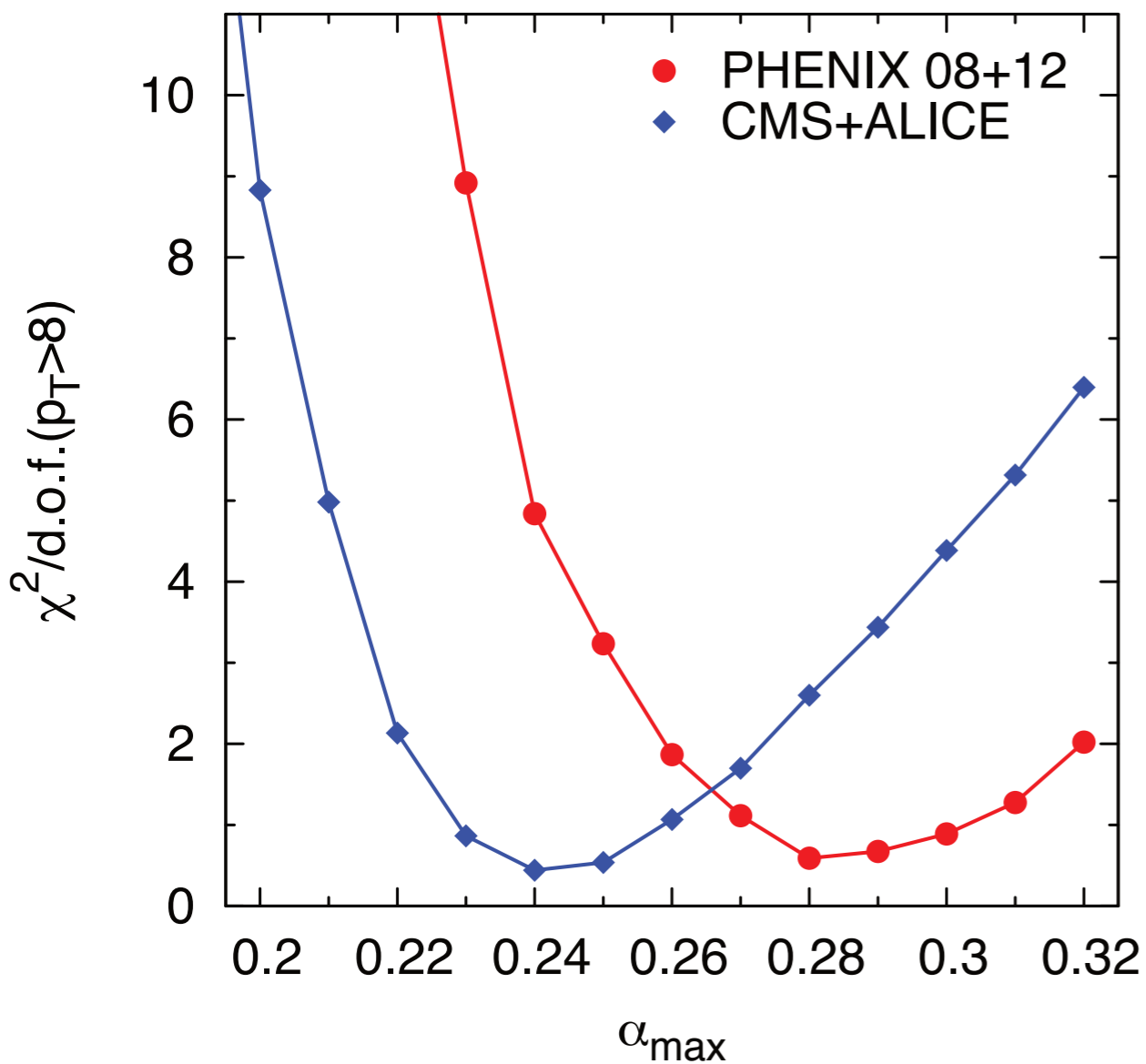
# Finding $q_{\text{hat}}$ from data at RHIC and LHC



Systematic comparison of energy loss models with data  
 Medium modeled by Hydro (2+1D, 3+1D)  
 **$p_T$  dependence matches reasonably well**

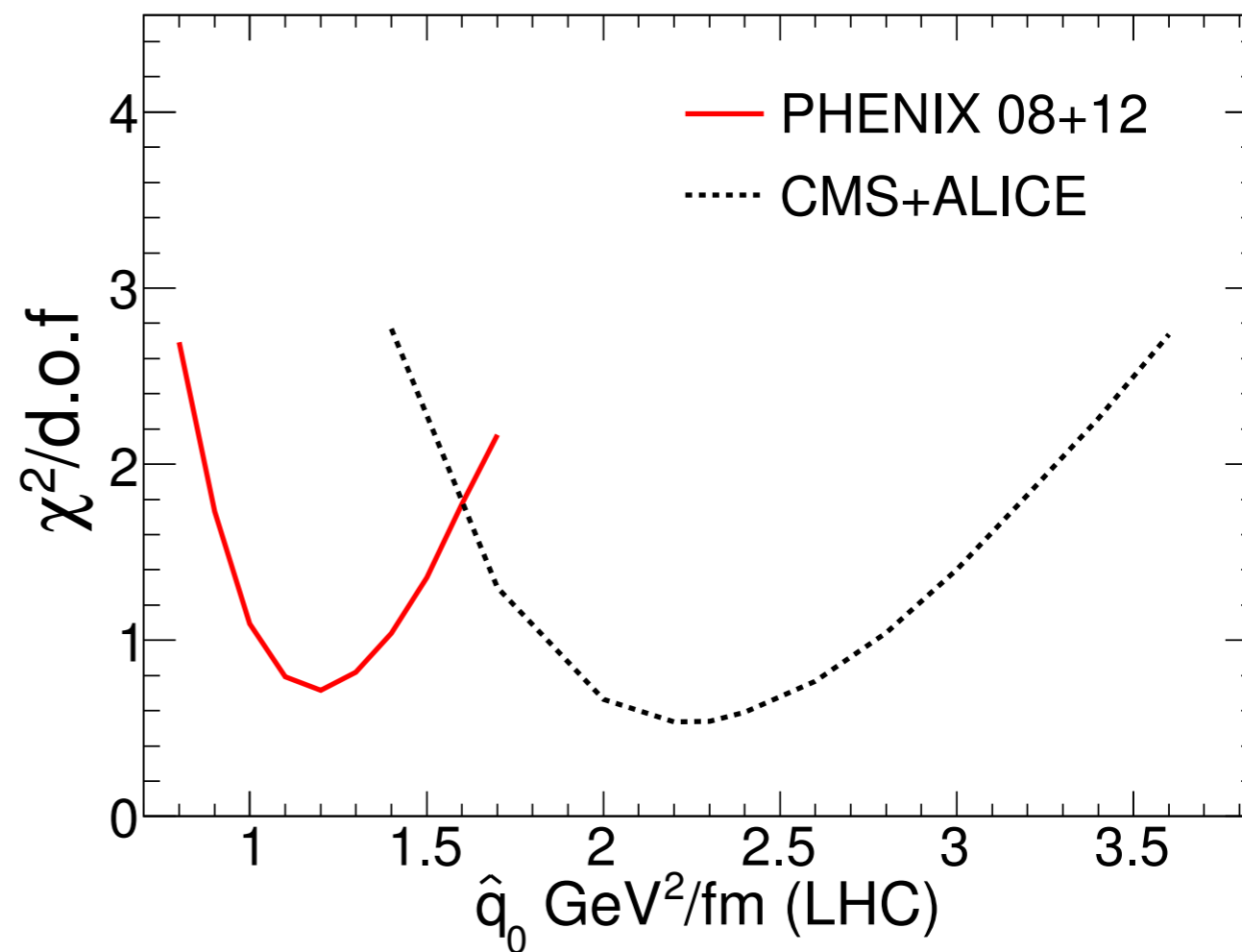
# Fitting the jet quenching parameter

## CUJET 2.0



CUJET:  $\alpha_s$  is medium parameter  
Lower at LHC

## HT-BW



HT: transport coeff is parameter  
Higher at LHC



# Are we done with qhat?

**Not at all!**

There are significant conceptual problems with the baseline models

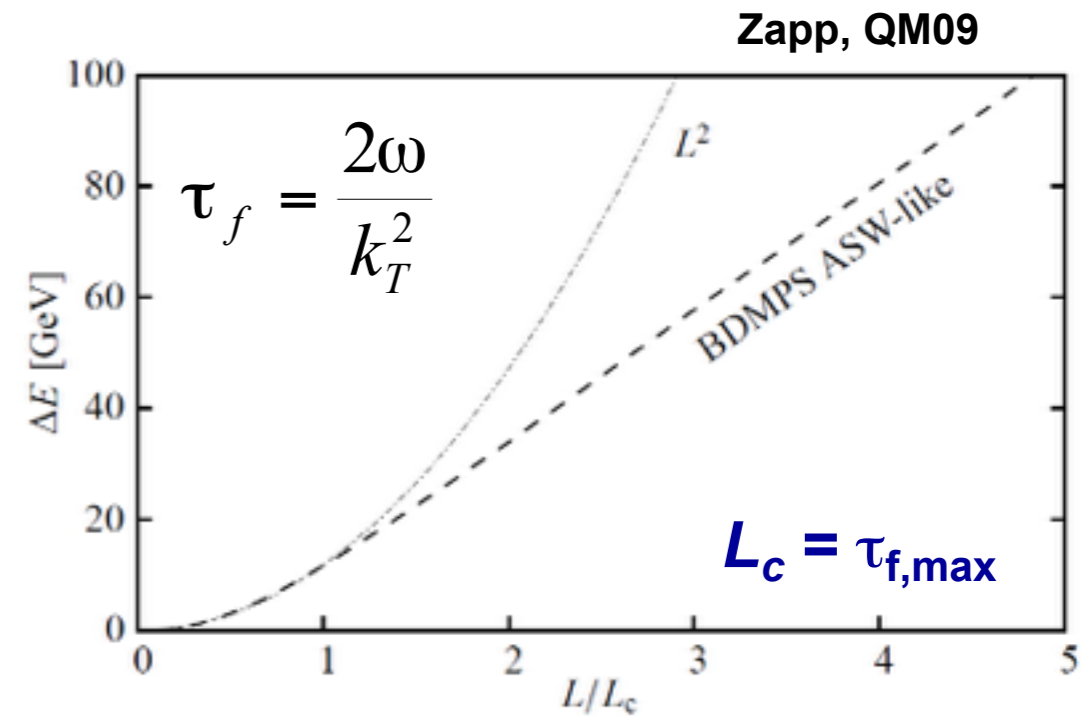
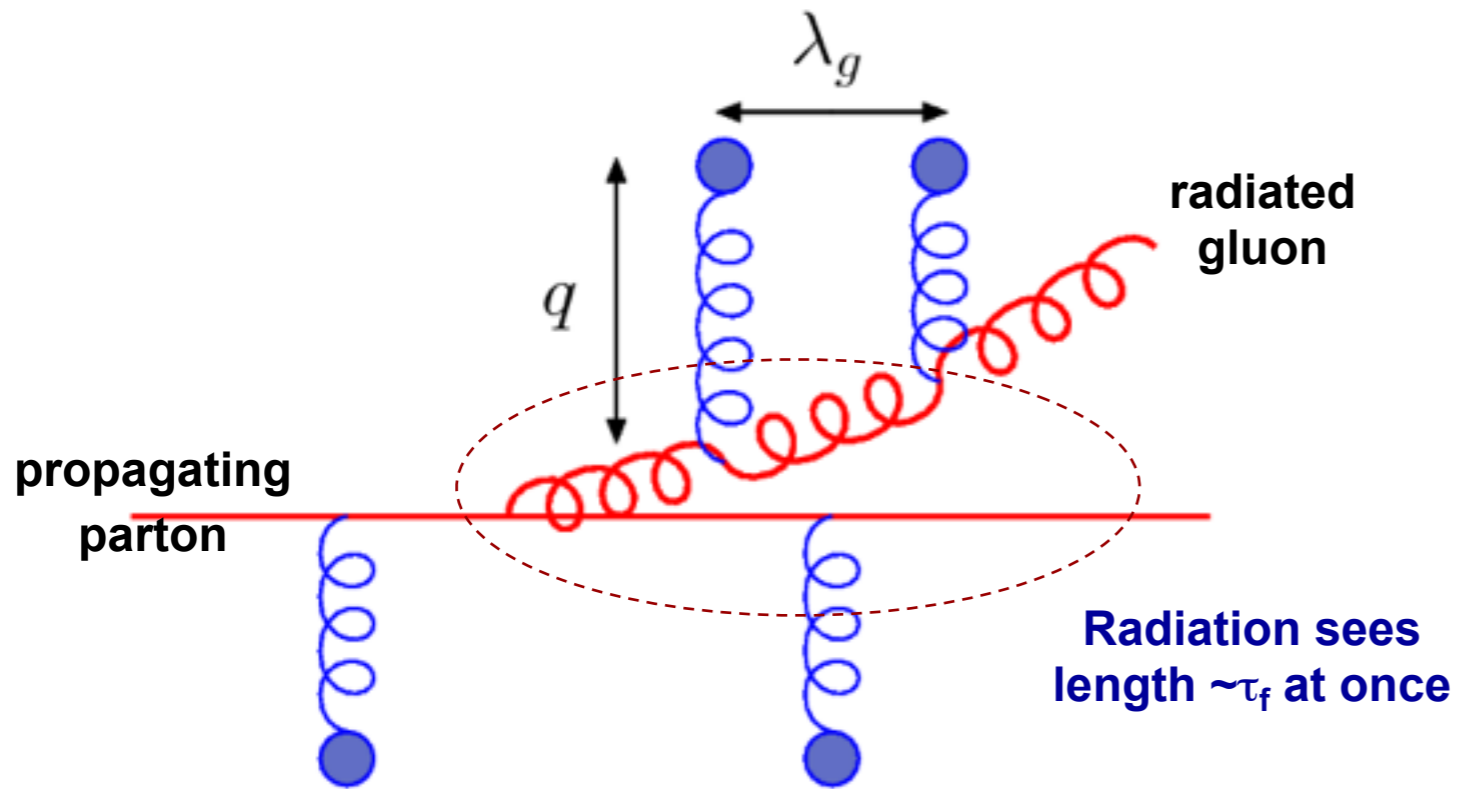
**Main open questions for  $R_{AA}$ -type observables:**

- **Large angle radiation,  $k_T \sim k$** 
  - Not treated in any of the ‘analytical’ calculations
  - Important for phenomenology
  - Path to solution: include NLO/recoil
- **Large  $x$ ,  $\Delta E \sim E$** 
  - Some large  $x$  results/estimates exist; still eikonal?
  - Probably not important for medium-high  $p_T$
- **Path averaging**
  - Not much work done; not simple due to interference
  - Possible solution: brute force; integrate path integral over scattering centers (Zakharov)
- **Multiple gluon emission**
  - Most calculations use independent emission
  - May suffice for leading hadrons, but jet observables need a more complete treatment

We can hope/argue that the impact of these on qualitative picture may be limited, but quantitative conclusions require a closer look

# Medium-induced radiation

Landau-Pomeranchuk-Migdal effect  
Formation time important



Energy loss depends on density:  $\lambda \propto \frac{1}{\rho}$

and nature of scattering centers  
(scattering cross section)

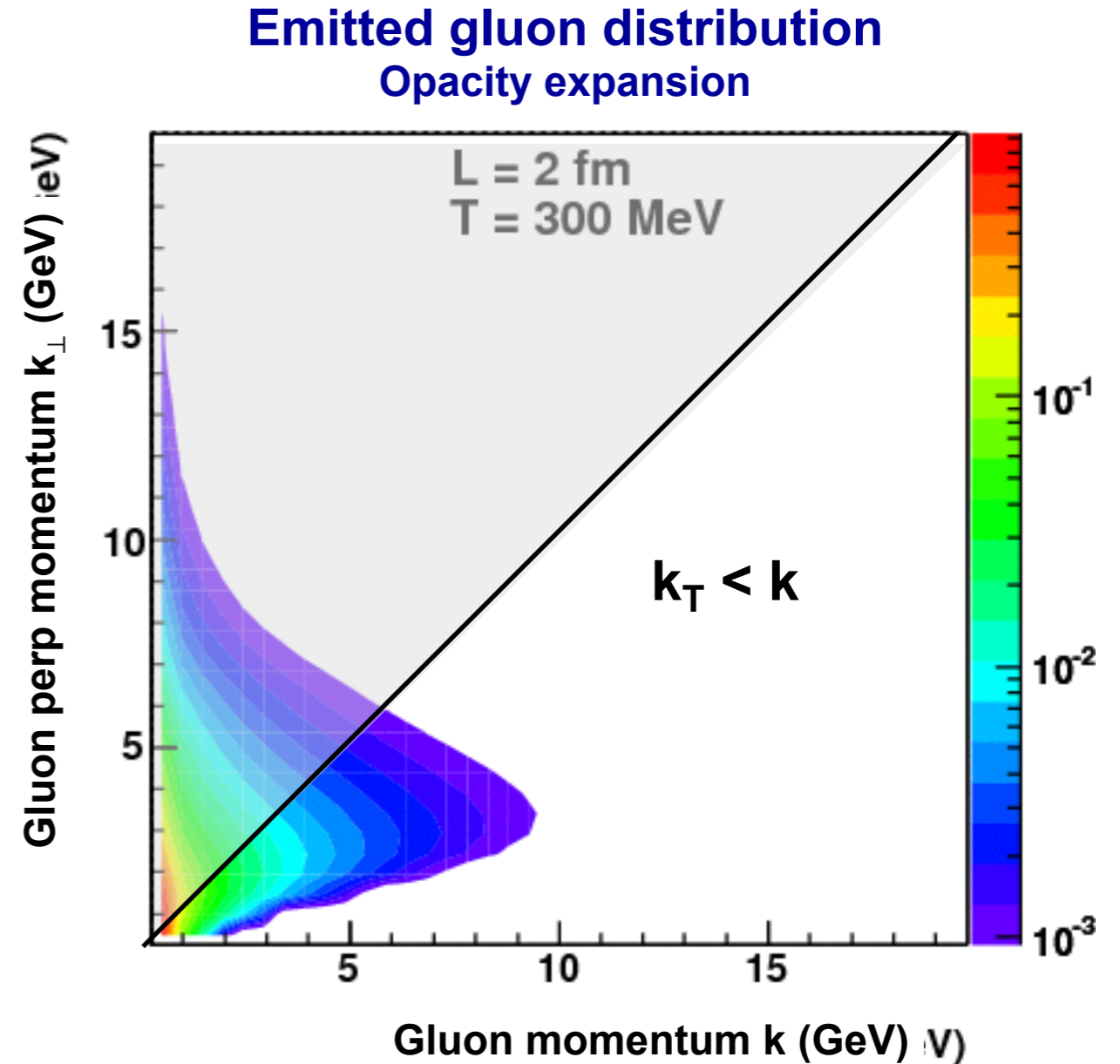
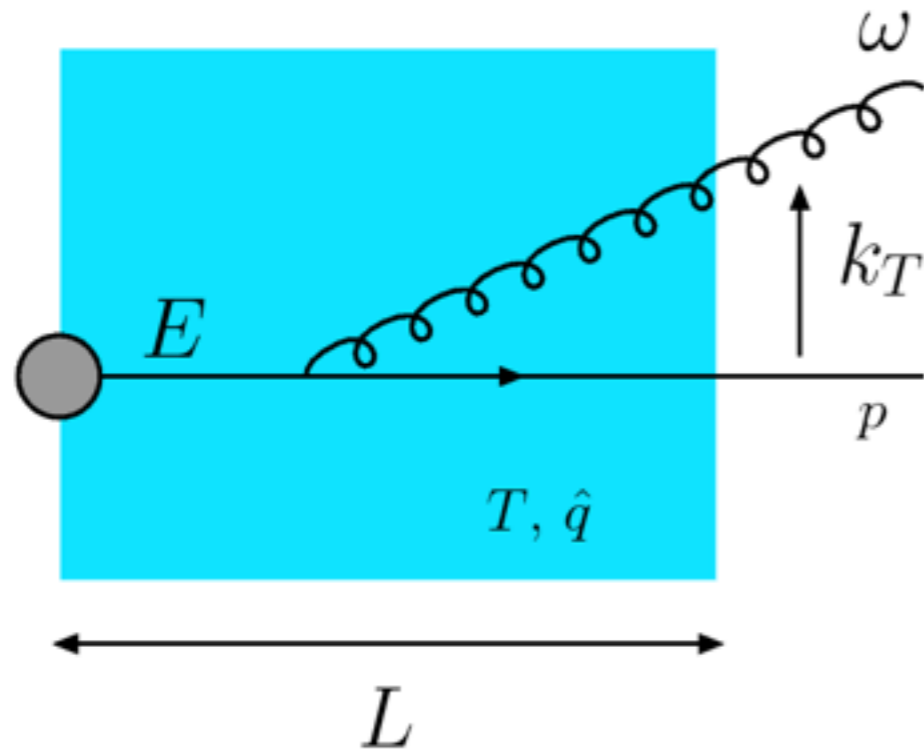
Transport coefficient  $\hat{q} \equiv \frac{\langle q_{\perp}^2 \rangle}{\lambda}$

If  $\lambda < \tau_f$ , multiple scatterings  
add coherently

$$\Delta E_{med} \sim \alpha_s \hat{q} L^2$$

# Large angle radiation

TECHQM 'brick report', arXiv:1106.1106



Calculated gluon spectrum extends to large  $k_{\perp}$  at small  $k$   
Outside kinematic limits

GLV, ASW, HT cut this off 'by hand'

# Effect of large angle radiation

Opacity expansion formalisms

Expand in powers of  $\frac{L}{\lambda}$

Different definitions of  $x$ :

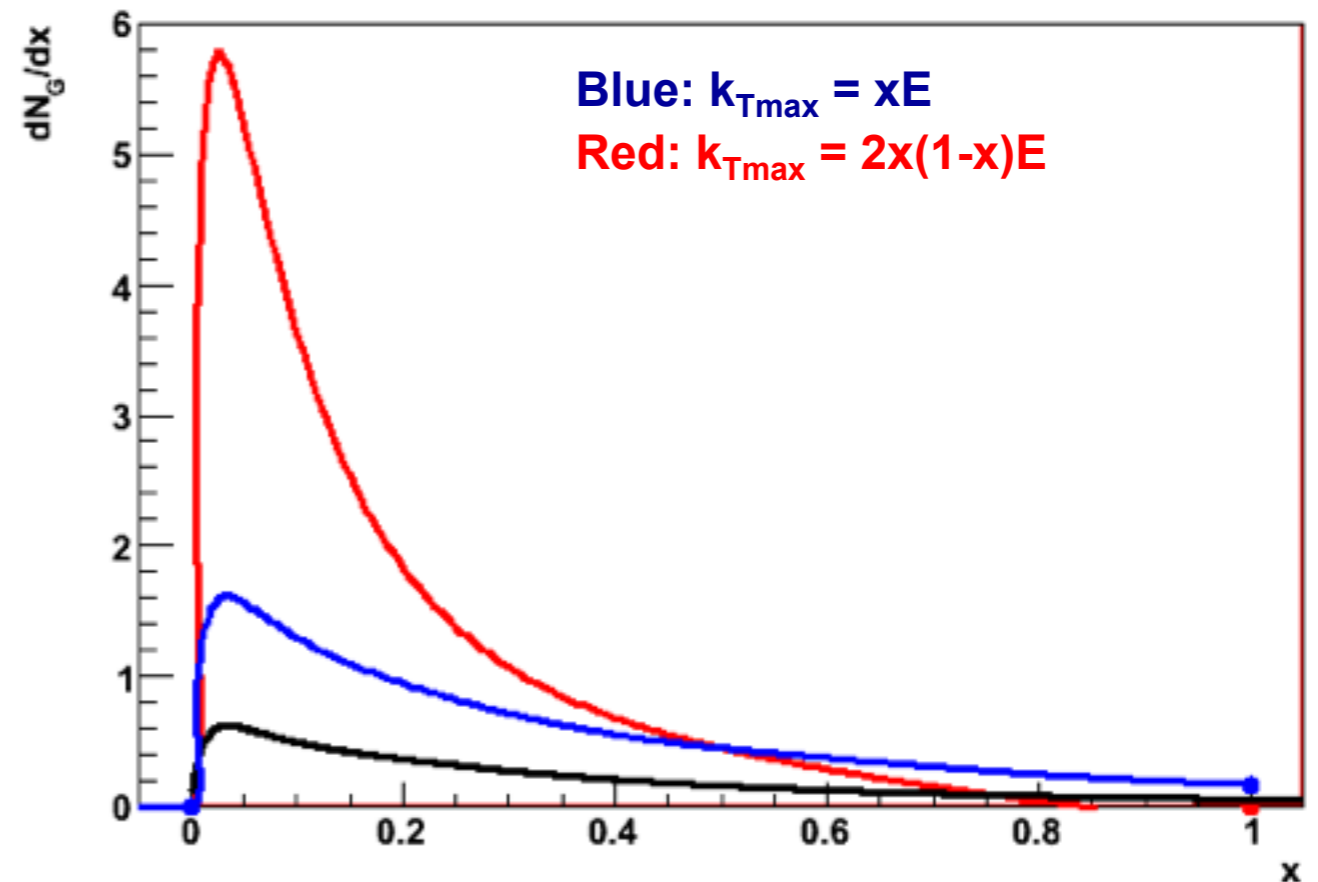
ASW:  $x_E = \frac{\omega}{E}$       GLV:  $x_+ = \frac{\omega_+}{E_+}$

Different large angle cut-offs:

$k_T < \omega = x_E E$

$k_T < \omega = 2 x_+ E$

Single-gluon spectrum

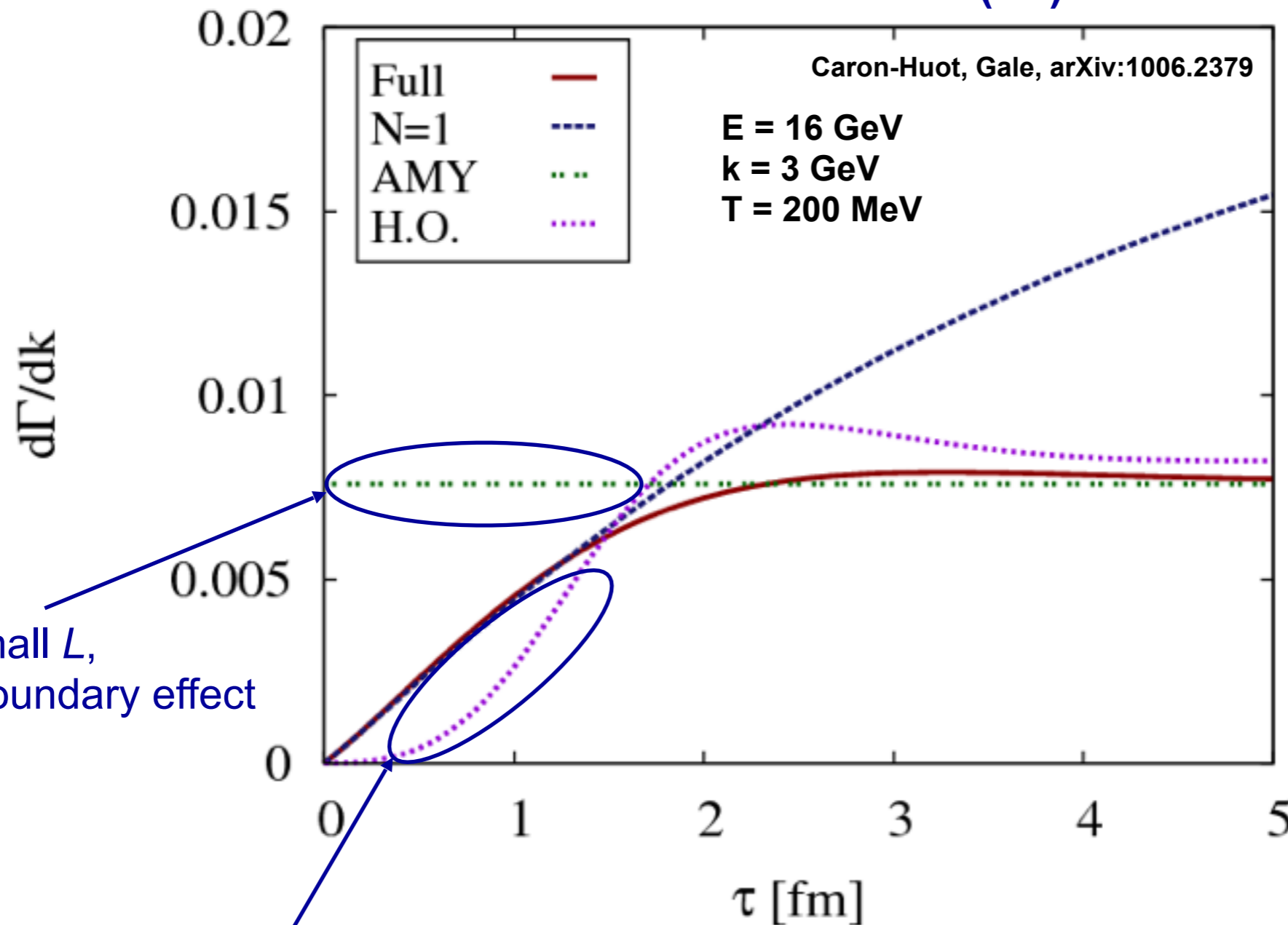


**Factor ~2 uncertainty  
from large-angle cut-off**



# $L$ -dependence; regions of validity?

Emission rate vs  $\tau$  ( $=L$ )



GLV  $N=1$   
 Too much radiation  
 at large  $L$   
 (no interference  
 between scatt centers)

Full =  
 numerical solution of  
 Zakharov path integral  
 = 'best we know'

AMY, small  $L$ ,  
 no  $L^2$ , boundary effect

H.O. = ASW/BDMPS like (harmonic oscillator)  
 Too little radiation at small  $L$   
 (ignores 'hard tail' of scatt potential)

Agreement of medium density for  
 AMY, GLV/CUJET fits is a coincidence  
 Multiple soft tends to give smallest E-loss,  
 but may be most accurate?

# Energy loss formalisms

- Large differences between formalisms understood
  - Large angle cut-off
  - Length dependence (interference effects)
- Mostly (?) ‘technical’ issues; can be overcome
  - Use path-integral formalism
  - Monte Carlo: exact  $E$ ,  $p$  conservation
    - Full 2→3 NLO matrix elements
    - Include interference

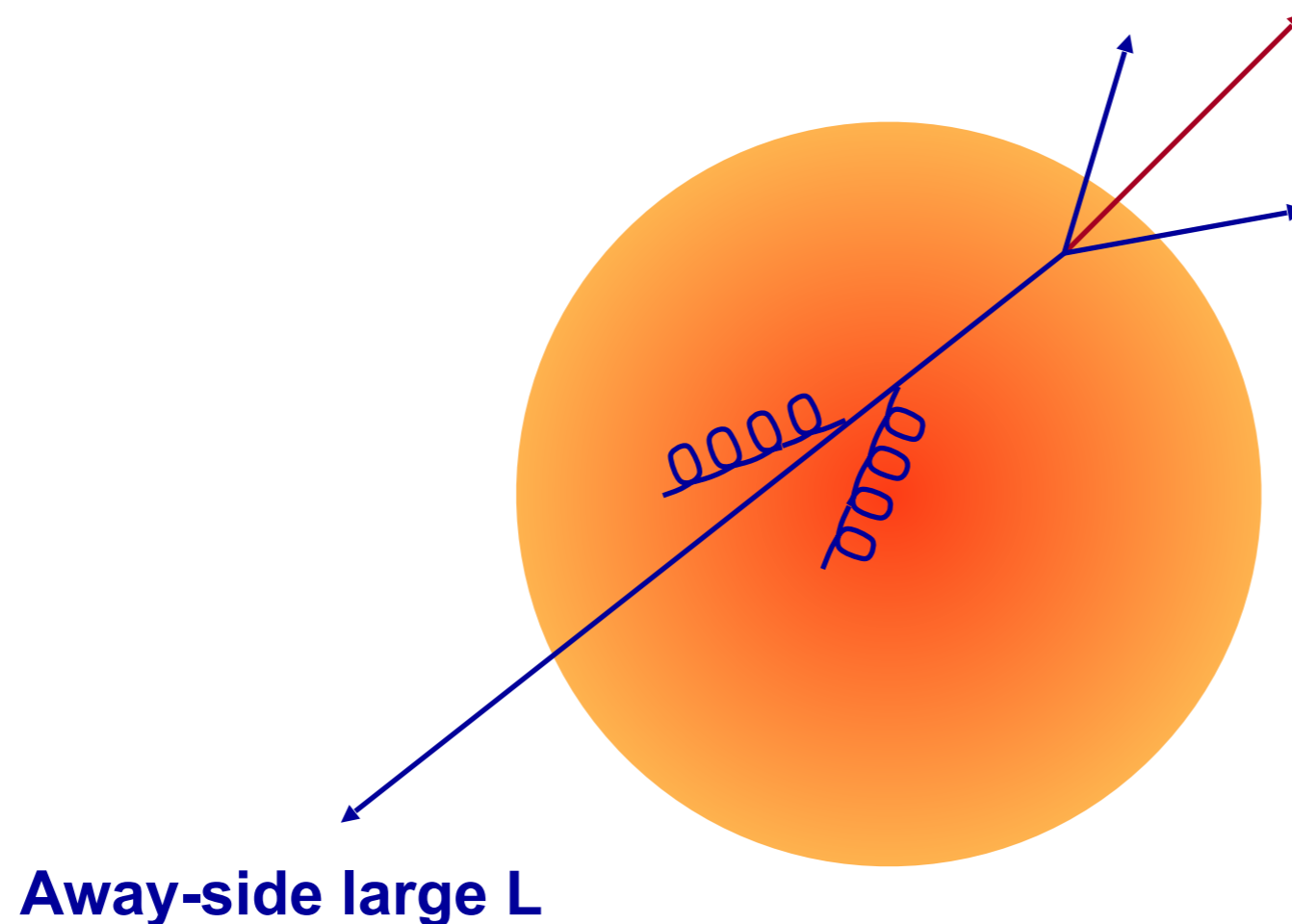
**Plenty of room for interesting and relevant theory work!**

Current progress on:

- Interference in multiple gluon emission: ‘antenna radiation’
- Some work on non-eikonal propagation
- Monte-Carlo approaches for  $E$ ,  $p$  conservation (JEWEL, q-PYTHIA, YaJEM, MARTINI)

# Path length dependence: 'surface bias'

Near side trigger,  
biases to small E-loss

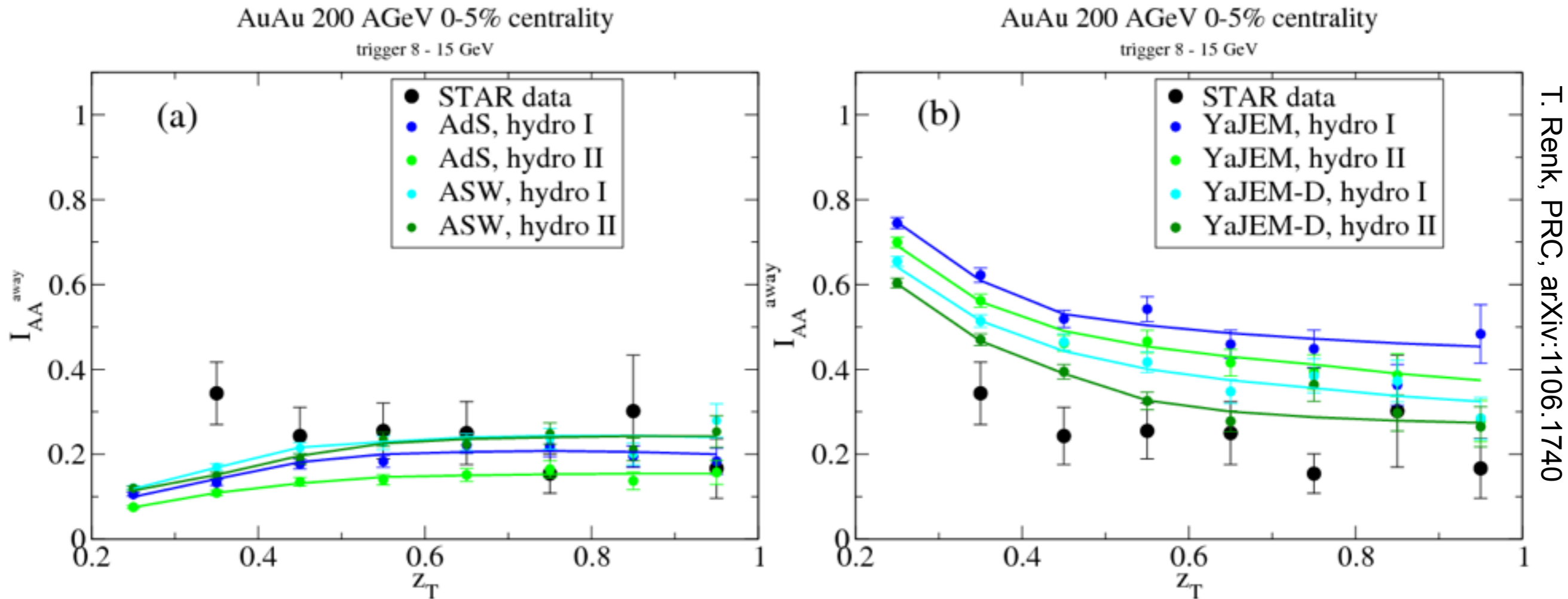


Away-side (recoil) suppression  $I_{AA}$  samples  
longer path-lengths than  $R_{AA}$

NB: other effects play a role: quark/gluon composition, spectral shape (less steep for recoil)

# Di-hadron modelling

Model 'calibrated' on single hadron  $R_{AA}$



$L^2$  (ASW) fits data  
 $L^3$  (AdS) slightly below

$L$  (YaJEM): too little suppression  
 $L^2$  (YaJEM-D) slightly above

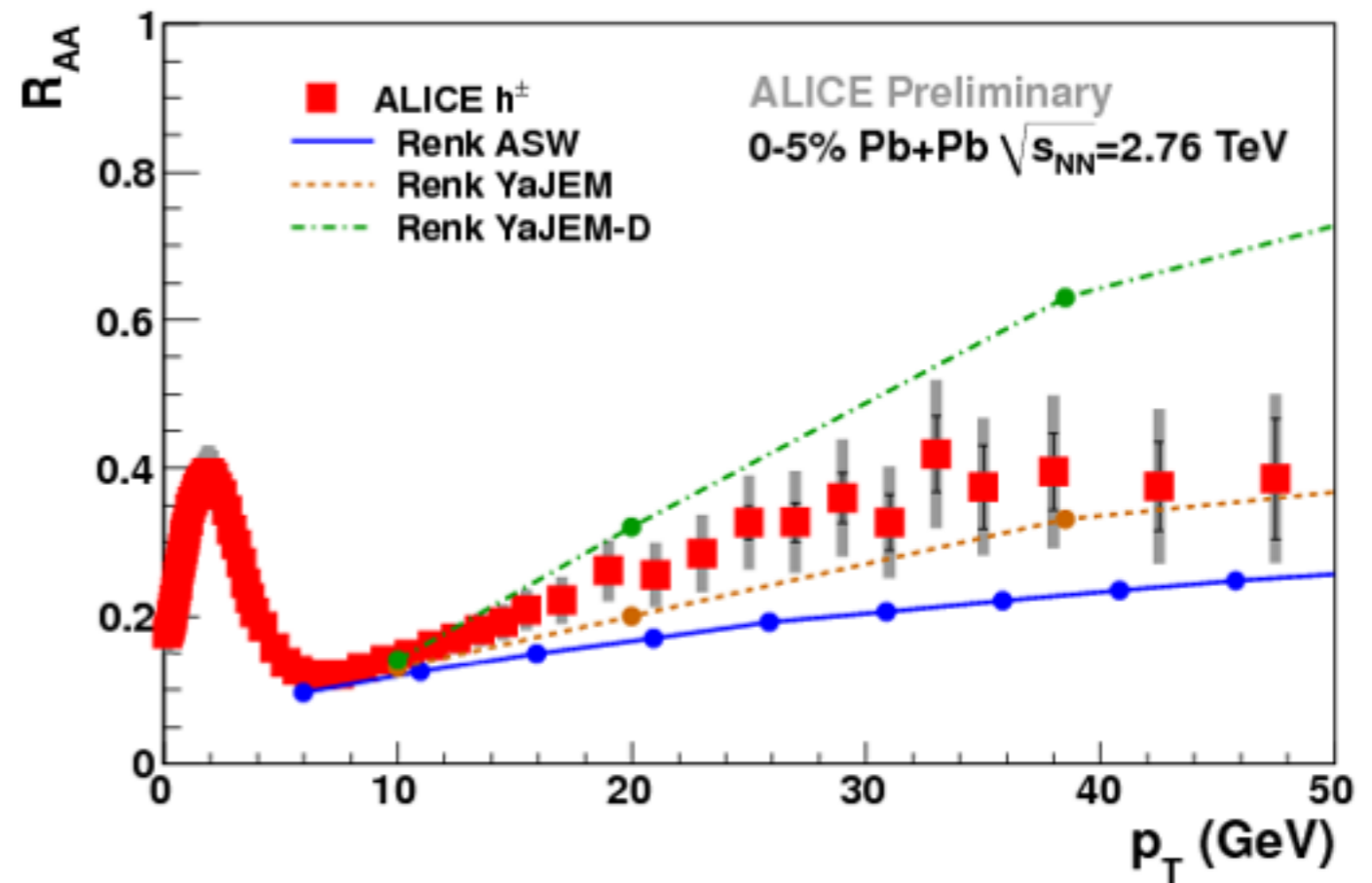
Modified shower  
 generates increase at low  $z_T$

Di-hadron suppression is (probably?) a more robust probe of path length dependence than the more obvious observables:  $v_2$ , centrality dependence

# Di-hadrons and single hadrons at LHC

Need simultaneous comparison to several measurements to constrain geometry and E-loss

Here:  $R_{AA}$  and  $I_{AA}$



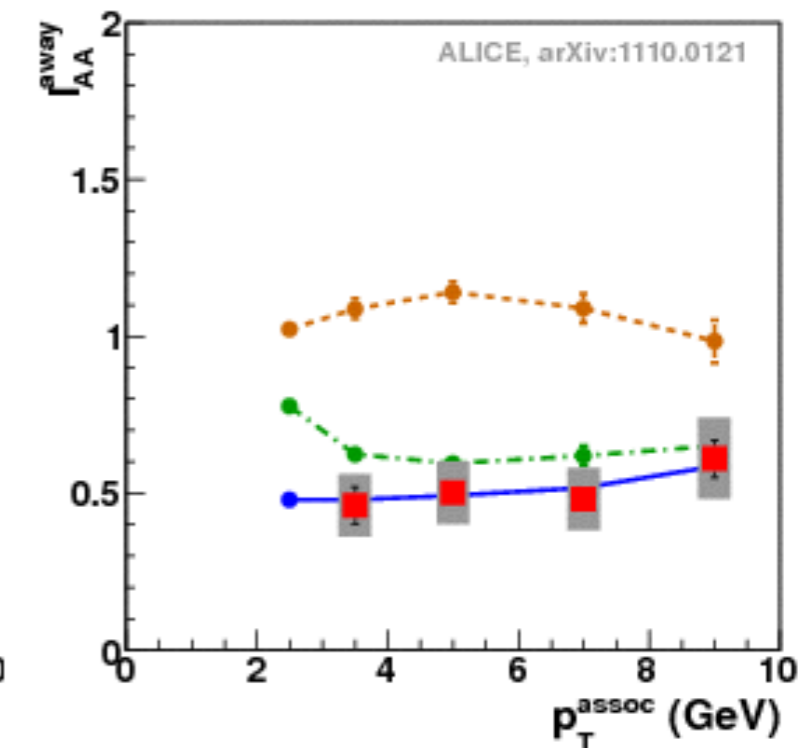
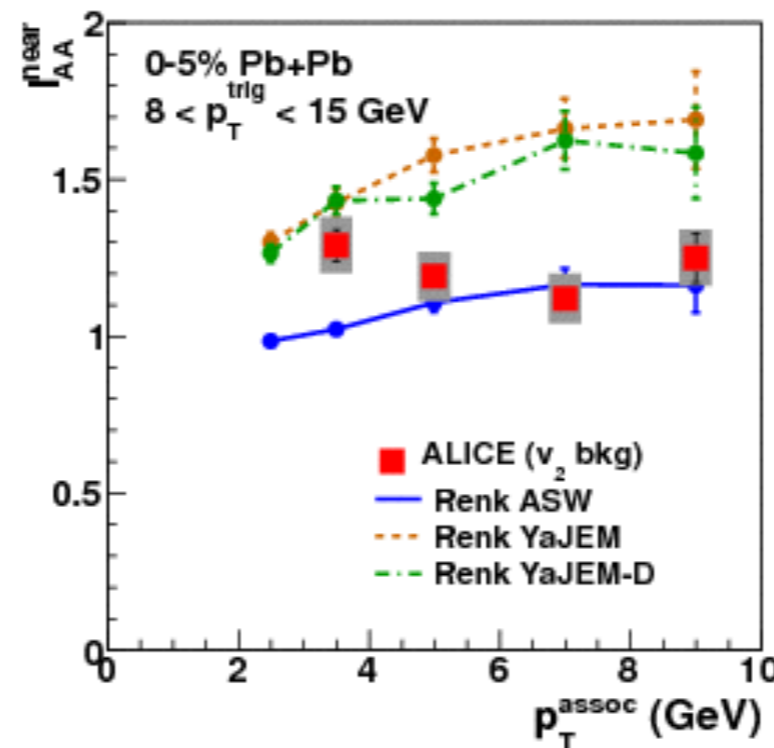
Three models:

ASW: radiative energy loss

YaJEM: medium-induced virtuality

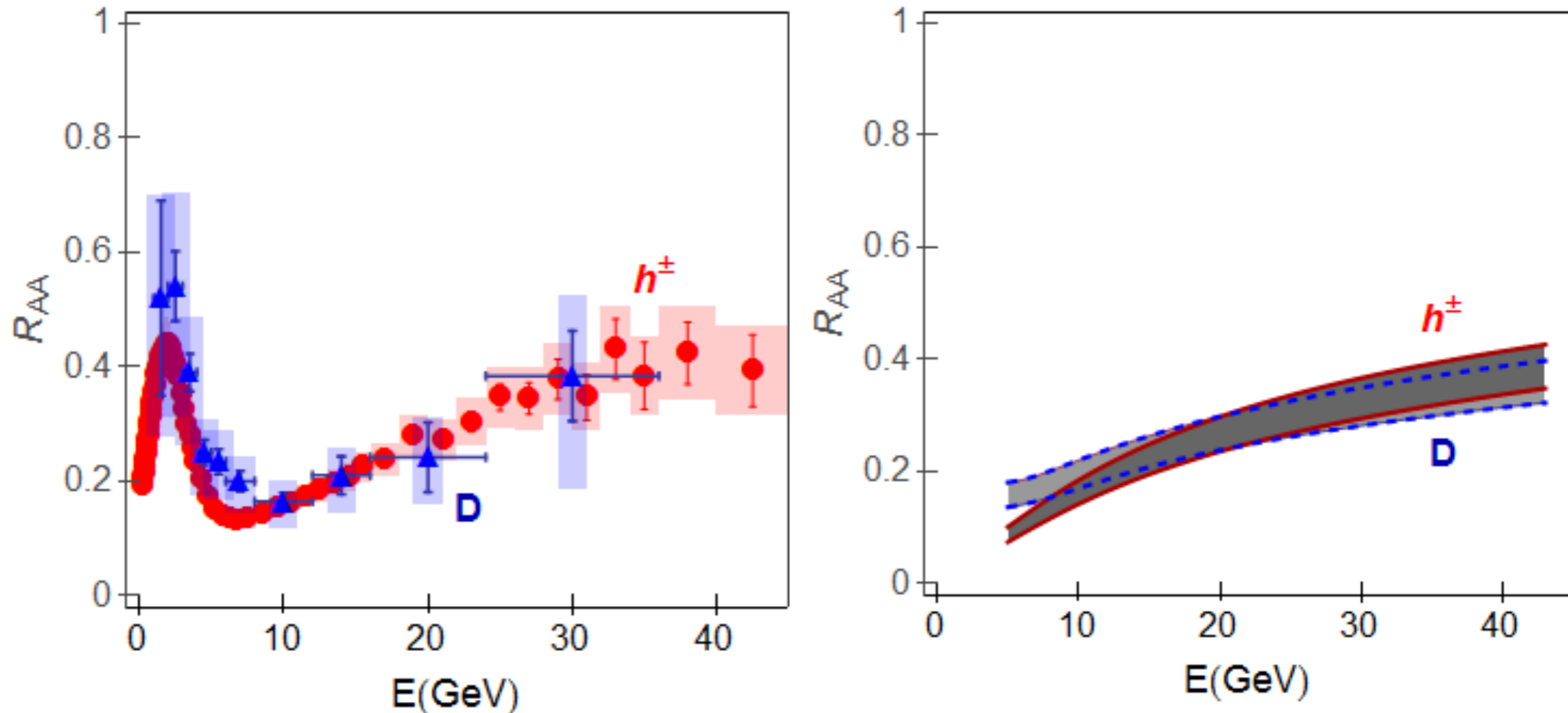
YaJEM-D: YaJEM with L-dependent virtuality cut-off (induces  $L^2$ )

NB: would like to see a more precise evaluation a la RHIC results



# Heavy flavour energy loss

M. Djordjevic<sup>2</sup>, PRL 112, 042302

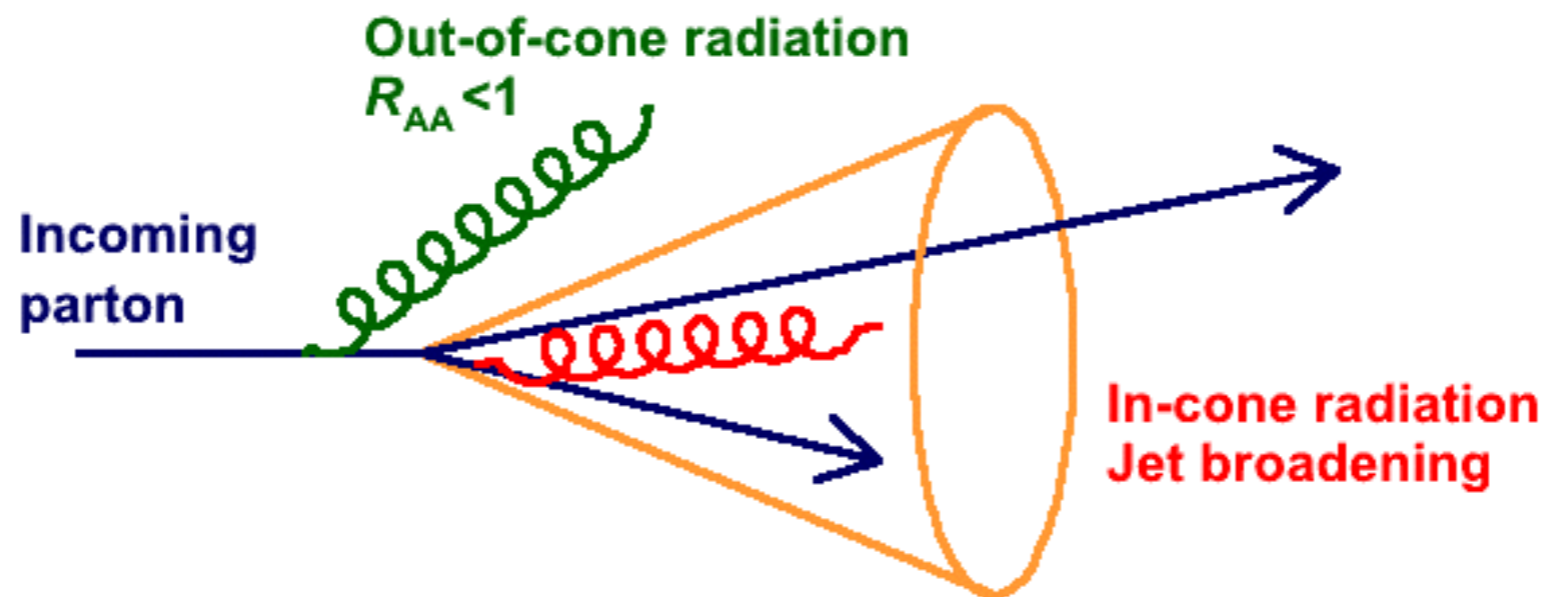


Latest calculations of radiative+collisional E-loss for heavy and light quarks agree with data

$R_{AA}$  similar for light hadrons and  $D$  mesons due to interplays of spectra shape, fragmentation with dead cone effect

# Jets and parton energy loss

**Motivation: understand parton energy loss by tracking the lost energy**



Qualitatively two scenarios:

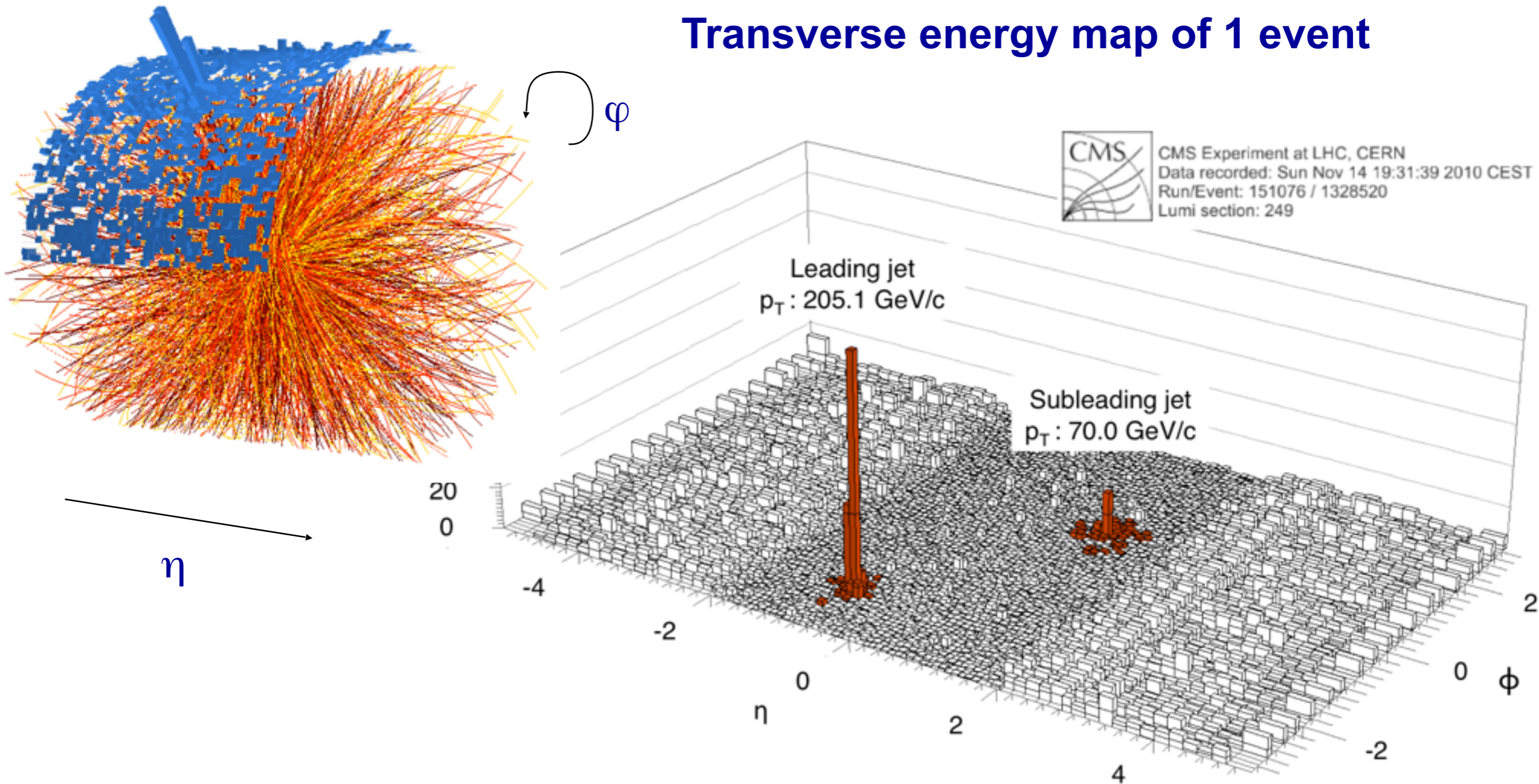
- 1) In-cone radiation:  $R_{AA} = 1$ , change of fragmentation
- 2) Out-of-cone radiation:  $R_{AA} < 1$

As usual: reality is somewhere in-between

# Jets at LHC

ALICE

Transverse energy map of 1 event



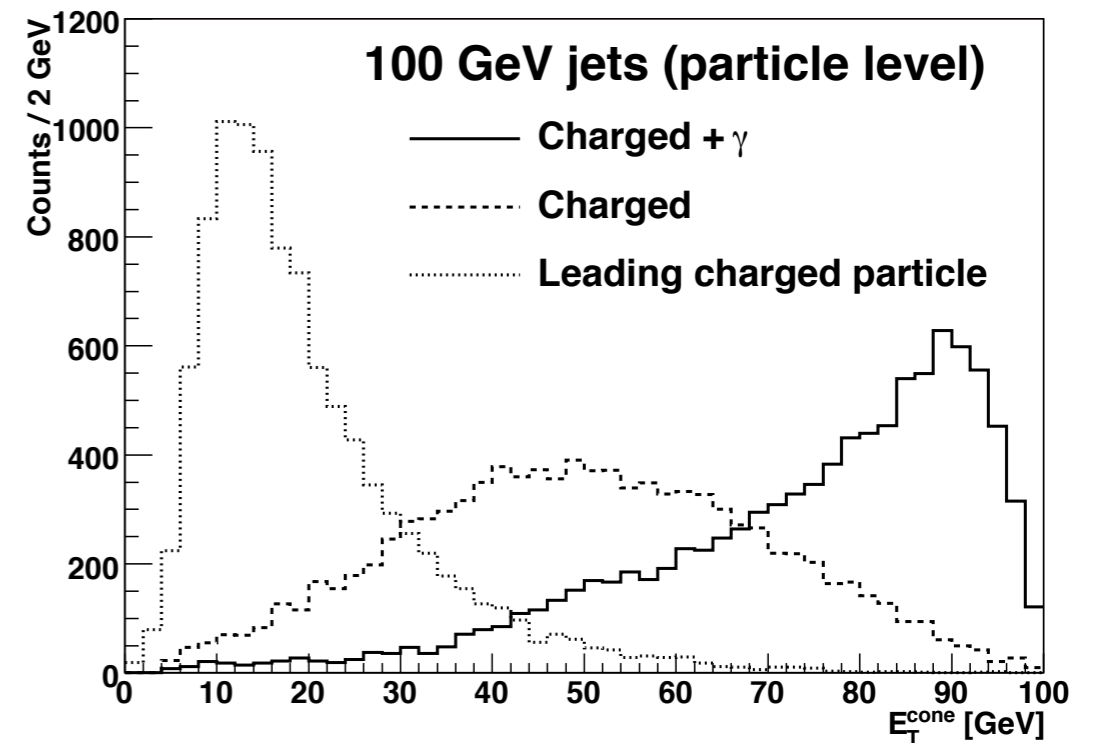
Clear peaks: *jets* of fragments  
from high-energy quarks and gluons  
And a lot of uncorrelated 'soft' background



# Charged and full jets

- Full jets: charged + neutral particles (except neutrinos)
  - Hadronic + Electromagnetic Calorimetry (ATLAS)
    - + tracking (particle flow; CMS)
  - Tracking + EMCal (ALICE)
- Charged jets: only charged particles
  - Used by ALICE because of limited acceptance of EMCal

## Reconstructed energy



Charge to neutral fluctuations!

Full jets preferred for original goal: recover jet energy  
In practice, differences are small, however....

# Detector corrections

Definitions:

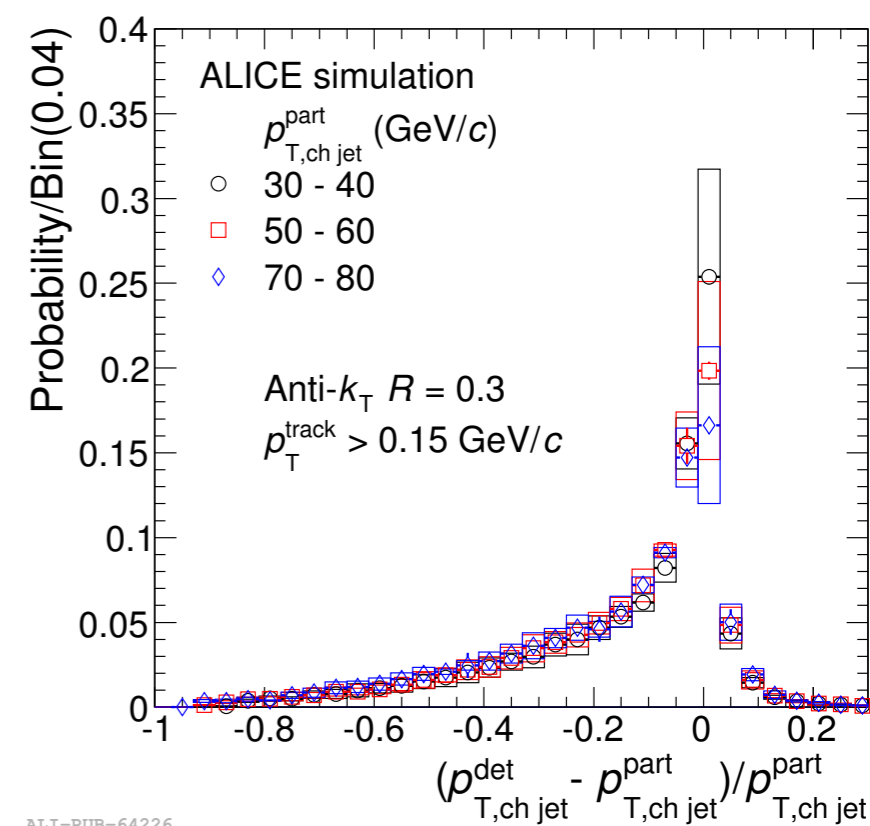
**Particle level:** as generated by event generator, e.g. Pythia

**Detector level:** as reconstructed (Pythia+detector simulation)

(Parton level: parton energy; ill-defined?)

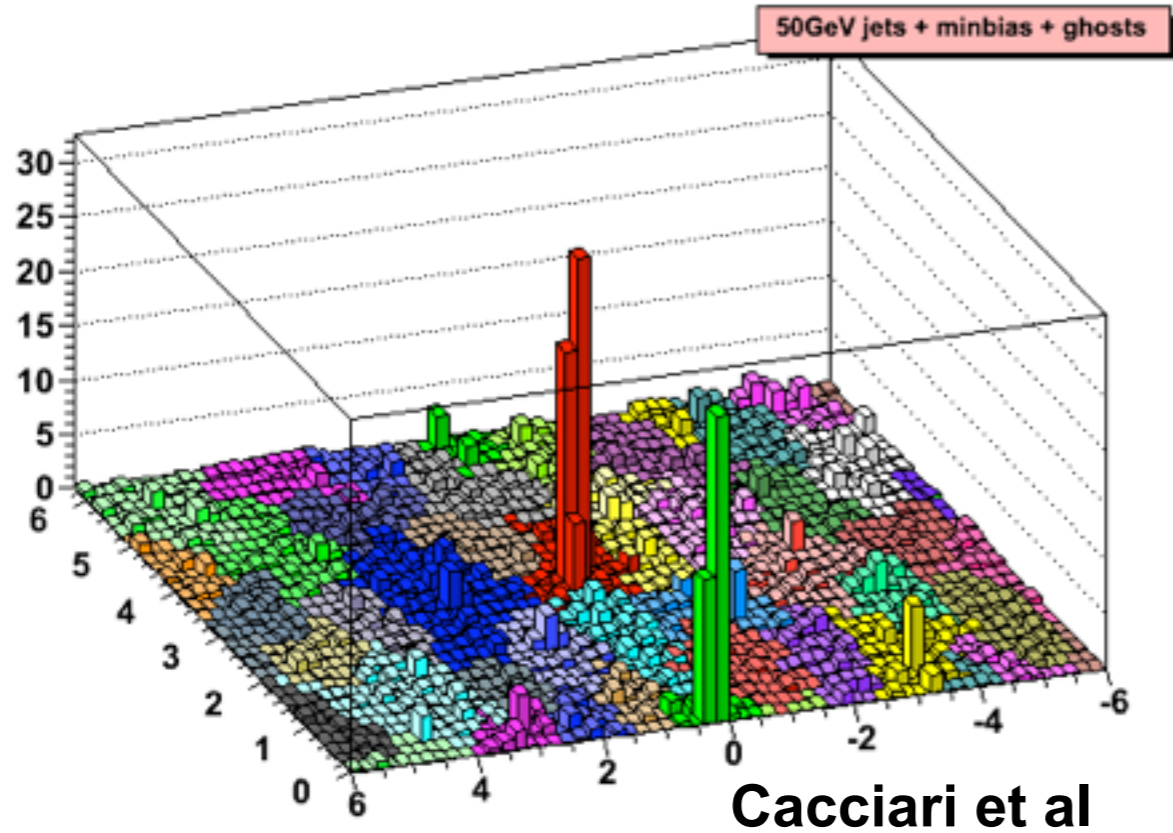
Standard practice:

- Charged jets are corrected to charged jets at the particle level
  - main effect: tracking efficiency
- Full jets are corrected to full jets at the particle level
  - Calorimetric jets: HCal response
  - Tracking+EMCal: Unmeasured hadrons (neutrons,  $K^0_L$ , tracking efficiency)



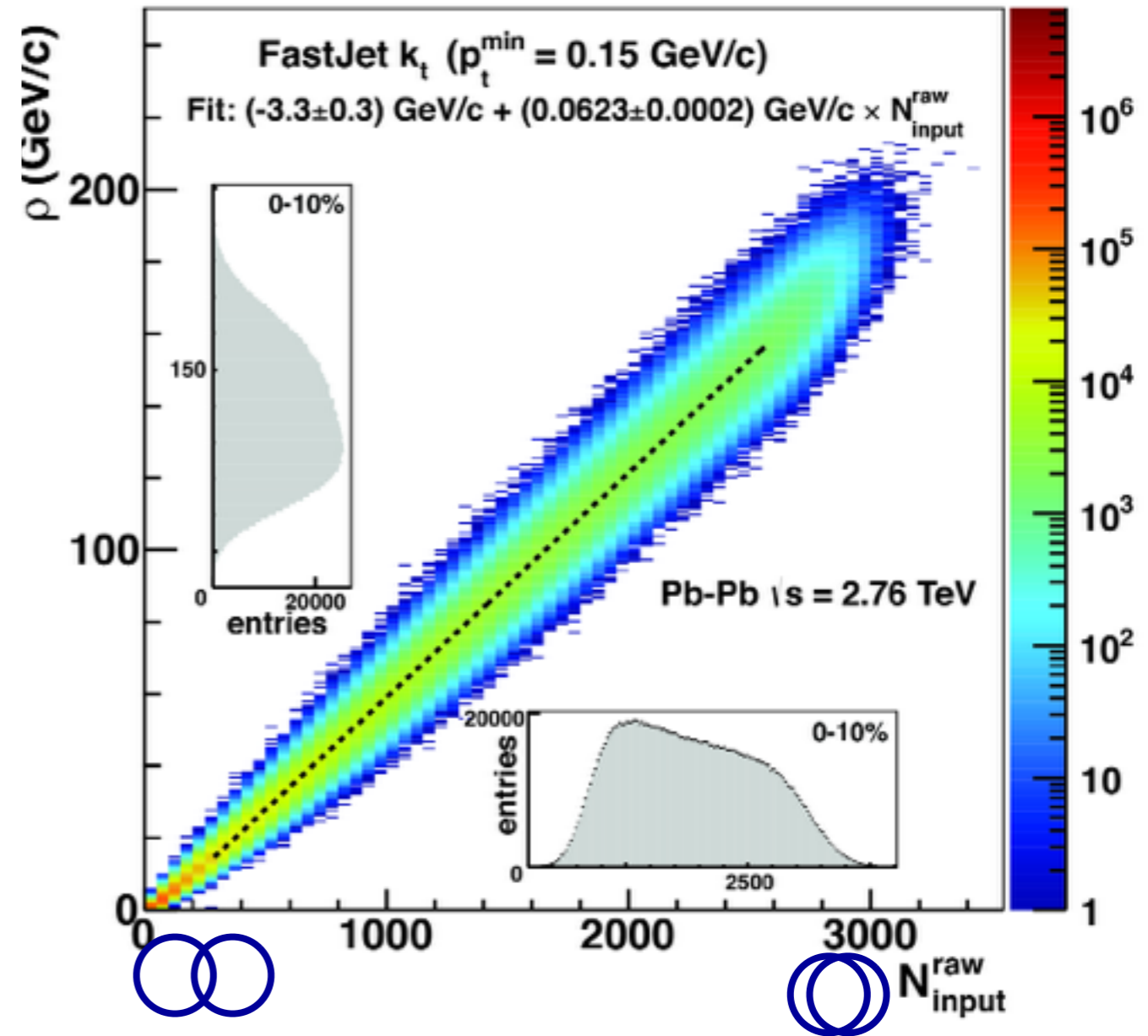
# PbPb jet background

## Jet finding illustration



$\eta$ - $\phi$  space filled with jets  
Many 'background jets'

## Background density vs multiplicity



Background contributes up to  $\sim 180$  GeV per unit area

Subtract background: 
$$p_{T,jet}^{\text{sub}} = p_{T,jet}^{\text{raw}} - \rho A$$

Statistical fluctuations remain after subtraction

# Pb+Pb jet $R_{AA}$

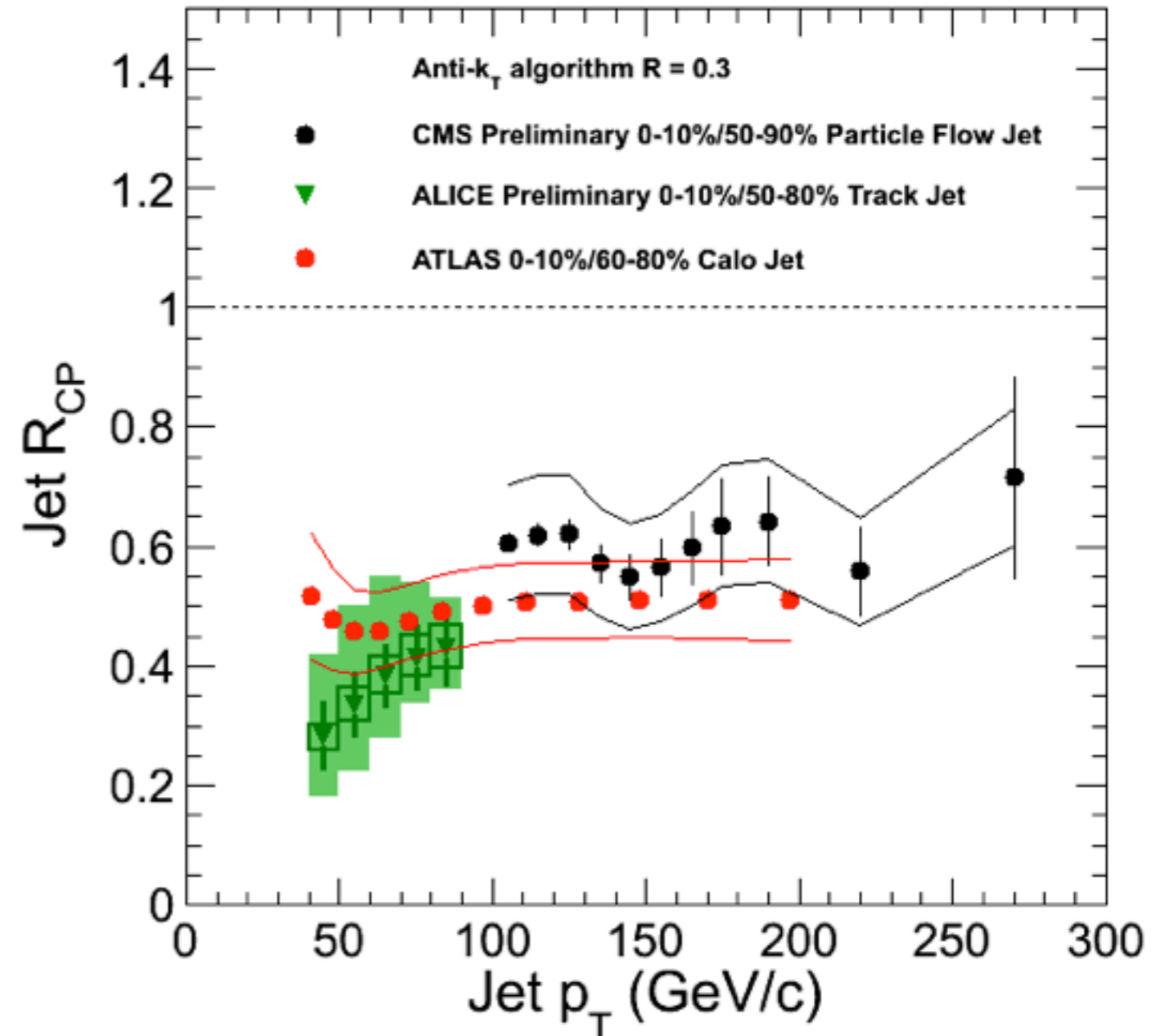
Jet  $R_{AA}$  measured by  
ATLAS, ALICE, CMS

Good agreement  
between experiments

Despite different methods:

ATLAS+CMS: hadron+EM jets

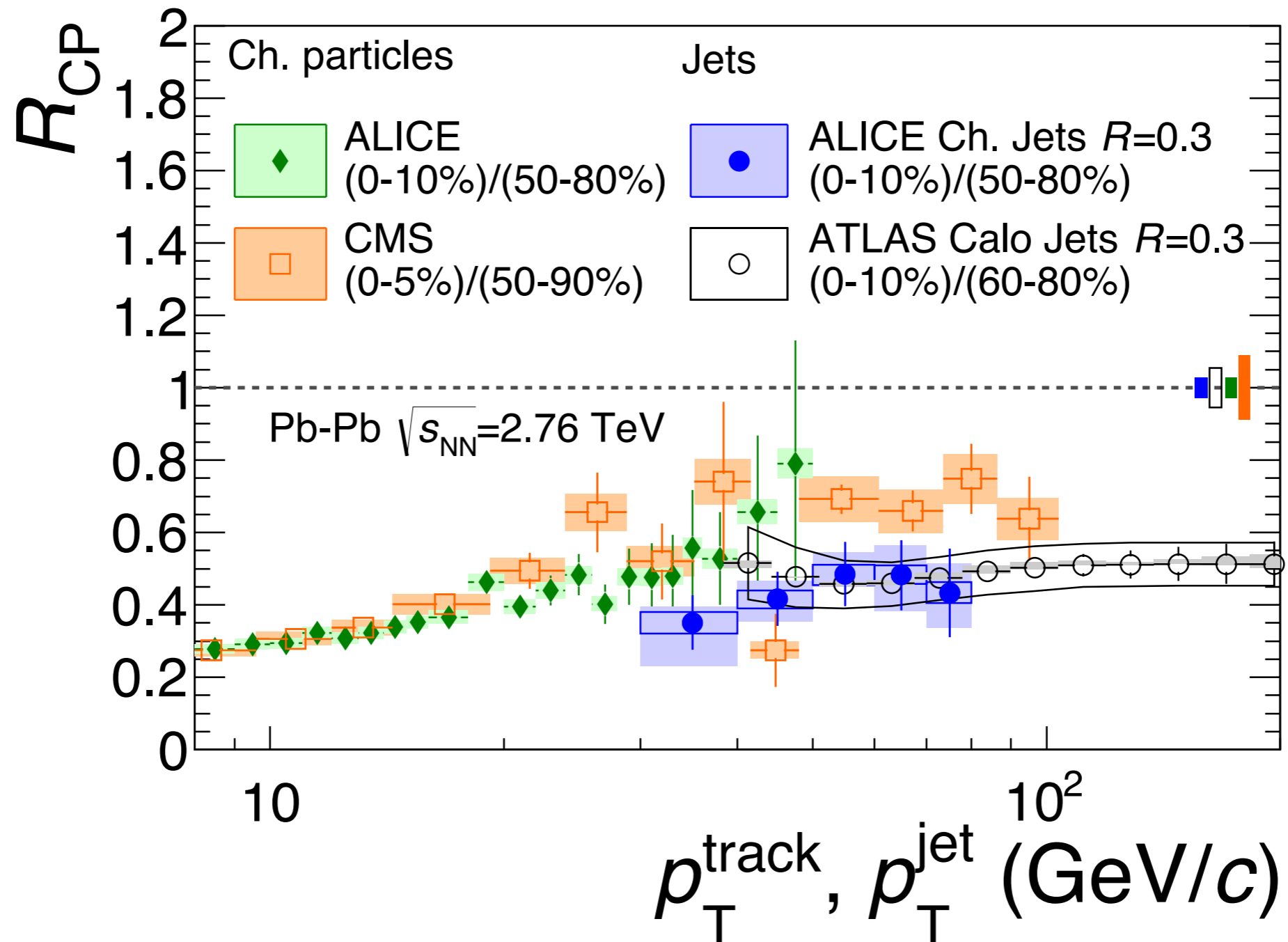
ALICE: charged track jets



$R_{AA} < 1$ : not all produced jets are seen;  
out-of-cone radiation and/or 'absorption'

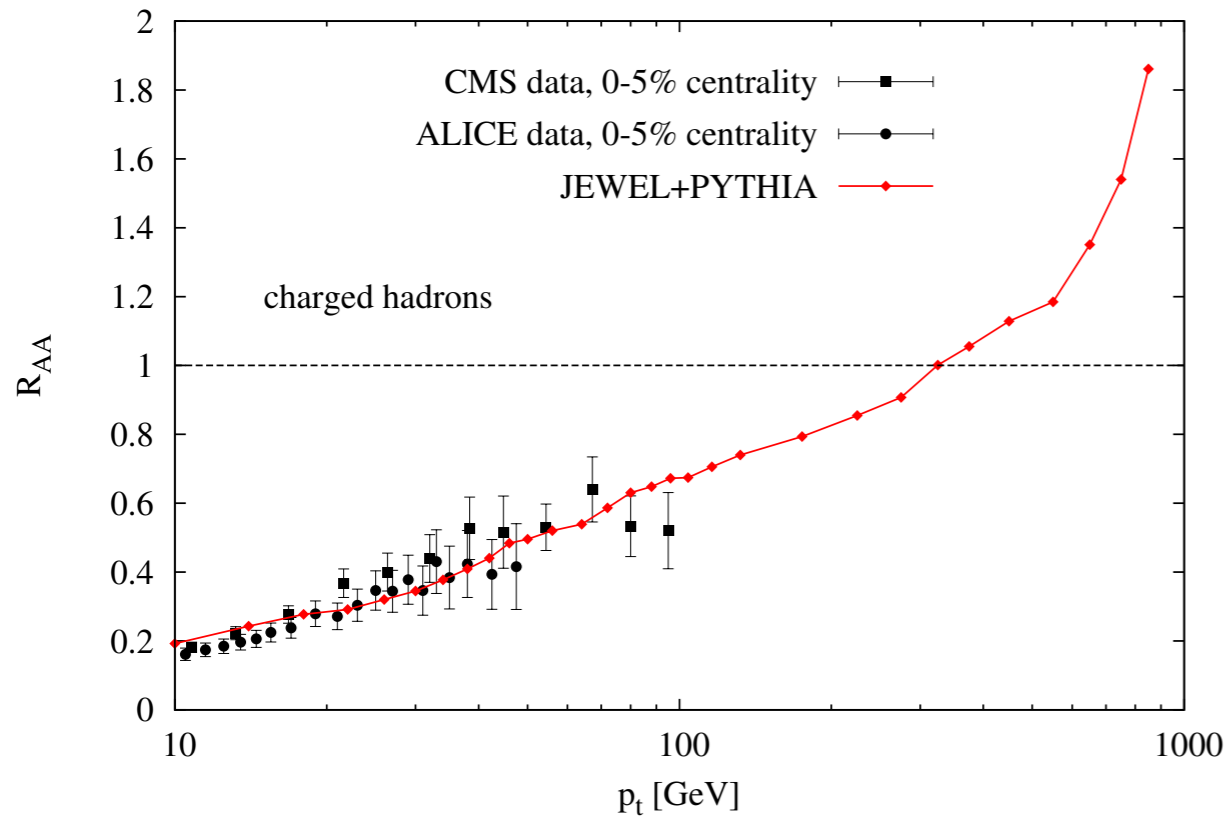
For jet energies up to  $\sim 250$  GeV; energy loss is a very large effect

# Comparing hadrons and jets

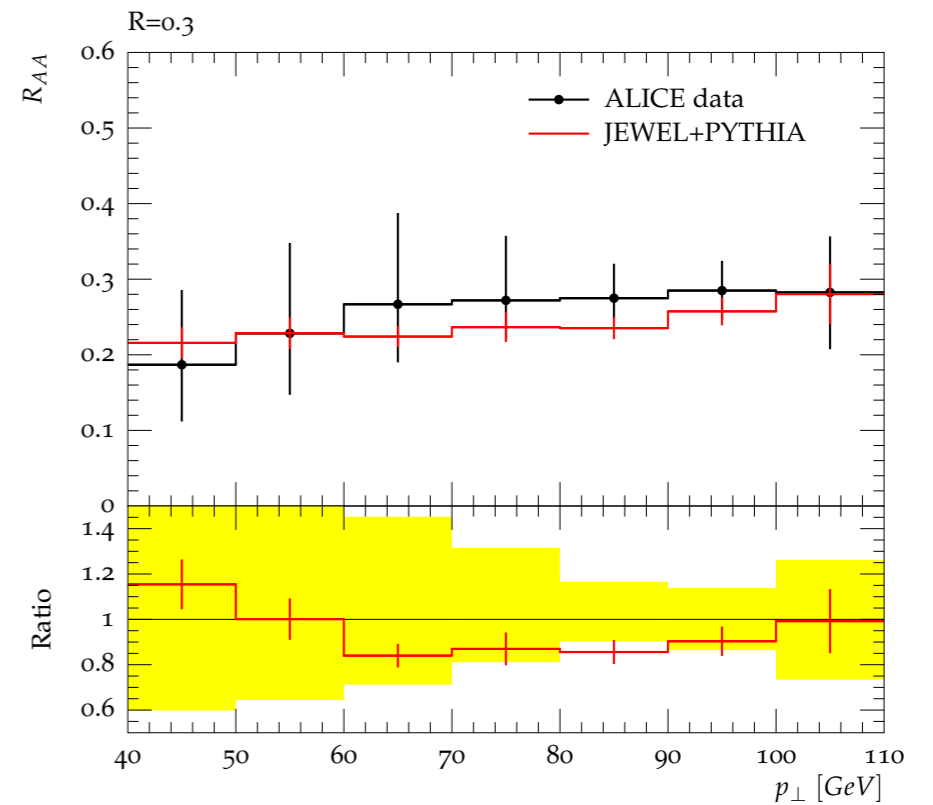
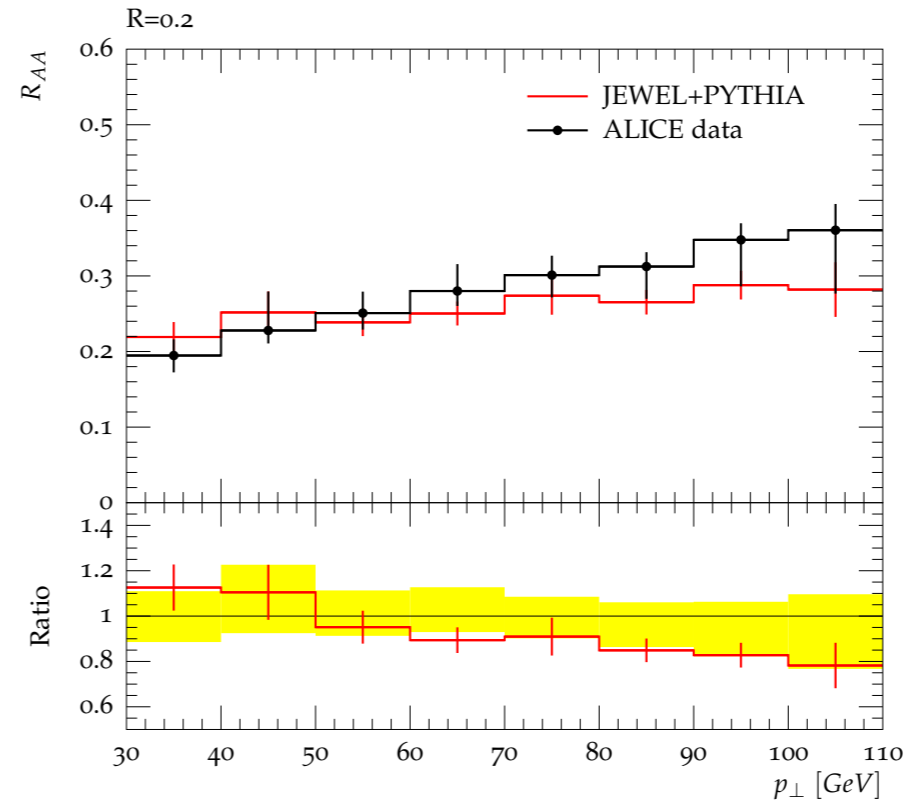


Suppression of hadron (leading fragment) and jet yield similar  
 Is this 'natural'? No (visible) effect of in-cone radiation?

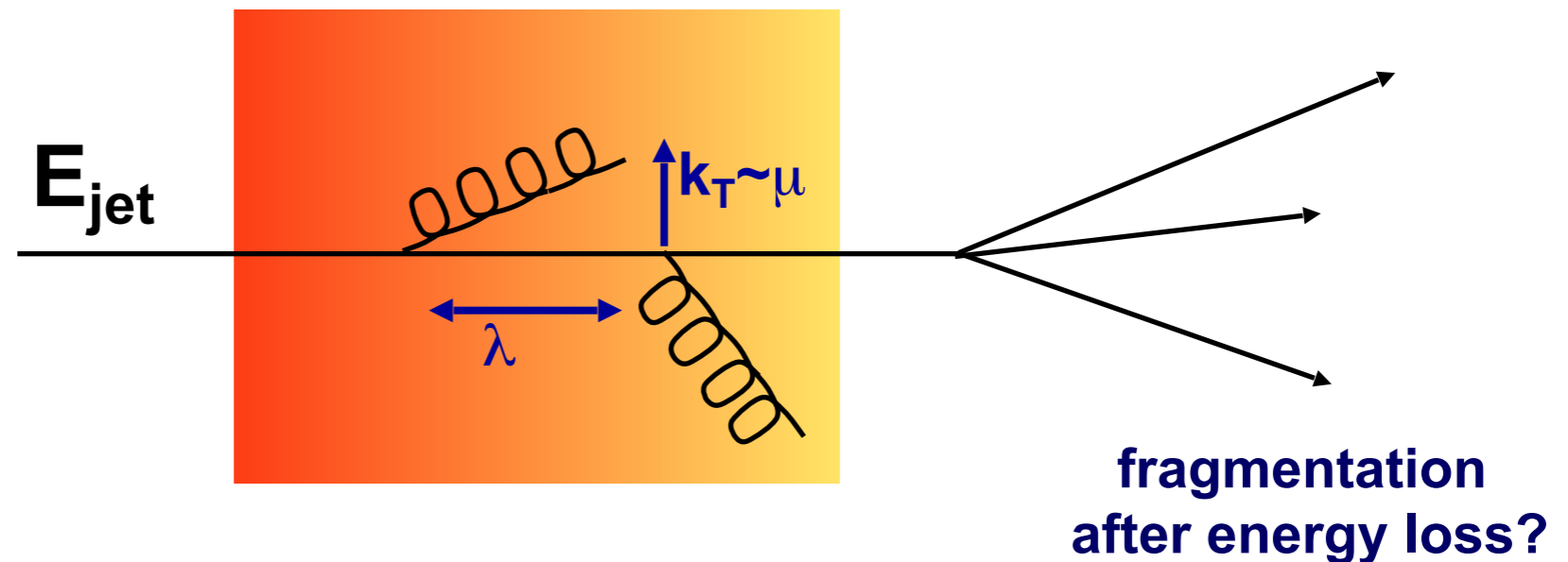
# Comparison to JEWEL energy loss MC



JEWEL shows the same feature:  
jet  $R_{AA} \sim$  hadron  $R_{AA}$



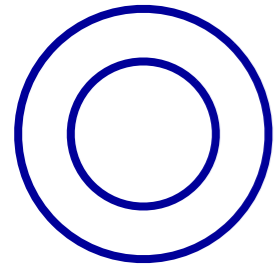
# Generic expectations from energy loss



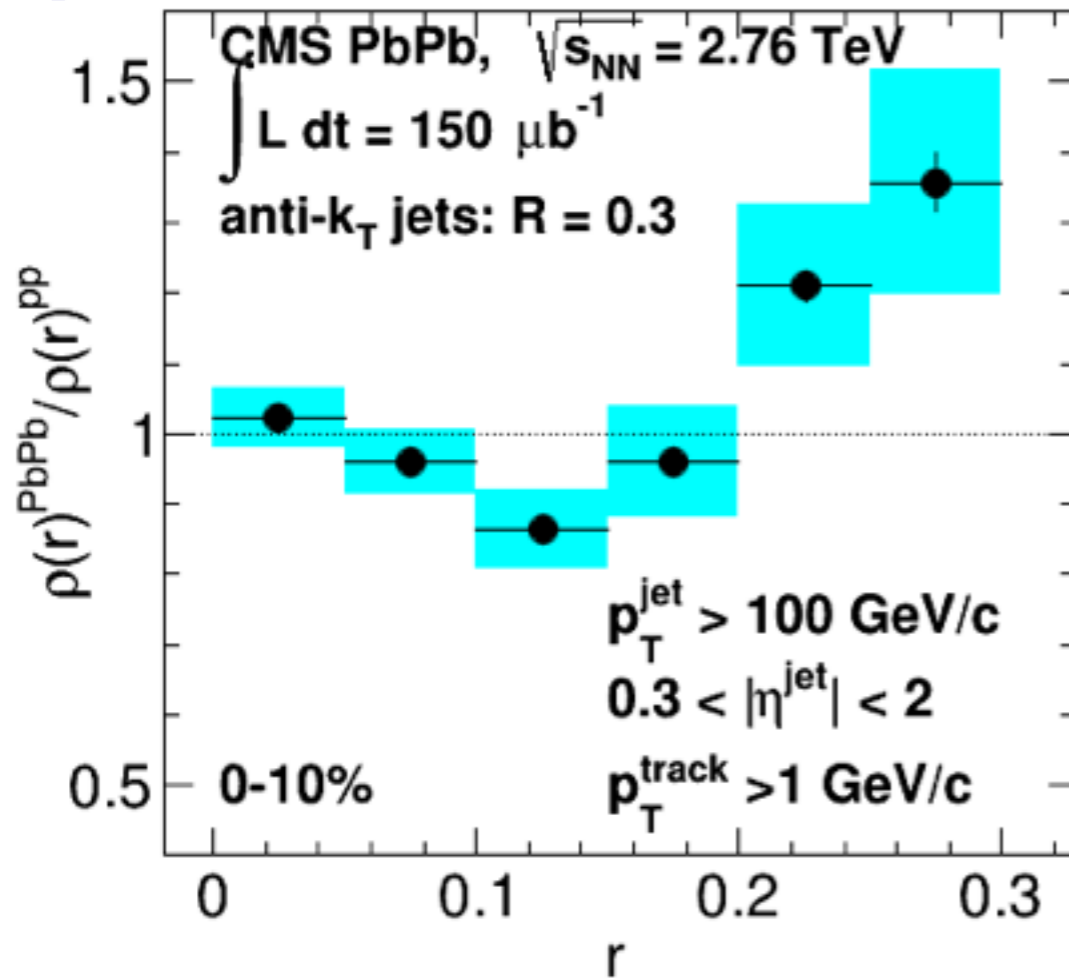
- Longitudinal modification:
  - out-of-cone  $\Rightarrow$  energy lost, suppression of yield, di-jet energy imbalance
  - in-cone  $\Rightarrow$  softening of fragmentation
- Transverse modification
  - out-of-cone  $\Rightarrow$  increase acoplanarity  $k_T$
  - in-cone  $\Rightarrow$  broadening of jet-profile

**Out-of-cone effects are large, so expect combination of all of the above**

# Changes in fragmentation



## Transverse fragment distributions



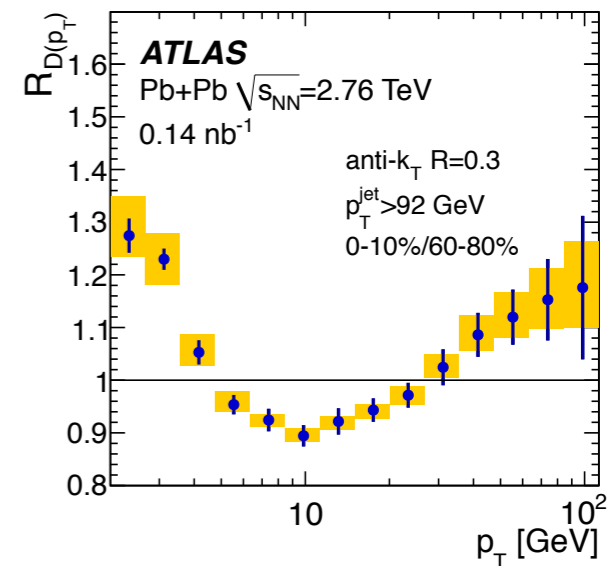
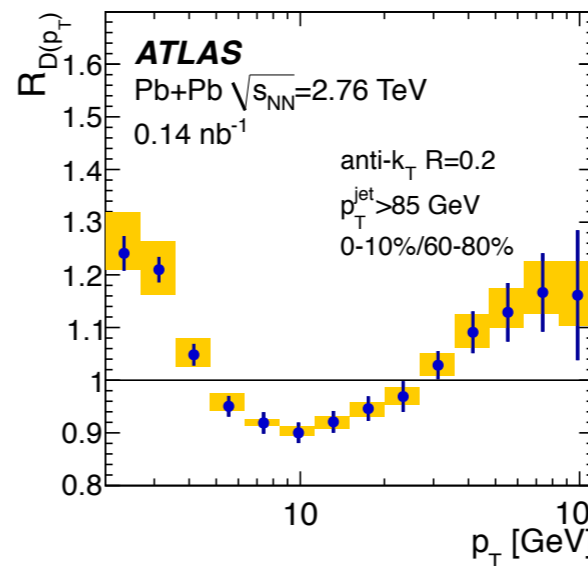
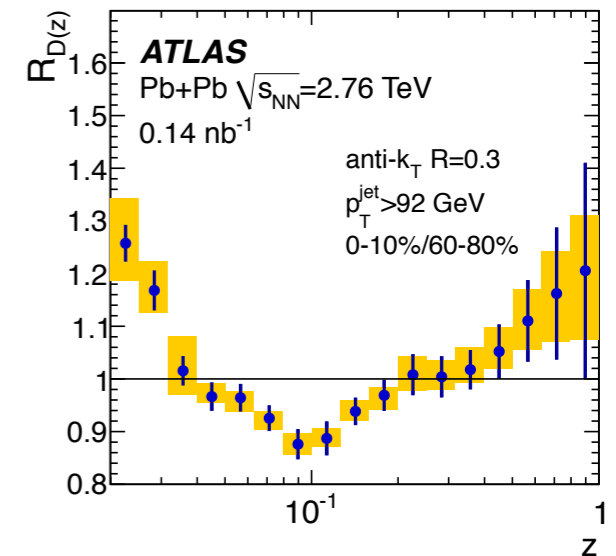
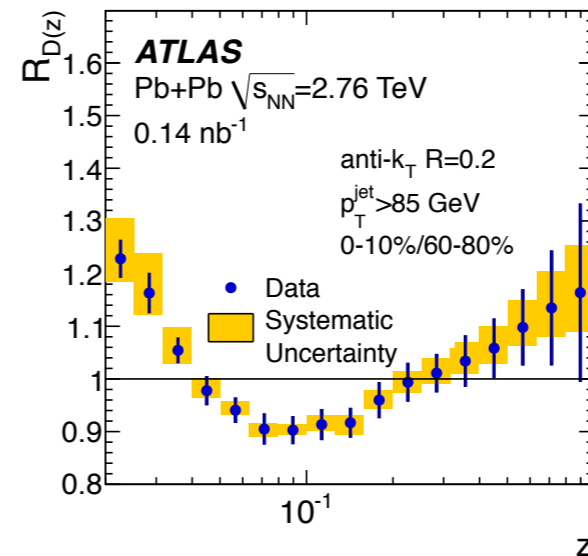
Enhancement at large  $r$ , low  $p_T$   
 ratio  $\sim 1$  at small  $r$ , large  $p_T$

Relation  $r \Leftrightarrow p_T$ : large  $p_T$  is at small  $r$

No modification at small  $R$ , large  $p_T$ : physics or auto-correlation?

## Longitudinal fragment distributions

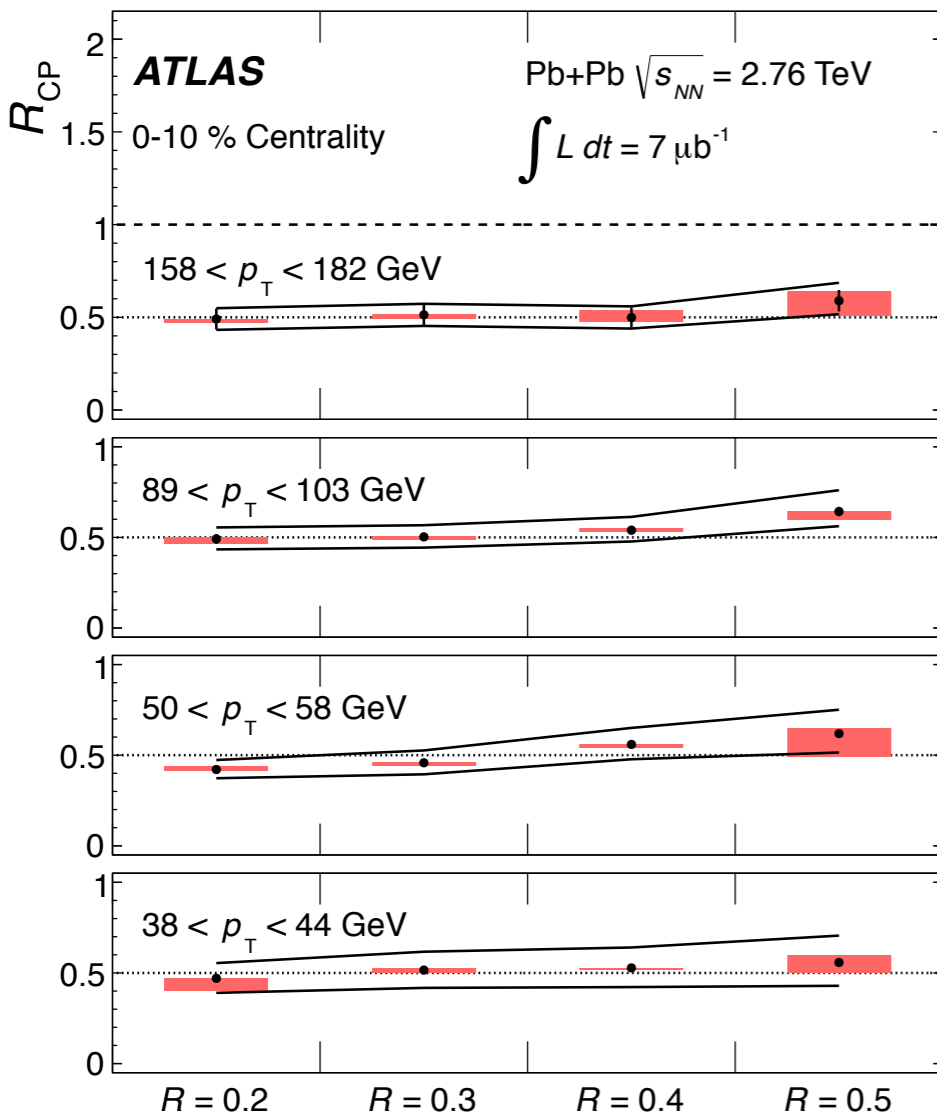
CMS, arXiv:1310.0878



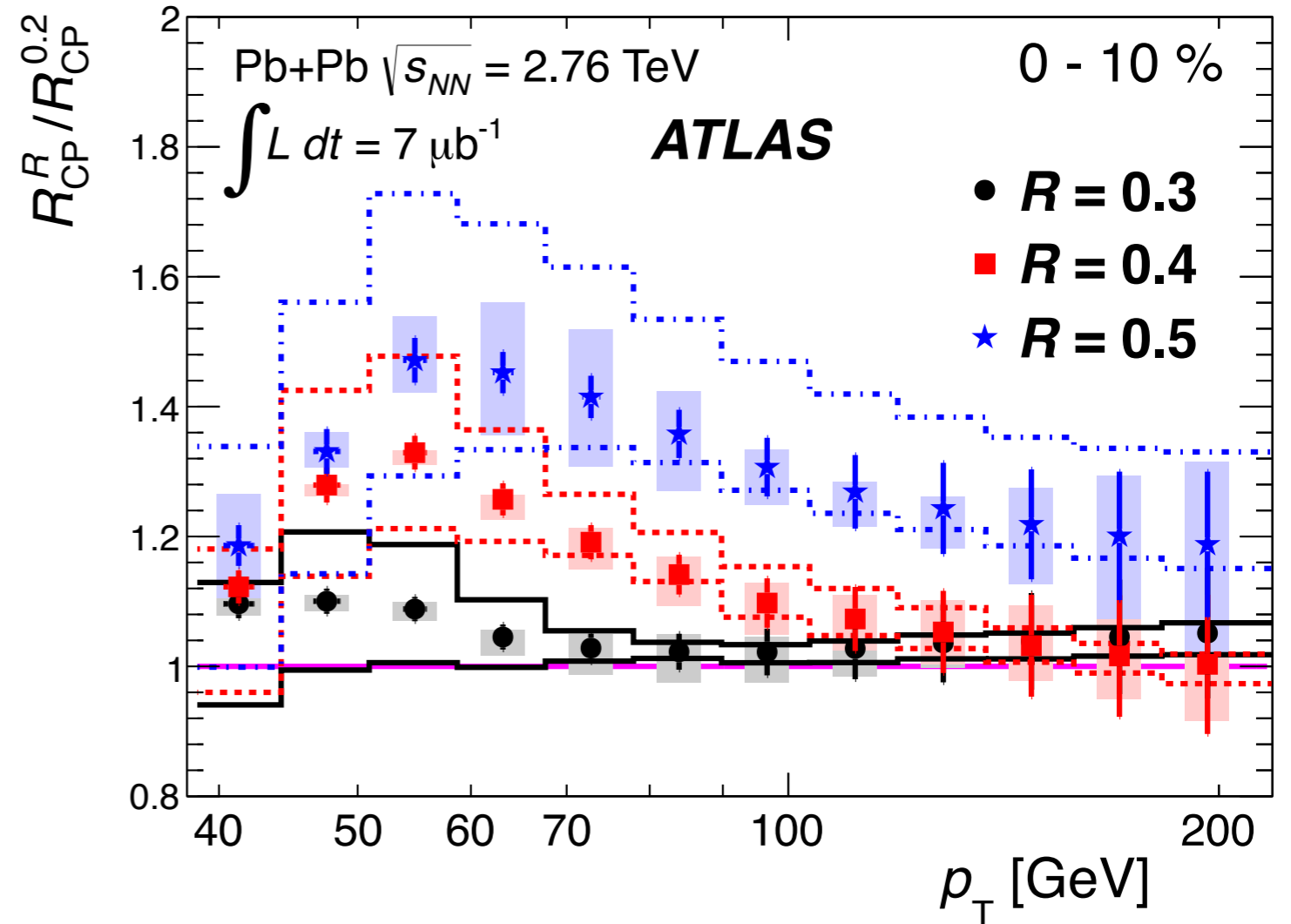
ATLAS, arXiv:1406.2979



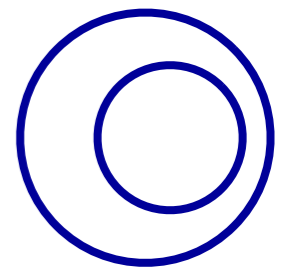
# Jet broadening: R dependence of $R_{AA}$



## Ratio of spectra with different R



Larger jet cone: ‘catch’ more radiation  $\rightarrow$  Jet broadening



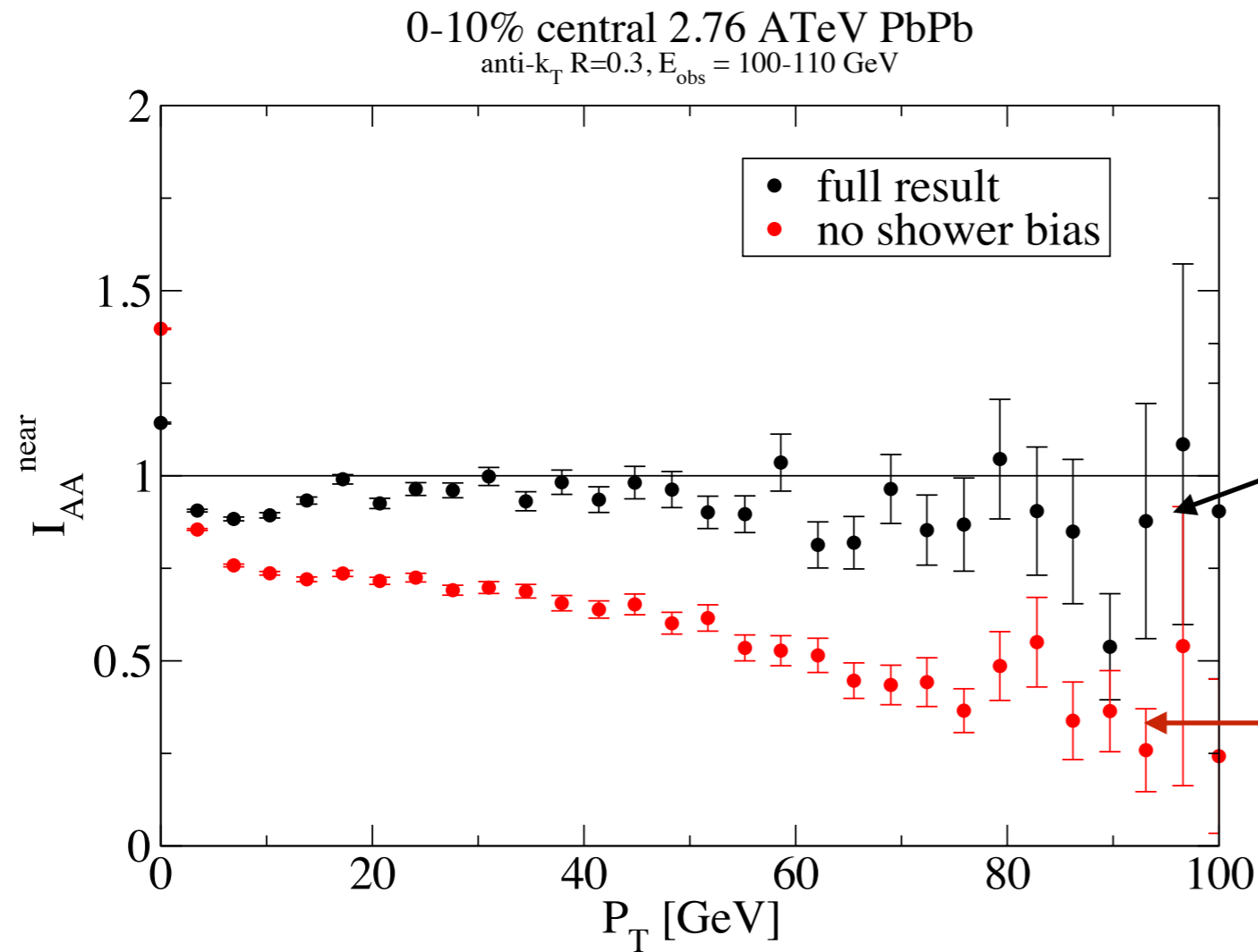
However,  $R = 0.5$  still has  $R_{AA} < 1$

– Hard to see/measure the radiated energy

# Comparison to models: YaJEM

T. Renk, arXiv:1212.0646

Ratio of fragment distributions



Selection on reconstructed jet energy

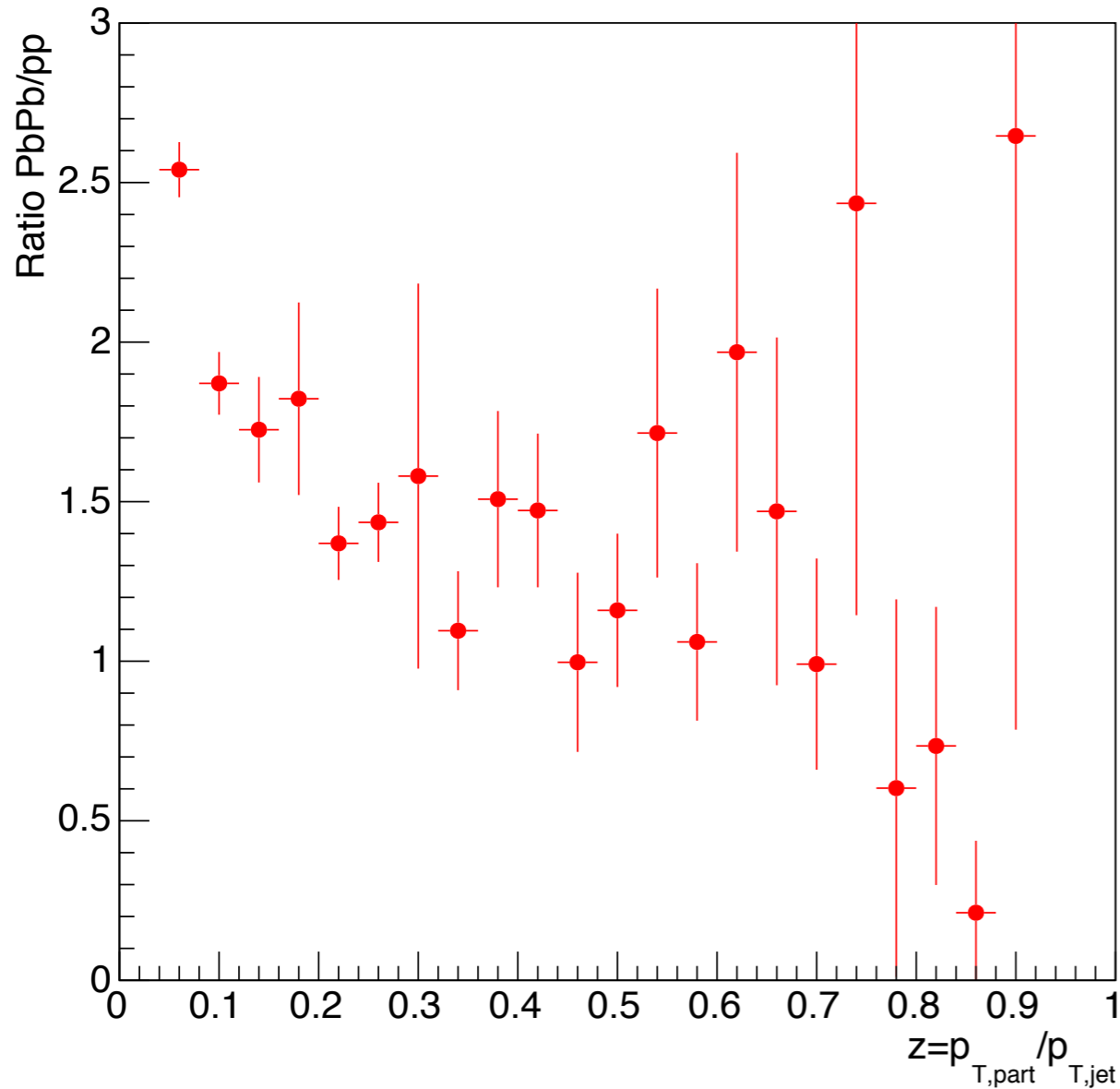
Naive expectation: no selection on reconstructed jet energy

Thorsten Renk: the increase towards  $R = 1$  at  $z = 1$  is natural consequence of the jet energy selection (bias effect)

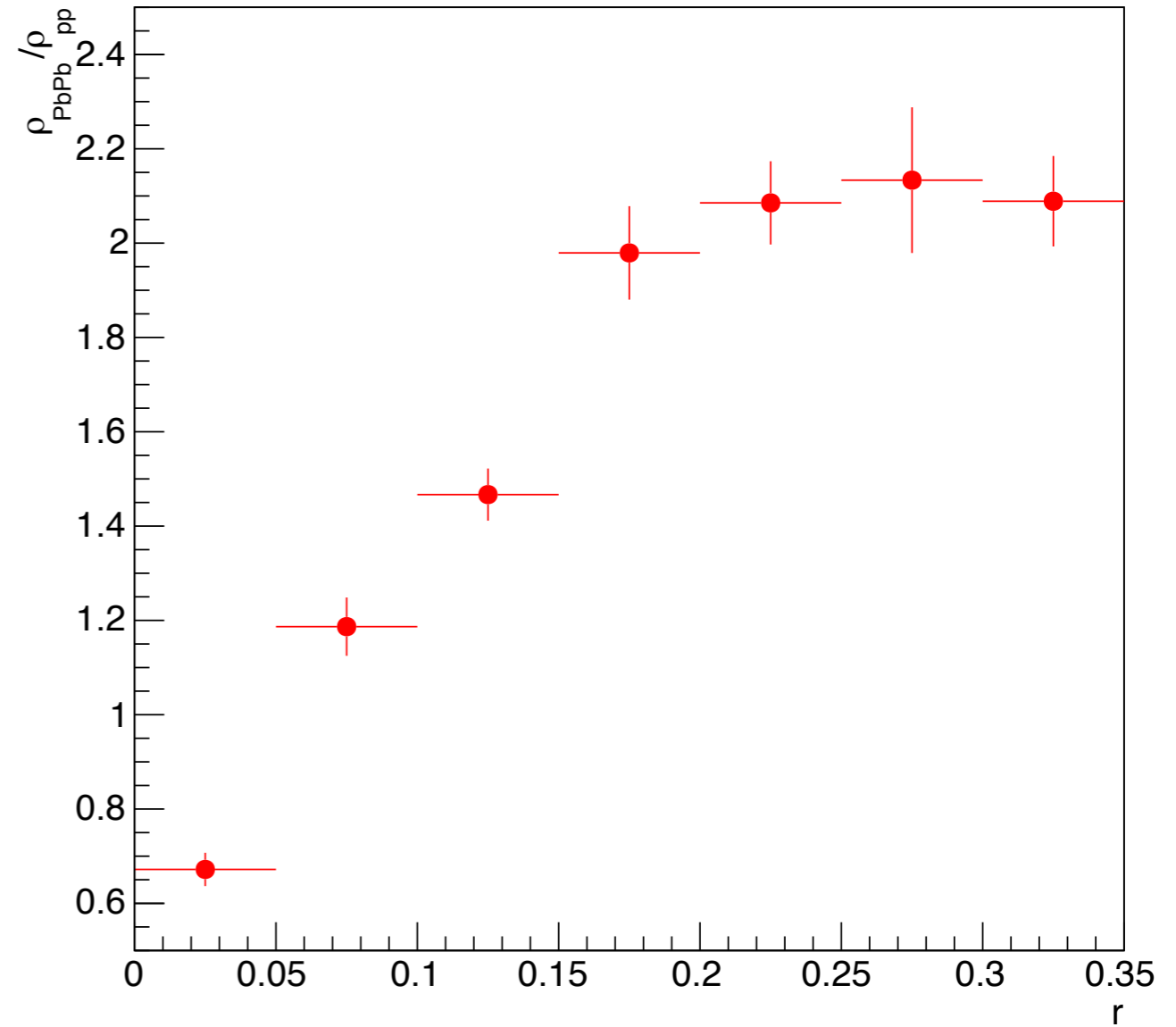
# q-PYTHIA results

See also: L. Apolinario, Lisbon jet workshop

## Longitudinal fragment distribution



## Transverse distribution

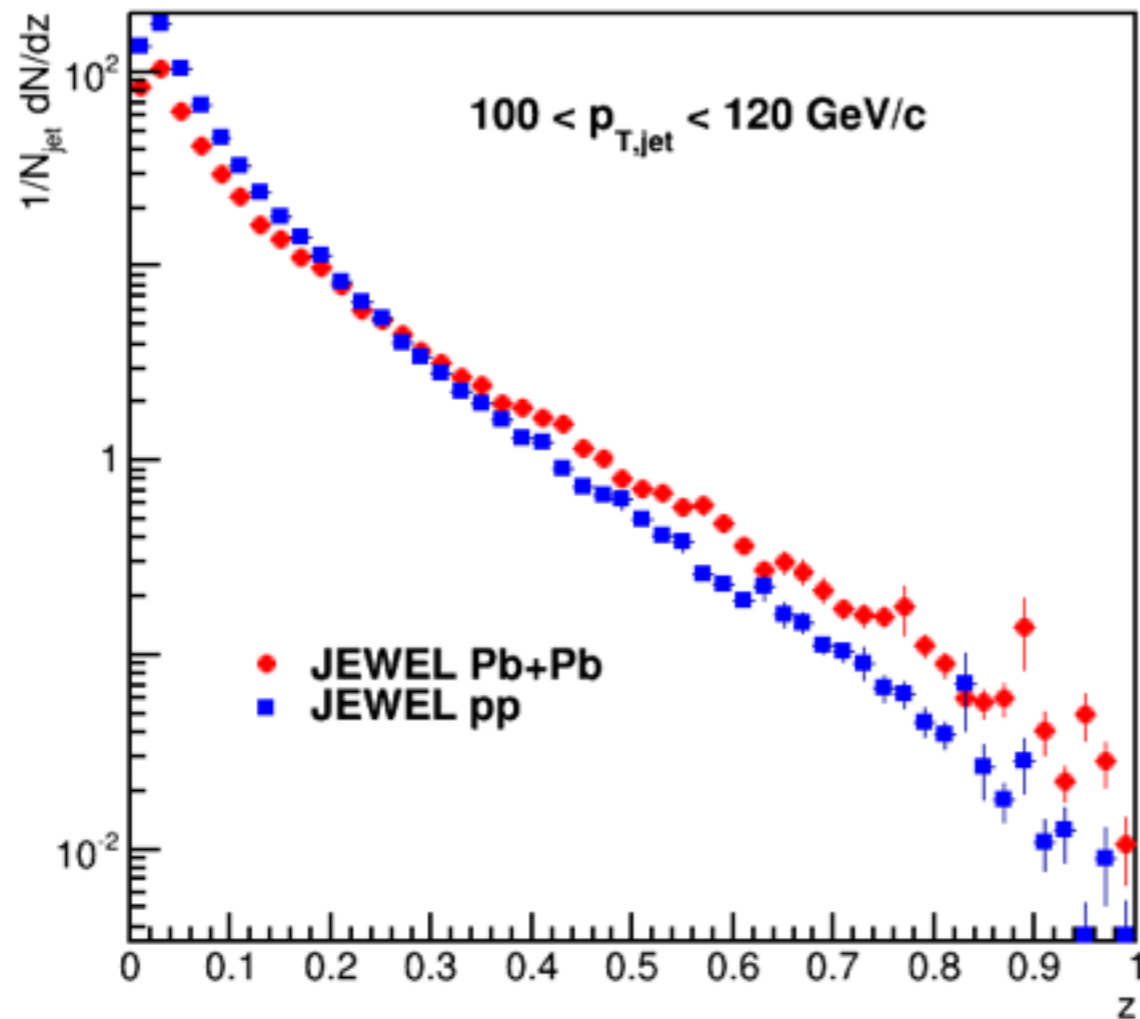


q-Pythia: enhancement at small  $z$ ,  
 $\sim 1$  at intermediate  $z$

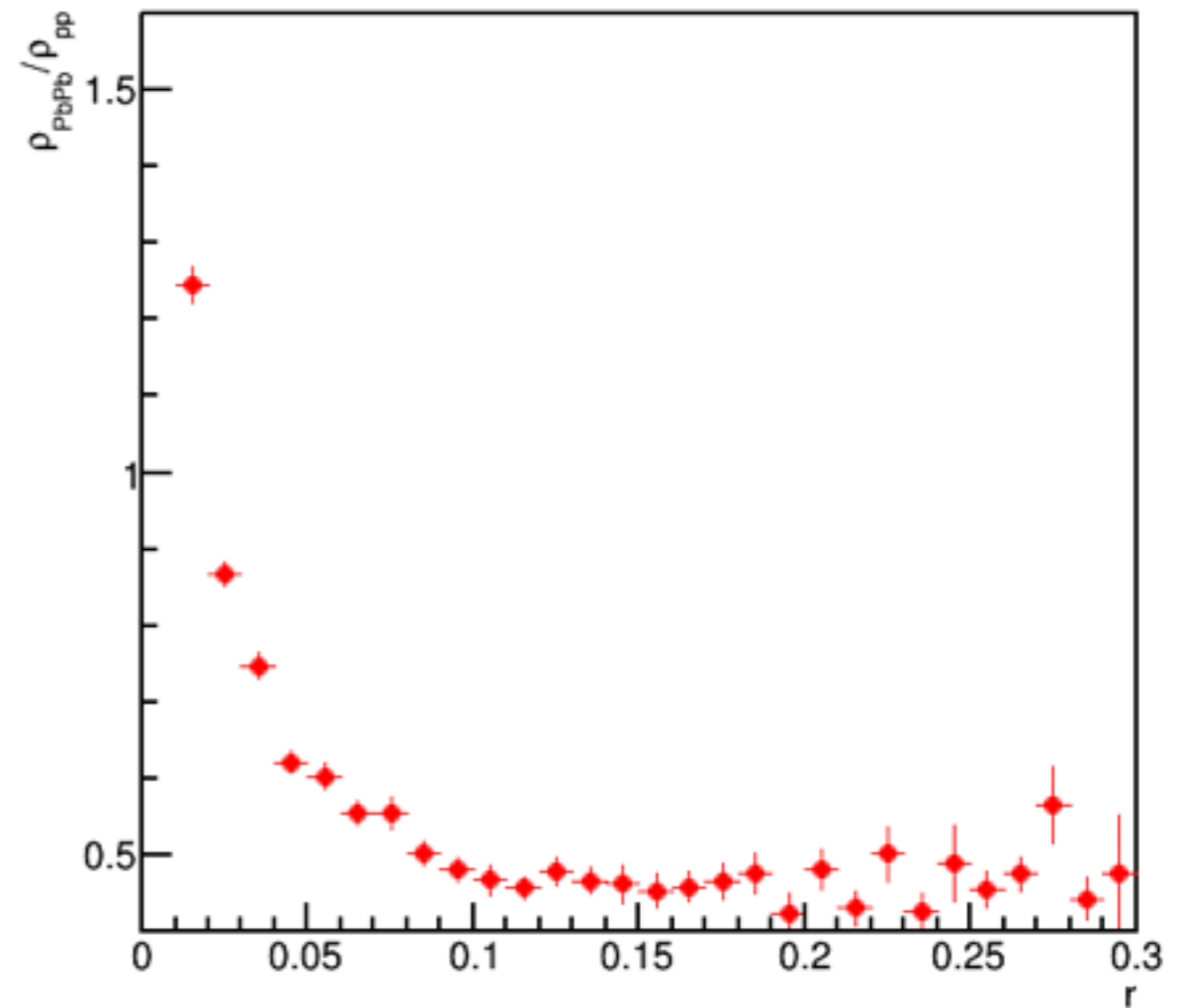
q-Pythia: enhancement at large  $r$ ,  
suppression at small  $r$

# JEWEL results for jet structure

## Longitudinal distribution



## Radial distribution



JEWEL: more fragments at high  $z$   
for medium-modified shower

JEWEL: more fragment  $p_T$  at  
small  $r$  for medium-modified shower

Trends opposite to q-PYTHIA  
retain relation small  $r \Leftrightarrow$  large  $z$

# Models for jet quenching

- q-PYTHIA: medium-induced branching
  - Energy-momentum conserved in shower
- JEWEL: medium-induced branching with MC formation time
  - Includes momentum exchange with medium
  - Complication: recoil; momentum leaks out of the jet (need to define boundary between medium and jet for calculational reasons)
- YaJEM: medium-induced virtuality
  - Model somewhat ad-hoc, but describes much of the observations
- PYQUENCH: medium-induced branching; ad-hoc implementation

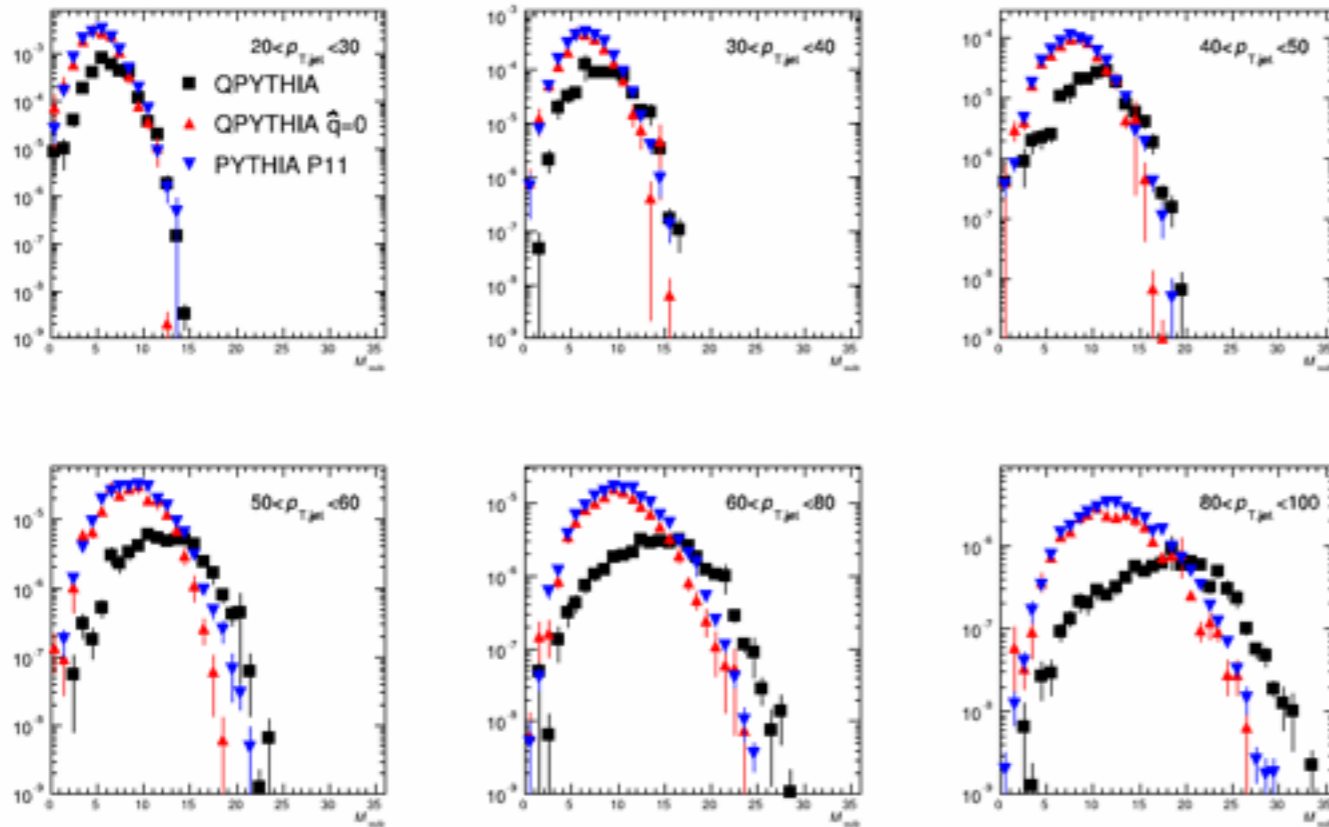
**⇒ Virtuality evolution may be a key concept?**

# Virtuality evolution and jet mass

Idea: jet mass is determined by virtuality of showering parton

Majumder, Putschke, Verweij

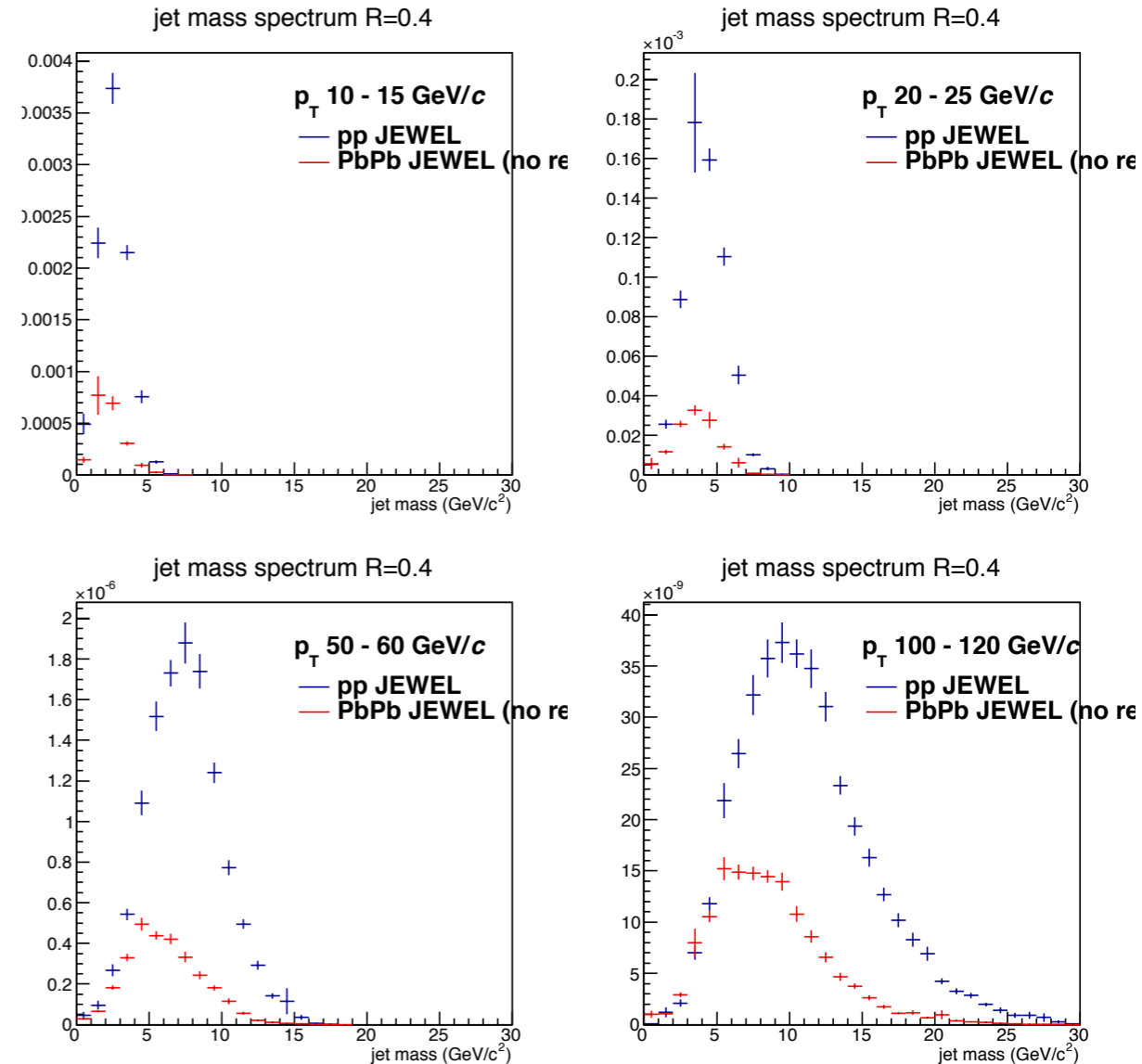
## q-PYTHIA



q-PYTHIA: medium effects  
increase jet mass

M. Verweij, private communication

## JEWEL



JEWEL: medium effects  
decrease jet mass

# Other ideas

- **Iancu, Blaizot et al:**

- At some soft scale  $\omega = \alpha_s \omega_c$ , **branching probability becomes  $\sim 1$**
- Medium-induced gluon splittings **favor  $x \sim 0.5$  (quasi-democratic)**
- Both effects would strongly modify in-medium showers; are they compatible with phenomenology? What are the limits of applicability?

- **Rajagopal, Casalderrey-Solana, Milhano et al:**

- What about strong coupling?
- Use **AdS/CFT** estimates and implement in PYTHIA for phenomenology
- Main observational impact from  $x_{stop}^G = x_{stop}^q \left( \frac{C_F}{C_A} \right)^{1/3}$

- **Tywoniuk, Mehtar-Tani, Salgado et al**

- Improve treatment of multiple gluon emissions in medium
- No angular ordering for medium-induced radiation
- Important interplay of scales: opening angle of jet vs  $Q_s$  etc

# Conclusion

- Inclusive particle  $R_{AA}$  follows expectations
  - $\hat{q}/T^3$  larger at RHIC than LHC
  - Modelling/calculations still need to be refined
- Jets, main observations:
  - $R_{AA} < 1$ , significant out-of-cone radiation
  - Longitudinal, transverse fragment distributions modified:
    - Enhancement at small  $z$ , large  $r$
    - Suppression at intermediate  $z$ ,  $r$
    - Very little change at small  $r$ , large  $z$
  - First comparisons to MC models:
    - JEWEL shows too much suppression at large  $r$ , small  $z$
    - q-PYTHIA: too much suppression at small  $r$ , large  $z$
  - Connection to virtuality, jet mass to be explored

**Clearly, there is physics in the jet fragmentation  
No clear picture yet, but we have a handle!**



**Extra slides**

# Hadron trigger vs jet trigger

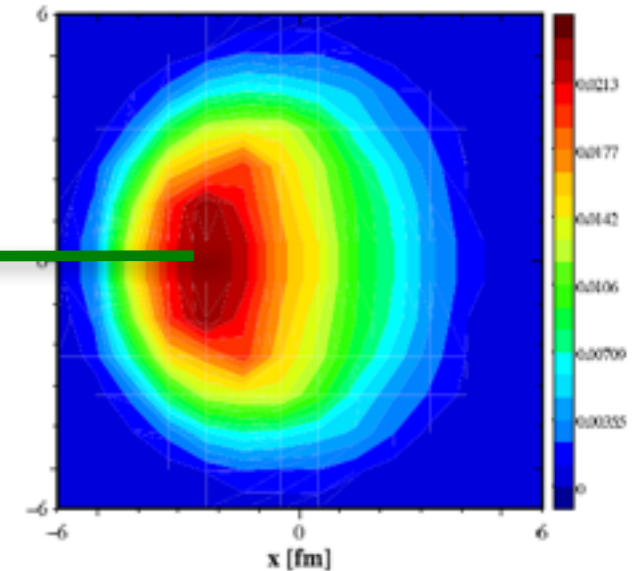
**Are jets an unnecessary complication?**

**If hadron and jet  $R_{AA}$  are similar, why not use hadron observables?**

**Hadron trigger: strong “surface bias”  
maximizes recoil path length**

**Hadron trigger** ←

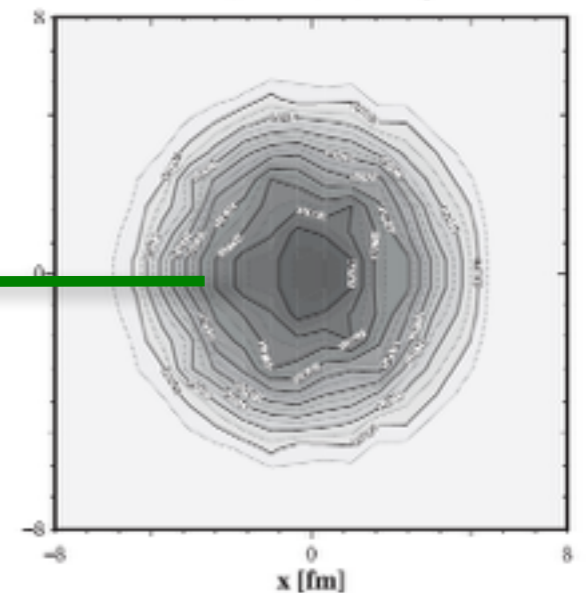
20–50 GeV Trigger, 0–10% 2.76 ATeV PbPb



**Full jet trigger: no geom. bias  
partially cancelled by bkg fluctuations**

**Jet trigger** ←

YaJEM, LHC (2+1)-D hydro



T.Renk, PRC85 064908

**Biases are different! Can be exploited to constrain models**

# Summary

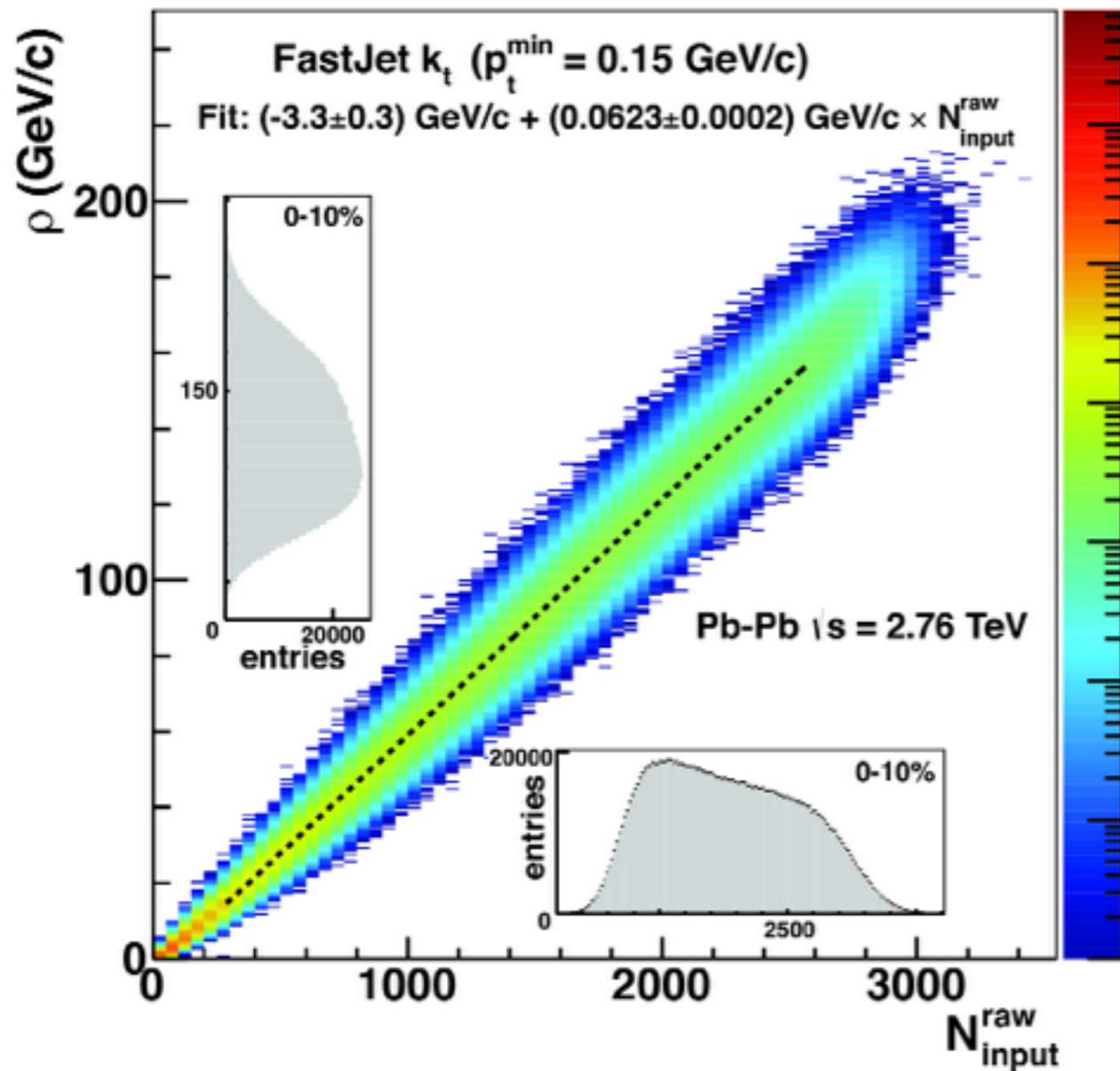
- Jets: a 'new' tool for parton energy loss measurements
  - Large out-of-cone radiation ( $R = 0.2-0.4$ )
    - Energy asymmetry
    - $R_{AA} < 1$ , similar to hadrons
    - $I_{AA} < 1$
    - Radial shapes
  - Remaining jet has small modifications:
    - Longitudinal and transverse structure similar at small  $r$ , large  $z$
    - Deviations at large  $r$ , low  $z$
  - Most of the radiation is at low  $p_T$ 
    - Scale set by medium temperature?
    - Democratic branchings?

**Interplays of many effects: impossible to read simple conclusions off the plots**

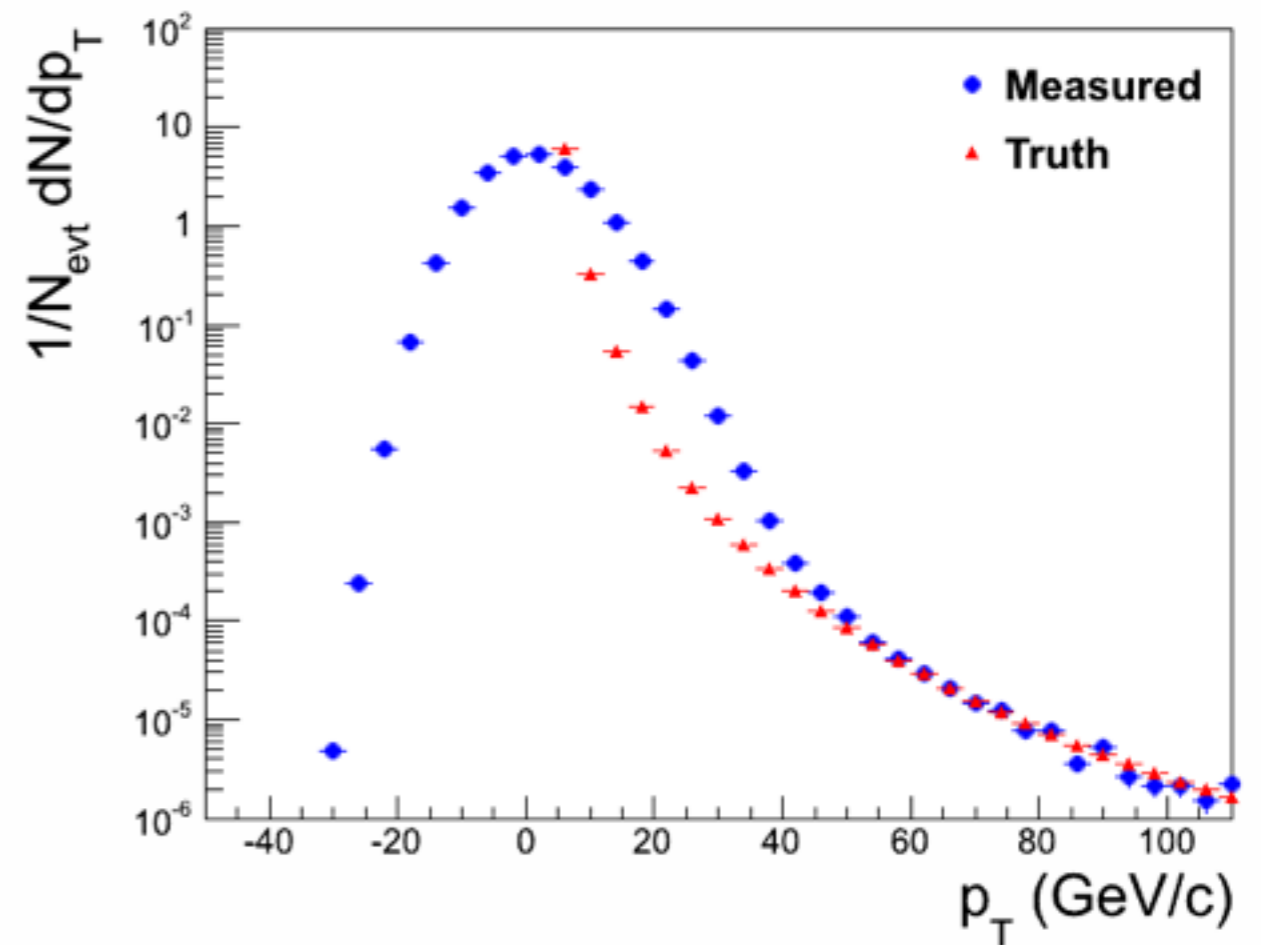
**Need (detailed) calculations to draw conclusions**  
e.g. JEWEL and YaJEM energy loss MCs agree  
with many of the observed effects

**Does this constrain the energy loss mechanism(s)?**  
Ongoing work...

# PbPb jet background



## Toy Model



Main challenge: large fluctuations of uncorrelated background energy

Size of fluctuations depends on  $p_T$  cut, cone radius

# Background jets

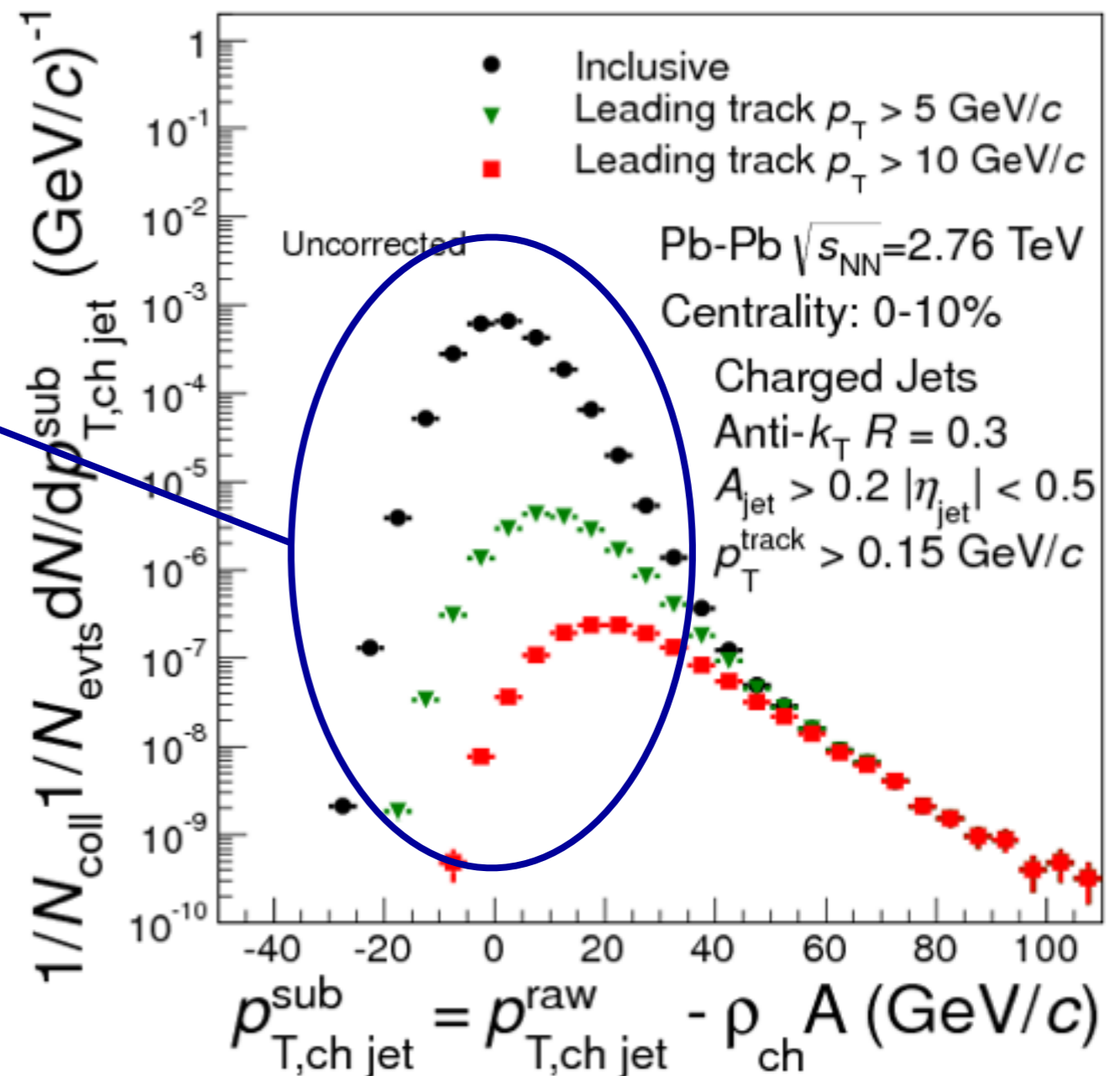
## Raw jet spectrum

Event-by-event background subtracted

**Low  $p_T$ : ‘combinatorial jets’**

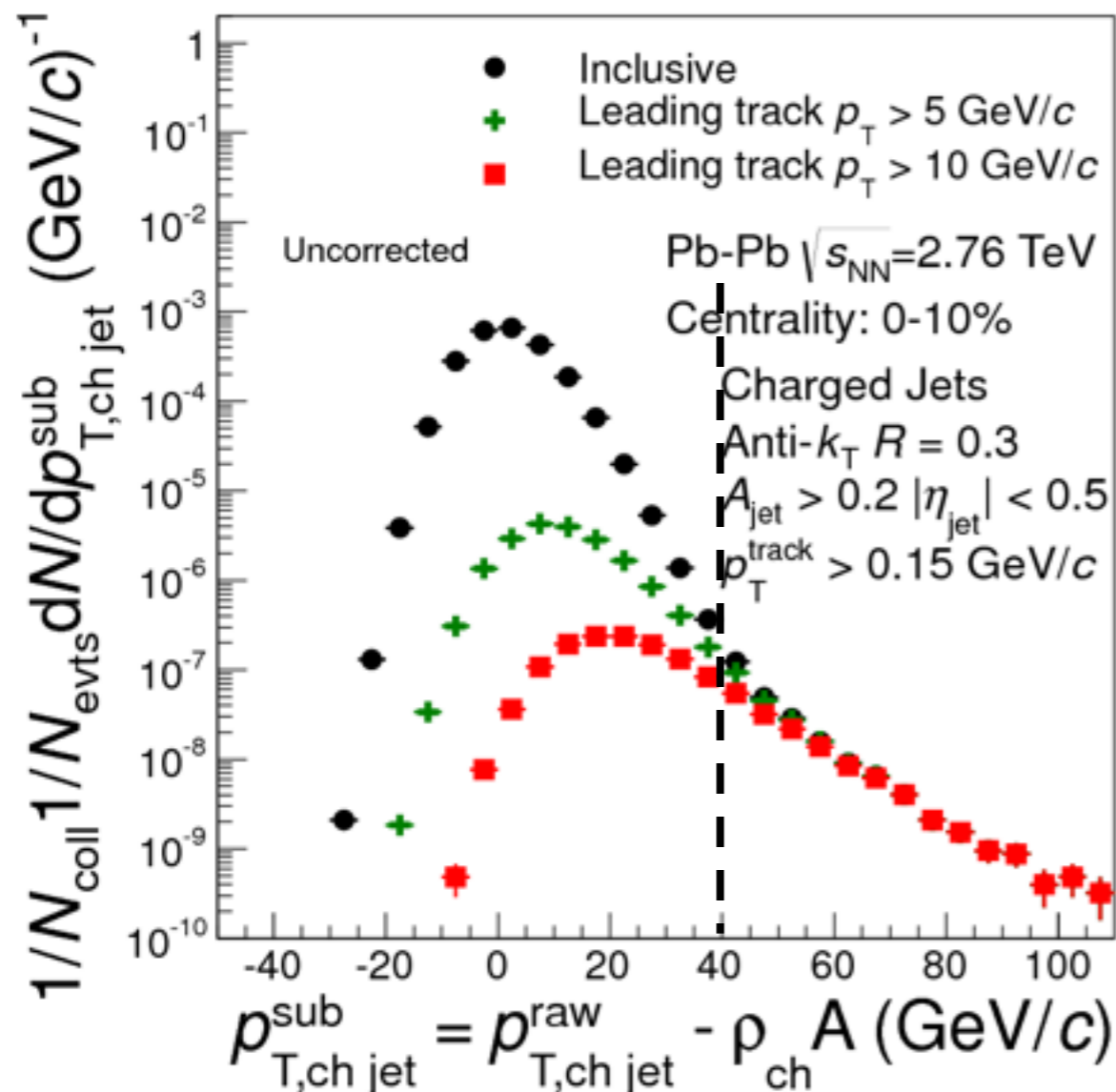
- Can be suppressed by requiring leading track
- However: no strict distinction at low  $p_T$  possible

**Next step: Correct for background fluctuations and detector effects by unfolding/deconvolution**

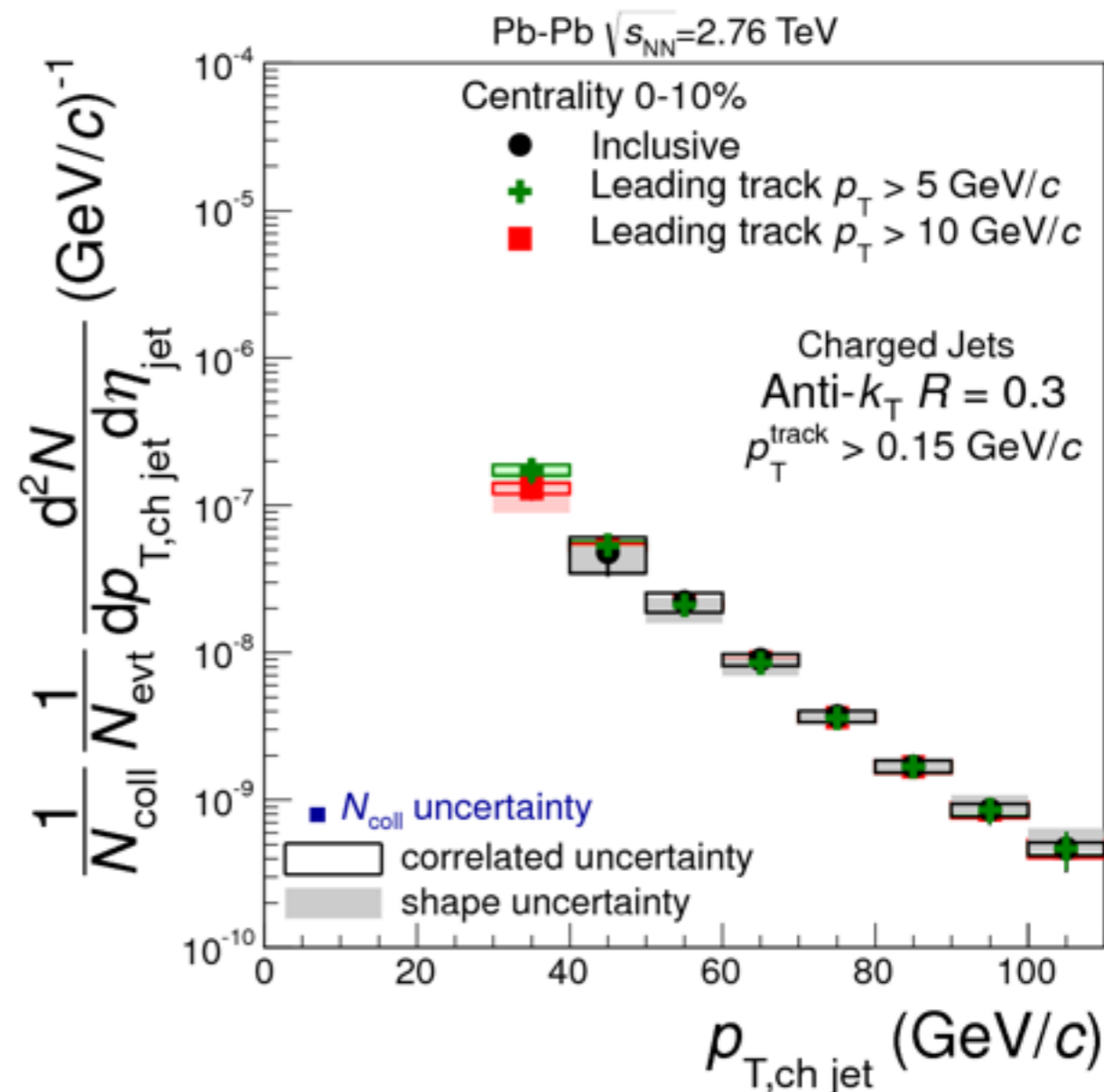


# Removing the combinatorial jets

## Raw jet spectrum



## Fully corrected jet spectrum

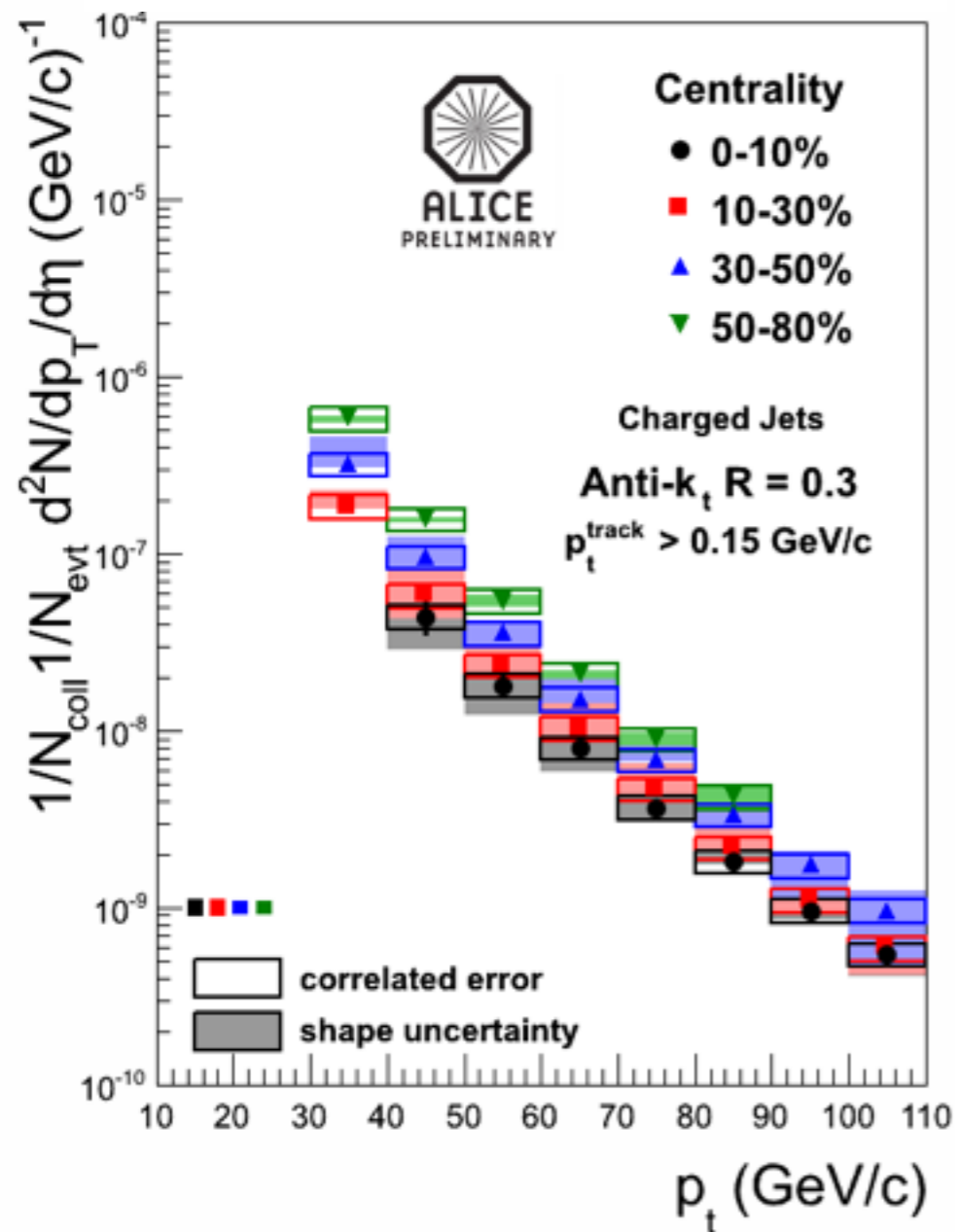


Correct spectrum and remove combinatorial jets by unfolding

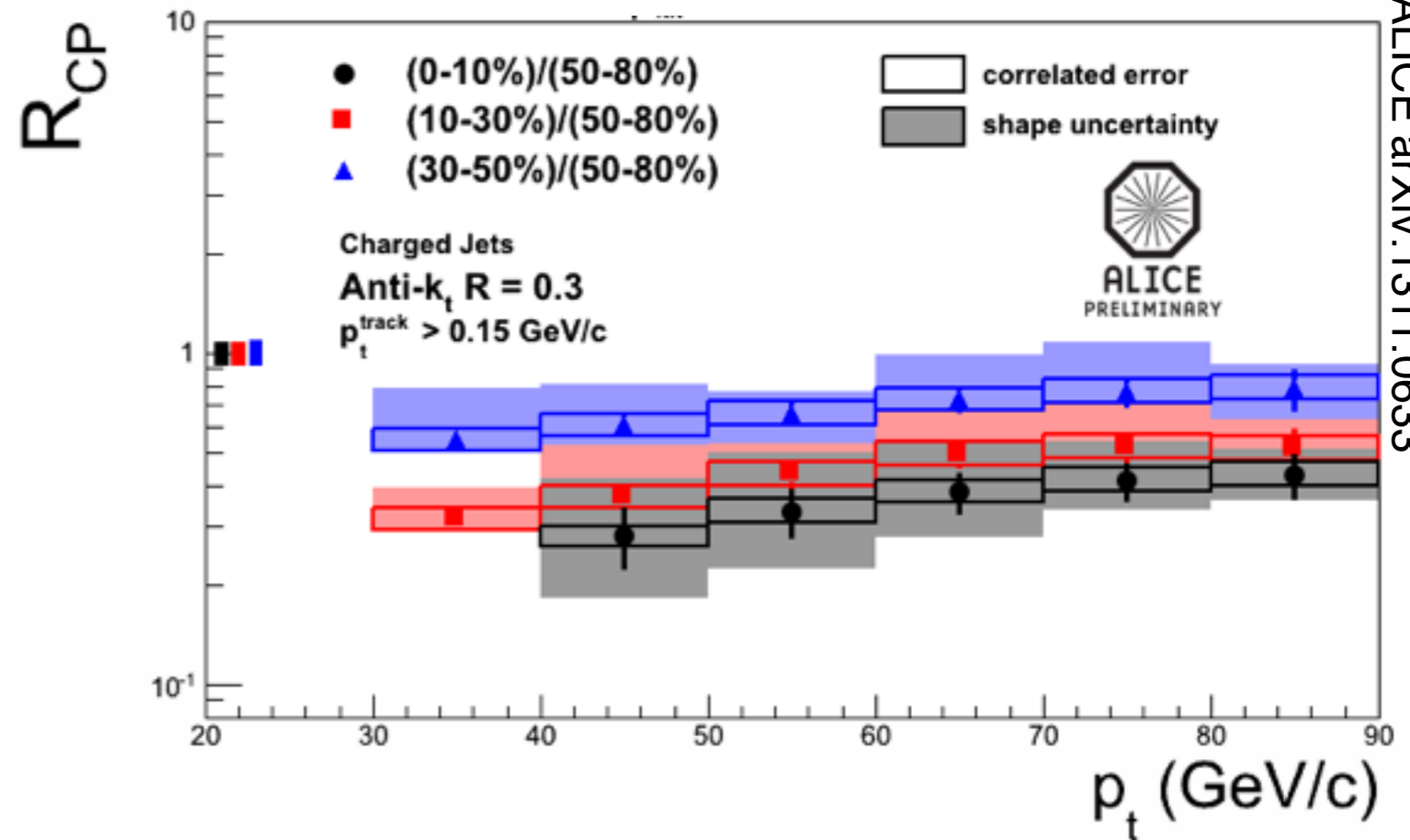
Results agree with biased jets: reliably recovers all jets and removed bk

# PbPb jet spectra

## Charged jets, $R=0.3$



## $R_{CP}$ , charged jets, $R=0.3$



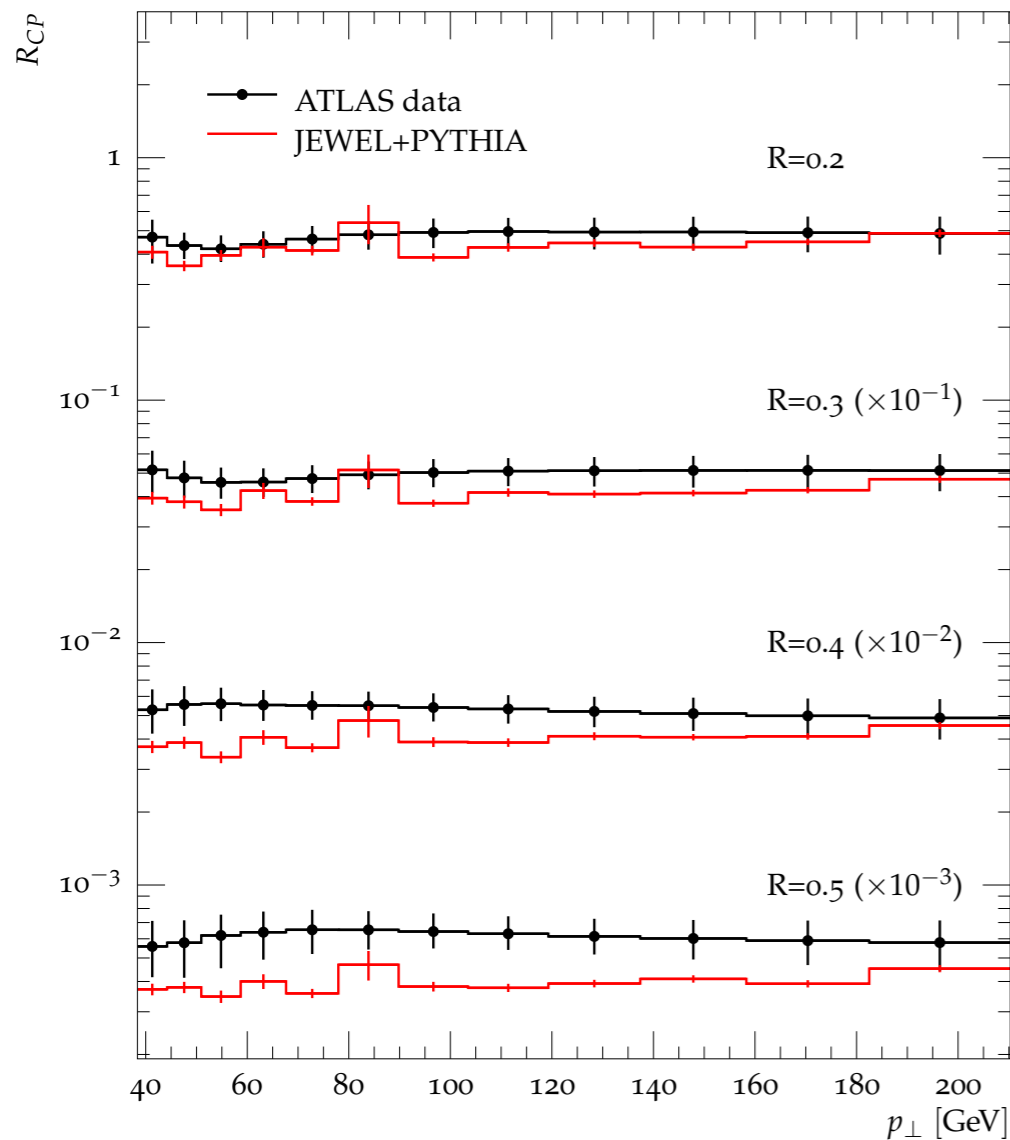
**Jet reconstruction does not 'recover' much of the radiated energy**

Jet spectrum in Pb+Pb: charged particle jets  
Two cone radii, 4 centralities

# Comparing to energy loss models

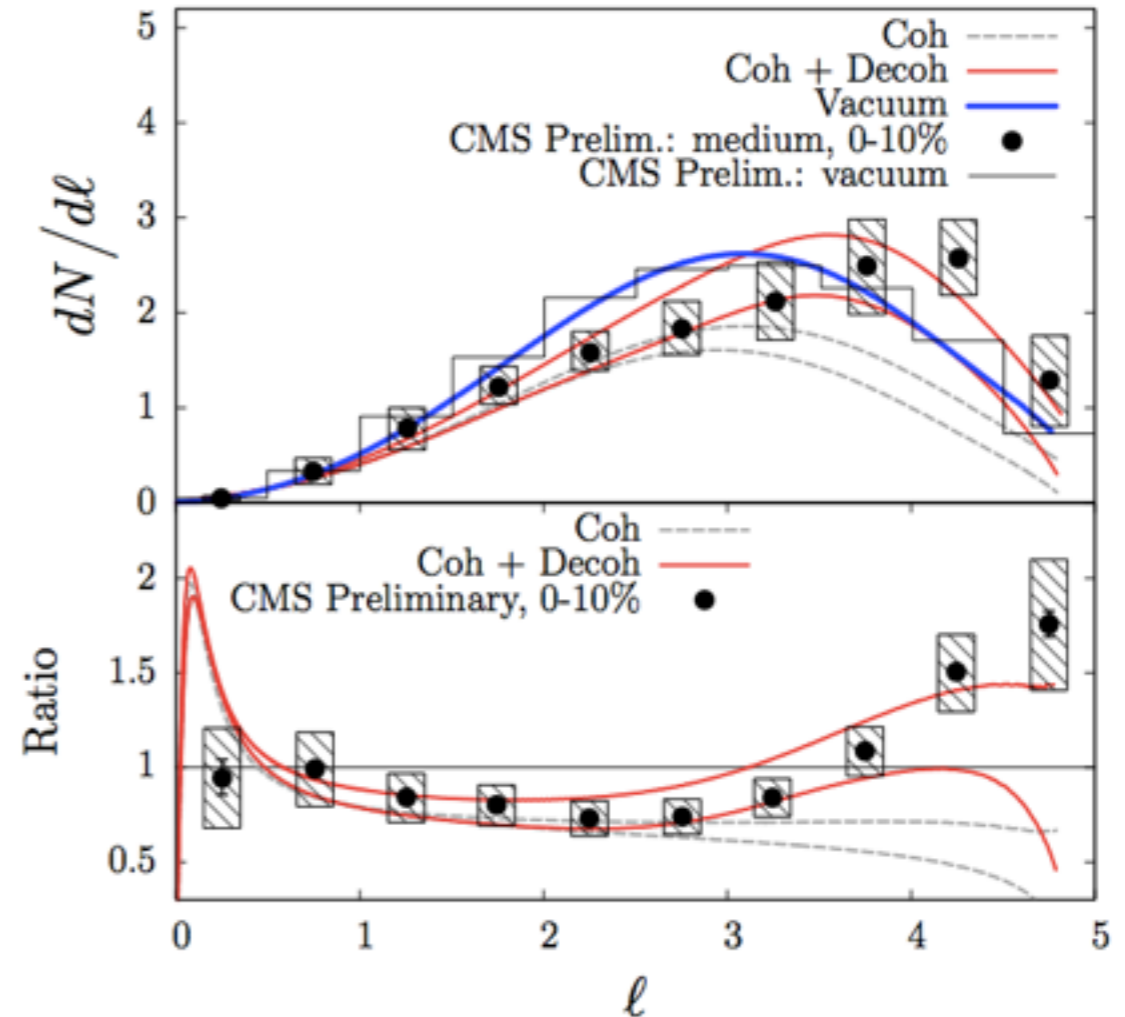
Jet observables: need explicit modelling of multi-particle final states

## JEWEL: $R_{CP}$ vs $R$



K. Zapp et al, arXiv:1212.1599

Mehtar-Tani, Tywoniuk, arXiv:1401.8293



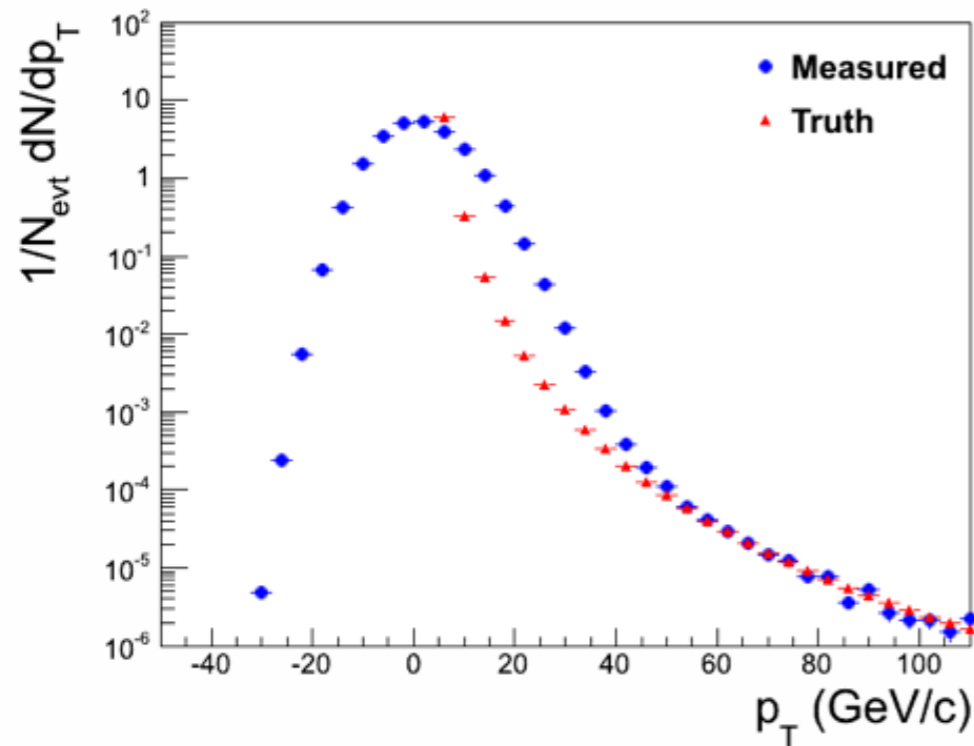
JEWEL gets the right suppression for  $R=0.2$ ,  
but not the increase with  $R$   
(Treatment of recoil partons?)

Fragment distributions sensitive  
to coherence effects  
(NB: no geometry model yet)

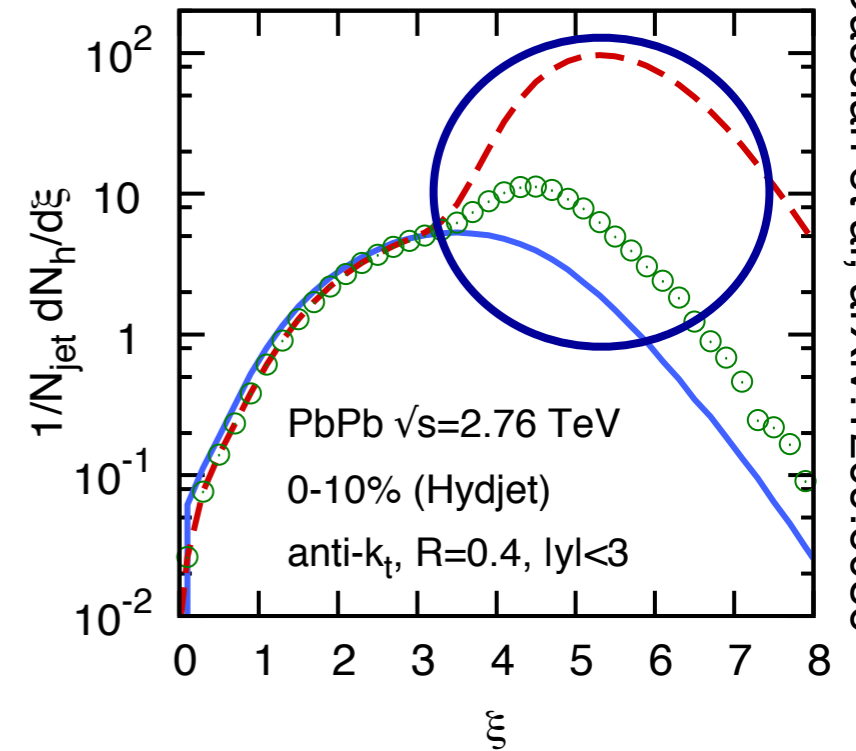
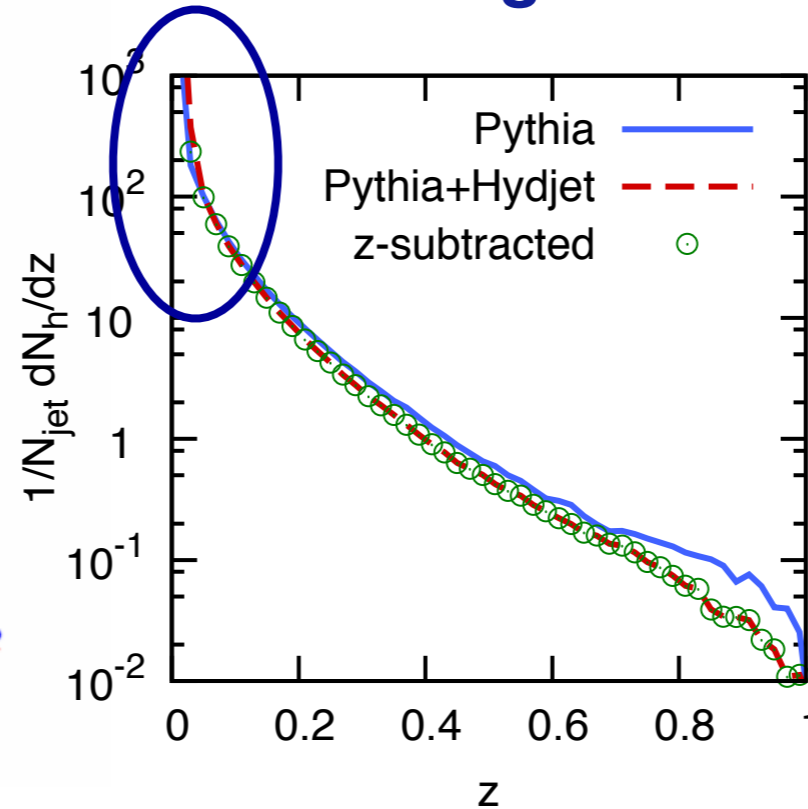


# Again: background fluctuations

## Toy model spectrum



## Fragment distributions (simulation)



**Background fluctuations migrate yield to higher  $p_T$**

**At fixed  $p_T$ : pick up above-average background contributions**

$$\xi \gtrsim 4 \Leftrightarrow p_T \lesssim 2 \text{ GeV}$$

**Current measurements mostly  $p_T > 2 \text{ GeV}$**

# Situation at RHIC, ca 2008

3 main calculations; comparison with same medium density profile

$$\hat{q} = \int_0^{q_{max}} dq_T^2 q_T^2 \frac{d\sigma}{dq_T}$$

**ASW:**  $\hat{q} = 10 - 20 \text{ GeV}^2/\text{fm}$

**HT:**  $\hat{q} = 2.3 - 4.5 \text{ GeV}^2/\text{fm}$

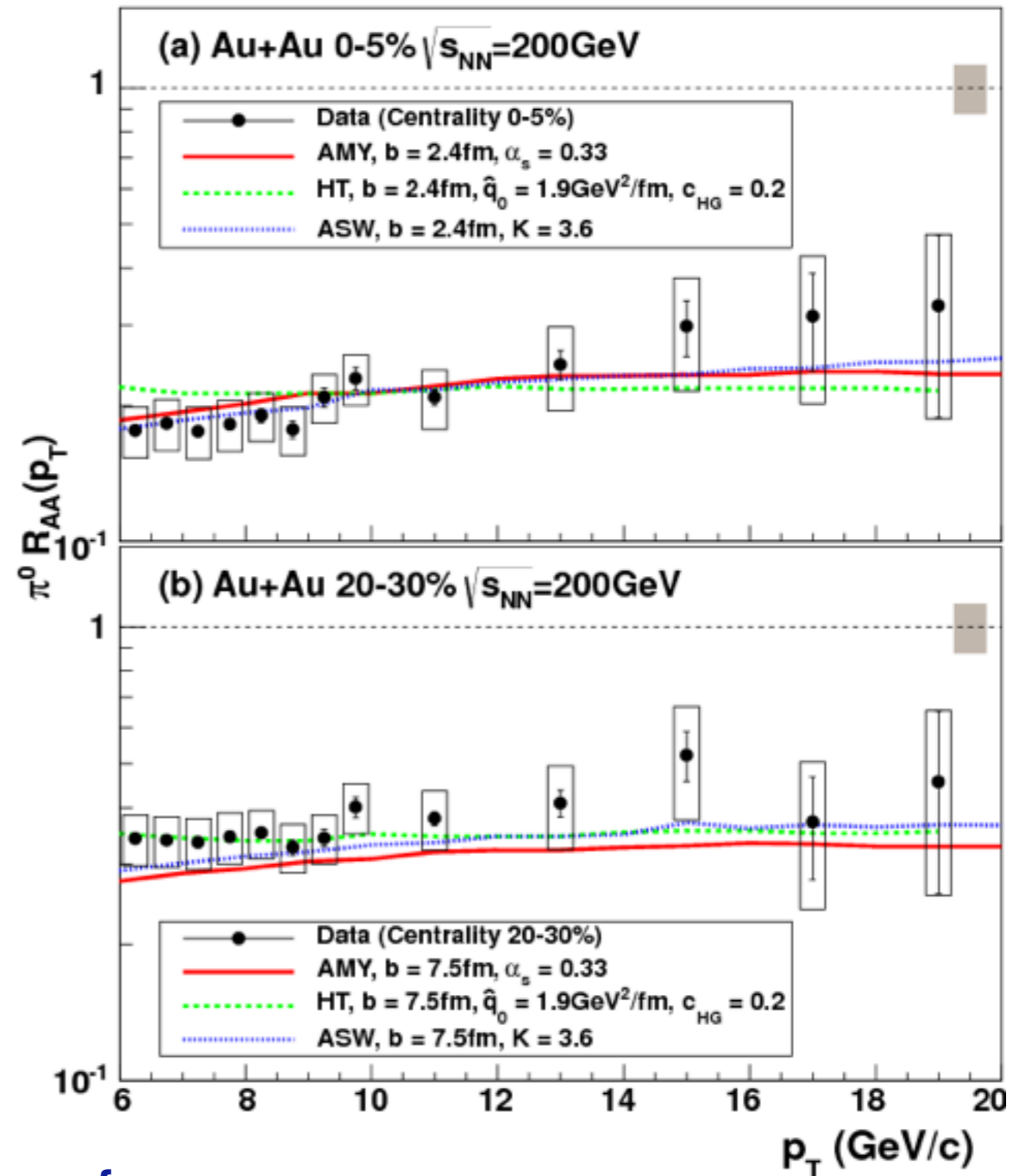
**AMY:**  $\hat{q} \approx 4 \text{ GeV}^2/\text{fm}$

Large density:

AMY:  $T \sim 400 \text{ MeV}$

Transverse kick:  $qL \sim 10\text{-}20 \text{ GeV}$

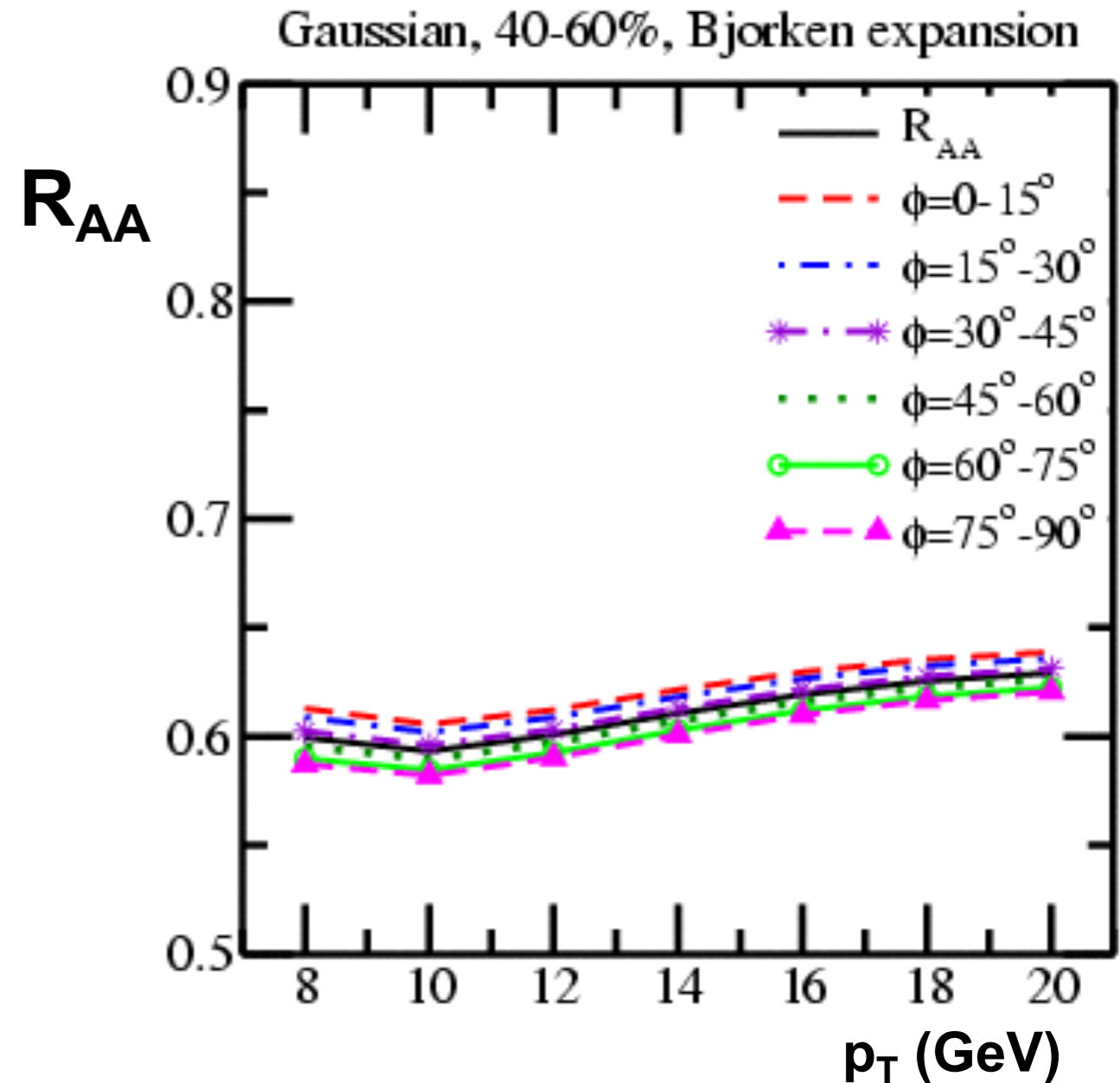
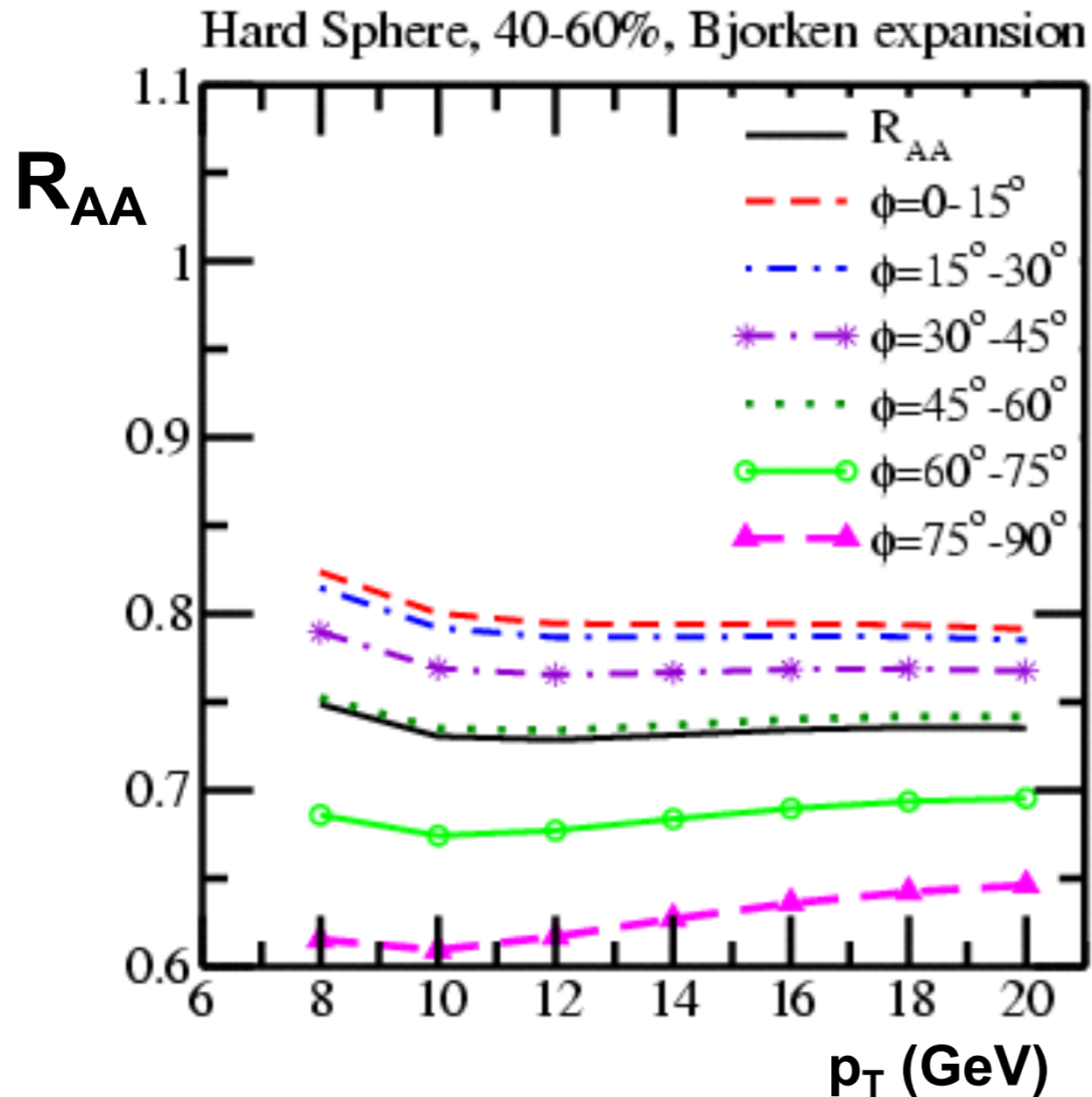
**Large uncertainty in absolute medium density**



One aspect: scattering potential/momentum transfer; see recent work by Majumder, Laine, Rothkopf on lattice

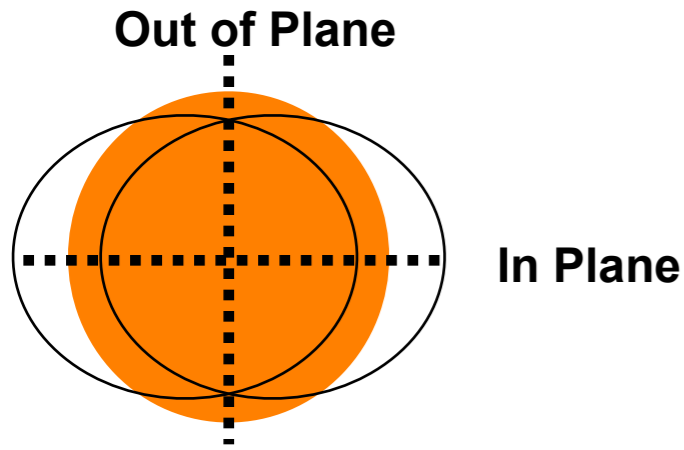
# Modelling azimuthal dependence

A. Majumder, PRC75, 021901



$R_{AA}$  vs reaction plane sensitive to geometry model

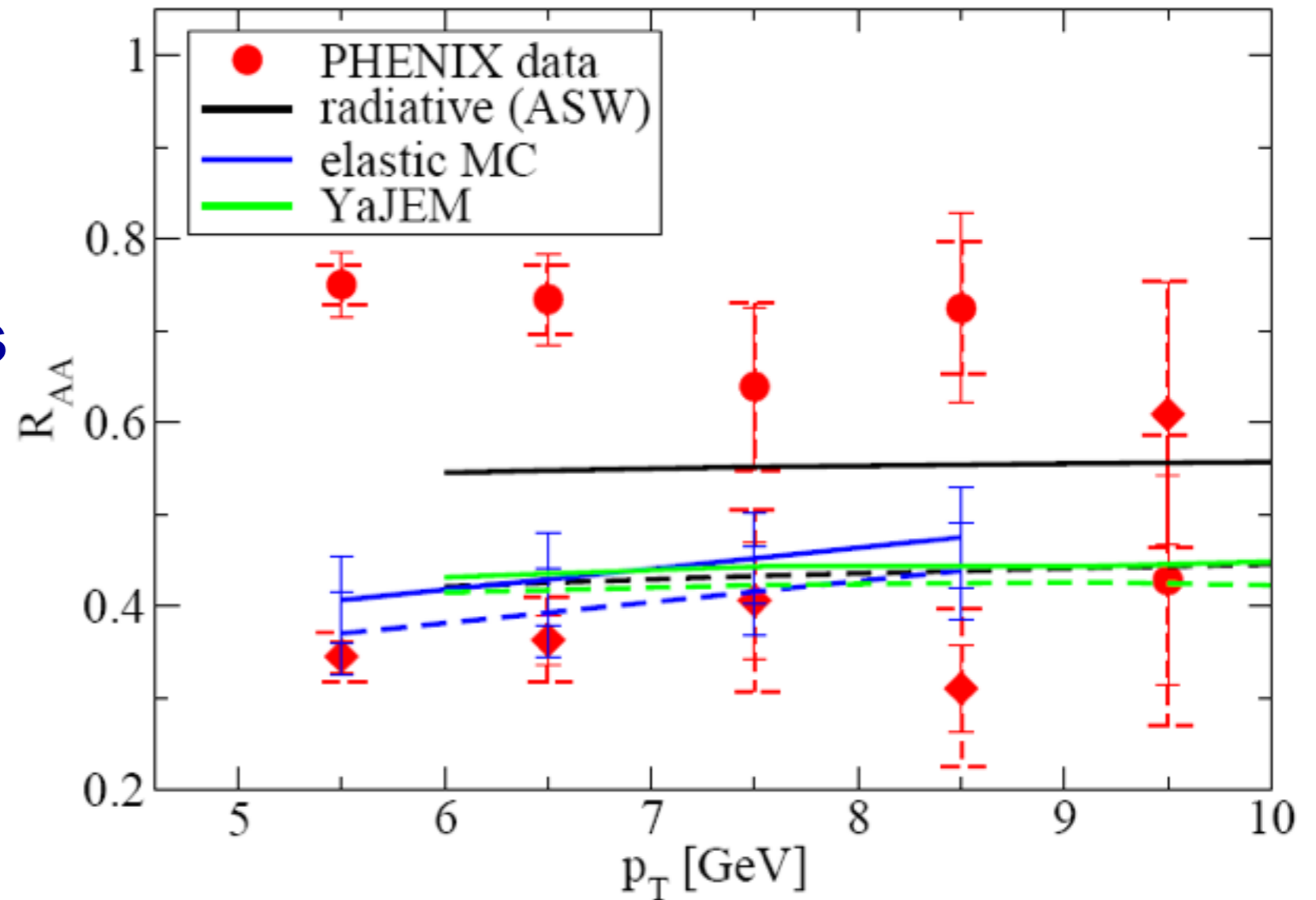
# $R_{AA}$ vs $\varphi$ and elastic e-loss



**Elastic E-loss gives small  $v_2$**

**Data require  $L^2$  or stronger path length dependence**

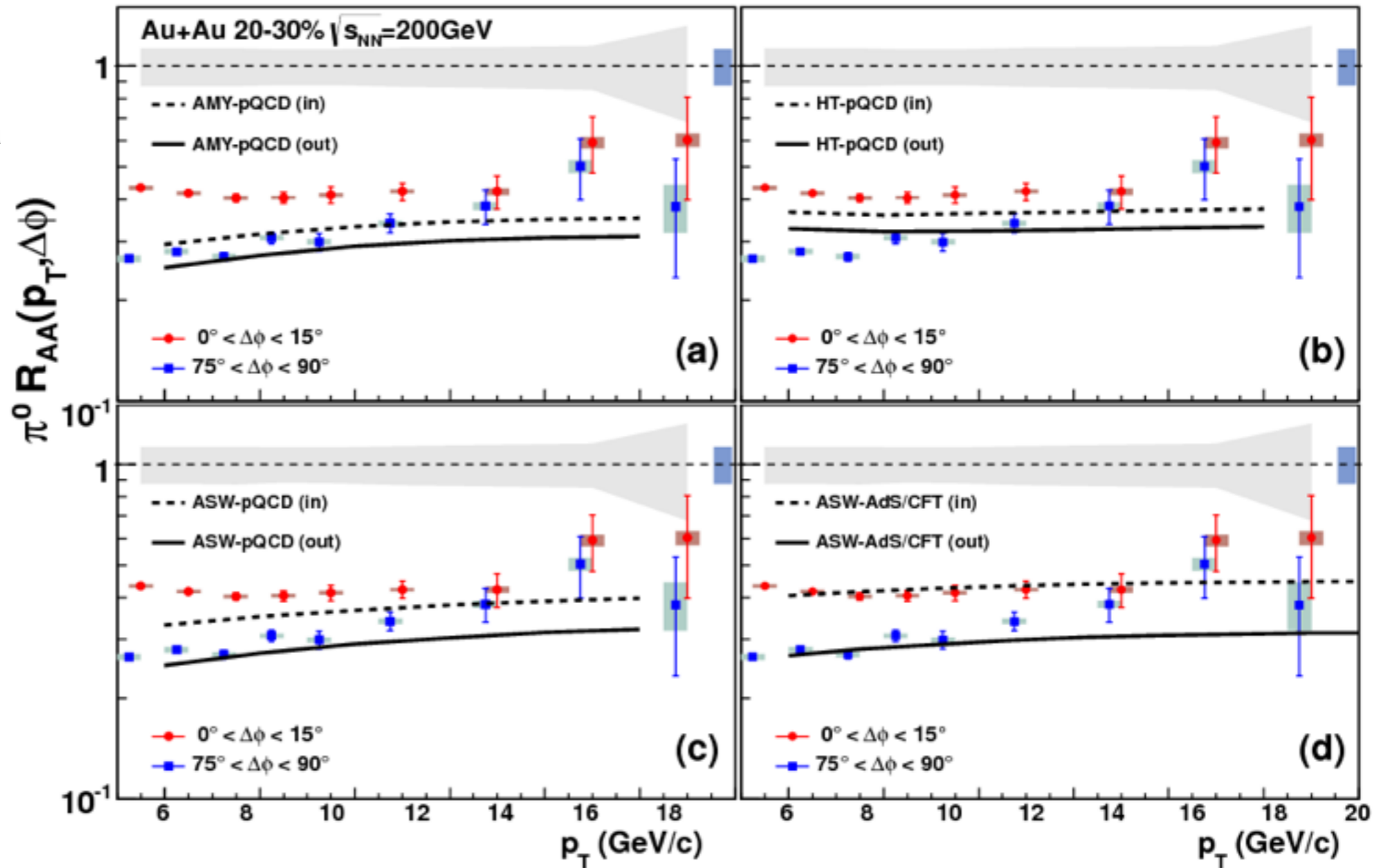
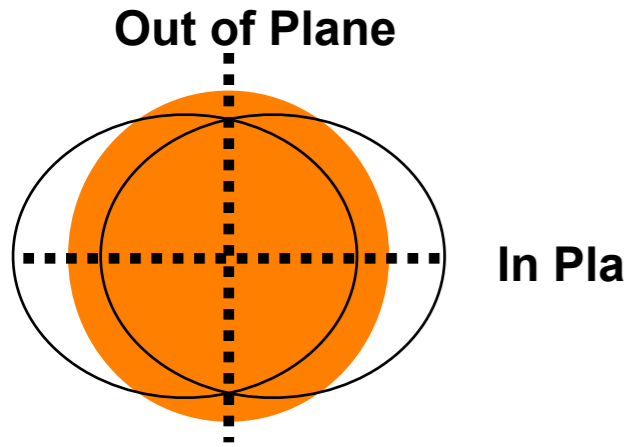
AuAu 200 AGeV, 40 - 50 %



**However, also quite sensitive to medium density evolution**

# Path length dependence: $R_{AA}$ vs $\varphi$

PHENIX, arXiv:1208.2254

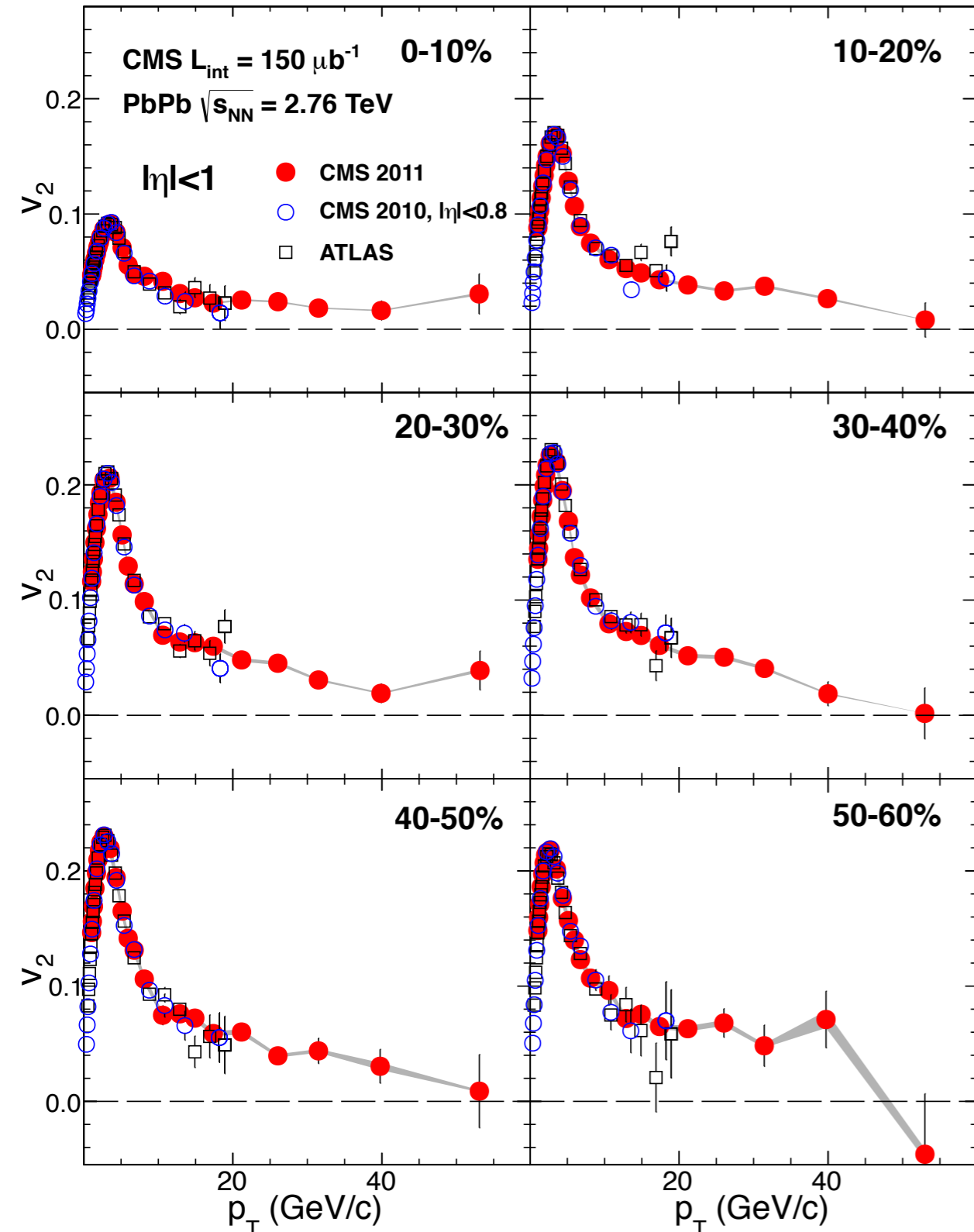


Suppression depends on angle, path length

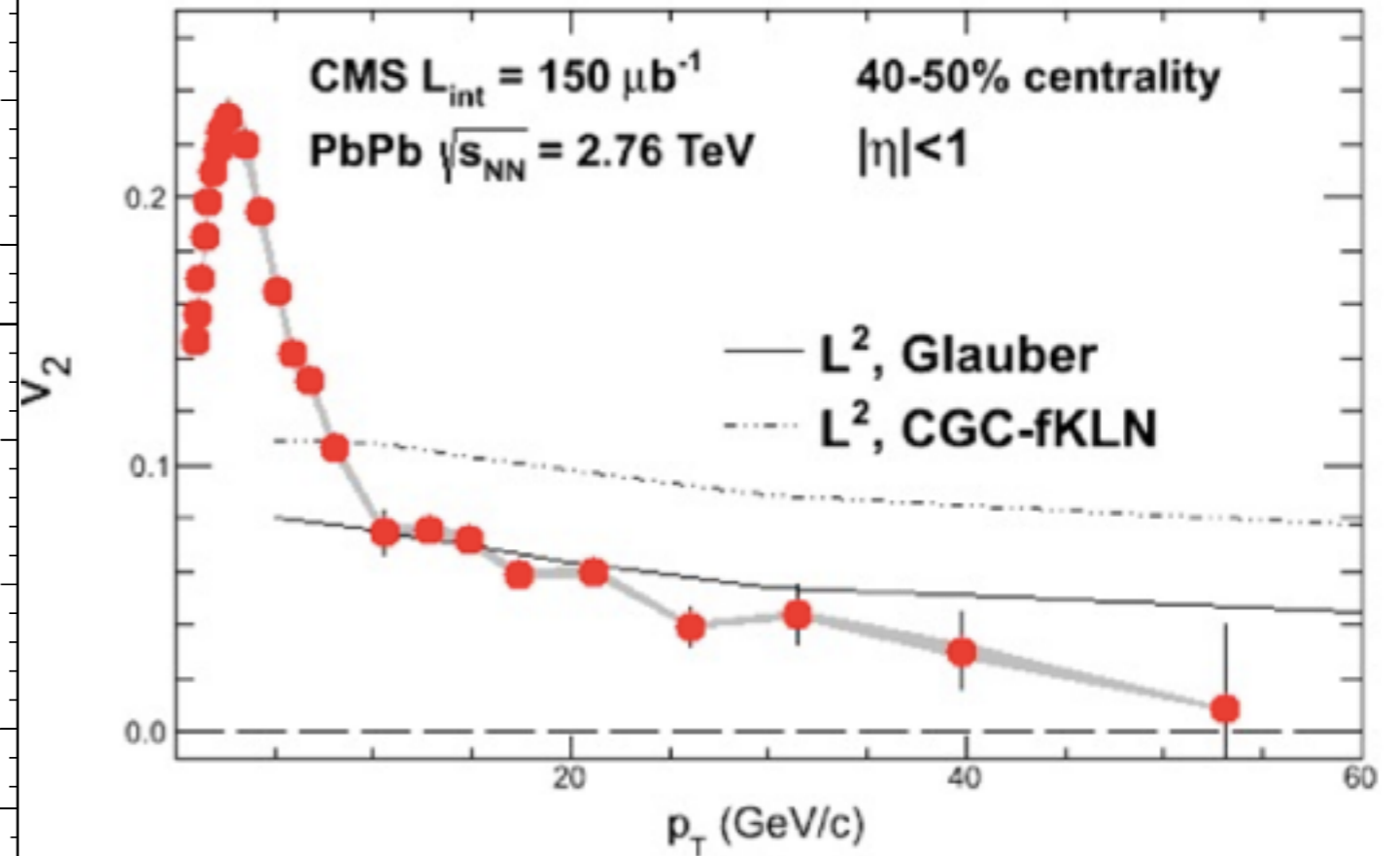
Not so easy to model: calculations give different results

# Reaction plane dependence at LHC: High- $p_T$ $v_2$

CMS, arXiv:1204.1850

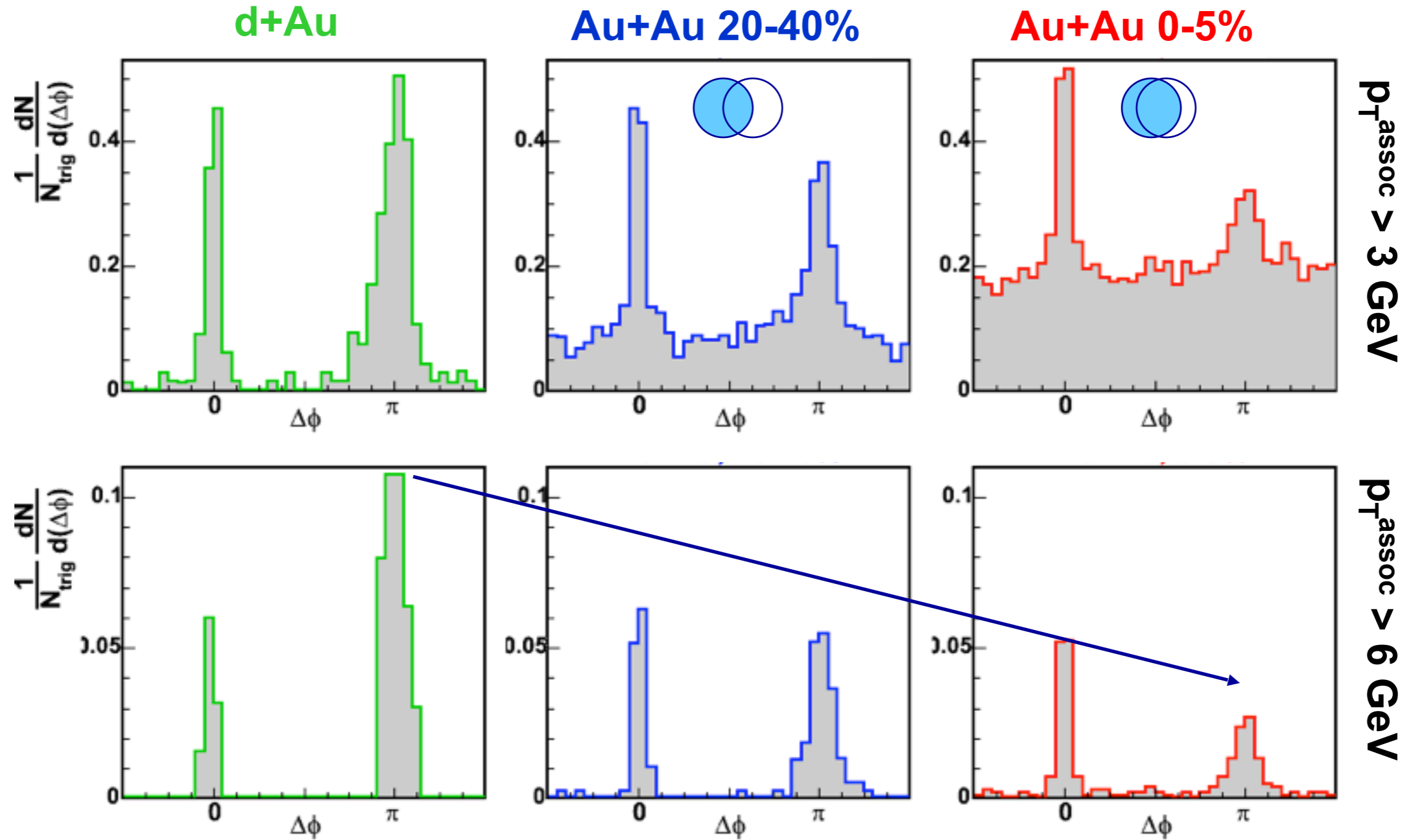


Model: B. Betz, M. Gyulassy, arXiv:1201.0281



Reasonable agreement between calculation and data for  $p_T > 10 \text{ GeV}$   
 (NB: simplified geometry, E-loss;  
 paper claims scale-dependence of  $\alpha_s$  main effect)

# Di-hadrons at high- $p_T$ : recoil suppression



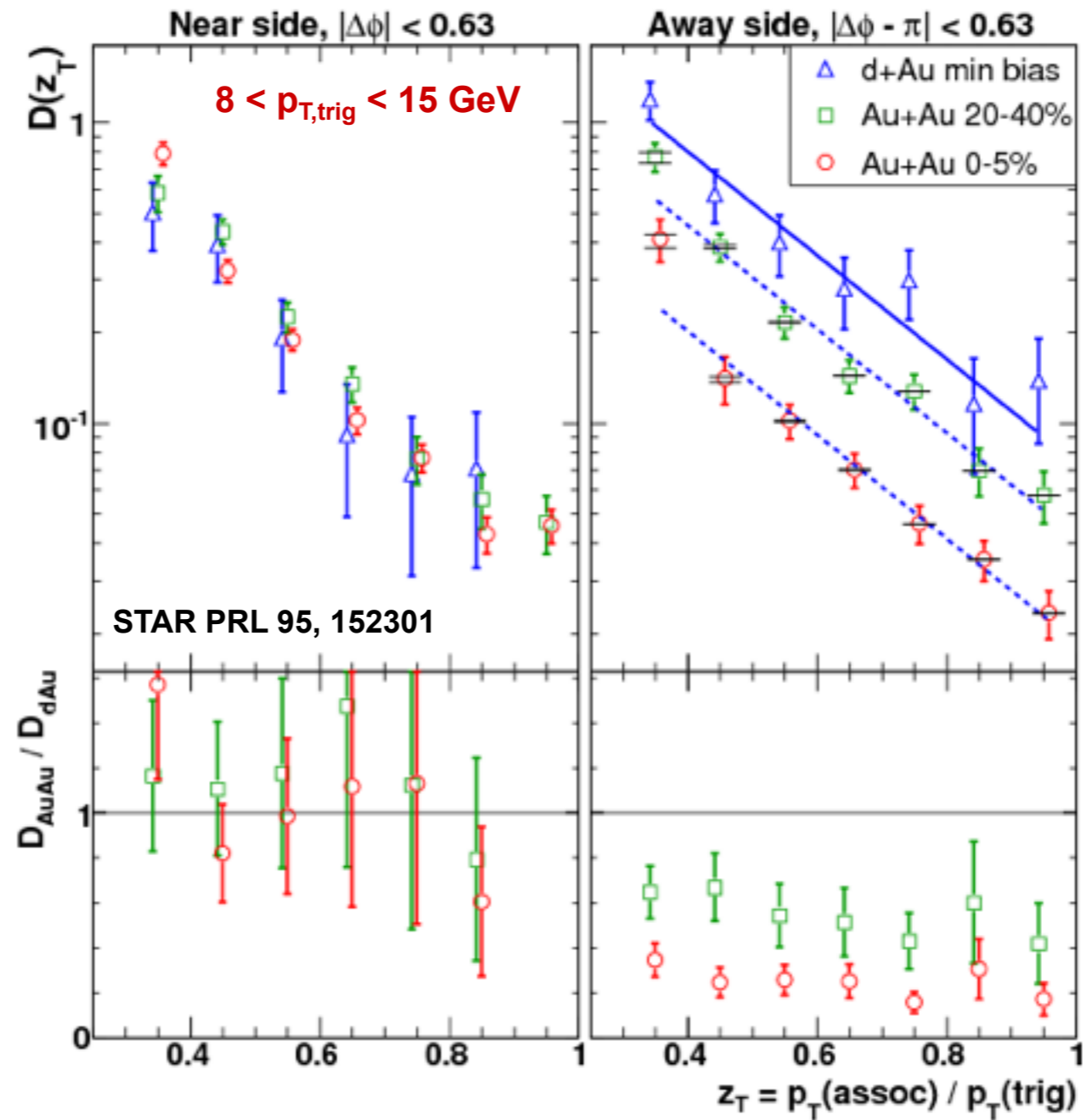
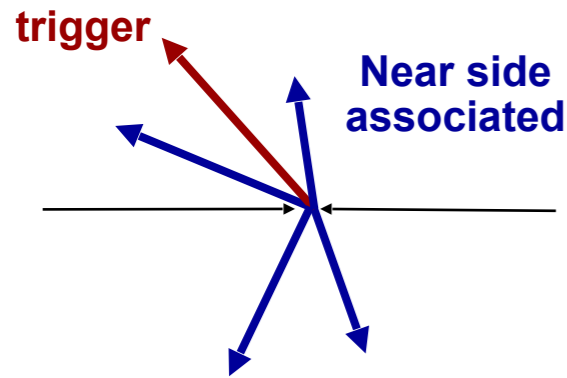
High- $p_T$  hadron production in Au+Au dominated by (di-)jet fragmentation

Suppression of away-side yield in Au+Au collisions: energy loss

# Dihadron yield suppression

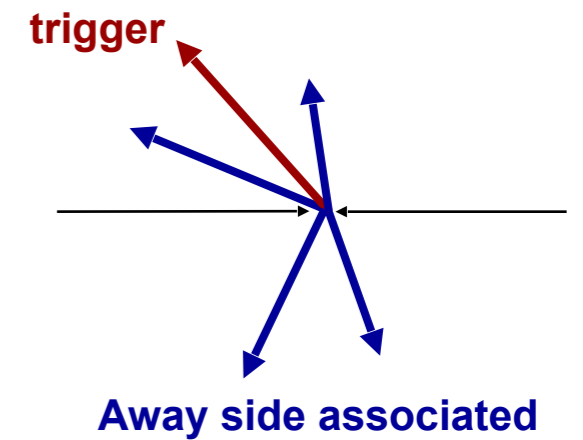
## Near side

Yield of additional particles in the jet



## Away side

Yield in balancing jet, after energy loss



**Near side: No modification**  
 ⇒ Fragmentation outside medium?

**Away-side: Suppressed by factor 4-5**  
 ⇒ large energy loss



# Four formalisms

## Multiple gluon emission

- **Hard Thermal Loops (AMY)**
  - Dynamical (HTL) medium
  - Single gluon spectrum: BDMPs-Z like path integral
  - No vacuum radiation
- **Multiple soft scattering (BDMPs-Z, ASW-MS)**
  - Static scattering centers
  - Gaussian approximation for momentum kicks
  - Full LPM interference and vacuum radiation
- **Opacity expansion ((D)GLV, ASW-SH)**
  - Static scattering centers, Yukawa potential
  - Expansion in opacity  $L/\lambda$   
( $N=1$ , interference between two centers default)
  - Interference with vacuum radiation
- **Higher Twist (Guo, Wang, Majumder)**
  - Medium characterised by higher twist matrix elements
  - Radiation kernel similar to GLV
  - Vacuum radiation in DGLAP evolution

**Fokker-Planck  
rate equations**

**Poisson ansatz  
(independent emission)**

**DGLAP  
evolution**

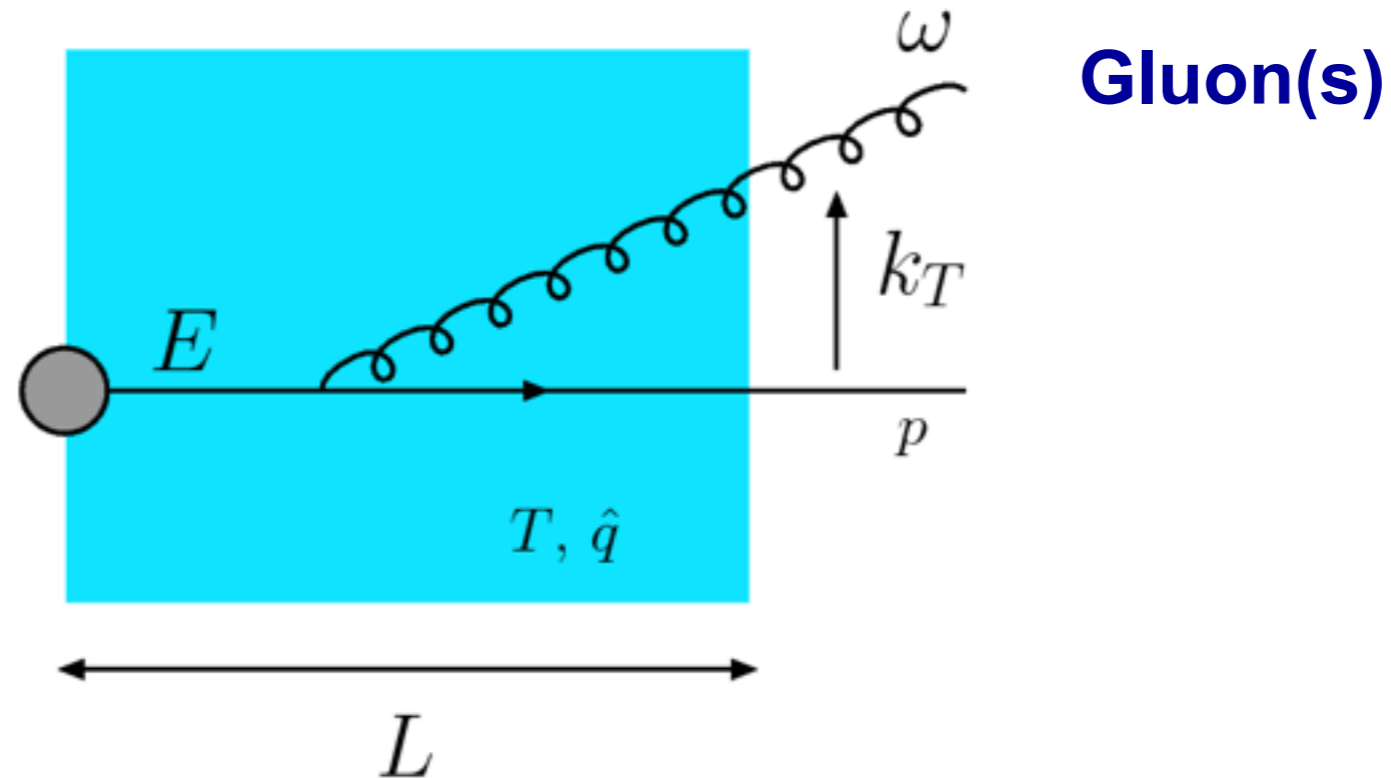
**All formalisms can be related to the same BDMPs-Z path  
integral formalism; different approximations used**

See also: arXiv:1106.1106

# The Brick Problem

TECHQM: Theory-Experiment Collaboration on Hot Quark Matter

arXiv:1106.1106



Compare energy-loss in a well-defined model system:

Fixed length  $L = 2, 5$  fm

Density  $T, \hat{q}$

Quark,  $E = 10, 20$  GeV

Compare outgoing gluon, quark distributions

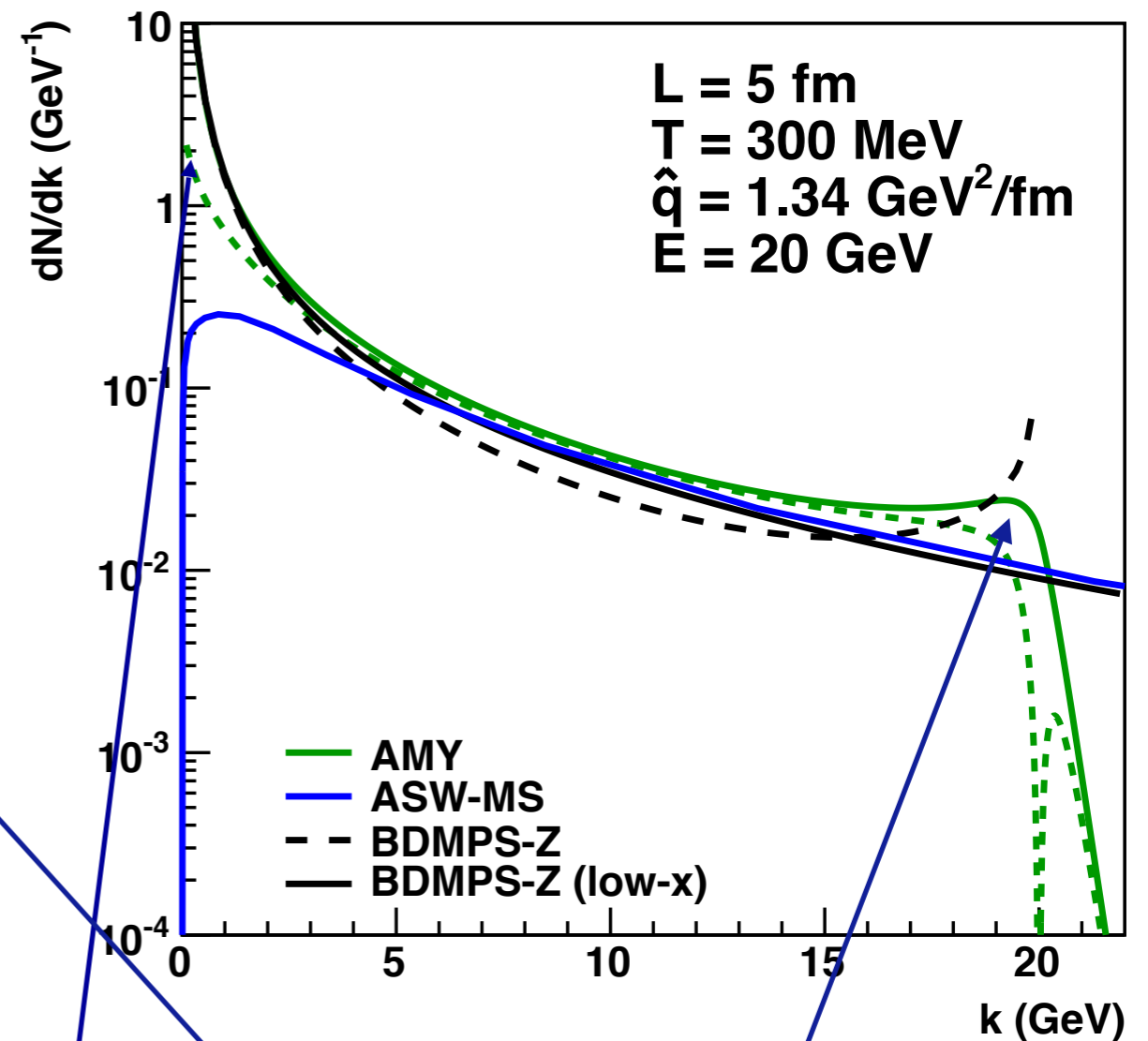
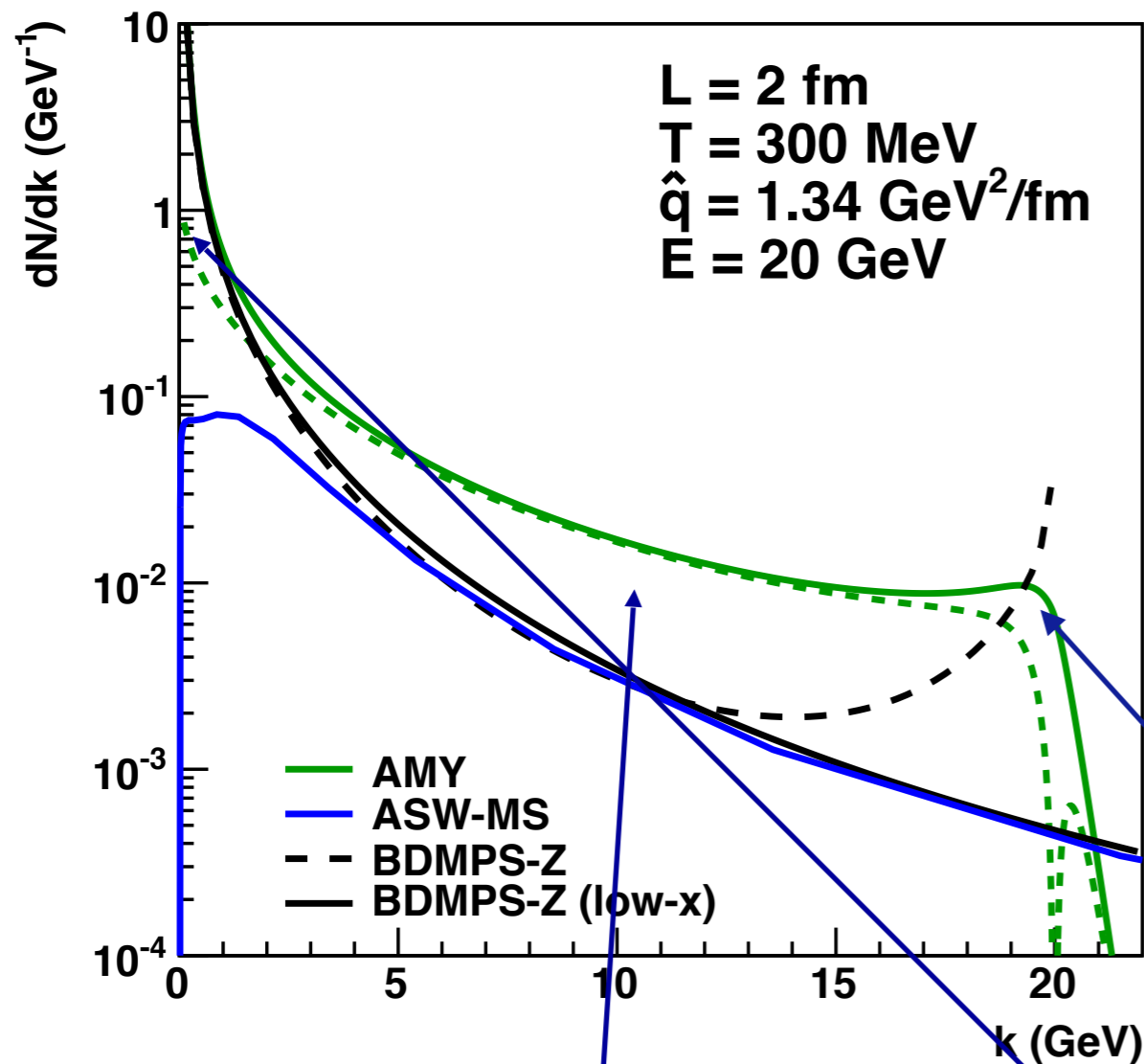
Two types of comparison: - Same density  
- Same suppression

and interpret/understand the differences

# Multiple soft scattering: BDMPS, AMY

L=2 fm Single gluon spectra

L=5 fm Single gluon spectra



**AMY: no large angle cut-off**

**+ sizeable difference at intermediate  $\omega$  at L=2 fm**

**Large x treatment in AMY more accurate**

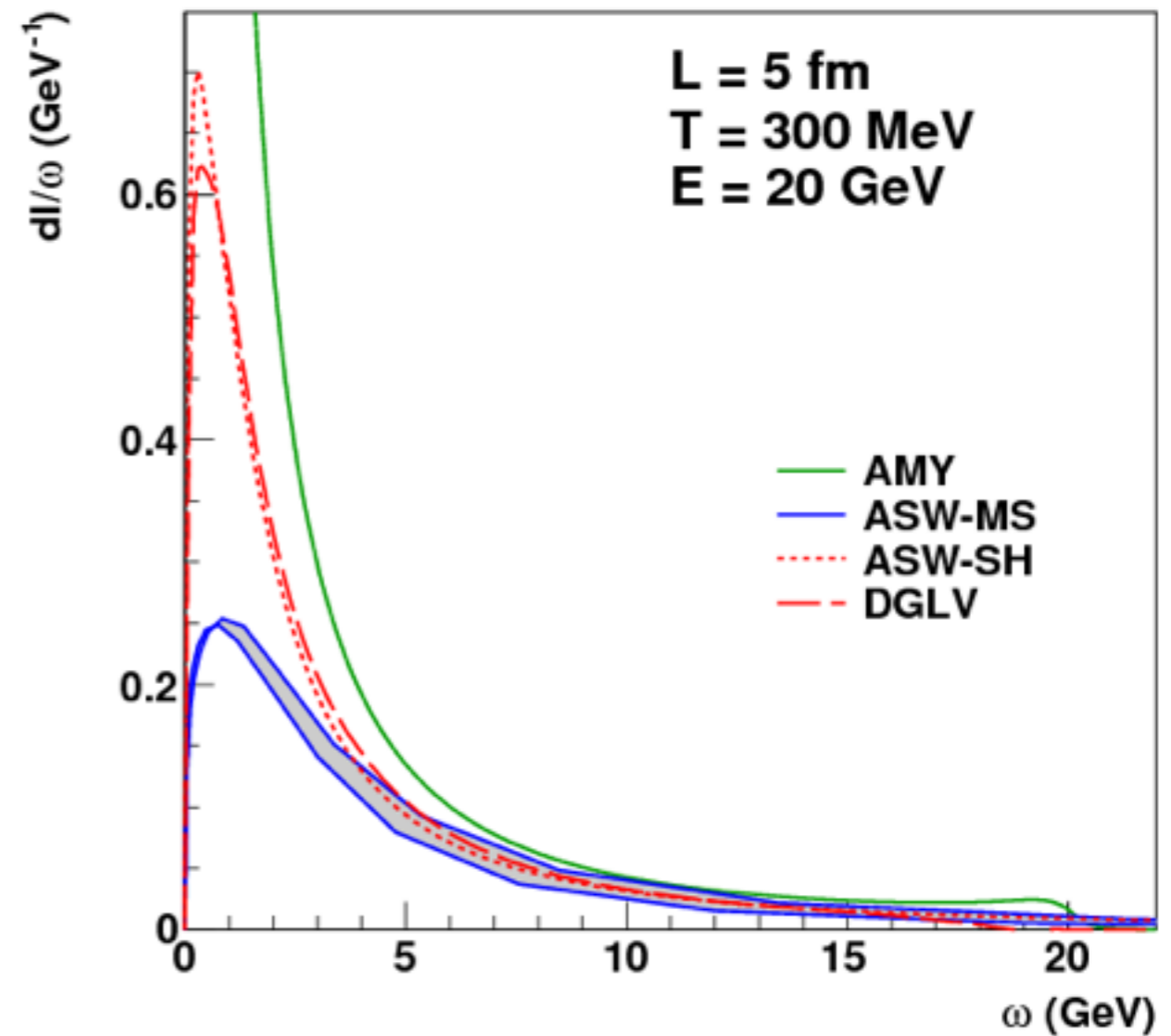
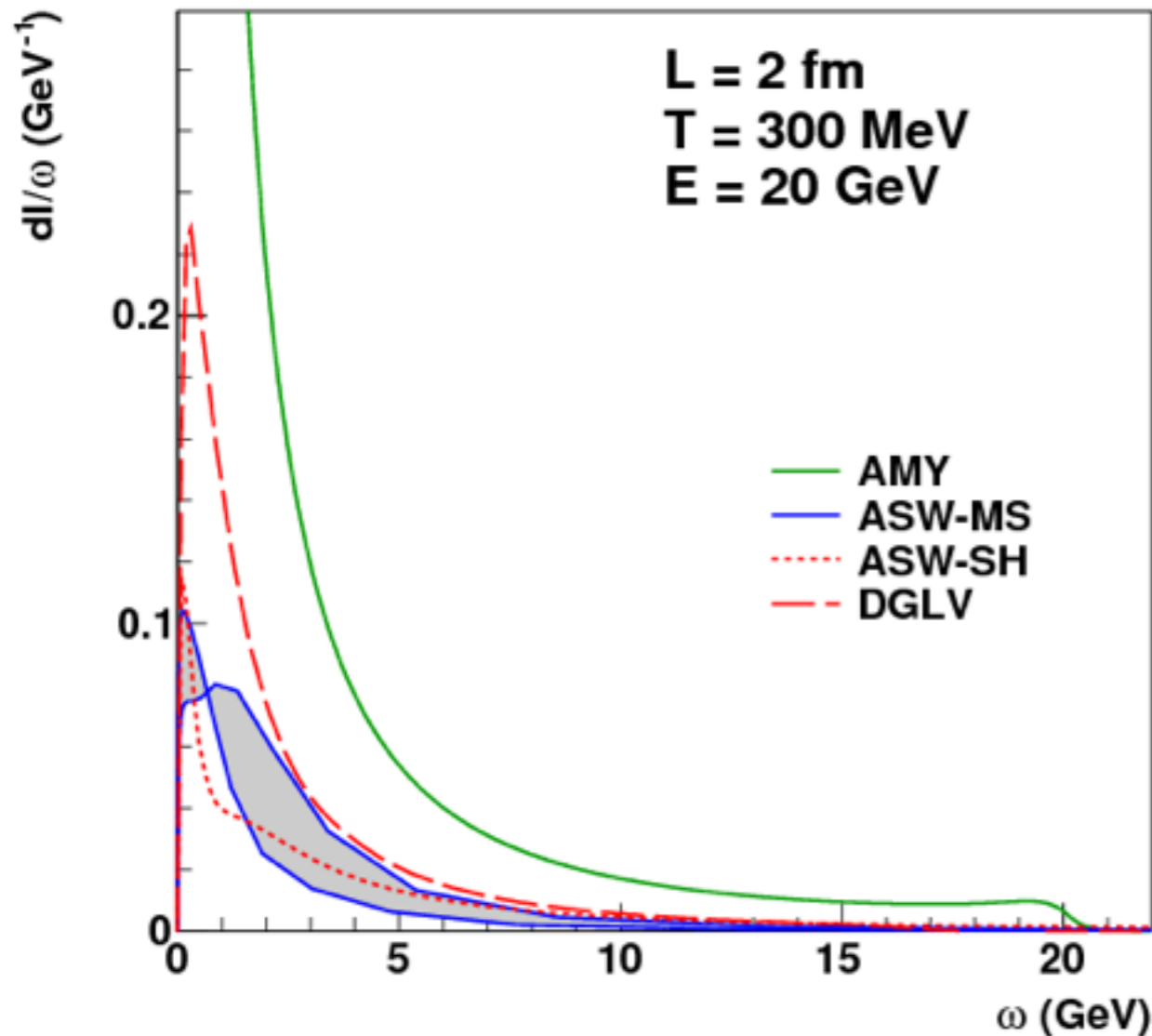
Using  $\hat{q}(T)$  based on AMY-HTL scattering potential

# Single gluon spectra

Same temperature

$L = 2$  fm

$L = 5$  fm



@Same temperature:  $AMY > OE > ASW-MS$

Size of difference depends on  $L$ , but hierarchy stays

# Multiple gluon emission — Poisson ansatz

**Average number of gluons:**

$$\langle N_{gluon} \rangle = \int \frac{dI}{d\omega} d\omega$$

**Poisson fluctuations:**

$$P(n) = \frac{1}{n!} \langle N_{gluon} \rangle^n e^{-\langle N_{gluon} \rangle}$$

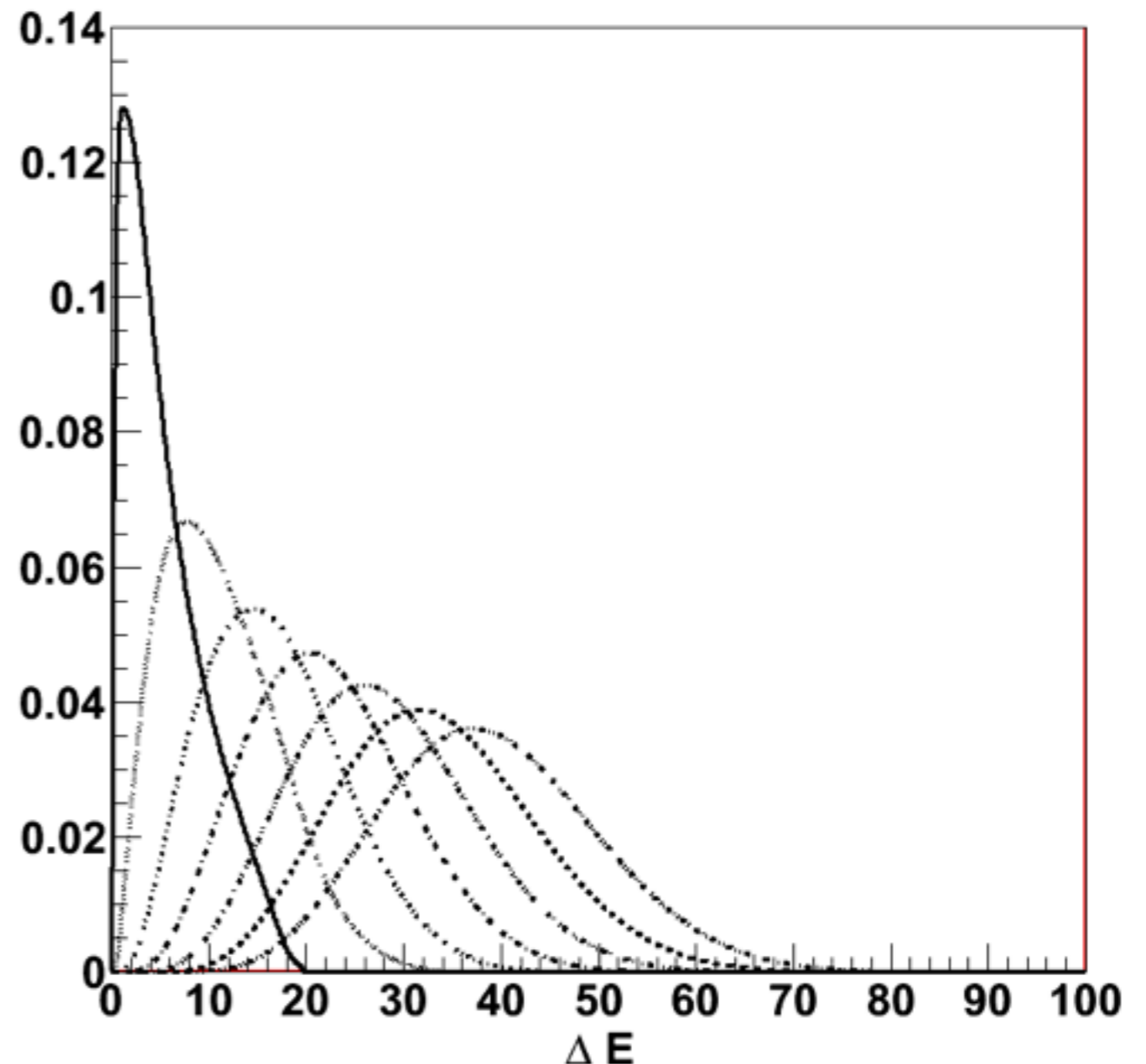
(assumed)

**Total probability:**

$$P(\Delta E) = \sum_{n=0}^{\infty} \frac{1}{n!} \left[ \prod_{i=1}^n \int d\omega_i \frac{dI(\omega_i)}{d\omega} \right] \delta \left( \Delta E - \sum_{i=1}^n \omega_i \right) \exp \left[ - \int_0^{\infty} d\omega \frac{dI}{d\omega} \right]$$

$$P(\Delta E) = p_0 \delta(\Delta E) + p(\Delta E)$$

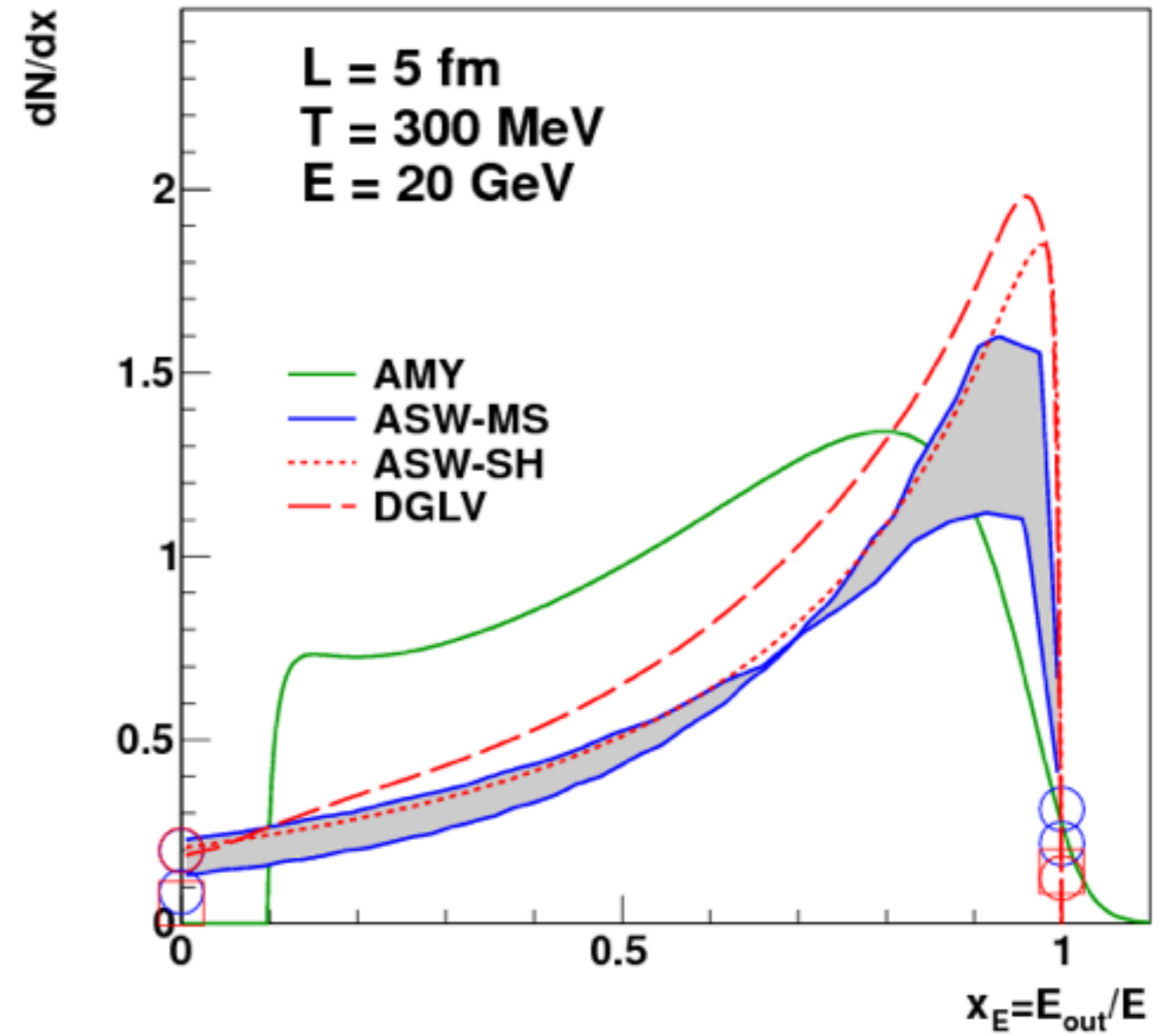
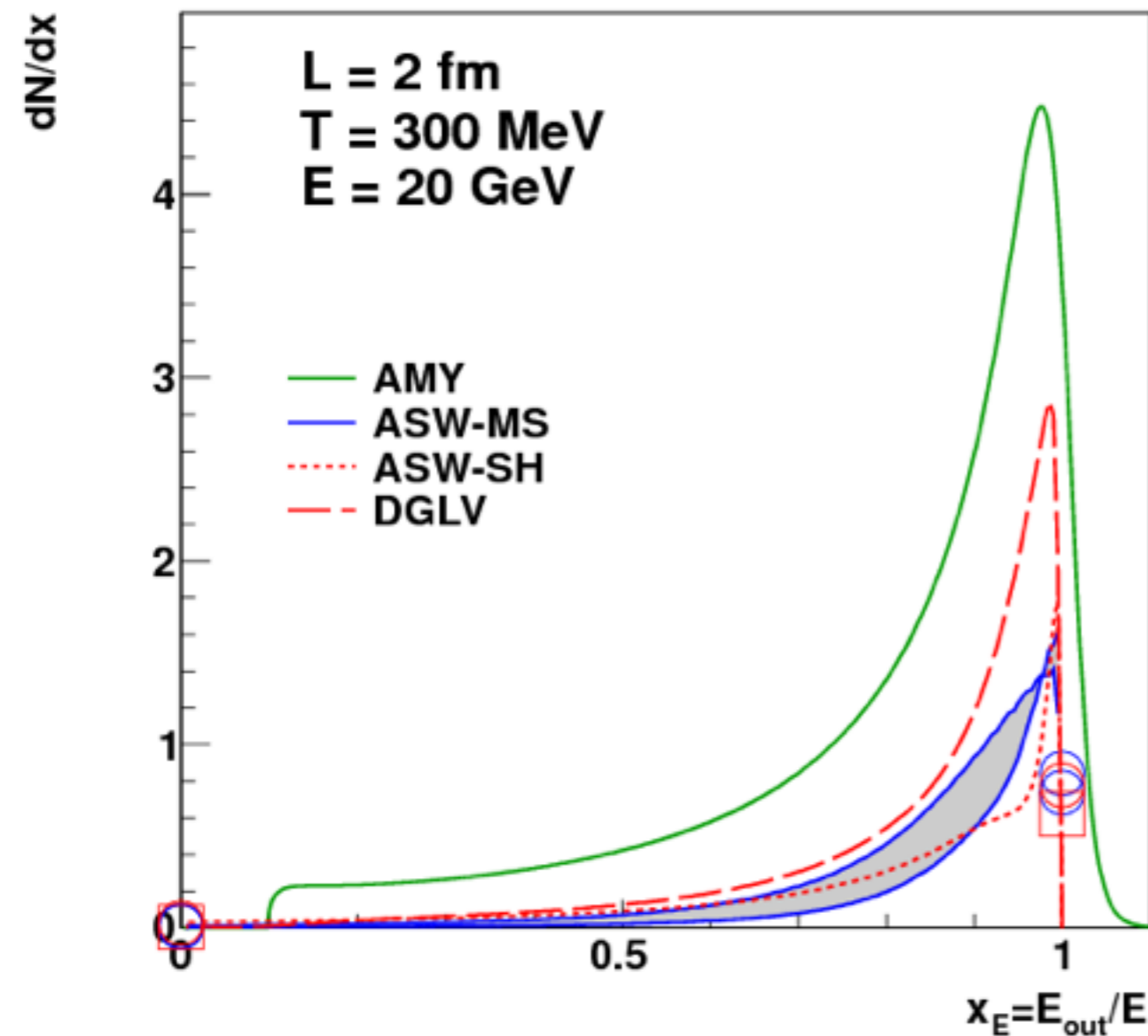
**Poisson convolution example**



**Main other approach: build into DGLAP (used for HT)**

# Outgoing quark spectra

Same temperature:  $T = 300$  MeV

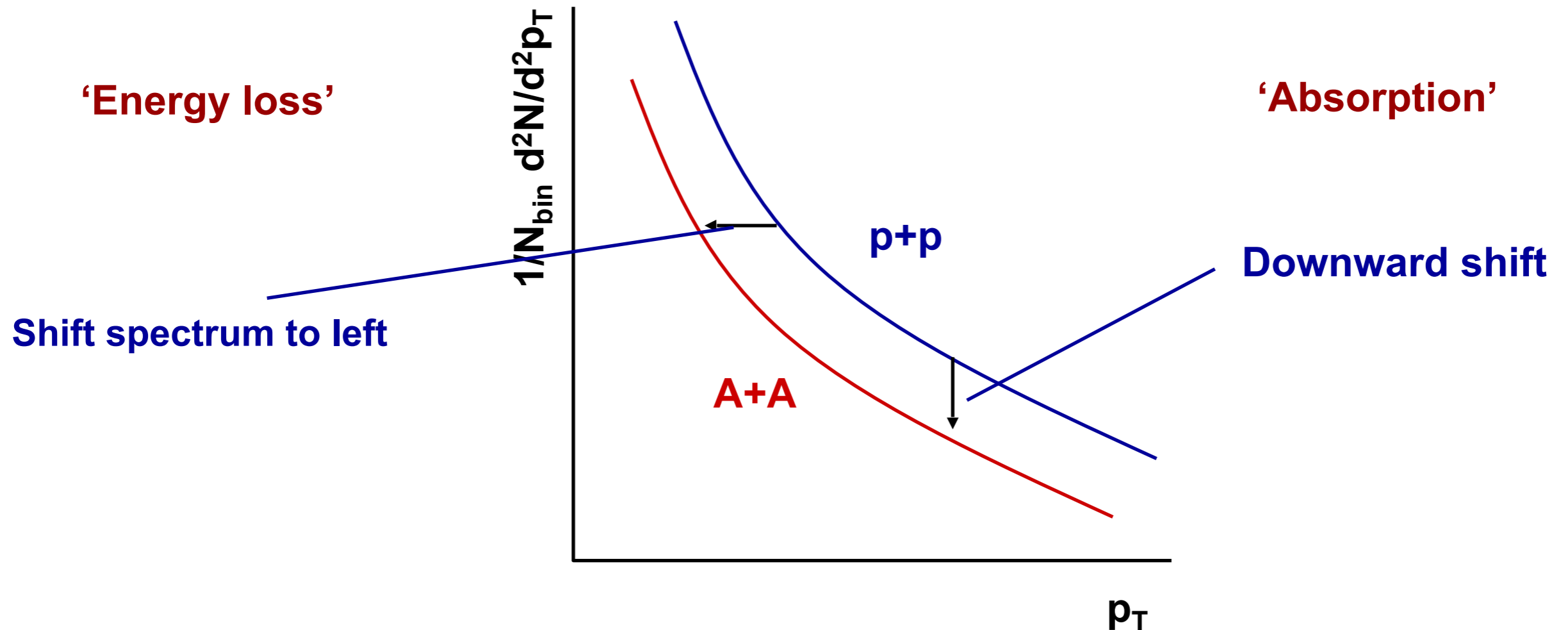


**@Same  $T$ : suppression  $AMY > OE > ASW-MS$**

**Note importance of  $P_0$**

# Nuclear modification factor $R_{AA}$

$$R_{AA} = \frac{dN/dp_T|_{A+A}}{N_{coll} dN/dp_T|_{p+p}}$$



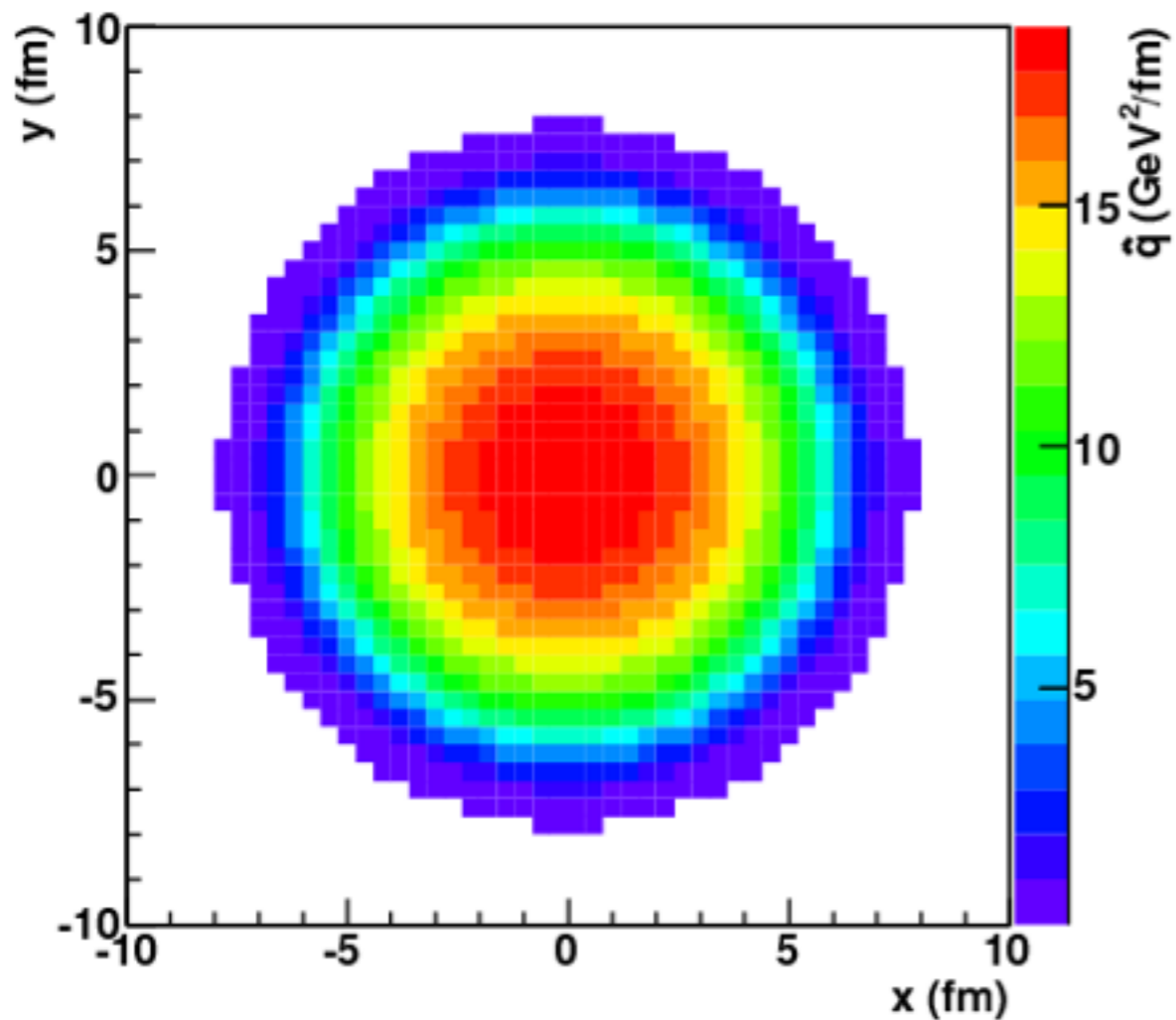
Measured  $R_{AA}$  is a ratio of yields at a given  $p_T$

The physical mechanism is energy loss; shift of yield to lower  $p_T$

The full range of physical pictures can be captured with an energy loss distribution  $P(\Delta E)$

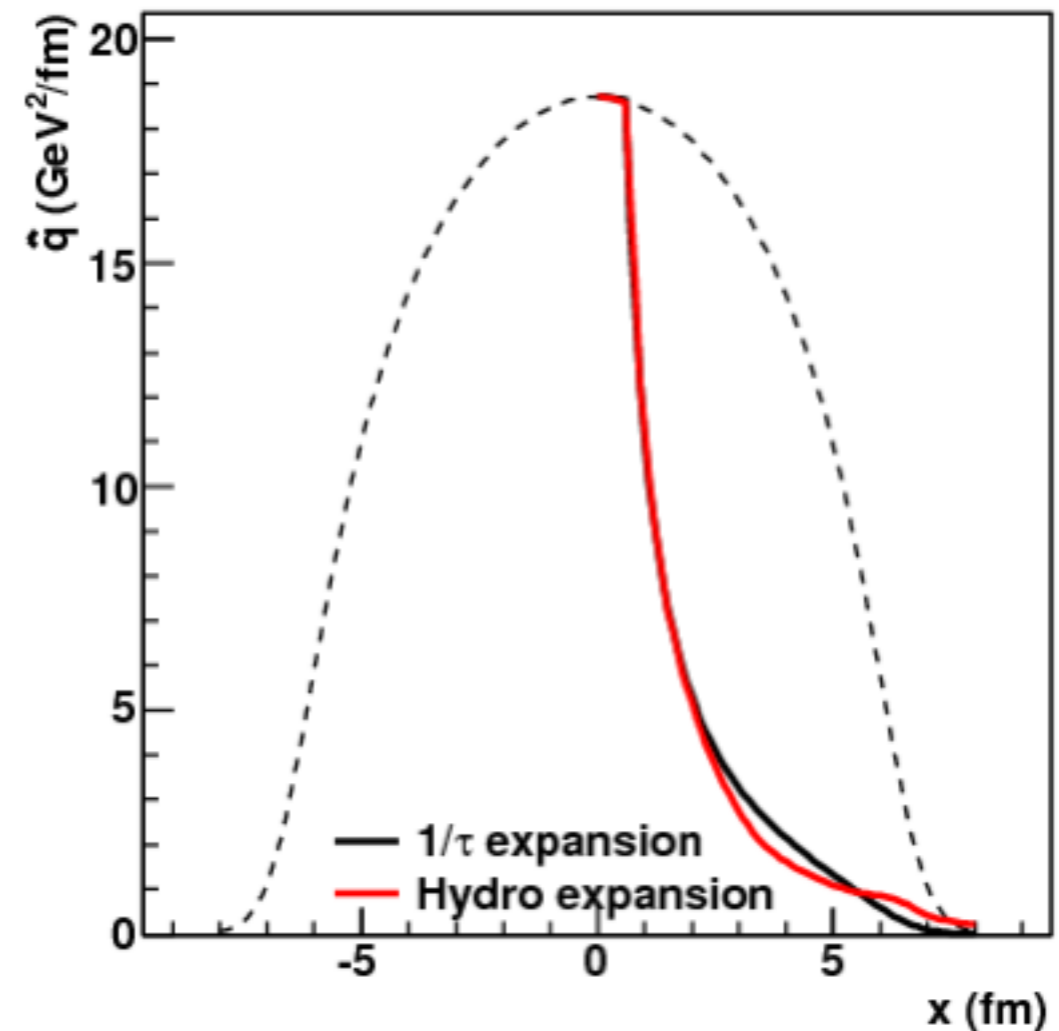
# Geometry

## Density profile



Profile at  $\tau \sim \tau_{\text{form}}$  known

## Density along parton path



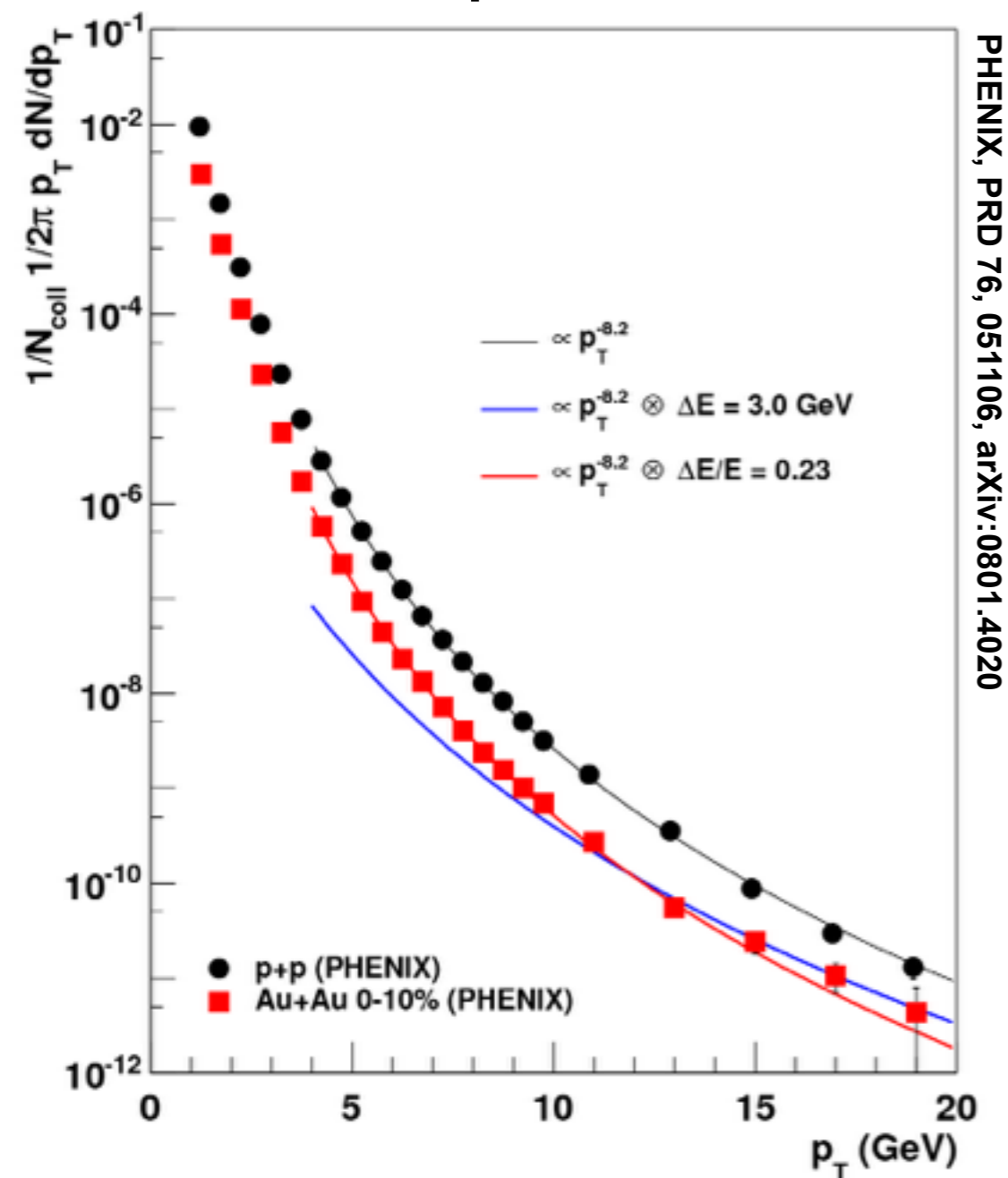
Longitudinal expansion  
dilutes medium  
⇒ Important effect

Space-time evolution is taken into account in modeling

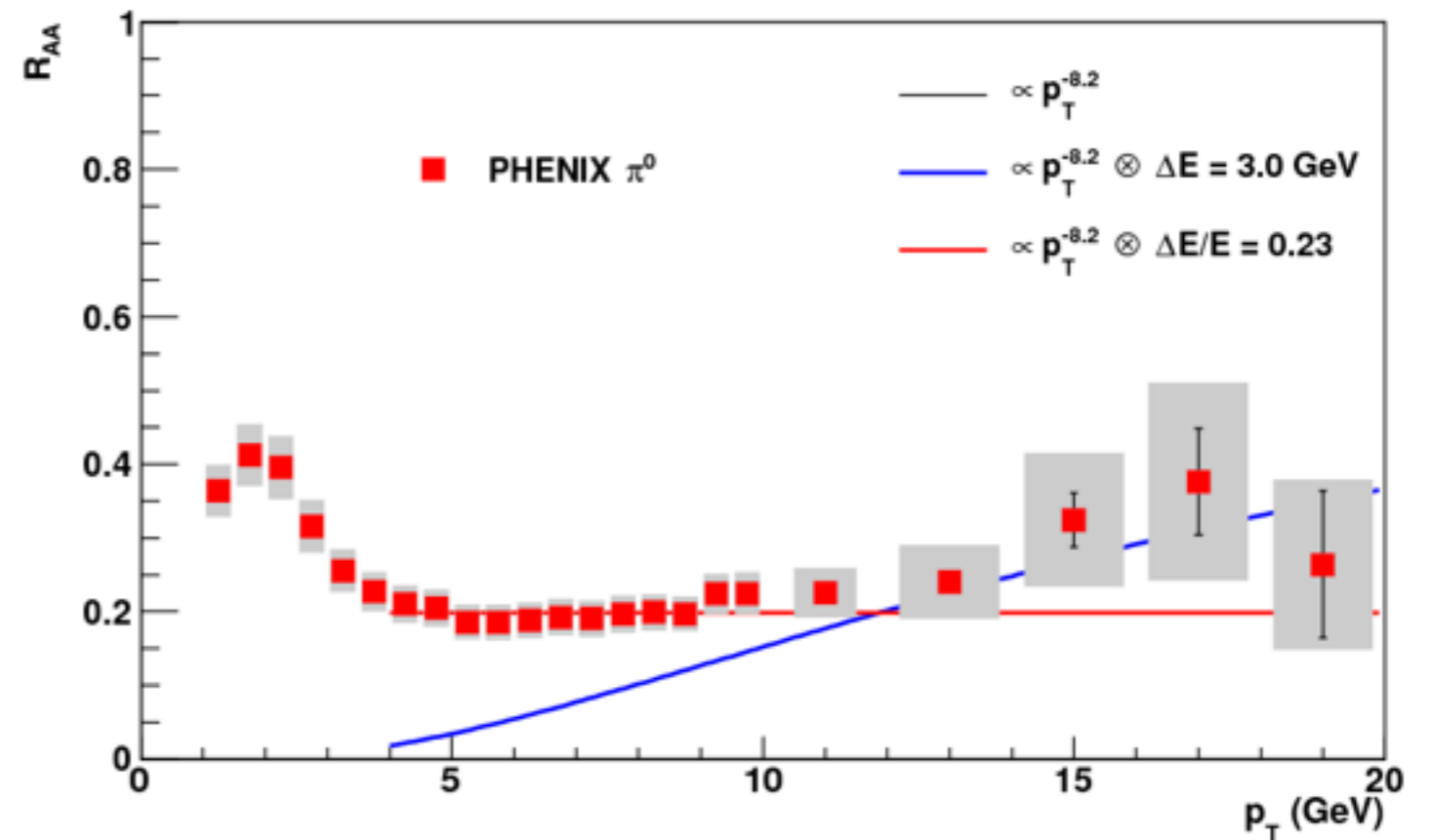


# Getting a sense for the numbers – RHIC

$\pi^0$  spectra



Nuclear modification factor



**Oversimplified calculation:**  
 -Fit pp with power law  
 -Apply energy shift or relative E loss  
**Not even a model !**

**Ball-park numbers:  $\Delta E/E \approx 0.2$ , or  $\Delta E \approx 3 \text{ GeV}$   
 for central collisions at RHIC**

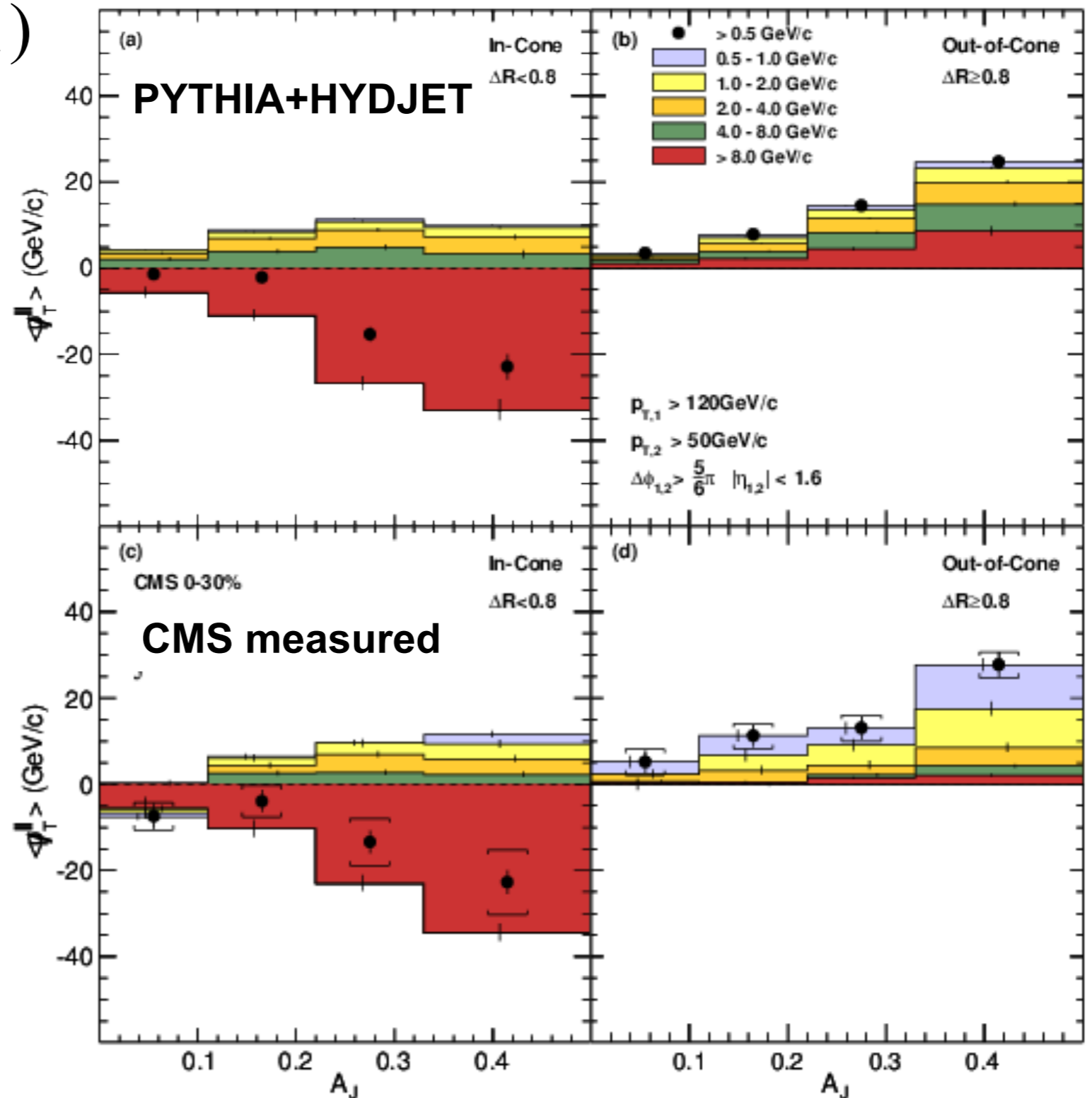
# Looking outside the jet cone

$$p_{T,miss}^{||} = \sum_{tracks} p_T \cos(\varphi - \varphi_{jet})$$

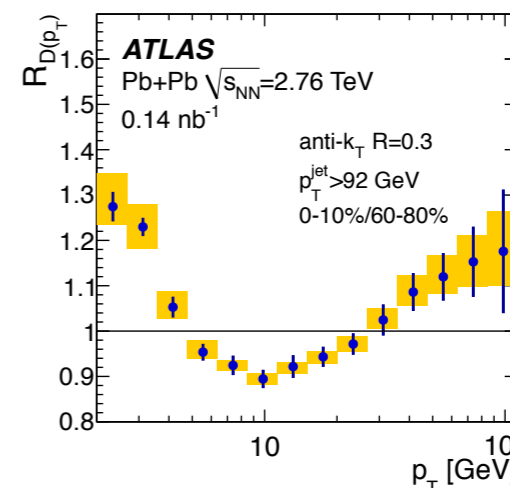
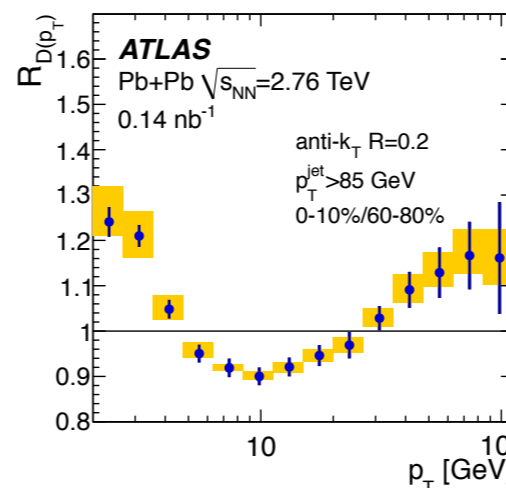
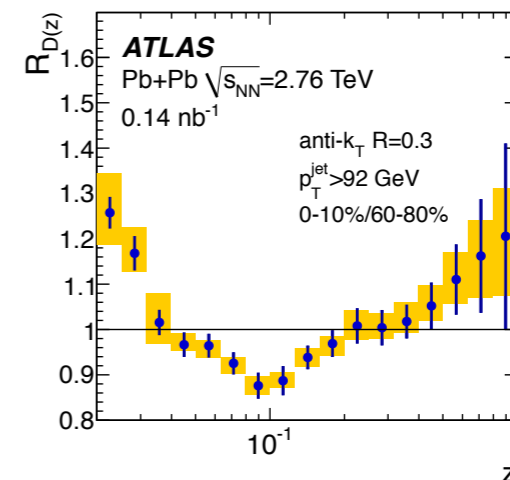
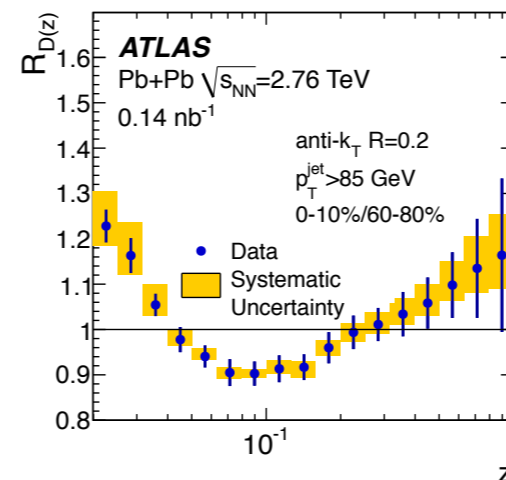
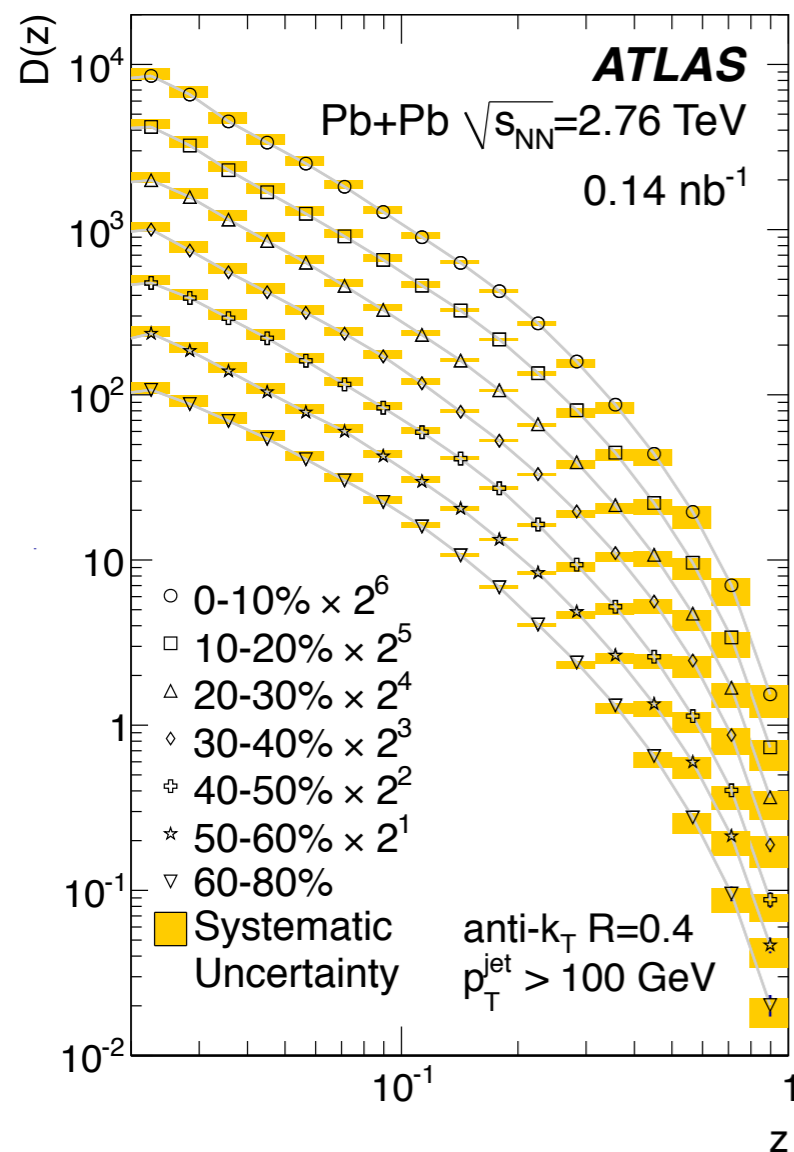
**Momentum imbalance restored by hadrons at large angle  $R > 0.8$  and small  $p_T < 2$  GeV/c**

**In Cone  $R < 0.8$**

**Out of Cone  $R > 0.8$**



# Longitudinal fragment distributions



ATLAS, arXiv:1406.2979

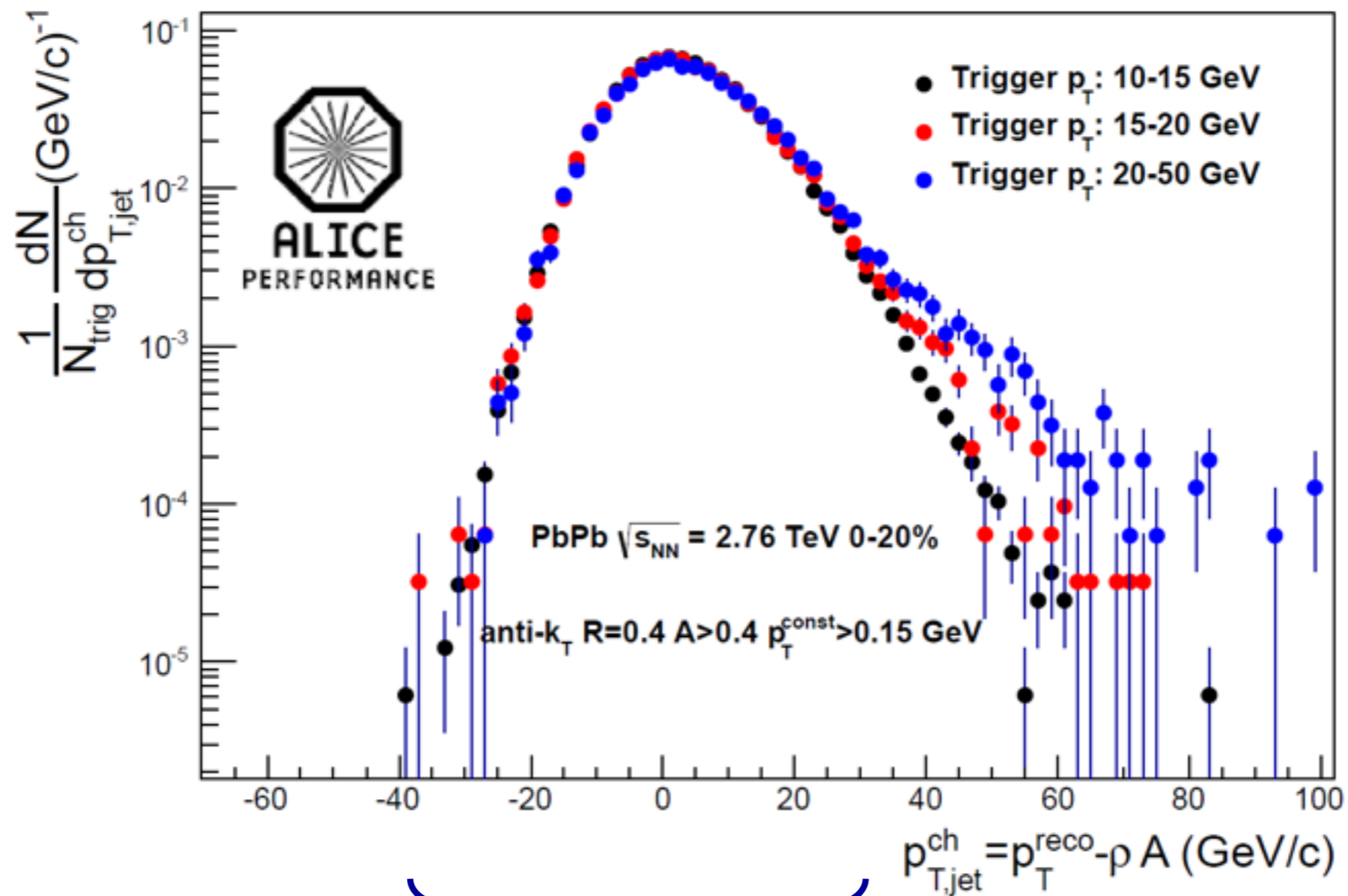
Characteristic pattern observed:

- enhancement at low p<sub>T</sub> < 3 GeV
- suppression at intermediate p<sub>T</sub>: 5-15 GeV
- enhancement (or close to 1) at high p<sub>T</sub> > 20 GeV

# Hadron-recoil jet measurements

# Hadron-triggered recoil jet distributions

G. de Barros et al., arXiv:1208.1518



$p_{T,jet} < 20$  GeV/c:  
 No change with trigger  $p_T$   
 Combinatorial background

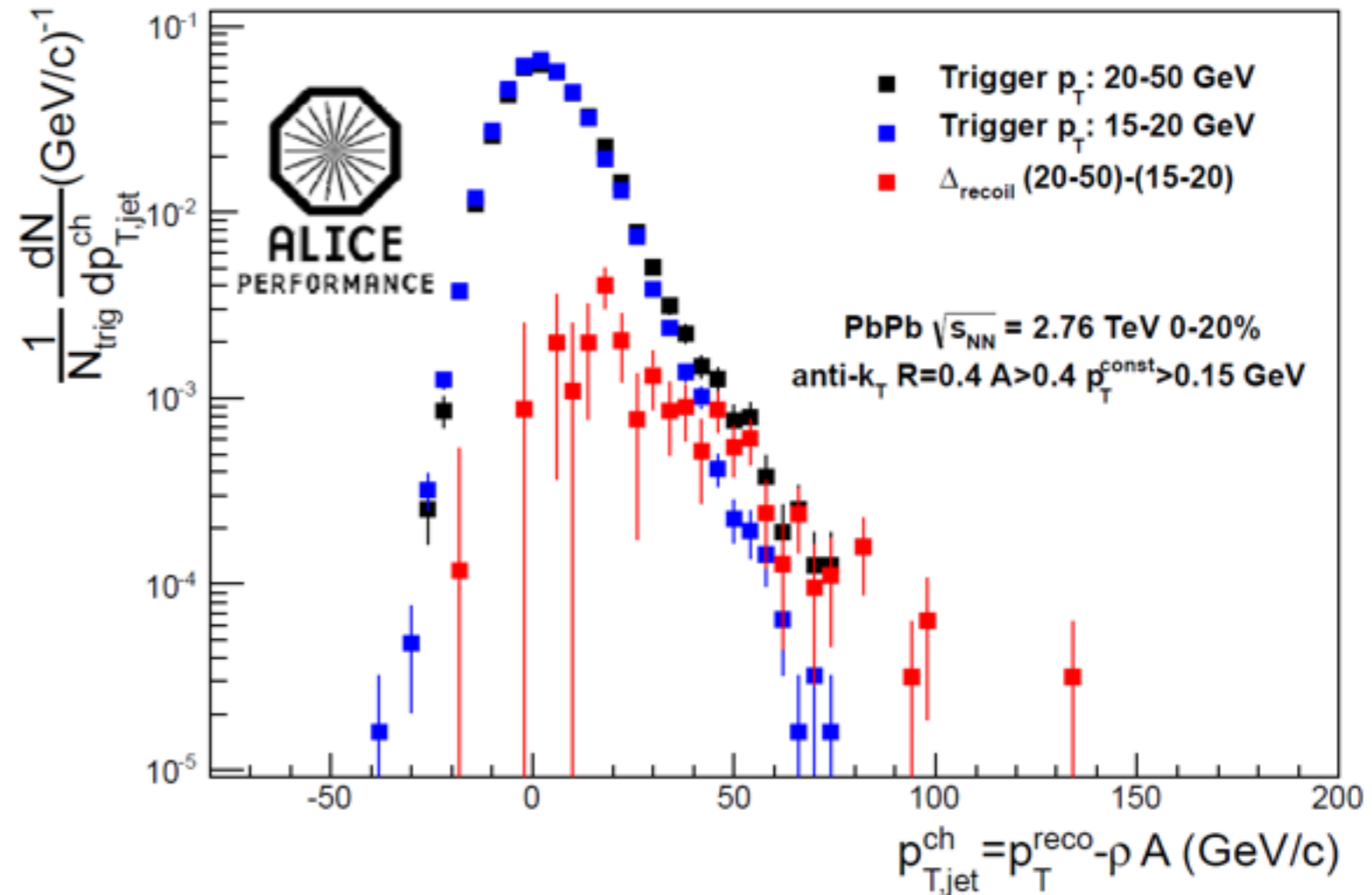
$p_{T,jet} > 20$  GeV/c:  
 Evolves with trigger  $p_T$   
 Recoil jet spectrum

# Background subtraction: $\Delta_{\text{recoil}}$

Remove background by  
subtracting spectrum with  
lower  $p_{\text{T}}^{\text{trig}}$ :

$$\Delta_{\text{recoil}} = [(20-50) - (15-20)]$$

Reference spectrum (15-20)  
scaled by  $\sim 0.96$  to account  
for conservation of jet  
density



$\Delta_{\text{recoil}}$  measures the change of the recoil spectrum with  $p_{\text{T}}^{\text{trig}}$

**Unfolding correction for background fluctuations and detector response**

# Ratio of Recoil Jet Yield $\Delta I_{AA}^{\text{PYTHIA}}$

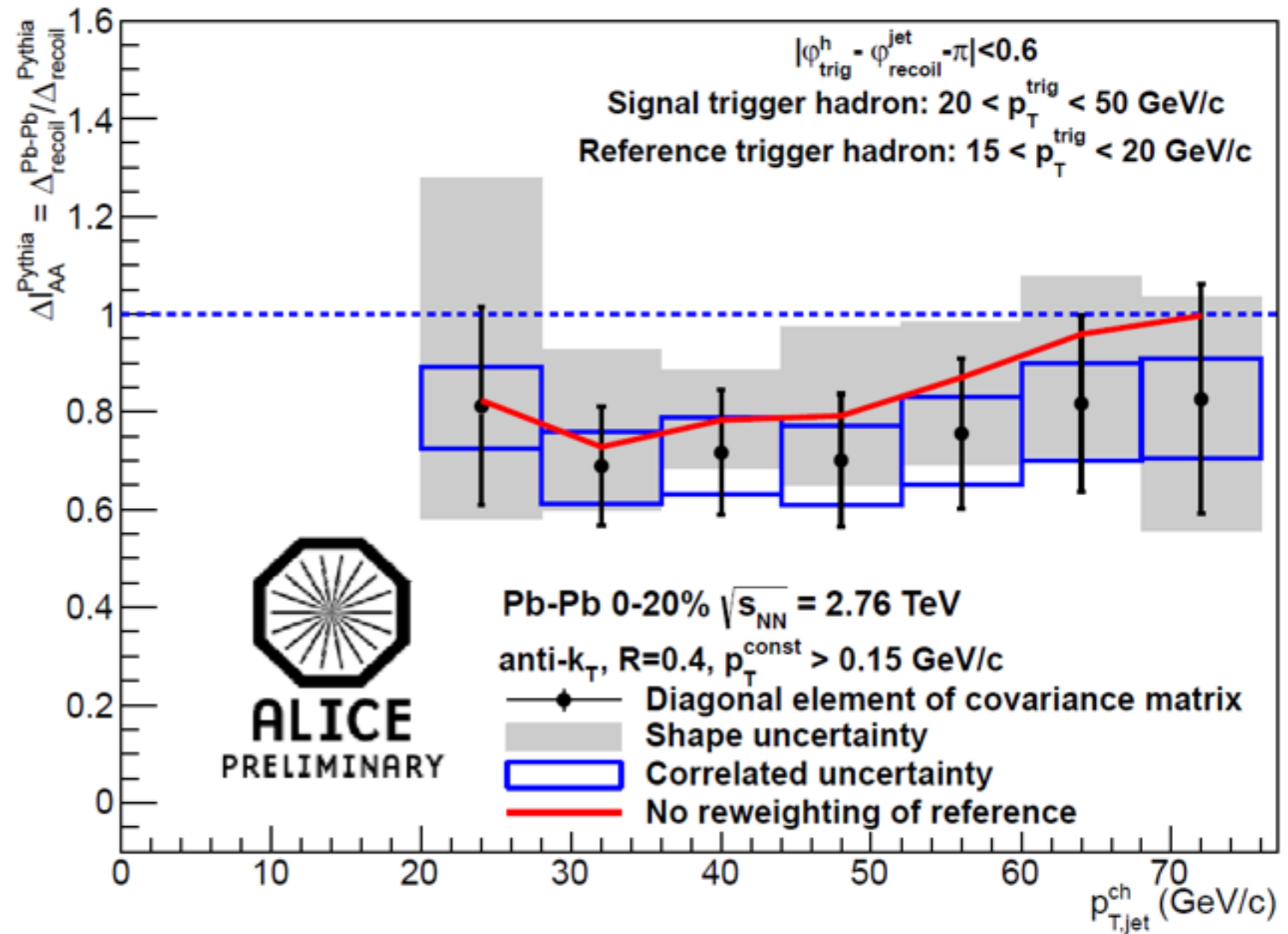
pp reference: PYTHIA  
(Perugia 2010)

$R=0.4$

Constituents:

$p_T^{\text{const}} > 0.15 \text{ GeV}/c$

no additional cuts  
(fragmentation bias) on  
recoil jets

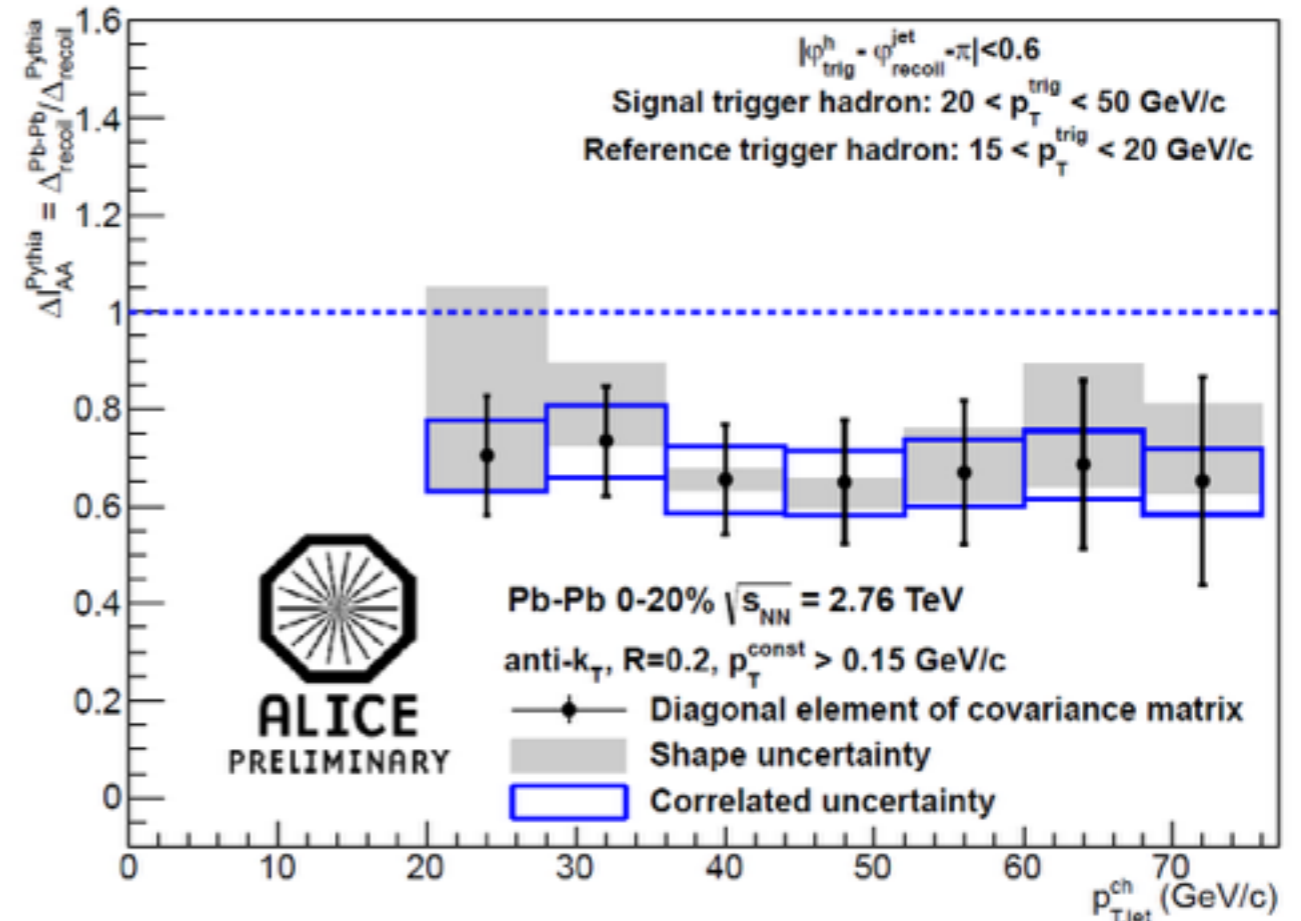
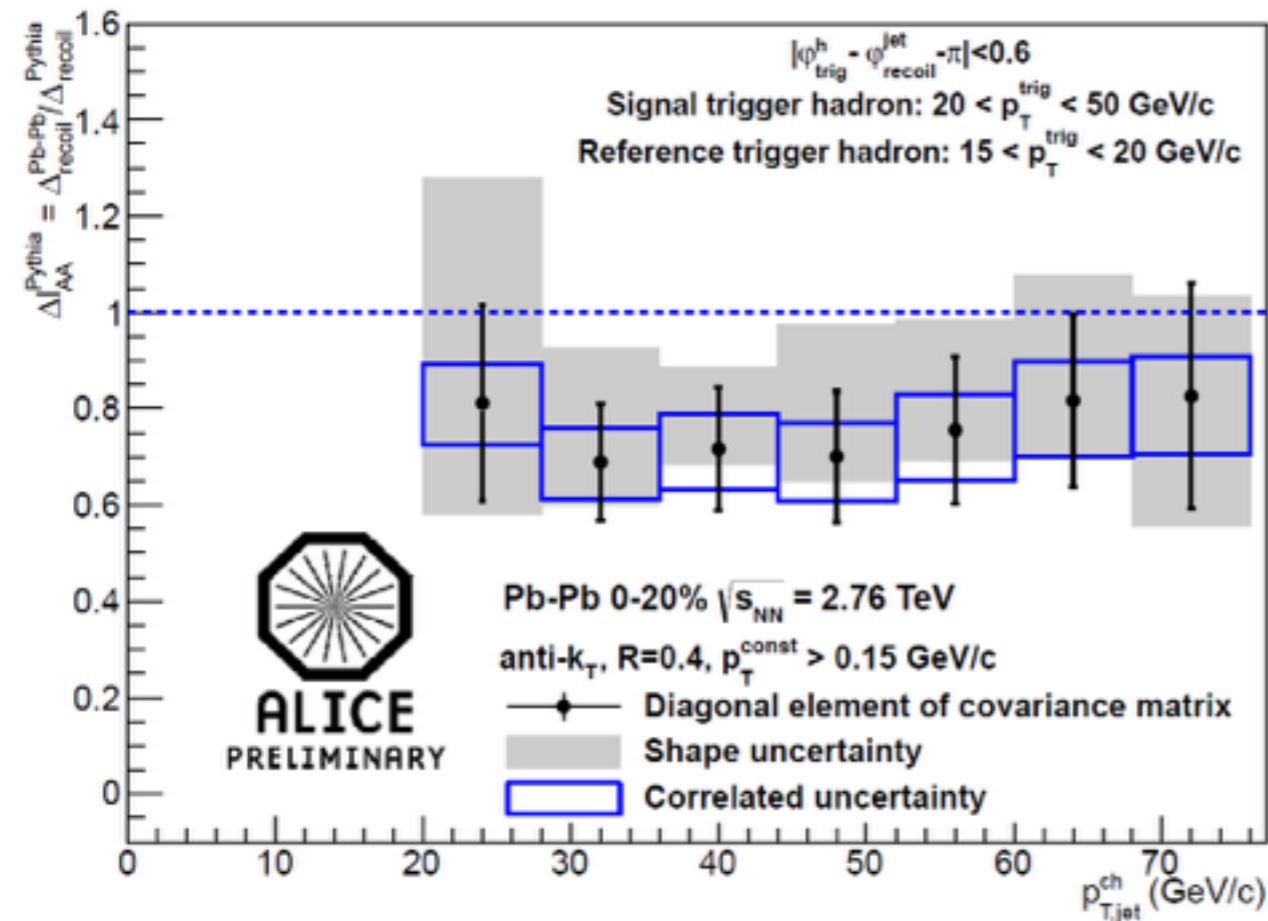


Recoil jet yield  $\Delta I_{AA}^{\text{PYTHIA}} \approx 0.75$ , approx. constant with jet  $p_T$

# Recoil Jet $\Delta_{AA}^{\text{PYTHIA}}$ : R dependence

**R=0.4**

**R=0.2**



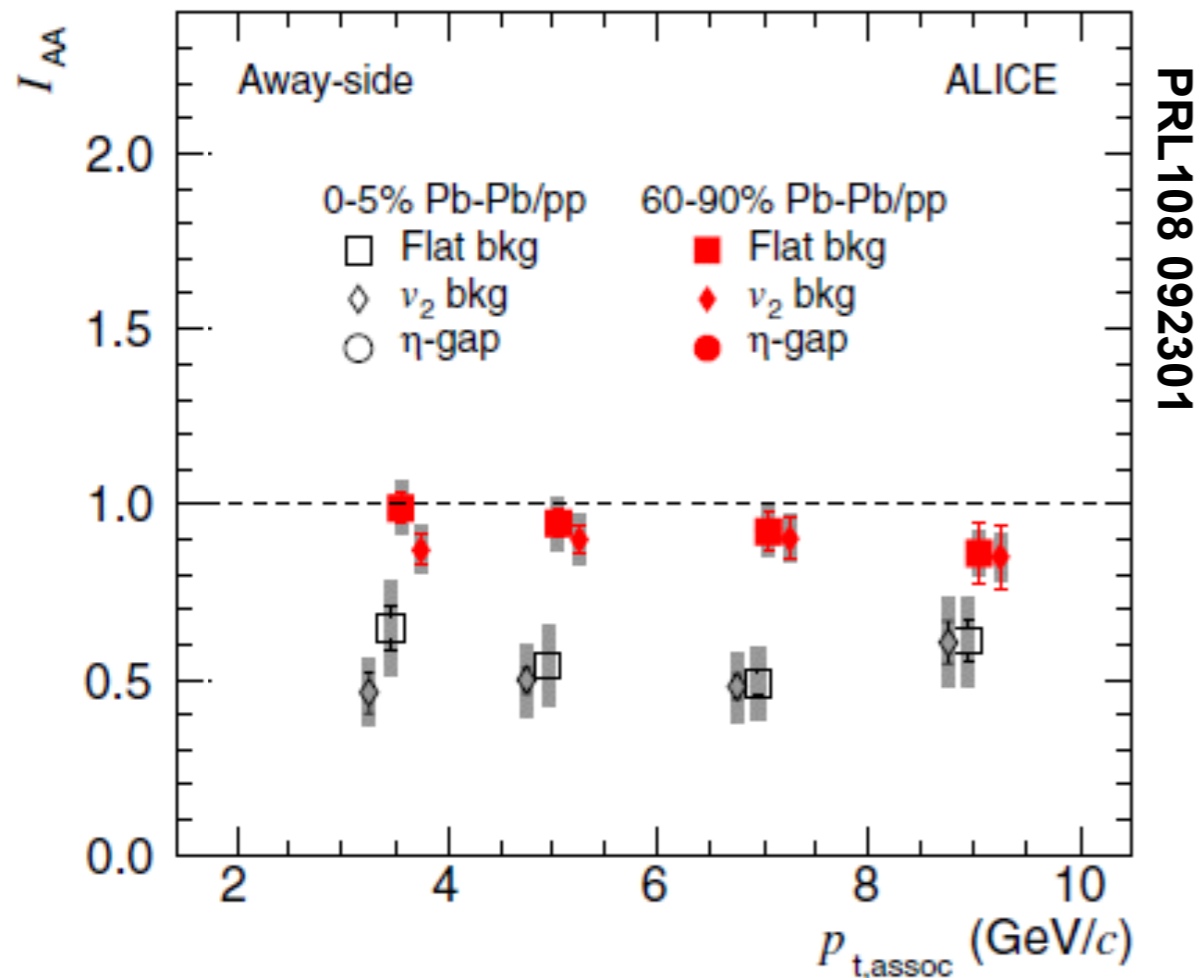
**Similar  $\Delta_{AA}^{\text{PYTHIA}}$  for R=0.2 and R=0.4**

**No visible broadening within R=0.4  
(within exp uncertainties)**



# Hadrons vs jets II: recoil

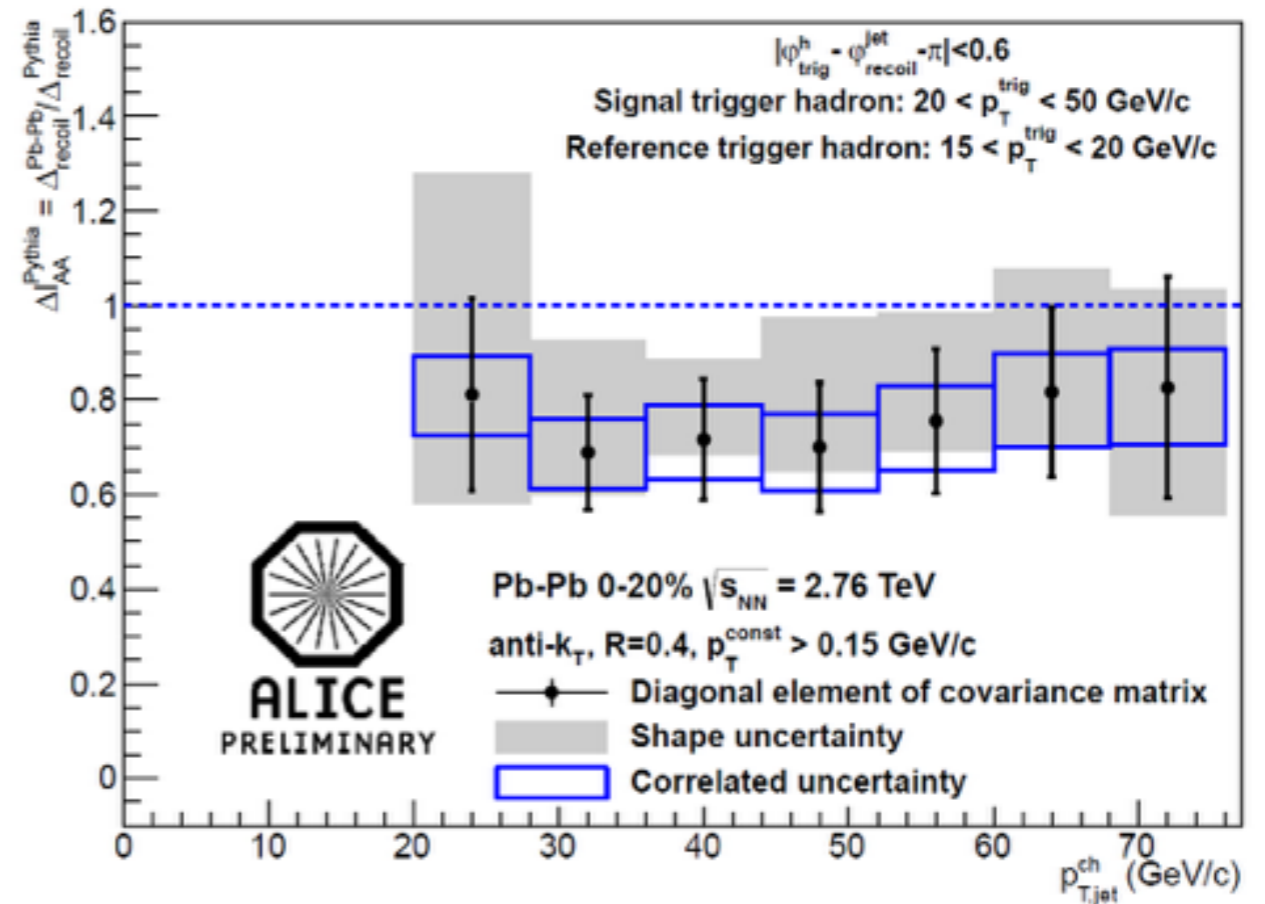
## Hadrons



**Hadron  $I_{AA} = 0.5-0.6$**

**In approx. agreement with models;  
elastic E-loss would give larger  $I_{AA}$**

## Jets

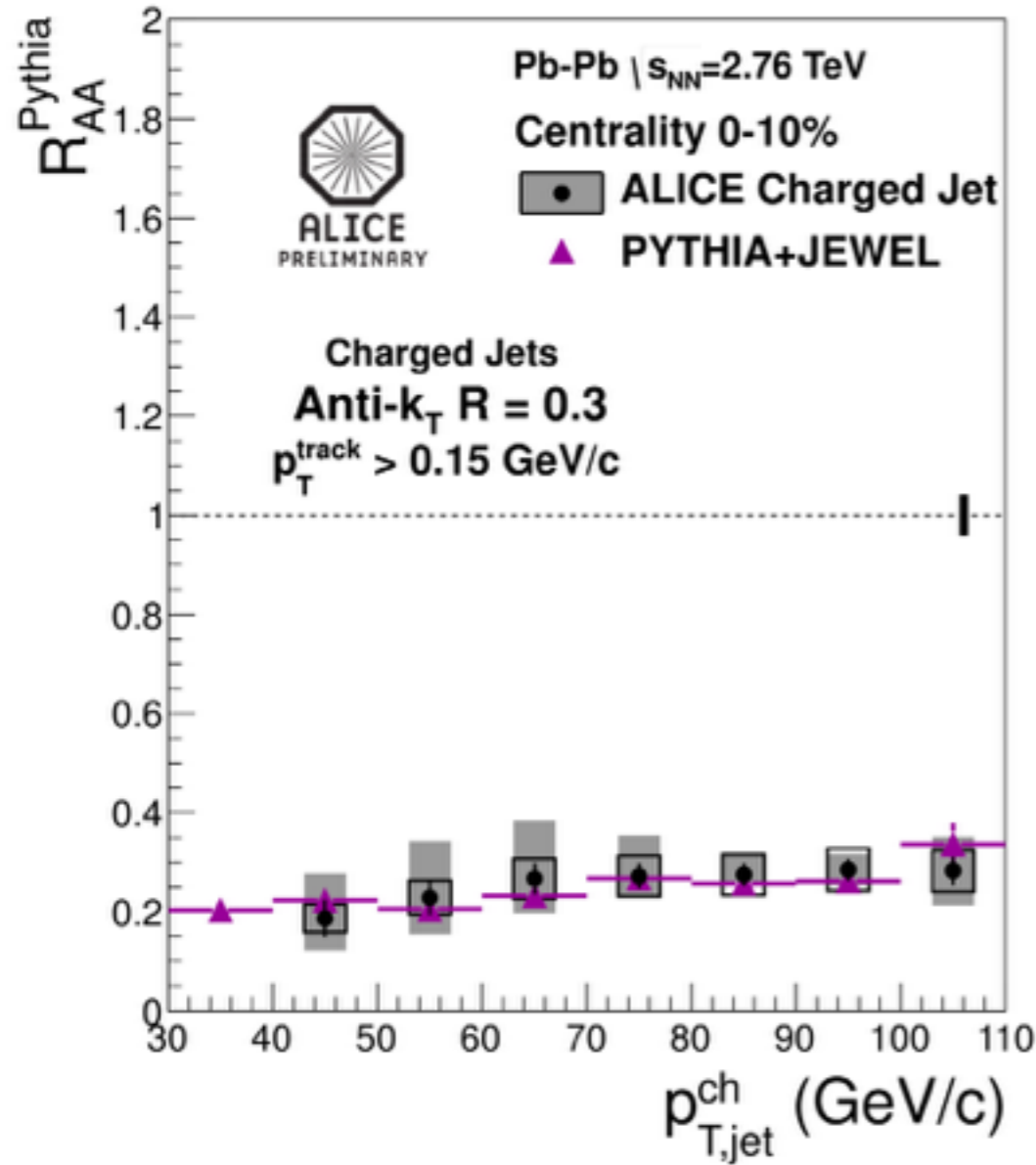


**Jet  $I_{AA} = 0.7-0.8$**

**Jet  $I_{AA} >$  hadron  $I_{AA}$   
Not unreasonable**

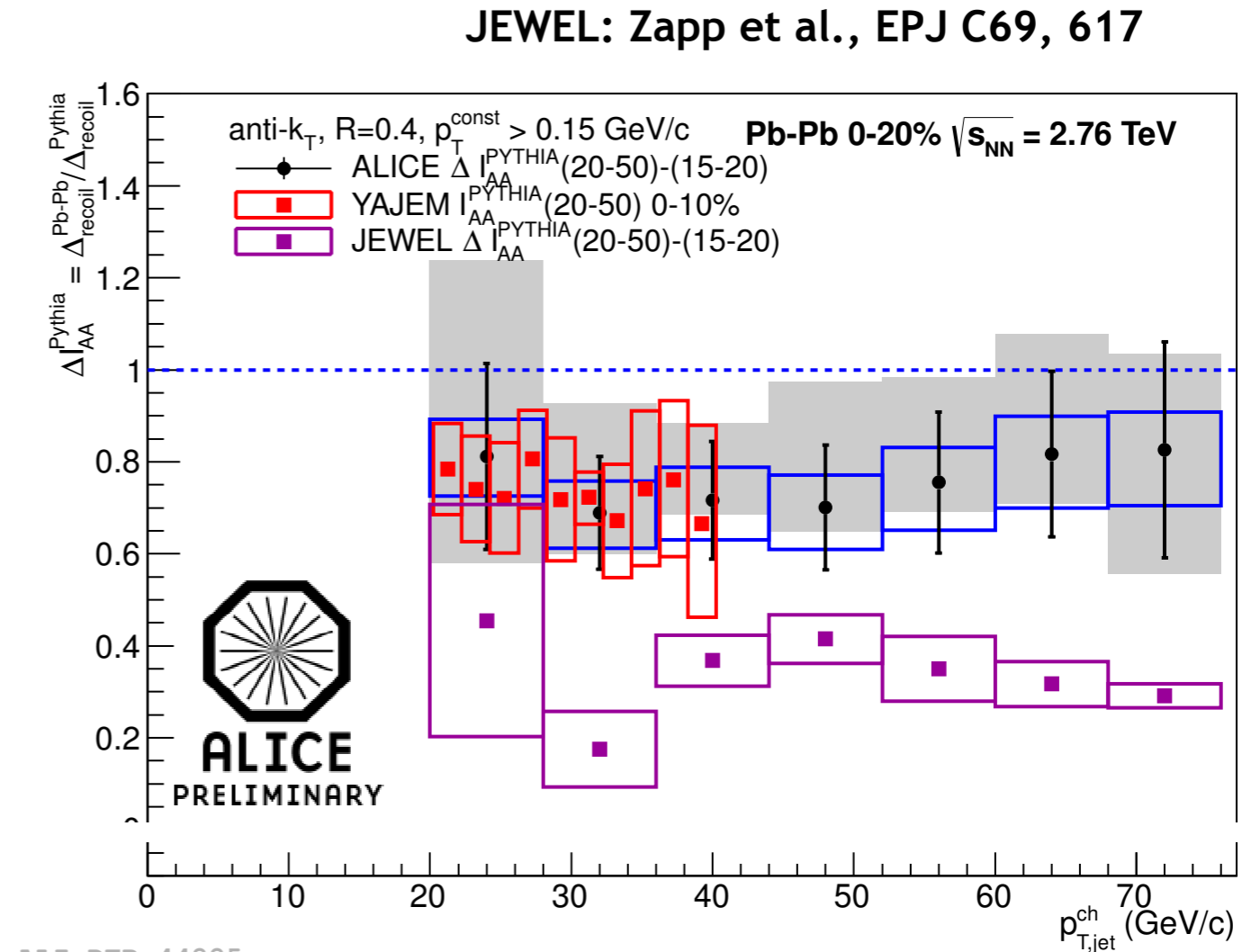
**NB/caveat: very different momentum scales !**

# Model comparison $I_{AA}$



ALI-DER-35933

**JEWEL correctly describes  
inclusive jet  $R_{AA}$**



ALI-DER-44225

**JEWEL  $\Delta I_{AA} \sim 0.4$ , below measured  
YAJEM agrees with measurement  
Difference in energy loss or geometry?**